


Study on Products from Fuel-rich Methane Combustion near Sooting Limit Temperature Region and Importance of Methyl Radicals for the Formation of First Aromatic Rings

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ABSTRACT

Productions of mono-/di-cyclic aromatic hydrocarbons as well as smaller stable species from extremely fuel-rich CH₄/air mixtures (equivalence ratio of 1.7–6.0 and fuel-to-mixture ratio of 15–38 mol.%) near sooting limit in terms of temperature, were investigated using a micro flow reactor with a controlled temperature profile at maximum wall temperature of 1300 K. Species measurements of O₂, H₂, CO, CO₂, CH₄, C₂H₂, C₂H₄, C₂H₆, benzene, toluene, styrene and naphthalene were performed with GC and GC/MS analysis. One-dimensional computations were also conducted with several detailed chemical kinetics. Most of the mechanisms comparably well predicted the smaller species except C₂H₂ (acetylene), which was overestimated by all the mechanism especially at moderate equivalence ratio ($\phi \leq 3.0$). There were large discrepancies between measured and computed mole fractions of benzene and naphthalene at high equivalence ratio ($\phi \geq 4.0$). Reaction path analysis indicated that reaction pathway branched from C₂H₃ reacting with methyl radical, which competes with C₂H₂ production, showed relatively low contribution to benzene formation at moderate equivalence ratio. Therefore, improvements of chemical kinetics with further consideration of reactions with methyl radical are necessary for precise prediction of products where abundant amounts of methyl radical exist.


KEYWORDS

Microcombustion; natural gas; reformed gas; polycyclic aromatic hydrocarbons (PAHs); soot precursors

Introduction

Products from fuel-rich combustion have been widely investigated mainly from two practical aspects. One aspect is to understand precise composition of reformed gases in fuel reforming process. Reformed gas is utilized for various systems such as engines (Tartakovsky and Sheintuch 2018) and fuel cells (Milcarek et al. 2019). While much CO and H₂ generation is expected with the increase of equivalence ratio, soot formation becomes a concern even at intermediate temperatures (around 1300 K) in the flame-assisted fuel cells due to its relatively long residence time. Therefore, it is important to know the reforming conditions to operate reformation systems with the best performance. Another aspect is to

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 Supplemental data for this article can be accessed on the [publisher's website](#).

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explicate the mechanisms of formation/growth of soot and its precursor aromatic species, which have harmful effects on human body and environment, while widely being used in industry as chemical materials. Many studies have been conducted at fuel-rich conditions to investigate sooting limits (Glassman 1988; Takahashi and Glassman 1984) and growth of soot and its precursors (Richter and Howard 2000; Wang 2011). These studies mainly focused on fuels containing two or more C-atoms. However, because the use of natural gas has been increasing, understanding of products from combustion of methane, which is a main component of natural gas, at fuel-rich conditions has become significantly important. As shown in Figure 1, measurements of soot, aromatic species and smaller species from fuel-rich methane combustion were conducted by employing several methods, e.g. premixed flat-flame burners (Ahmed et al. 2016; Alfè et al. 2010; Castaldi, Vincitore, Senkan 1995; Li et al. 2012; Marinov et al. 1996; Melton, Vincitore, Senkan 1998; Xu and Faeth 2000), jet-stirred reactor (Cong and Dagaut 2008) and plug-flow reactors (Köhler et al. 2016; Skjøth-Rasmussen et al. 2004) near atmospheric pressure.

Modelling studies on growth of soot precursors such as polycyclic aromatic hydrocarbons (PAHs) in methane flame (Chernov et al. 2014; Jin et al. 2015; Marinov et al. 1996; Slavinskaya and Frank 2009) were also carried out. However, there is a gap in fuel-to-mixture ratio between the flame studies (approximately 27–65 mol.% at $\phi \geq 2$), which are close to practical conditions, and the reactor studies (less than 1 mol.%). This is because of the limitation of a self-sustained flame in the flame studies and large dilution to suppress temperature change in the reactor studies. As rate of formation of first aromatic ring is

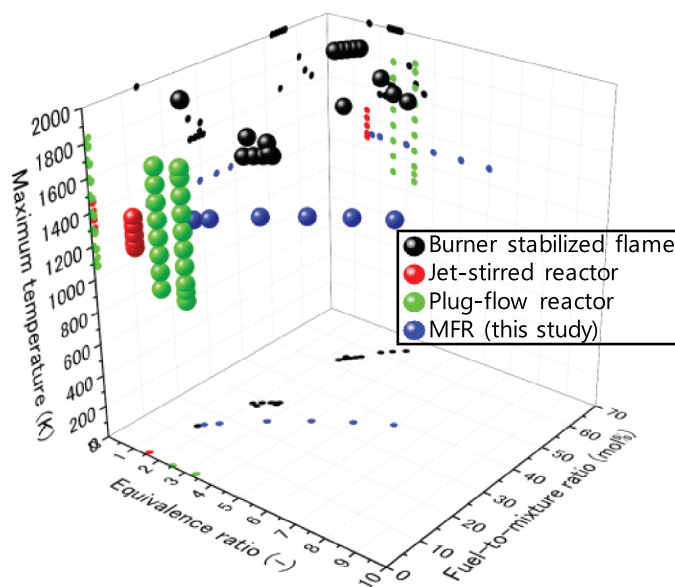


Figure 1. Experimental conditions of soot and species measurements for fuel-rich CH_4 combustion near atmospheric pressure operated by various methods: burner stabilized flames (Ahmed et al. 2016; Alfè et al. 2010; Castaldi, Vincitore, Senkan 1995; Li et al. 2012; Marinov et al. 1996; Melton, Vincitore, Senkan 1998; Xu and Faeth 2000); jet-stirred reactor (Le Cong and Dagaut 2008); plug-flow reactors (Köhler et al. 2016; Skjøth-Rasmussen et al. 2004); and a micro flow reactor with a controlled temperature profile (this study).

a primary factor to control soot formation (Glassman 1988), investigation of gas-phase species at both of high equivalence ratio and high fuel-to-mixture ratio conditions is necessary for further understanding of products from fuel-rich methane combustion. Particularly, it is important to gain new insight into the formation of the first aromatic ring under conditions where significant amount of methyl radical exists, as well as PAH growth with such as methyl addition/cyclization (Shukla, Miyoshi, Koshi 2010). To realize the extremely fuel-rich conditions, i.e. high equivalence ratio and high fuel-to-mixture ratio, a micro flow reactor with a controlled temperature profile (Maruta et al. 2005) (MFR) was employed in this study.

