Old Dominion University ODU Digital Commons

Engineering Management & Systems Engineering Theses & Dissertations

Engineering Management & Systems Engineering

Spring 2014

An Investigation into the Analysis of Truncated Standard Normal Distributions Using Heuristic Techniques

John Walter Ralls Old Dominion University

Follow this and additional works at: https://digitalcommons.odu.edu/emse etds



硣 Part of the Industrial Engineering Commons, and the Operational Research Commons

Recommended Citation

Ralls, John W.. "An Investigation into the Analysis of Truncated Standard Normal Distributions Using Heuristic Techniques" (2014). Doctor of Philosophy (PhD), dissertation, Engineering Management, Old Dominion University, DOI: 10.25777/h3td-q049 https://digitalcommons.odu.edu/emse etds/114

This Dissertation is brought to you for free and open access by the Engineering Management & Systems Engineering at ODU Digital Commons. It has been accepted for inclusion in Engineering Management & Systems Engineering Theses & Dissertations by an authorized administrator of ODU Digital Commons. For more information, please contact digitalcommons@odu.edu.

AN INVESTIGATION INTO THE ANALYSIS OF TRUNCATED STANDARD NORMAL DISTRIBUTIONS USING HEURISTIC TECHNIQUES

by

John Walter Ralls
B.S. December 2001, United States Merchant Marine Academy
M.E.M. August 2005, The George Washington University

A Dissertation Submitted to the Faculty of Old Dominion University in Partial Fulfillment of the Requirements for the Degree of

DOCTOR OF PHILOSOPHY

ENGINEERING MANAGEMENT

OLD DOMINION UNIVERSITY May 2014

Approved by:
C. Ariel Pinto (Director)
Shannon Bowling (Member)
Resit Unal (Member)
Charles Daniels (Member)

ABSTRACT

AN INVESTIGATION INTO THE ANALYSIS OF TRUNCATED STANDARD NORMAL DISTRIBUTIONS USING HEURISTIC TECHNIQUES

John Walter Ralls
Old Dominion University, 2014
Director: Dr. C. Ariel Pinto

Standard normal distributions (SND) and truncated standard normal distributions (TSND) have been widely used and accepted methods to characterize the data sets in various engineering disciplines, financial industries, medical fields, management, and other mathematic and scientific applications. For engineering managers, risk managers and quality practitioners, the use of the standard normal distribution and truncated standard normal distribution have particular relevance when bounding data sets, evaluating manufacturing and assembly tolerances, and identifying measures of quality. In particular, truncated standard normal distributions are used in areas such as component assemblies to bound upper and lower process specification limits.

This dissertation presents a heuristic approach for the analysis of assembly-level truncated standard normal distributions. This dissertation utilizes unique properties of a characteristic function to analyze truncated assemblies. Billingsley (1995) suggests that an inversion equation aids in converting the characteristic functions for a given truncated standard normal distribution to its corresponding probability density function. The heuristic for the inversion characteristics for a single doubly truncated standard normal distribution uses a known truncated standard normal distribution as a probability density function baseline. Additionally, a heuristic for the analysis of TSND assemblies building

from the initial inversion heuristic was developed. Three examples are used to further demonstrate the heuristics developed by this dissertation.

Mathematical formulation, along with correlation and regression analysis results, support the alternate hypotheses presented by this dissertation. The correlation and regression analysis provides additional insight into the relationship between the truncated standard normal distributions analyzed. Heuristic procedures and results from this dissertation will also serve as a benchmark for future research.

This research contributes to the body of knowledge and provides opportunities for continued research in the area of truncated distribution analysis. The results and proposed heuristics can be applied by engineering managers, quality practitioners, and other decision makers to the area of assembly analysis.

This dissertation is dedicated to my wife, family and friends whom have loved and supported me throughout the course of this research process and whose continual encouragement enabled my success.

ACKNOWLEDGMENTS

I would like to thank my dissertation advisors Dr. C. Ariel Pinto and Dr. Shannon Bowling for their support, guidance, and patience throughout the course of this research. Their expertise in their respective fields was invaluable. Additionally, there were several individuals and staff members of Old Dominion University whom have contributed to the successful completion of this dissertation, thank you. I would also like to specifically thank my guidance committee members Dr. Resit Unal and Dr. Charles Daniels for their insights, and professionalism.

I am thankful for the support of my family and for their patience with me as I worked to complete this dissertation. To my wife Lindsey, thank you for your encouragement and support. To my parents Stephen and Laura Ralls, thank you for keeping me on task and for setting the example. To other family members and friends, thank you for enduring with me on this journey.

Finally, I thank God for providing me the strength, discipline, knowledge and perseverance to finish this work and for providing me with the needed support along the way.

NOMENCLATURE

cdf Cumulative Distribution Function

pdf Probability Density Function

Z Standard Score (i.e., z-score) =
$$\frac{x-\mu}{\sigma}$$

USL Upper Specification Limit

LSL Lower Specification Limit

n Sample Size

μ Mean

μ_t Truncated Mean

σ Standard Deviation

σ_t Truncated Standard Deviation

 σ^2 Variance

 σ_{t}^{2} Truncated Variance

x A Random Variable

 $\varphi(t)$ Characteristic Function

∞ Infinity

α significance level

Note – This nomenclature list provides a representative sample of nomenclature used within this dissertation. The scope of this dissertation is not intended to include general, referenced, or other nomenclature common to this field. Please refer to applicable references for nomenclature details beyond the scope of this work.

TABLE OF CONTENTS

	rage
LIST OF TABLES	x
LIST OF FIGURES	
INTRODUCTION	
1.1 Problem Statement	
1.2 Research Questions	
1.3 Research Contributions to the Body of Knowledge	3
BACKGROUND OF THE STUDY	5
2.1 Literature Review Overview	
2.2 Assembly Selection and Applications	9
2.3 Assembly Analysis	13
2.4 Heuristics, Frameworks, and Other Methodologies	
2.5 Research Hypotheses	41
METHODOLOGY	42
3.1 Research Method Overview	
3.2 Comparative Review and Research Gaps	
3.3 Truncated Standard Normal Distribution Analysis	
3.4 Hypothesis Testing	
RESULTS	58
4.1 TSND Analysis Results and Heuristics	58
4.2 Hypothesis Testing Results	58
4.3 Simulation Examples	61
CONCLUSIONS AND RECOMMENDATIONS	63
5.1 Research Question Conclusions	
5.2 Research Assumptions and Limitations	
5.3 Future Research Opportunities	
REFERENCES	70
APPENDICES	92
APPENDIX A: EQUATIONSAPPENDIX B: TSND ANALYSIS RESULTS	92
APPENDIX B: TSND ANALYSIS RESULTS	96
APPENDIX C: CORRELATION AND REGRESSION ANALYSIS	
APPENDIX D: TSND ANALYSIS EXAMPLES	165
APPENDIX E: CATEGORIZATION INFORMATION	
APPENDIX F: LITERATURE REVIEW VARIABLES	
APPENDIX G: CATEGORIZATION AND COMPARATIVE ANALYSIS	
APPENDIX H: RESEARCH HYPOTHESIS H ₃ TESTING RESULTS	200
APPENDIX I: HEURISTIC - TSND BASELINE USING CF INVERSION	226