MFR comprises a quartz tube whose inner diameter is smaller than ordinary quenching diameter, and an external heat source which gives a stationary temperature profile along the inner surface of the reactor, as show in the upper part of Figure 2. Heated by the external heat source, MFR is capable of handling combustion of mixtures even outside of the flammability limits. In our previous studies on near sooting-limit flames using MFR (Dubey et al. 2016; Nakamura et al. 2014), four types of flame and soot responses were observed depending on equivalence ratio and inlet flow velocity: only flame; flame with

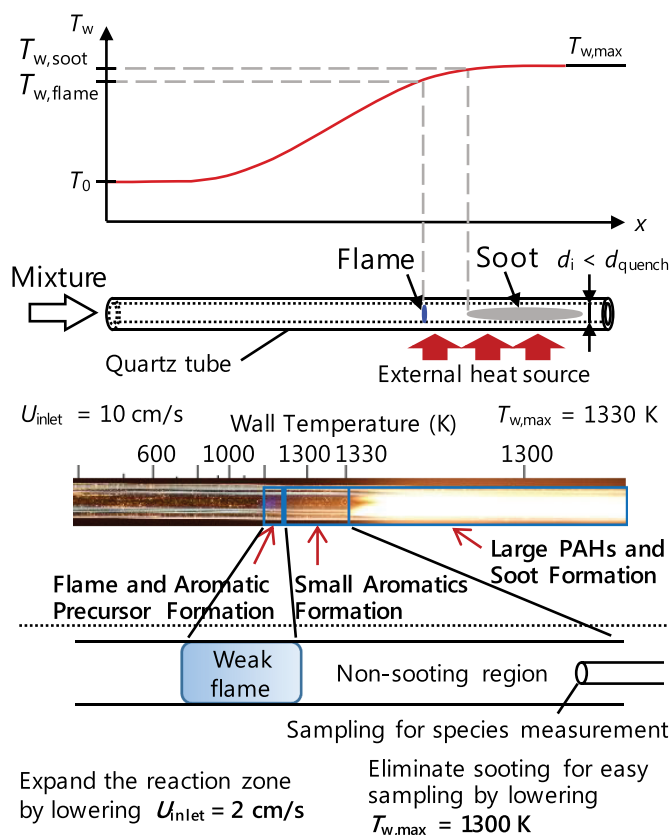


Figure 2. Schematic and direct image (Dubey et al. 2016) of flame and soot observation in MFR.

soot; only soot; and none of them. For the second case, flame and sooting regions were spatially separated in the flow direction, as shown in [Figure 2](#).

Two types of flame regime exist at fuel-rich conditions depending on inlet flow velocity: weak flame in low and normal flame in high inlet flow velocity conditions. At low inlet flow velocity (weak flame) conditions, gas temperature is strongly governed by wall temperature because of small heat release from the reaction zone and also small Peclet number which is the nature of MFR. Consequently, a rapid increase in gas temperature is suppressed resulting in no need of high dilution of mixtures. From these characteristics of MFR at low inlet flow velocity conditions, the extremely fuel-rich conditions can be realized and a series of phenomena up to a certain temperature range, i.e. only gas-phase reactions even near sooting limit, can be extracted by controlling maximum wall temperature ($T_{w,max}$). In our previous studies applying this method, species measurements of PAHs for fuel-rich acetylene (Nakamura et al. 2014) and *n*-/*iso*-cetane (Nakamura et al. 2015) were performed. Flame positions and species measurement of C_1 – C_2 species for fuel-rich methane/air at $T_{w,max} = 1200$ K were also investigated (Dubey et al. 2019). In addition to the production of the smaller species reported in (Dubey et al. 2019), it is important to know that of aromatic species where the production becomes significant as well as near sooting limit in terms of temperature, as shown in [Figure 3](#).

In this study, species measurements of C_0 – C_2 species and aromatic hydrocarbons for extremely fuel-rich methane/air mixtures at $T_{w,max} = 1300$ K, where near sooting limit and production of aromatic species drastically starts increasing as shown in [Figure 3](#), were performed by GC and GC/MS connected to MFR. One-dimensional computations were also performed with several chemical kinetics to investigate the species productions.

Experimental method

[Figure 4](#) shows a schematic of experimental setup. A quartz tube with an inner diameter of 2 mm was used as a reactor channel.

CH_4 /air mixtures were supplied to the reactor at a mean inlet flow velocity of 2 cm/s. Equivalence ratio (ϕ) was varied over a range of 1.7–6.0 (fuel-to-mixture ratio of 15–38 mol.%) by controlling flow rates of fuel and air with mass flow controllers. Experiments were conducted at atmospheric pressure. From our previous studies for CH_4 /air mixtures in MFR (Dubey et al. 2016; Nakamura et al. 2014), soot formation was

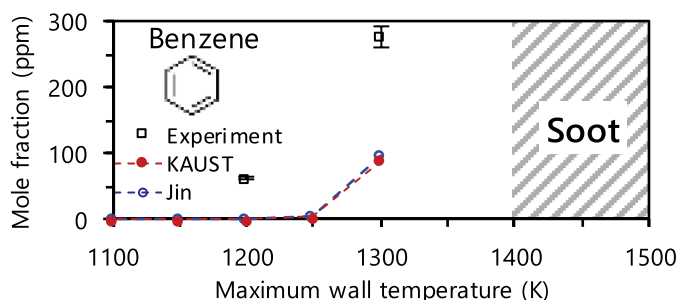


Figure 3. Benzene production as a function of maximum wall temperature at $\phi = 6.0$ in MFR. See following sections for experimental and computational methods.

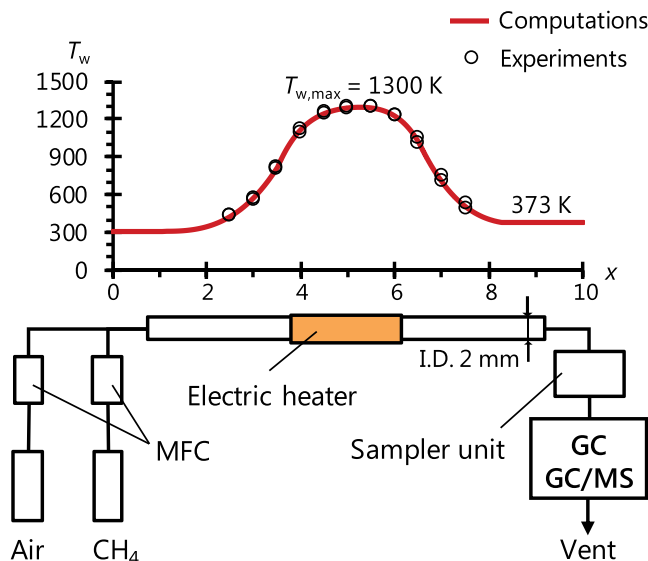


Figure 4. Schematic of experimental setup. The temperature profile shown in the figure was measured in experiments and used in computations.

observed at $T_{w,max} = 1300$ K with $T_{w,max}$ -region of approximately 4-cm-long heated by a hydrogen/air flat-flame burner as an external heat source. In this study, an electric heater was attached to the reactor as the heat source aiming to shorten the length of $T_{w,max}$ -region, which was approximately 0.5 cm long. Consequently, soot formation was not observed at $T_{w,max} = 1300$ K but clearly observed at $T_{w,max} = 1400$ K. Therefore, a stationary temperature profile with the range of 300–1300 K was provided to focus on gas-phase products near sooting limit. The temperature profile of the inner wall surface of the reactor was measured with a K-type thermocouple inserted from the downstream of the reactor. Exhaust gas was directly introduced into a sampler unit from the exit of MFR through a sampling line. The line was heated as 373 K to prevent water condensation. Sampled gas was then analysed by GC (Shimadzu GC-2010 Plus) or GC/MS (Agilent 7890/5975).

O₂, H₂, CO, CO₂, CH₄, C₂H₂, C₂H₄ and C₂H₆ were measured by GC. For GC analysis, the sampling volume was set to 50 μ l and a coupled two MICROPACKED-ST (3.0 m \times 1.0 mm I.D.) capillary column was employed. A barrier discharge ionization detector (BID) was adopted as a detector and its temperature was set to 483 K. Standard gases were used for the quantification of the species.

Benzene, toluene, styrene and naphthalene were measured by GC/MS. For GC/MS analysis, the sampling volume was set to 500 μ l and DB-5 ms Ultra Inert (60 m \times 0.25 mm I.D.) was employed as a column. Temperatures of the ionization source and quadrupole were set to 513 K and 439 K, respectively. Note that for GC/MS experiment, 21%O₂/1%Ar/N₂ synthetic air was used as “air”. Internal standard method was applied for calibration of benzene using Ar as an internal standard substance along with standard gas of benzene. Relative response factors were applied for quantification of toluene, styrene and naphthalene. In addition to the measured species, cyclopentadiene, ethylbenzene, xylene isomers, indene and methyl-naphthalene were identified but their signals were too small to

be quantitatively discussed. Helium was used as a carrier gas for both of GC/BID and GC/MS experiments. Experiments were repeated at least three times for each condition and uncertainties in measured mole fractions were shown as error bars.

Computational method

To validate various chemical kinetic models and to conduct analysis of productions of the measured species, computations were performed by modelling the MFR system. The flow field in MFR can be assumed as reactive flow without boundary layer at low inlet flow velocity conditions. The usage of one-dimensional computations for MFR was justified by comparison of one- and two-dimensional computations (Grajetzki et al. 2019). Therefore, one-dimensional steady-state computations were conducted using PREMIX code in ANSYS Chemkin-Pro v19.0 with an additional term of convective heat transfer between the gas and the reactor wall in a gas-phase energy equation (Maruta et al. 2005). Computational conditions (mixture compositions, inlet flow velocity, wall temperature profile (Figure 4) and pressure) were the same as those in the experiment. Computational domain was set to 0–10 cm. Species mole fractions at $x = 10$ were compared with experimental results. Computed species profiles of the aromatic species in MFR are shown in Supplementary Fig. S1. Previous studies (Kizaki et al. 2015; Saiki and Suzuki 2013) reported that radical quenching effect on a quartz surface in the heated narrow channel under atmospheric pressure is negligibly small. Therefore, any surface reaction mechanism for radical quenching effect was not considered in this study. As detailed chemical kinetic models, KAUST-Aramco PAH Mech 1.0 (Selvaraj et al. 2016) (397 species, 2346 reactions, includes up to C_{24} ; hereafter called as KAUST), Jin mechanism (Jin et al. 2017) (238 species, 1689 reactions, includes up to C_{18} ; Jin) and PRF + PAH mechanism (Version 1412, December 2014) (CRECK Modeling Group, 2014) (176 species, 6067 reactions, includes up to C_{20} ; CRECK) were used.

Results and discussion

Results of species measurement and computation

Figure 5 shows experimental and computational results of mole fractions of O_2 , H_2 , CO, CO_2 , CH_4 , C_2H_2 , C_2H_4 , C_2H_6 , benzene, toluene, styrene and naphthalene. Results are stated in three parts: small species up to C_1 species; C_2 hydrocarbons; and mono-/di-cyclic aromatic hydrocarbons.