P	age
APPENDIX J: HEURISTIC - TSND ASSEMBLY USING CF INVERSION	229
VITA	233

LIST OF TABLES

Table	Page
B.1 – TSND Analysis Results	97
C.1 – Pearson Correlation for ft(z) - ASSY, fT(z) - standard	100
C.2 - Pearson Correlation for ft(z) - ASSY, fT(z) - adju stdev	101
C.3 – Pearson Correlation of Analysis Ratios	102
C.4 – Regression Analysis for ft(z) - ASSY, fT(z) - standard	103
C.5 – Regression Analysis for ft(z) - ASSY, fT(z) – adju stdev	104
D.1 – Truncated Distribution Simulation Range, 10,000 Samples (-2 to 2)	166
D.2 – Pearson Correlation of Example 1	166
D.3 – Regression Analysis of Example 1	166
D.4 - Truncated Distribution Simulation Range, 10,000 Samples (-3 to 3)	169
D.5 - Pearson Correlation of Example 2	169
D.6 – Regression Analysis of Example 2	169
D.7 – Truncated Distribution Simulation Range, 10,000 Samples (-4 to 4)	172
D.8 – Pearson Correlation of Example 3	172
D.9 – Regression Analysis of Example 3	172
F. 1 – Literature Review Table	181
G.1 - Comparative Review Results Heuristic Type/Benchmark Method	194
G. 2 - Comparative Review Results Heuristic Type/Test Method	195
G.3 - Comparative Review Results Sel. Assy, Heuristic Type, Data Source	195
G.4 - Comparative Review Results Test Method	197
G.5 – Comparative Review Truncation and Data Source w/Heuristic	197

Table	Page
G.6 - Comparative Review Optimization Techniques	198
G.7 – Categorization Table from Comparative Review	199
H.1 – H3 Hypothesis Pearson Correlation of fT(z) and ft(z) - CF	219
H.2 – H3 Hypothesis Regression Results of fT(z) and ft(z) - CF	219
H.3 – H3 Hypothesis Test Summary Table	220

LIST OF FIGURES

Figure		Page	
1.	Literature Map	8	
2.	Research Process Overview	43	
3.	Comparative Review - Selective Assembly/Heuristics/Truncation	48	
4.	Comparative Review Heuristics/Benchmarking/Truncation	48	
5.	Comparative Review - Heuristic Type & Testing Methods	49	
6.	Comparative Review – Testing Methods & Truncated Assembly	49	
7.	Comparative Review - Heuristic Data Sources of Truncated Assembly	50	
8.	Heuristic - Analysis for Truncated Standard Normal Distribution	52	
9.	Truncation Assembly Level Example (Simplified)	53	
10.	TSND Assembly CF Inversion Heuristic	53	

CHAPTER 1

INTRODUCTION

1.1 Problem Statement

Engineering, manufacturing, financial analysis, risk management, insurance and numerous other industries deal with assembly relationships when assessing their specific areas of interest. Whether that area of interest deals with the assembly of machined parts having an upper and lower specification, financial and portfolio analysis, or analysis variables affecting insurance (e.g., weather conditions, location, age, risk factors, etc.), these areas deal in assessment of truncated standard normal distributions. Numerous probability distributions have been utilized across these fields to accurately describe phenomena readily seen in typical, everyday occurrences.

Research in truncated standard normal distribution assemblies is lacking. As a result, heuristics and analysis methods are limited or non-existent, and the practical application of data or tools in this field is not readily identifiable. The use of the assembly-level truncated standard normal distributions have particular relevance when bounding data sets, evaluating tolerances, identifying quality measures, and for decision makers. Also lacking are assembly-level truncation tables for varying assembled truncated standard normal distributions for two pair combinations.

While an assembly may have numerous parts, the subassembly portions can generally be simplified and reduced to a manageable size. In their simplest form assemblies should be able to be reduced into at least two parts. Therefore, one of the initial problems addressed by this research is focused on providing decision makers a

heuristic to analyze the assembled truncated standard normal distributions for two parts.

This research question and others are presented in the next section.

1.2 Research Questions

This research is designed to address the following questions:

- 1. What are the research gaps relative to truncated standard normal distribution analysis and is there an opportunity to address a portion of these gaps?
- 2. Does the analysis of two truncated standard normal distributions (i.e., assemblies) provide a quality indicator and/or an enhanced understanding of characteristics of truncated distributions with respect to assemblies?
- 3. To what extent can heuristic techniques be employed to aid in truncated standard normal distribution analysis? What relationships can be inferred from the analysis of truncated standard normal distributions?
- 4. Can qualitative or quantitative data sets be developed to assist decision makers and/or quality practitioners with an enhanced understanding of truncated standard normal distributions (single and assemblies)?
- 5. Will correlations, goodness-of-fit, or other testing methods provide meaningful data from truncated standard normal distribution (single and/or assemblies) and other known distributions?

1.3 Research Contributions to the Body of Knowledge

This research addresses important gaps in the body of knowledge including:

- A lack of understanding related to the distribution characteristics resulting from the assembly of two truncated standard normal distribution (e.g., final assembly characteristics between two piece parts for identical TSND).
- A lack of heuristics or other methods/frameworks for engineering managers,
 quality practitioners and other decision makers.
- The characteristics/relationships between assembled parts utilizing truncated standard normal distributions (e.g., via correlation and regression analysis).
- Qualitative or quantitative data often found in quality tables or other properties for truncated standard normal distributions (using characteristic functions).

This research contributes to the body of knowledge by:

- Providing a practical heuristic based method for characteristic function inversion of a single doubly truncated standard normal distribution.
- Providing heuristic and mathematical formulations associated with assemblylevel truncation between at least two distributions.
- Providing an approach to the assembly-level truncated standard normal
 distribution analysis through the inversion of the distributions assembled
 characteristic function. This approach provides an alternative method for
 engineering managers, quality and other practitioners to analyze and respond
 to process variation decision making.

- Expounding on the relationship between truncated standard normal
 distributions and their assembly using empirical analysis methods (e.g.,
 mathematical formulation, characteristic function evaluations, heuristics, etc.).
- Providing decision makers and quality practitioners with qualitative and quantitative data for analysis of data sets using truncated distribution assemblies.
- Providing observations and evaluations relative to the additive relationship of truncated distributions (e.g., graphical, by inspection, etc.).
- Providing correlation and regression analysis results for a given truncated standard normally distributed sub-assembly and a truncated final assembly.
 These forms of analysis aid in identifying relationships between the analyzed distributions.

CHAPTER 2

BACKGROUND OF THE STUDY

2.1 Literature Review Overview

An extensive literature review was performed in the following primary areas of research: truncated distributions, selective assembly, heuristics, and assembly sequencing. The review is primarily centered on my interest in assembly and design. Specifically, this research interest included a review of methodologies that could be utilized by an engineering manager, quality practitioner, or other decision maker. While researching these topics it became evident that assembly methods and sequencing spanned multiple interdisciplinary fields with numerous secondary areas of consideration for this research topic. The primary areas of research that were examined dealt with applications that were associated with assemblies and decision making.

Secondary areas of literature review included tolerance design, optimal target setting, extreme value theory (EVT), storage management systems, inventory management systems, and a limited review of simulation methods. These secondary areas of investigation are addressed in limited capacity in this literature review and provide context and application insight to this research.

Hart (2005) states that research can generally be classified according to its design features and its intended outcomes. Hart (2005) also identifies that the literature review is important because without it you will not acquire an understanding of your topic. The literature review aided in the completion of a comparative review of scholarly works to assess research gaps and to gain insight into TSNDs and other areas of application.

Hart (2005) described the following research techniques which were utilized as part of this dissertation:

- Construction of parameters for the review topic (e.g., literature mapping)
- Identification of issues in research design (e.g., research gap analysis)
- Identification if an approach for the literature review process
- Presentation of methods, fallacies in arguments, and/or identification of other aspects for the literature review process.

The literature review for this dissertation began its focus in three main areas with the purpose of identifying knowledge gaps. The initial focus of my review was on assembly selection and sequencing techniques. Findings from that review were generally reduced to two major areas: assembly selection/sequencing/systems (i.e., physical methods) and applications (i.e., industrial and/or academic application). That review identified and assisted in bounding the context and scope of this research.

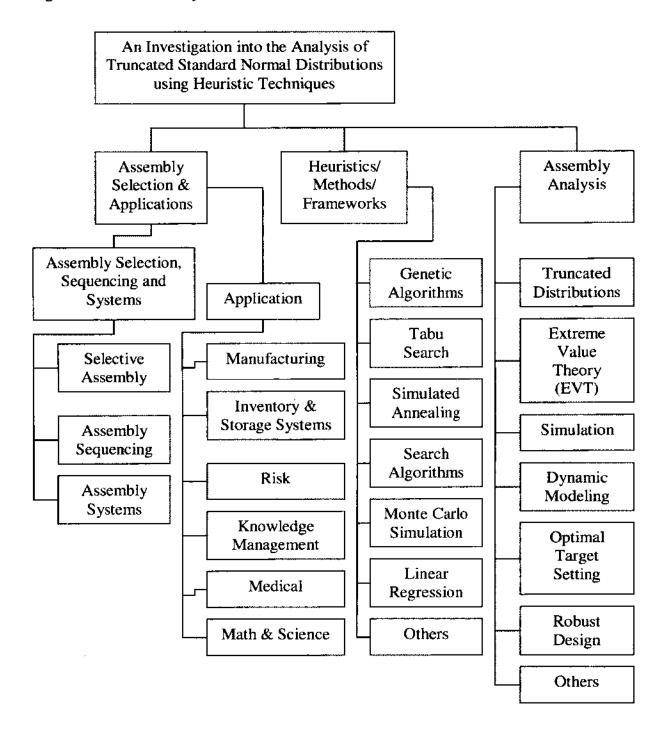
Given the interrelated nature of the literature review the second main area for my review involved the evaluation of heuristics/frameworks/methods used as part of assembly selection. The primary reason for this was to identify decision making, sequencing, or other methods that have been used in various applications and to identify predominant methods used in assembly assessments.

Finally, the most extensive portion of my review and a significant portion of this research centered on the analysis of methods associated with assemblies. The primary focus of this research being with truncated standard normal distribution and their analysis. Secondary insights revealed numerous other analysis methods such as dynamic modeling, EVT, simulation, and robust design techniques.

The literature review identified that a knowledge gap exists relative to the relationship associated with the assembly of truncated portions of standard normal distributions. It also identified the applied use of the characteristic function as a means to determine the probability density for a truncated standard normal distribution. Additional gaps exist relative to comparative analysis of truncations, approximation methods, heuristics and application methods were also evaluated. The literature review that follows identifies a breakdown and high-level review of an extensive sample of scholarly works from this field.

An overview of the literature mapping performed for this dissertation is shown in Figure 1. The research method for this work is addressed in Chapter 3.

Figure 1: Literature Map



2.2 Assembly Selection and Applications

2.2.1 Selective Assembly, Sequencing, Systems and Applications

Work in the area of subassembly design information appears to be very limited.

Selective assembly appears to be the predominant literature available regarding assembly selection design. Several works initially appeared to be relevant or near relevant to this field of research, they are:

Whitney (2005) was identified as a scholar in the area of mechanical assemblies. This work is comprehensive and describes the methods of designing workstations and systems for assemblies. Whitney's work provided some insight in subassemblies but focused primarily on mechanical assemblies, part interrelationships, assembly sequencing, design for assembly techniques, and product architecture. The utility of this work in this dissertation came in the form of general assembly insight and enhanced understanding of mechanical assemblies.

Kannan and Jayabalan (2001) proposed a method for lot partitioning using selective assembly groups. They also examined an example of three mating parts with different standard deviations and provided steps for group tolerances of these assembled parts. This particular work did not address assembled parts or associated truncation analysis addressed by this work.

Selective Assembly is a means by which high-precision assemblies may be fabricated from relatively low precision components (Pugh, 1986). In Pugh's conference preceding on the partitioning of selective assembly he introduces the idea of partitioning a component population into groups prior to random assembly. Later Pugh discusses how these selective assemblies can be used to assemble components that could not meet

specifications if they were not selected in such a fashion. Pugh (1986) indicates that selective assembly works by dividing component distributions into two or more groups, randomly choosing components and limiting their group creation by discarding groups beyond three standard deviations.

Cittolin (1997) used filter and assembly sequencing methods to group and sequence assembly combination. Review of this literature was limited to applications of methods dealing with the selection of relevant possibilities associated with assembly sequencing minimization. This study did not address truncations. The paper also compares its approach with other methods.