First, results for O_2 , H_2 and C_1 species are examined. The measured O_2 mole fraction increases as equivalence ratio increases. This tendency is caused by a suppression of reactions that highly contribute to consumption of O_2 , e.g. CO and CO_2 production in C_1 reaction pathway, competing with proceeding of reaction pathway in higher hydrocarbons. KAUST and Jin quantitatively predict the measured O_2 mole fraction, while CRECK underestimates O_2 mole fraction especially at high equivalence ratio. The measured H_2 mole fraction increases as equivalence ratio increases until $\phi = 3.0$, and then shows almost a constant value at higher equivalence ratio. KAUST and Jin qualitatively reproduce the measured H_2 mole fraction, while CRECK shows increasing trend. The measured CO mole fraction increases at moderate equivalence ratio and decreases at high equivalence ratio as

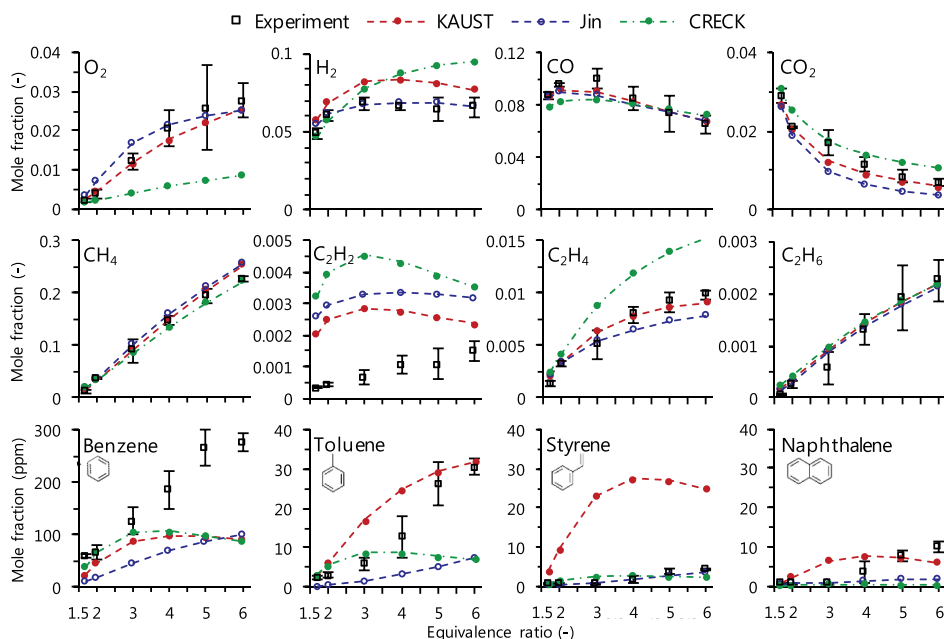


Figure 5. Measured (open square) and computed (circle with line) mole fractions of O_2 , H_2 , C_1 – C_2 and aromatic species for CH_4 /air mixtures at $\phi = 1.7$ – 6.0 (fuel-to-mixture ratio of 15–38 mol.%) and $T_{w,max} = 1300$ K.

equivalence ratio increases, having a peak at around $\phi = 3.0$. The measured CO_2 mole fraction decreases as equivalence ratio increases. All the mechanisms predict the measured CO and CO_2 mole fractions well. The measured CH_4 mole fraction shows a linear increase with increasing equivalence ratio. The computational CH_4 mole fraction with CRECK agrees with the experimental result, while KAUST and Jin slightly overestimate CH_4 mole fraction at high equivalence ratio. For these O_2 , H_2 and C_1 species, which show larger mole fractions among the measured species, the mechanisms reproduce the experimental results comparably well.

Secondly, results for C_2 hydrocarbons are examined. Measured mole fraction of C_2H_2 , one of the most important aromatic/soot precursors, monotonically increases as equivalence ratio increases. However, none of the mechanisms predicts this trend especially at high equivalence ratio: KAUST and CRECK have a peak at $\phi = 3.0$ and then tend to decrease; Jin shows almost a constant value at high equivalence ratio. It is notable that all the mechanisms overestimate C_2H_2 mole fraction over the equivalence ratio. This overestimation of C_2H_2 will be discussed in Section 4.2. The measured C_2H_4 mole fraction marks the largest value among C_2 hydrocarbons, but its increasing trend becomes gradually small as equivalence ratio increases. KAUST quantitatively reproduces the measured C_2H_4 mole fraction. Although Jin slightly underestimates C_2H_4 mole fraction at high equivalence ratio, it agrees with the experimental result at moderate equivalence ratio. CRECK shows larger value than measured C_2H_4 mole fraction by a factor of more than 1.5 at high equivalence ratio. The measured C_2H_6 mole fraction shows a linear increase with increasing equivalence

ratio. All the mechanisms quantitatively predict C_2H_6 mole fraction. As a brief summary for prediction of C_2 hydrocarbons, model dependence in C_2H_2 mole fraction is significant compared to C_2H_4 and C_2H_6 mole fractions.

Finally, mono-/di-cyclic aromatic hydrocarbons such as benzene, toluene, styrene and naphthalene were quantitated at $T_{w,max} = 1300$ K. The measured benzene mole fraction increases as equivalence ratio increases. KAUST and CRECK agree with the experimental result at moderate equivalence ratio ($\phi \leq 3.0$), while they show almost constant values or even a slightly decreasing trend at high equivalence ratio ($\phi \geq 3.0$). Consequently, discrepancy between the measured and computed benzene mole fractions becomes large as equivalence ratio increases. In contrast, Jin qualitatively reproduces the upward trend in measured benzene mole fraction over the equivalence ratio. However, it underestimates benzene mole fraction by a factor of 3. Measured toluene and styrene mole fractions also increase as equivalence ratio increases. KAUST predicts toluene mole fraction well although it overestimates styrene mole fraction. Jin qualitatively predicts toluene mole fraction even though it slightly underestimates the mole fraction, and agrees with the measured styrene mole fraction. Comparing the computed toluene and styrene mole fractions of KAUST with those of Jin, the latter mechanism shows smaller value than the former one. For both toluene and styrene mole fractions, CRECK shows similar trend as is obtained in prediction of benzene mole fraction, i.e. decreasing trend at high equivalence ratio. A drastic increase in measured naphthalene mole fraction is observed at around $\phi = 4.0$, which none of the mechanisms predicts the trend; KAUST has a peak at $\phi = 4.0$ followed by decreasing trend at higher equivalence ratio; Jin monotonically increases over the equivalence ratio; and CRECK shows approximately an order of the magnitude smaller than the measured naphthalene mole fraction. For these mono-/di-cyclic aromatic hydrocarbons, it is found that improvements of reaction mechanisms are required especially for production of benzene at $\phi \geq 4.0$.

From these comparisons, significant discrepancies between measured and computed mole fractions were observed for C_2H_2 and benzene, which show relatively large mole fractions and are major aromatic/soot precursors. Therefore, discussion focusing on these species will be conducted in the following sections.

Overestimation of C_2H_2 mole fraction

All the mechanisms overestimated C_2H_2 mole fraction as mentioned in the previous section. Figure 6 shows computational results of C_2H_2 mole fraction performed with various mechanisms including four additional chemical mechanisms (Metcalf et al. 2013; San Diego Mechanism, 2016; Smith, Tao, Wang 2016; Yang et al. 2017), and the experimental result.

Computational results of the smaller species with the additional mechanisms are shown in Supplementary Fig. S2. The additional mechanisms do not include PAH formation, but are recently updated. Even these new mechanisms, however, overestimate C_2H_2 mole fraction. The overestimation of C_2H_2 is also reported in flame (Li et al. 2012; Xu and Faeth 2000), plug-flow reactor (Köhler et al. 2016) and shock tube (Herzler et al. 2019) studies for methane fuel. Most of the computational results with the additional (non-PAH) mechanisms show smaller values than those of the PAH mechanisms. However, even considering production of benzene, which possibly shows the largest amount among

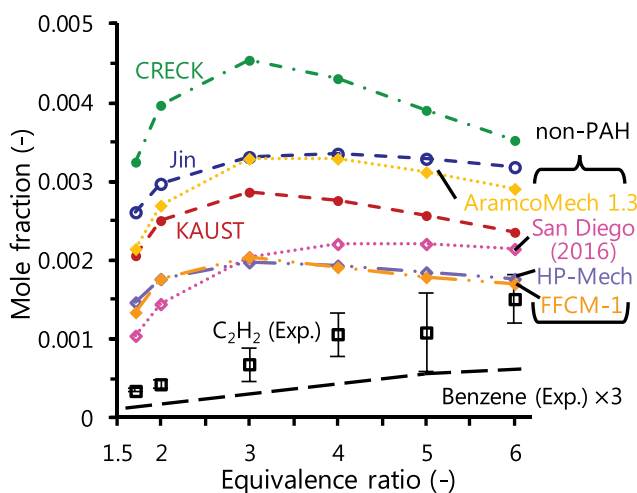


Figure 6. C_2H_2 prediction performed by various chemical kinetics: KAUST (Selvaraj et al. 2016), Jin (Jin et al. 2017) and CRECK (CRECK Modeling Group, Politecnico di Milano 2014) as mechanisms including PAH growth; AramcoMech 1.3 (Metcalfe et al. 2013), San Diego mechanism (2016) (San Diego Mechanism web page, University of California at San Diego 2016), HP-Mech (Yang et al. 2017) and FFCM-1 (Smith, Tao, Wang 2016) as non-PAH mechanisms. Black long broken line shows the mole fraction of measured benzene by a factor of 3.

aromatic hydrocarbons in this situation, all the mechanisms still overestimate C_2H_2 mole fraction especially at moderate equivalence ratio ($\phi \leq 2.0$). This is also obvious from comparison of the computational results with AramcoMech 1.3 (non-PAH) and KAUST, which is based on AramcoMech 1.3. Considering PAH growth decreases the mole fraction of C_2H_2 at high equivalence ratio ($\phi \geq 2.0$) and the reduced amount is in similar magnitude to the threefold value of benzene mole fraction computed with KAUST. Although the PAH sub-set contributes to improving the discrepancy at high equivalence ratio, little effect is observed on prediction of C_2H_2 mole fraction at moderate equivalence ratio. Therefore, this discrepancy is considered to be mainly caused by insufficient modelling in lower hydrocarbon chemistry more than that in growth of aromatic species.

Figure 7 shows results of sensitivity analysis performed for C_2H_2 mole fraction at equivalence ratios of 1.7, 4.0 and 6.0 with Jin and HP-Mech, which shows relatively small C_2H_2 mole fraction among the mechanisms. Top 10 sensitivity coefficients were taken from locations at maximum rate for C_2H_2 production. Reactions with indexes of R_x are presented here for discussion.

For the both mechanisms, hydrogen-oxygen reactions (R_1 , R_2), initial-stage reactions of methane (R_6 , R_8 , R_{10}) and reactions involving C_2H_2 (R_{11} , R_{12}) show high sensitivity coefficients of C_2H_2 mole fraction at moderate equivalence ratio. Hydrogen-oxygen reactions such as R_1 ($H+O_2=O+OH$) and R_2 ($O+H_2=H+OH$) highly affect to other combustion characteristics as well, e.g. laminar burning velocity (See Supplementary Fig. S3 for sensitivity coefficients of the laminar burning velocity of methane at varied equivalence ratios performed with Jin and HP-Mech). R_8 ($CH_3+H(+M)=CH_4+(M)$) was also sensitive to the laminar burning velocity in the both mechanisms as well. Therefore, it seems to be strict to improve the model prediction of C_2H_2 by modifying these reactions. R_6 ($CH_3+HO_2=CH_4+O_2$) shows a negative sensitivity to C_2H_2 mole fraction. The rate constants for