Pugh (1992) identifies the use of statistical selective assembly as a means to produce high-precision assemblies from relatively low-precision components. Pugh (1992) also elaborates on the random selection of components from with a group assembly as a means to meet specification when a group of components has a high variability. In this paper Pugh discusses the systematical truncation and normal distributions in addressing component distributions. Other author such as Desmond and Setty (1961) and Mansoor (1961) have also provided input with regard to selective assembly. Selective assembly partitioning (e.g., truncation) was identified as a primary area of consideration within this dissertation.

In 1994, Malakooti's study identified that one of the problem's in design of assembly line balancing (ALB) dealt with the allocation of work elements. This problem was termed assembly line balancing and specifically documents that the failure of workstations and other unforeseen circumstances can result in unnecessary idling of the production line. This particular study addresses aspects of ALB through the use of single

and multiple decision making criteria which included quantities of stations, buffer size, cycle time, and total cost of operation. Assembly line balancing has potential applications of truncation analysis with assemblies. In this work Malakooti also provides several examples with computational experiment results. As a result, it can then be inferred that an applications of truncation analysis toward this knowledge gap would support improvements in the area of assembly line buffering.

As a contrast to Malakooti, Lee 1994 presents a method for the automatic generation of assembly sequencing. Lee's work states that by adjusting the assembly coefficients of subassembly selection indices according to a given assembly environment, an optimal assembly sequence can be generated. Truncation analysis application in the area of assembly planning was not identified by Lee.

So and Scott (1994) studied a production control model for a product comprised of matching components (i.e., a heart valve). The study addressed aspects of part assemblies assuming "N" possible categories. In their study So and Scott identify high level concepts of assembly but did not include aspects or discussion of truncation, EVT, or other specific work assembly methods. A greedy heuristic sequencing rule for other general cases was used by the authors.

Whitney (2006) identifies key characteristics associated with mechanical assemblies, data flow chains and tolerance analysis. His research focuses on utilizing key characteristics for conveying design intent. Whitney (2006) focused on complex assemblies at the design level.

In 2007, Lee and Shin presented a method for the automatic determination of assembly partial orders from a liaison graph representation. This work identified an

approach for the extraction of subassemblies. The application of this literature to this dissertation was limited to knowledge gap identification and insight into industry assembly and subassembly methods. Additionally, Agard and Kusiak (2004) utilized data mining algorithms for the selection of subassemblies. Neither of these works appeared to address the knowledge gap addressed by this dissertation.

Kwon, Kim, and Chandra (1999) identified a selective assembly procedure for components composed of two mating parts. While this product focuses on product clearance, the focus of this research dealt with component characteristics of a normal distribution with equal variance. This study presented limited application to truncated portions or assemblies.

De Fazio, Rhee and Whitney (1999) presented an assembly sequence analysis (ASA) for applications involving design-for-assembly (DFA). The paper detailed subassembly partitioning based on criterion based searches. The paper also identified genetic algorithm search techniques for us in assembly sequencing.

Abe, Murayama, Oba, and Narutaki (1999) reviewed part removal verifications associated with disassembly sequences related to assembly planning systems. Their research focused on reducing verification times associated with subassemblies. As part of their research, they employed a genetic algorithm and heuristics to aid in the generation of assembly sequencing. While not specifically focused on truncation assembly analysis, Abe et al. (1999) provided application insight and documentation of industry use of heuristics as part of subassembly analysis.

Lee and Saitou (2007) presented a systematic approach to early product design in order to achieve a cost-effective design. Their work identified that critical dimensions

were adjusted through subassembly partitioning as part of the assembly process. The paper also identified that a genetic algorithm was used in selection processes. The application of this literature to this dissertation was limited to knowledge gap identification and insight into assembly sequencing. Truncation analysis methods presented in this work could potentially be applied in this area.

2.3 Assembly Analysis

2.3.1 Truncated Distributions

Work in the area of truncated distributions continues to progress. Research and studies in this area aid quality practitioners, engineers, and decision makers in multiple fields. For example, Johnson and Thomopolous (undated) presented reference tables for use by works for left-truncated normal distributions. Similarly, Khasawneh, Bowling, Kaewkuekool, and Cho (2005) presented greater detail on Truncated standard distributions for singly truncated and doubly truncated cases in two separate scholarly works. In another work Johnson and Thomopoulos (undated) provided a slightly different approach toward addressing an approximation method for doubly-truncated cases using a computer model. None of these works utilized a distributions characteristic function or addressed assembly level distribution approaches.

Dhrymes (2005) developed the moments of truncated distributions in dummy endogenous variable models. An interesting aspect of this study to this research was the approach to normalization of a truncated distribution used within the study. Dummy endogenous variables were also used to address the mean and variance of the distribution.

Finally, the author formulated theoretical equations for determination of the moments of truncated distributions.

In a study in 2003 Ostermeier examined incremental truncations as a method for pairing DNA. As part of this literature review a myriad of industries were included for relevant aspects of truncation and assembly, in this case DNA. A Key point made in this scholarly work was that the experimental determination of the distributions used would require extensive, cost-prohibitive, sequencing. Additionally, the author examined the use of incremental truncation libraries and also a uniform distribution of truncation lengths. The author also provided a comparative review of different truncation methods along with comparison of different DNA truncations.

Horrace (2005) formalized analytical results on the n-dimensional multivariate truncated normal distributions. His paper focused on one-sided truncations at arbitrary points and provided results related to linear transformations along with supporting proofs and mathematical theory. The application of this document was directed toward the field of economics. The specific application of Horrace (2005) to this research was with respect to the comparative review and research gap identification support.

2.3.2 Characteristic Functions and Inversion Theorems

A literature review in the area of Characteristic functions and their inversion was the result of the EVT study. As part of this review the details related to a distributions characteristic function were identified. Relevant equations from this review are identified in Appendix A. Billingsley (1995) provided over-arching support for both characteristic functions and general inversion principles. S. Sheffield (2011) amplified the work

provided by Billingsley (1995). Abadir and Magdalinos (2002) provided specific insight into the characteristic function of a singly doubly truncated normal distribution and applications.

Shephard (1992), Kawata (1969), Bernadic and Candel (2012), and Abate and Whitt (1991) provided examples for the application and inversion of a Characteristic function. Inversion principles in these references along with inversion formulas identified by Billingsley (1995) were utilized in Appendix A and adapted for the evaluation of assemblies. Billingsley (1995) and S. Sheffield (2011) identify that characteristic function for the sum of two characteristic functions is the product of their respective characteristic functions (i.e., similar to moment generating functions).

2.3.3 Extreme Value Theory (EVT) and Value At Risk (VaR)

Castillo, Hadi, Balakrishnan, and Sarabia (2005) provided overarching insight in the area of Extreme Value Theory. Use of this resource with a sampling of journal articles and other literature enabled knowledge gap identification and served as grounding for technical fundamentals in the area of truncated distribution analysis (i.e., through principles identified in scholarly reviews regarding EVT).

Raschke (2012) examined right truncation exponential distributions and an estimator for finite sample sizes of truncation points. Raschke also introduced the use of an inverse mean squared error to evaluate the estimator's behavior. Raschke comments on EVT as it relates to truncated distributions as it relates to sample size. Monte Carlo simulations and examples were used by the author to examine different truncation points and sample sizes.

Blanchet and Liu (2012) introduced change of measure techniques for rare-eventanalysis of heavy tailed. Monte Carlo simulations were used by the authors to aid in the estimation of rare event probabilities and to present a "good" Markovian approximation of conditional distribution of the rate event being analyzed.

Kuwahara and Mura (2008) used a weighted stochastic simulation algorithm (SSA) and a Monte Carlo simulation method to analyze rare events of biochemical systems. Case studies are used to analyze the proposed method and effectiveness along with an explanation of the proposed algorithm using weight (SSA).

Drees et al. (2005) estimated the far tail portions of distributions functions using EVT as a framework. The authors developed weighted approximations to the tail of the distribution and other empirical data. An Anderson-Darling type test of the null hypothesis was used to demonstrate that the distribution belongs to an EVT domain of attraction.

Using Monte Carlo experiments Stoyanov and Rachev (2007) reviewed the impacts of tail behavior for varying sample sizes (in addition to value-at-risk). The effects on the tail distributions were further analyzed along with the convergence rate as part of their analysis. The authors concluded that a simple tail truncation improves the convergence rate and that asymptotic distribution reliability improves with large sample sizes (e.g., 5000+) for specific cases.

Peng and Qi (2009) studied maximum likelihood estimates of extreme value indices between -1 and -1/2. They also generalized irregular cases and cases of an unknown extreme value index. Peng et al. (2009) in addition to Chavez-Demoulin and Roerhl (2004) provided a general overview on the understanding and application of EVT.

Bermudez and Kotz (2009) examined varying methods for the use of the generalized Pareto distribution (GPD) and their application to estimation methods. This literature focused on applications to EVT and its approach was to review and identify options of GPD parameter estimation. The first paper focused on methods such as maximum likelihood (ML), method of moments (MOM), and probability weighted moments (PWM). The second paper (a continuation) focused on the application of methods to real world data.

Brazauskas and Kleefeld (2009) proposed a method for fitting generalized Pareto distribution (GPD) associated with trade-offs between robustness and efficiency. Using a "trimmed moments" method as a basis the authors used simulations and their method to fit GPD to historical data. Utility was provided following application to areas of risk measurement and ratemaking. The authors utilized a large sample size to provide a mean and relative efficiency between various methods.

Carpinteri, Cornetti, and Puzzi (2005) used extreme value theory in the form of a statistical model to evaluate materials. Prior comparisons using EVT and a Multi-Fractional Scaling Law (MFSL) are used in their evaluation. A model and correlation between for their area of interest is drawn (e.g., fracture energy and crack surface parameters). The authors further used experimental data available in literature to confirm their approach. The utility of this work toward this dissertation was relative to problem solving and decision making approaches.

Brooks, Clare, Dalle Molle, and Persand (2005) examined various EVT models for VaR. The authors used GPD, ML and a semi-nonparametric methodology in their reviews. Comparative analysis was performed by the authors including nonparametric

tail index estimates of GPD threshold levels. The relevance of this literature to this dissertation was in application and understanding of sample and comparative approaches. Simulation was further used in data analysis as part of the authors approach.

Debolt, Guillou, and Rached (2005) used a generalized probability weighted moment method (GPWM) to study the asymptotic behavior of estimation tools presented. The authors provided proofs and generalized weighted moment estimators. This work was used in conjunction with Bermudez and Kotz (2009) to better understand research gaps that exist in assembly methods. An understanding of the extremes was intended to better support an understanding of TSNDs.

2.3.4 Simulation

Yanoff and Weirich (2010) discuss the philosophical and epistemological implications of simulation, simulation representation, and policy decisions. The paper argued that simulation is "an important new tool for the social sciences" and that simulation "shares features with both models and experiments." The key purpose of review of this literature was in expanding my breadth of knowledge in the philosophical approaches that could be applied to this research.

Bradley and Gupta (2004) analyzed data associated with the sum of "n" independent non-identically distributed uniform random variables. In this work the authors use Fourier theory to derive an explicit formula for this approach by inverting the characteristic function. This research is one example associated with approaches used in the summation of a uniform distribution. However, no research has been identified in the areas of TSND assembly analysis using characteristic function inversion heuristics.

In a 1999 study Kosfeld and Quinn evaluated storage and retrieval system strategies to improve production throughput capabilities. The study identified that the use of simulation models allowed prioritization and performance prediction for different strategies. From the proceedings of this winter simulation conference, the authors addressed a method of locating empty bins for storage in order to increase throughput. Although, this research did not address subassemblies it did address storage system modeling and throughput. The study base lined simulations using known parameters to benchmark their model. The study then performed throughput simulations to estimate performance improvement from their methods. These approaches were considered when developing the research approach for this dissertation.

Bates, Buck, Riccomagno, and Wynn (1996) identified experimental design and modeling as part of optimization and sensitivity analysis of large systems. The study provides an example for simulation (i.e., emulation) in large system analysis.

Breedis (2001) presented a simplified approach to subassembly design using Monte Carlo analysis. The primary focus of this review was on the author's methods and problem approach. The study identified key variables for evaluation of the simulations performed.

2.3.5 Dynamic Modeling

Dynamic Variation Reduction was developed by R. Musa (2007) as part of a dissertation relating to strategic and dynamic variation reduction for assembly lines.

Musa (2007) proposed a method to reduce variation for assemblies by developing inspection plans based on:

- Historical data for existing products, or simulated data for newly developed products
- Monte Carlo Simulation and Optimization Search Techniques
- Sought to minimize the cost function for the total of inspection, rework, scrap,
 and failure costs

Musa's research developed methods to utilize data in near real time to dynamically reduce variation by assigning the inspected subassembly parts together and he also proposed mating inspected subassembly items through the use of dynamic rolled yield throughput maximization (DTM). Musa (2007) also proposed heuristics for inspection based DTM.

Musa, Sturges, and Chen (2006) identified an inspection methodology for inspection planning using CAD data and simulation. The author proposed a methodology for out-of-tolerance quality characteristics for subassembly. Monte Carlo simulation was used as part of their model development.

Musa and Chen (undated and 2006) presented work on a dynamic throughput maximization study performed after inspection of a batch of subassemblies. This work presented the authors' approach using meta-heuristic algorithms. The study also compared ant colony heuristics to simulated annealing (SA) algorithms. The primary focus of this review was toward a review of the heuristic application used in subassembly design.