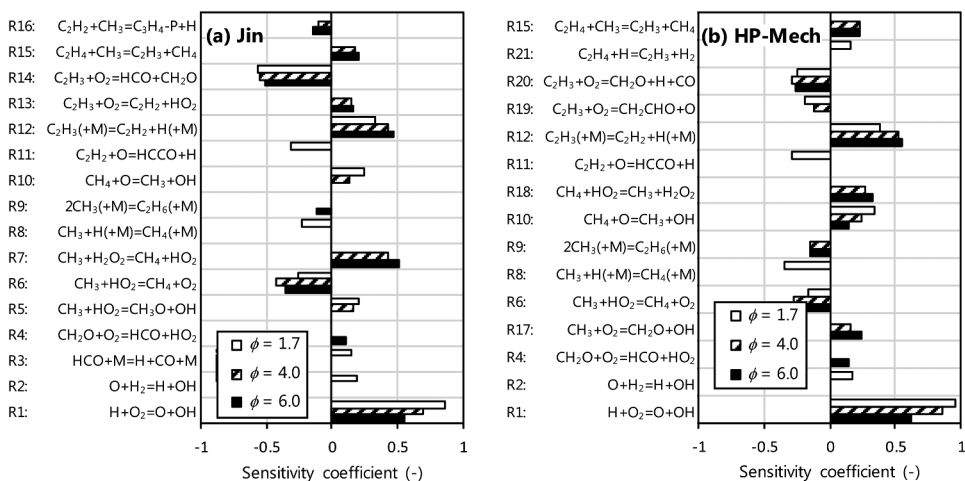


Figure 7. First order, A-factor sensitivity coefficients for C_2H_2 mole fraction at $\phi = 1.7, 4.0$ and 6.0 performed with (a) Jin and (b) HP-Mech. Top 10 sensitive reactions at location of maximum rate of C_2H_2 production for each condition are shown.

R6 obtained from experimental (Hong et al. 2012; Scire, Yetter, Dryer 2001) and theoretical (Jasper, Klippenstein, Harding 2009; Mai et al. 2014; Zhu and Lin 2001) studies included relatively large uncertainty (by a factor of ~ 10 in the former and ~ 5 in the latter) (Onda et al. 2019). Slightly higher rate constant than that used in AramcoMech 1.3, HP-Mech, FFCM-1 and Jin was suggested in (Onda et al. 2019), and the suggested rate constant seems reasonable for the result of sensitivity analysis in this study. R10 ($CH_4+O=CH_3+OH$) has been studied well (Baulch et al. 2005) and difference of the rate constants used in the mechanisms was within a factor of approximately 1.2. R11 ($C_2H_2+O=HCCO+H$) is a main reaction of C_2H_2 consumption competing with $C_2H_2+O=CH_2+CO$. Branching ratio of the two reactions was suggested as approximately 0.8:0.2 with little dependence on temperature (Baulch et al. 2005; Nguyen, Vereecken, Peeters 2006). Similar branching ratios (0.8:0.2) and rate constants (within a factor of approximately 1.2) were used in the most mechanisms except CRECK and San Diego (2016). CRECK used much lower rate constants of the both reactions, therefore, these lower rate constants are considered as one of the factors that led to the significant overestimation of C_2H_2 mole fraction compared to the other mechanisms. However, a rate constant of R11 used in San Diego Mechanism web page, University of California at San Diego (2016) was also lower than that used in the other mechanisms at low to intermediate temperatures. Therefore, in addition to reactions that contribute to consumption of C_2H_2 , reactions that suppress/compete with production of C_2H_2 need to be examined further. R12 ($C_2H_3(+M)=C_2H_2+H(+M)$) was one of those reactions that highly contributes to C_2H_2 production under the current conditions. The high- and low-pressure limit rate constants for R12 reported by (Knyazev and Slagle 1996; Miller and Klippenstein 2004) were in fairly good agreement and were used in the most of the mechanisms. However, other major pathways of vinyl such as reactions of $C_2H_3+O_2$, which compete with the decomposition reaction leading to C_2H_2 , were varied depending on mechanisms. The reactions of $C_2H_3+O_2$ included in each mechanism are shown in Table 1.

Table 1. Reactions of $C_2H_3 + O_2 = \text{products}$ included in the mechanisms.

Products	KAUST	Jin	CRECK	Aramco Mech 1.3	San Diego (2016)	HP-Mech	FFCM-1
R14: HCO+CH ₂ O	✓	✓	✓	✓	✓	✓*	✓
R19: CH ₂ CHO+O	✓		✓	✓	✓	✓*	✓
						✓*	
R13: C ₂ H ₂ +HO ₂		✓	✓		✓	✓*	✓
CH ₂ CO+OH			✓				
OCHCHO+H						✓*	
R20: CH ₂ O+H+CO	✓			✓		✓*	

* Pressure-dependent rate coefficients are used.

The main products of $C_2H_3 + O_2$ were considered as HCO + CH₂O (R14) at lower temperatures and CH₂CHO + O (R19) at higher temperatures (Curran 2019). In addition to these channels, $C_2H_3 + O_2 = C_2H_2 + HO_2$ (R13) was considered as the third significant channel in most of the mechanisms. Although most of the mechanisms include those reactions, it was indicated that the collisional stabilization of $C_2H_3O_2$ competes with R14 and R19 at higher pressure (>10 atm) and that OCHCHO + H and CHCHO + OH (not included in any of the mechanisms) were more significant product channels than R13 (Goldsmith et al. 2015). The pressure-dependent rate constants for $C_2H_3 + O_2$ reactions are considered only in HP-Mech and better if they are considered in the other mechanisms as well. In addition to these reactions, recently studied reactions in C_2H_2 chemistry (e.g. $C_2H_2 + HO_2$ reactions (Gimenez-Lopez et al. 2016)) could be candidates to be updated in the mechanisms. Therefore, it is indicated that reactions related to C_1 – C_2 species need to be further investigated and that improvements of chemical kinetics in lower hydrocarbon chemistry are required for accurate prediction of C_2H_2 especially at moderate equivalence ratio.

Formation of benzene

To investigate formation of benzene for fuel-rich combustion of CH₄, reaction path analysis was performed with KAUST and Jin as shown in Figure 8. Main reaction pathway from CH₄ to C₂H₄ is not shown in the figure because it was identical for both mechanisms. There are mainly three benzene formation pathways: (P1) C₄H_x + C₂H_y reactions; (P2) C₃H_x + C₃H_y reactions; (P3) cyclic species reactions. As examined in Section 4.1, KAUST quantitatively reproduced the measured benzene mole fraction at moderate equivalence ratio ($\phi \leq 3.0$), while Jin reproduced the overall upward trend in benzene mole fraction even at high equivalence ratio ($\phi \geq 4.0$). Formation of benzene will be discussed at two typical cases: $\phi = 2.0$ for the moderate equivalence ratio case; and $\phi = 6.0$ for the high equivalence ratio case.