Musa, Chen, and Ghoniem (undated) extended previous work from Musa et al. (2006) regarding dynamic variation reduction and throughput via development of a

mathematical part matching model for variation reduction. In this study the authors propose a 3-rule heuristic and another model for throughput maximization.

Huang, Liu, and Musa (2004) proposed a method for process plan evaluation to provide rapid evaluation for process plan decision making. The authors approach uses Monte Carlo simulation to aid in the analysis through analysis of deviations assuming normal or uniform distributions. This research did not address truncated distributions or their assembly.

Das and Sarin (1988) used a dynamic programming approach along with a heuristic procedure to address part arrival dates in a multi-job stochastic assembly system. Application of this literature was limited to review of the heuristic approach by the authors.

Seidmann and Tenenbaum (1994) developed a dynamic part-allocation policies for a Flexible Manufacturing System (FMSs) having finite storage capacity. The paper evaluates modeling approaches to evaluate part-routing policies. Additionally, several closed-loop heuristic policies were proposed and provide near optimal FMS performance results. This journal article was examined for application to truncation analysis and part allocation.

Gutierrez, Hausman, and Lee (1995) studied a matching problem and dynamic control rules relative to optimal system performance. The authors proposed a heuristic and provided examples of performance improvements relative to their proposed heuristic. The authors identified a computationally infeasible dynamic programming formulation along with a myopic control procedure for general application to sorting and matching problems.

Selection techniques for a dynamic model framework along with alternative model framework for multistage stochastic programming models were reviewed (Puelz, 2002). The author used empirical test from historical data to benchmark the framework.

2.3.6 Robust Design

Carlson and Doyle (2002) studied aspects of robust design and complexity dealing with highly optimized tolerance (HOT). This particular study focuses on highly structured and robust designs. This work also performed a comparative review by leveraging examples and model systems.

In a 2001 study by Caleb Li and Chou the optimal process mean and associated variables were identified to aid in minimizing the expected quality loss for the works identified parameters. The variables considered by these authors were those quality characteristics typically associated with quality (e.g., smaller-the-better, nominal-the-best, etc). The approach examined direct and indirectly measurable quality characteristics.

2.3.7 Optimal Target Setting

This dissertation reviewed the area of Optimal Target setting for general oversight and applicability to TSNDs. In general the techniques used in optimal target setting could have applicability at the application level. The following articles and summaries expand current knowledge in the area of optimal target setting:

Bouchard, Elie, and Imbert (2010) studied Markovian optimal stochastic control problem under stochastic target constraints. The direct approach was merely reviewed for applicability and bounding of the research gap from this dissertation.

In Yang, Gui, Kong, and Wang (2009) the authors present a quality prediction model for optimal-setting control of a manufacturing process in a metallurgical industry. Yang et al. (2009) identifies the use of a kind of hierarchical strategy for determination of an optimal set point for raw material portioning. The authors compare the efficiency improvement to an example system in an alumina smelting.

In 2003, Bai and Kwong studied the use of target setting values and heuristics to develop "inexact" optimal target settings. In this particular approach the authors utilized a fuzzy optimization model for target value determination and an inexact genetic algorithm was used to solve the problem. Both heuristics and optimal target setting were used as part of this work.

Ohtsubo (2004) evaluated risk minimization for Markov decisions with a target set. Ohtsubo's study considered the risk associated threshold probability along with the passage time for a target set. The paper also identified the use of value iteration methods and presented a policy improvement method (e.g., a heuristic).

Kim, Michekena, and Papalambros (2003) used target cascading to model a multilevel optimization problem. The authors utilized design targets (cascaded to lower levels) by partitioning their problem into small sub-problems. The authors then formulated an optimization model to minimize deviations from their propagated targets. While the authors do not specifically cite the use of heuristics or a specific simulation technique the authors presented a coordination strategy (e.g., essentially a heuristic) to address their problem. The authors took steps toward simplification of their models (e.g., smaller model structures) and to reduce their model and analysis complexity.

Krzysztofowicz (1990) presented a critique of a target setting problem with exponential utility. The framework of this critique was reviewed in consideration as part of this dissertation. The utility and reason for review was primarily with respect to the application and decision steps/considerations as part of the problem formulation and analysis.

In a 2006 work Cooper, Georgiopoulos, Kim, and Papalambros utilized "analytical target setting" to perform target setting within the context of an enterprise.

The paper addresses a partitioned decision making process. The paper was reviewed as part of an introspective approach for the comparative review and heuristic development for this dissertation.

Huang, Cheung, and Liang (2006) utilized a multi-agent system to solve for optimal design using analytical target cascading. This approach and methodology was cited as having gained more ground as a methodology for an optimal design approach. The primary use of this literature was to identify other gaps and approaches which may lend insight into the research gaps from this dissertation.

Li's (2004) research focused on optimal manufacturing settings to minimize quality loss for the identified production system. The author's work found that the use of smaller tolerances for both sides or adjustment of the process mean were unsuccessful at minimizing the quality loss. The author also used a pokayoke procedure and truncated quadratic loss function to solve the solution when setting the process mean at an optimal point to minimize the expected quality loss.

Bisgaard (1997) explored the experimental determination of tolerance limits of mating components of an assembled product. Bisgaard provided a functional approach for setting tolerances in assembly when applied to high-volume products. The research concluded that the application may be reasonable for setting tolerances when the data can be reasonably amortized or in higher risk applications. It is important to note that while this study did address tolerance design it did not address the use of truncated distributions in any aspect of its application.

Ramirez-beltran (1995) demonstrated a real-world application of an integer programming problem. The focus of this study was on finding an optimal solution for a labor cost problem. The paper utilized a matrix method for optimization and a branch and bound heuristic algorithm. The author utilized a numerical example to demonstrate the utility of the method (and its effectiveness).

Baykasoğlu (2001) used mathematical programming tools to model multiple objective optimization problems. Baykasoğlu's study cites a trend in industry to solve these types of mathematical problems using heuristic optimization techniques (e.g., Tabu search, genetic algorithm, and simulated annealing). A multi-objective Tabu search heuristic was proposed in this study and results presented demonstrate the proposed heuristics utility.

Nussbaum, Sepúlveda, Singer, and Laval (1998) studied approximation methodologies for sequencing and resource allocation problems. The authors presented a declarative problem solving framework for specification and sequencing problem solving. A focus of this study was on optimization heuristics and procedures and their parameterization.

2.3.8 Other Methods and Applications

Mease, Nair, and Sudjuanto (2004) described a statistical formulation for determination of optimal binning strategies for various loss functions and distributions and compare the results to heuristics. This research provides direct insight into the knowledge gap existing among truncated distribution along with binning and quality applications that could be applied in future expansion of the research presented by this dissertation.

Moorhead and Wu (1998) addressed parameter design methodology by developing a model and data-analysis strategy for a general loss function. The authors presented a methodology that utilized a location-scale model and their study cited approximation as a form of utility in substantiating their model performance. The authors also identified that the utility of their method extended the scope of parameter design of nominal-the-best to include a more general loss function (including subjective interpretation of improved generality).

Xiaoping and Jingjing (2009) presented a model and algorithm for evaluation storage bins for a transport problem. Binning applications have relevance to assembly techniques and the case study presented by this work utilized existing (known) outcomes to approach the idea of storage bin availability improvement. In Xiaoping and Jingjing (2009) also studied the control of optimization methodologies related to storage bin capacity in transport problems. Relevance of these papers to this dissertation was primarily in approaches used for identification and review of the heuristic.

Zhu and Oommen (1997) studied a problem in which a detection function was used to evaluate an object with "N" locations (bins) for the purpose of maximizing

resource allocations. One of the main observations from this study is that the target distribution is assumed to be unobservable, where as prior research focus on known target distributions. The relevance of this is in understanding prior approaches considered when attempting to understand evaluations of unknown distributions. Here the authors seek to obtain "good" rather than optimal selection criteria for their process.

Jun, Jacobson, and Swisher (1999) used discrete event simulation to improve patient flow and for resource allocation. The paper used modeling techniques relative to discrete-event-simulation. Liu and Cheung (1997) also studied continuous review inventory models. The focus included review of exponentially distributed variables along with other key operating characteristics for the inventory model. The authors utilized numerical examples to validate their model and provided a level of demonstration of its effectiveness.

Mazzola and Schantz (1995) developed an optimal allocation model of a single facility production environment. Branch and bound heuristics along with Tabu Search heuristics were utilized in their approach. The primary utility of this study was the understanding and review of definitions employed with heuristics employed in the author's research.

Wilson and Roach (2000) identified a methodology for the automatic generation of computerized solutions to the container stowage problem. The methodology presented heuristic rules for "good" but not optimal solutions. The primary focus of this literature review was for application to assembly planning and heuristics. A re-occurring trend in the application of heuristics in these areas appears to be relative to practical application (i.e., good solutions versus optimal).

Pourbabai (1992) utilized a mixed non-Markovian queuing network with infinite capacity nodes to model an automated assembly system problem. The study focused on identifying the minimum required local storages by using a stochastic optimization model and a heuristic algorithm to solve for and approximate results for the simulation study. Pourbabai (1992) also discusses a strategy for the selection of a required amount of local storages for workstations of a flexible assembly line system. While this research is relevant to this research topic, it does not specifically address the research gap identified by this area of research.

Pourbabai (1989) described the design of a finite capacity assembly model and quality control station that used a Markovian queuing system performance model and an optimization model to select optimal storage sizes. This study also utilized a Poisson arrival process as part of the performance model. The paper identifies a simulation model and focuses on observations noted as part of the simulation results; findings presented suggest that explicitly considering random variables dependencies makes performance analyses of a complicated stochastic network difficult.

2.4 Heuristics, Frameworks, and Other Methodologies

Heuristics techniques can be broadly characterized as exploratory problem solving techniques. Merriam-Webster.com identifies the following heuristic definition:

"Involving or serving as an aid to learning, discovery, or problem-solving by experimental and especially trial-an-error methods."

Heuristics is a very broad knowledge base that aids in effective problem solving and serves as a way to "frame new problems" (Michalewicz and Fogel, 1998). A review of Michalewicz et al. (1998) uncovered various useful problem-solving heuristics and approach techniques. The development of a heuristic or improving heuristics could include a variety of techniques found similar to prior heuristic research, such as:

Michalewicz et al. (1998) provided insight in the area of heuristics. This literature provided insight into heuristics such as simulated annealing, tab search, model overviews; various search methods, and other algorithms that served as a foundational basis for numerous aspects of this research. For the purpose of this paper the basis of numerous heuristic definitions were cited from this source.

Chiang, Kouvelis, and Urban (2002) developed optimal and heuristic solutions methodologies for evaluation of workflow interference. The paper focused on application of these methodologies from a facility layout perspective by examining branch and bound heuristics along with Tabu search heuristics. While facility applications are relevant to assembly (i.e., storage of assemblies) the primary utility of this study dealt with application and heuristics approaches.

Lozano, Adenso-Diaz, Eguia, and Onieva (1999) used a Tabu search heuristic in a cellular manufacturing design. The heuristic proposed systematically explored feasible machine cell configurations in part family determinations. The heuristic was benchmarked against two simulated annealing approaches and other heuristics.

A 1997 study by Salhi developed a constructive heuristic for a location problem.

The author tested the proposed heuristic against other location problem methods.

Cao and Ho (1987) model a production line with limited storage capacity as a cyclic network with finite buffers. In this analysis Cao and Ho identify a new technique called "perturbation analysis of discrete event dynamic systems." The paper identifies that its main purpose is to investigate perturbation analysis of a closed queuing network with blocking and its application to the optimization of the system throughput in a tandem production line with a finite storage capacity. The simulation results identified that the estimate of the derivative of the throughput and the estimate of the derivative of the time required to complete a finite number of services is unbiased. Finally, the paper also utilized Monte Carlo simulation as a viable method for this optimization approach.

Rochat and Semet (1994) evaluated a vehicle routing problem using two proposed heuristics to find a "good" solution. This study was considered to further evaluate heuristics in a similar application and for evaluation techniques used to compare the heuristic against a baseline configuration.

Naddor (1975) identified heuristic decisions for inventory policy. The heuristic involved knowledge of the mean, standard deviation of demand along with other variables for the model. This brief article provides an overview of the heuristic and limited application.

Park, Kang, and Park (1996) proposed an algorithm associated with integer programming formulation of a bandwidth packing problem. A heuristic was proposed and utilized a column generation technique as part of the algorithm. The authors further tested the algorithm using random problems. Of particular interest is that the authors compare their heuristic to a previously benchmarked method. The authors also provide a brief discussion of "good" vs. optimal solutions.

Patterson and Rolland (2002) explored network design and presented a heuristic with a methodology that utilized an adaptive reasoning technique. The authors also generalized their formulation and measured its effectiveness. The primary utility of this study toward this research dealt with the heuristic approach methodology.

Zhang, Wang, Cheok, and Nee (2003) proposed a knowledge-based selection procedure/rules (e.g., heuristic) to provide a unique name based search mechanism geared toward component reuse (i.e., reapplication).

Meller and Bozer (1996) presented a heuristic (i.e., simulated annealing) for facility layout. The significance of this particular study with respect to this dissertation was the approach method for performance comparison and application utility of the study toward heuristic and algorithm development. This study primarily focused on production facilities and achieving a good solutions for a series of 200 plus problem sets and provided a relatable and practical application and approach for the methods developed by the authors.