First, in Figure 8a at $\phi = 2.0$, P1 branches from C₂H₃ reacting with methyl radical. This is an important reaction proceeding to C₃ pathway under large amounts of methyl radical exist (Fahr, Laufer, Tardy 1999). The pathway then proceeds up to C₄ species, which produces benzene by C₂H₂ addition. P2 proceeds through propyne (C₃H₄-P) and propargyl (C₃H₃), which are initiated from C₂H₂ reacting with methyl radical, followed by benzene formation. The reaction pathway of C₃ species is known to be significant for benzene formation (Miller and Melius 1992). However, contributions of these P1 and P2 to benzene formation show only 11% and 10% respectively at moderate equivalence ratio. For benzene formation of KAUST at this condition, P3 is dominant (71% of contribution in total). Particularly, reaction pathway

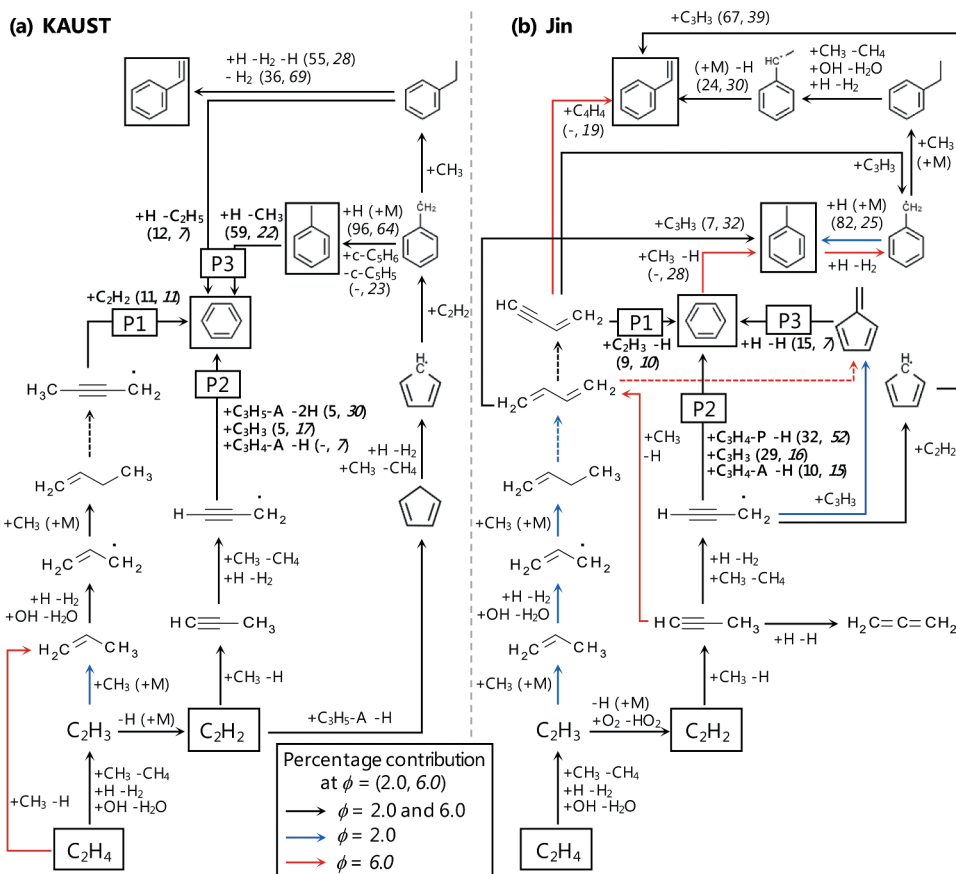


Figure 8. Reaction pathways of benzene formation analysed with (a) KAUST and (b) Jin at a maximum rate of benzene production, and $\phi = 2.0$ and 6.0 . Numbers in parenthesis are percent contribution to production of benzene, toluene and styrene. The measured species are shown in boxes.

which proceeds via toluene marks the highest contribution (59%). P3 proceeds via cyclopentadienyl ($c\text{-C}_5\text{H}_5$) and benzyl ($\text{C}_6\text{H}_5\text{CH}_2$), which play important roles in formation/growth of aromatic species reacting with methyl radicals (Moskaleva, Mebel, Lin 1996; Shukla, Miyoshi, Koshi 2010; Slavinskaya and Frank 2009). In contrast, a dominant reaction pathway for benzene formation in Figure 8b at $\phi = 2.0$ is P2, which shows 71% of contribution. While P3 appears in Jin as well, it proceeds via fulvene, which is different from the one in KAUST, and shows only 15%. This difference is mainly because $c\text{-C}_5\text{H}_5 + \text{C}_2\text{H}_2 = \text{C}_6\text{H}_5\text{CH}_2$ (R22) is not included in Jin, resulting in smaller mole fractions of benzene and toluene than those in KAUST, as mentioned in Section 4.1 (Figure 5).

When R22 was added to Jin as a trial, computational result showed larger mole fractions of the aromatic species than those performed by the original mechanism, and quantitatively reproduced measured benzene mole fraction at moderate equivalence ratio (Supplementary Fig. S4). This was because, as can be seen in Figure 8a, enhancing reaction pathway via benzyl promotes production of toluene and ethylbenzene ($\text{C}_6\text{H}_5\text{C}_2\text{H}_5$), which produces styrene, as well as benzene. As a result, the computed toluene mole fraction showed closer

agreement with the measured mole fraction, while the computed styrene mole fraction slightly overestimated the measured mole fraction. There are, however, other possible pathways for reaction of $c\text{-C}_5\text{H}_5 + \text{C}_2\text{H}_2$ such as subsequence of indene formation through cycloheptatrienyl radical (Fascella et al. 2005), which is not included in the either mechanism. Therefore, close investigation is required to confirm the feasibility of the rate constant of R22 but it was implied that whether including R1 highly affects benzene formation via toluene at moderate equivalence ratio from this trial computation. Considering the overestimation of C_2H_2 at moderate equivalence ratio, it is suggested that improvements of chemical kinetics are required for reactions relevant to P1, which relatively less contributes to benzene formation in this situation, such as $\text{C}_2\text{H}_3 + \text{CH}_3$ reaction (Richter and Howard 2000) as it competes with C_2H_2 production where abundant amounts of methyl radical exist.

Secondly, for the cases of $\phi = 6.0$, it is found that P2 is the dominant pathway of benzene formation for both KAUST and Jin. While P2 in Jin shows 83% of contribution to benzene formation, that in KAUST shows 54%. Even considering relatively high contribution of P3 in KAUST, the proportion of P2 in KAUST is still smaller than that in Jin. This is mainly because $\text{C}_3\text{H}_3 + \text{C}_3\text{H}_4 \rightarrow \text{benzene} + \text{H}$ (R23), which is the most dominant reaction for benzene formation in Jin, is not included in KAUST. Therefore, R23 is considered as one of the factors that caused the different tendency in computed benzene mole fraction between Jin and KAUST at high equivalence ratio mentioned in Section 4.1. Consequently, the discrepancy between measured and computed benzene mole fraction for KAUST is enlarged at high equivalence ratio.

To examine the effect of R23 on benzene mole fraction at high equivalence ratio, a trial computation was conducted by adding R23 to KAUST (Supplementary Fig. S5). It was figured out that adding R23 increased the computed benzene mole fraction but it was still smaller than the measured value by a factor of 1.6, and that detailed improvements of chemical kinetics are required to sufficiently reproduce the measured benzene mole fraction. It should be also noted that there was no significant influence on computed mole fractions of the other measured species by adding the reaction.

Large amounts of CH_3 exist under the current conditions as shown in Figure 9.

Although radicals such as CH_2 and C_2H_3 could also be a candidate that enhance the growth of aromatic hydrocarbons (Liu et al. 2015; Shukla and Koshi 2012), reactions with CH_3 would be significantly of importance in benzene formation from the combustion of fuel-rich methane. One possible pathway to benzene formation, which does not appear in Figure 8, is subsequence of $c\text{-C}_5\text{H}_5 + \text{CH}_3$ reaction leading to fulvene (Moskaleva, Mebel, Lin 1996; Sharma and Green 2009). Jin shows importance in the benzene formation from fulvene: $\text{fulvene} + \text{H} \rightarrow \text{benzene} + \text{H}$ (Jasper and Hansen 2013) (R24), which would be due to high H/C ratio in methane combustion, whereas fulvene formation is included only from C_2 to C_4 pathways. In contrast, KAUST includes the fulvene production channel from $c\text{-C}_5\text{H}_5 + \text{CH}_3$ reaction but does not include benzene formation with R24. Therefore, improvements of chemical kinetics are necessary for better prediction of especially benzene mole fraction at extremely methane-rich conditions, where potentially abundant amounts of methyl radical exist, with further consideration of their impacts on formation/growth of the cyclic species.

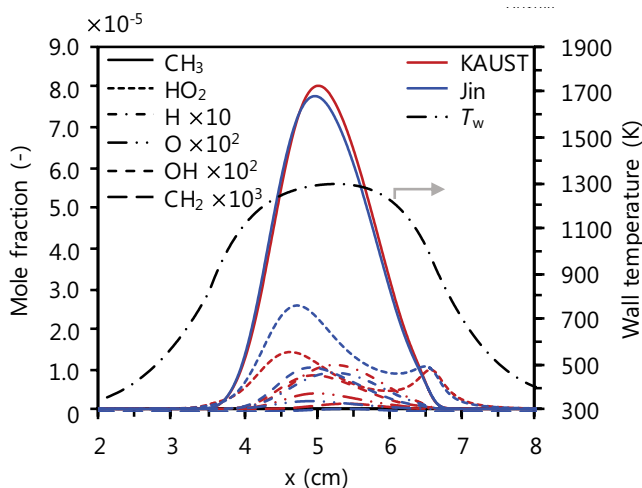


Figure 9. Profiles of typical radicals for CH_4/air mixtures at $\phi = 6.0$ computed with KAUST (red lines) and Jin (blue lines).

Conclusions

Species measurements for extremely fuel-rich CH_4/air mixtures near sooting limit conditions, which were equivalence ratio of 1.7–6.0 (fuel-to-mixture ratio of 15–38 mol.%) and maximum wall temperature of 1300 K, were conducted by using a micro flow reactor with a controlled temperature profile combined with GC/BID and GC/MS. KAUST-Aramco PAH Mech 1.0, Jin mechanism and CRECK mechanism were validated with mole fractions of O_2 , H_2 , CO , CO_2 , CH_4 , C_2H_2 , C_2H_4 , C_2H_6 , benzene, toluene, styrene and naphthalene. Computational results of KAUST-Aramco PAH Mech 1.0 and Jin mechanism reproduced mole fractions of most of the measured smaller species, i.e. O_2 , H_2 and C_1 – C_2 species comparably well, while all the models overestimated mole fraction of C_2H_2 . One- and two-ringed aromatic hydrocarbons (benzene, toluene, styrene and naphthalene) were quantitated in the experiment and mole fractions of those species were found to increase as equivalence ratio increased. KAUST-Aramco PAH Mech 1.0 agreed with measured benzene mole fraction at moderate equivalence ratio ($\phi \leq 3.0$), while it was not able to reproduce the upward trend observed in the experiment at high equivalence ratio ($\phi \geq 4.0$). Although Jin mechanism underestimated benzene mole fraction over the equivalence ratio, it qualitatively reproduced the experimental result. Reaction path analysis of benzene formation performed for the two mechanisms indicated that a reaction pathway via toluene and a reaction of propargyl + propyne significantly affect benzene formation at respectively moderate and high equivalence ratios. There are, however, discrepancies between experimental and computational results of especially benzene as well as C_2H_2 . Therefore, improvements of chemical kinetics with greater attention to methyl radical reactions related to production of C_3 species and production/growth of cyclic species are necessary.

Declaration of conflicting interests

The authors declare no potential conflicts of interest with respect to the research, authorship and/or publication of this article.

Funding

This work was supported by the JSPS KAKENHI Grant number JP16H06068, Japan Society for the Promotion of Science [JSPS KAKENHI Grant number JP16H06068].

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