Thakur, Nair, Wen, and Tarasewich (2000) used Beam Search (BS) based heuristics to identify optimal or near optimal product lines. The authors test their heuristic on 300 simulated problems with applications. They also compare their search

technique with a Genetic Algorithm (GA) based heuristic and conclude that their BS based heuristic is more effective than the GA used in identifying optimal or near optimal solutions quickly. The authors provide examples to illustrate their heuristic and their model.

Coverdale and Wharton (1976) identified an improve heuristic for a Nonlinear Cutting Stock Problem. This particular study focuses on the cutting operations by constraining material cutting patterns to improve residual scheduling via pattern enumeration. The results of the paper also compare heuristic performance using different methods for the analysis.

Rubin (1990) proposed a mixed-integer model and suggested heuristics to obtain a suboptimal but "good" solution to reduce computational cost using linear programming. A linear programming heuristic based method was the second method used as part of this review. The results were compared using a Monte Carlo simulation with Gaussian data.

Kulm (1977) identified that the absences of theoretical or empirical hypothesis raised questions on two different problem-solving heuristics. The critique also raised questions on understanding a clear or consistent meaning of the term heuristic.

Nair, Thakur, and Wen (1995) used beam search heuristics to improve upon prior heuristics for the product line design and selection. Nair et al. used computations from over 400 simulations to demonstrate improvement in five defined performance measures. Their solutions resulted in improve optimality for the design simulation resulting in "good" solutions.

Barish (1962) examined the present and future scopes of management science, operations research, and industrial engineering. The framework and approach used to

identify conceptual relations between provided useful backgrounds to the author on similar comparative approaches used in these fields. Application of this literature review was primarily from an introspective approach for this dissertation.

2.4.1 Search Methods (Local and Exhaustive)

Exhaustive search methods are those methods that "check each and every solution in a search space until the best global solution has been found (Michalewicz and Fogel, 1998). Michalewicz et al. also suggest that exhaustive search methods are usually not practical for real world applications due to the large search areas, potential quantity of feasible search possibilities, and uncertainty in obtaining knowing whether the best solution has been found for a given search. They later note that local search methods/algorithms present a more reasonable alternative to exhaustive search techniques for providing satisfying results from defining the current solution, transformation and formulation of a new solution and its merit evaluation, solution exchange or retention, repetition of technique until no transformation improves the current solution.

2.4.2 Algorithm and Optimization Techniques

Michalewicz et al. (1998) identify a Greedy Algorithm as a type of algorithm that attacks "a problem by constructing complete solutions in a series of steps." The simplicity of this type of algorithm lends itself to greater application. They indicate that Greedy Algorithms perform the following:

- Assign Values for all of the decision variables
- Make the best available decision based on an assumed heuristic and available information

Shortfalls – local optimum at each step may not result in a global optimum

Aggarwal, Orlin, and Tai (1997) explored applications of genetic algorithms to demonstrate the utility of knowledge based mechanisms. Application of this study was limited to understanding the utility of genetic algorithms in a given application and heuristic comparison methods.

A 1994 study by Park and Kim developed a heuristic algorithm to address aspects of production planning problems for an assembly system. The particular focus of this study was on assembly systems operating on a make-to-order basis. In particular, this study utilized packaging examples of automobile subassemblies toward the minimization of inventory holding costs. This review considered the process and application of heuristics which were considered to better understand the type and application of specific heuristics dealing with assembly line systems.

Kannan, Jayabalan and Jeevanantham (2003) utilized genetic algorithms to find the best combination of the selective assembly groups necessary to minimize assembly variation. This method focused on linear assembly. The paper itself focuses on minimizing component tolerances and variation.

Ponnambalam, Aravindan, and Rao (2003) presented a mixed model sequencing problem using genetic algorithms for assembly lines. Their focus was the investigation of genetic algorithms and also performed a comparison of exiting vs. proposed GA's by consideration of variation at multiple assembly levels (e.g., raw materials, product, subassembly, etc.). The dissertation application of this study was primarily focused on the method and heuristic approach by the authors.

Sanderson (1997) used a tolerance model to estimate part configurations based on maximum likelihood using a filter algorithm. Sanderson then stated that the resulting configurations could then be used to evaluate the ability to assemble as it relates to clearance likelihood from the problem constraints. This was also applied to the ability to assemble of subassemblies.

Kwok, Driessen and Phillips (2002) utilized a matching algorithm to address a problem associated with multiple-target-multiple-agent scenarios. The study was primarily focused towards robotics; however, focus was applied to optimal assignment algorithms. The paper also addresses heuristics on a limited basis. Klincewicz (1990) solved a freight transportation problem using facility location techniques. Of specific interest from this review was the method employed by the author in heuristic evaluation. Since facility location problems are potentially derivative of the large assembly sequencing or selection process this paper provided relative insight to support the approach for this dissertation. A flow chart of the basic heuristic model was developed

and computational efforts were performed to identify the impacts when compared to a known optimal solution.

2.4.3 Branch and Bound

Branch and Bound is a heuristic that works on the idea of successive partitioning of the search space (Michalewicz et al., 1998). The authors also find that this type of heuristic eliminates areas of interest by evaluating successive partitions of a search space and eliminating a bounded region that does is beyond the constraints of the next branch being compared within the problem. Michalewicz et al. (1998) also note that the heuristic allows for the search to be minimized without performing a detailed analysis of a portion of the problem.

2.4.4 Simulated Annealing

Bohachevsky, Johnson and Stein (1986) was reviewed for initial applicability and potential to this research. Bohachevsky et al. (1986) described generalized simulated annealing for the "optimization of functions having many local extrema" and methods for improved optimums of other problems. This paper identifies simulated annealing as an optimization derived from "the annealing process of metals in which final crystalline configurations are possible depending on the rate of the cooling process."

Ohlemüller (1997) used simulated annealing for solving a minisum location problem. Tabu search was utilized in this study. Efficiency of the method was presented along with results relative to the expected deviation. Finally, the author's study is consistent with other approaches of finding "good" solutions (e.g., vs. optimal).

2.4.5 Tabu Search

Tabu search (TS) is a meta-heuristic that is "based on the premise that problem solving, in order to qualify as intelligent, must incorporate adaptive memory and responsive exploration (Glover and Laguna, n.d.)." In Glover and Laguna's short article in their 1997 book they indicate that the "adaptive memory feature of TS allows the implementation of procedures that are capable of searching the solution space economically and effectively." It is interesting to note that Tabu search heuristics are not memory less like some semi-random search processes. Glover and Laguna (n.d.) identifies that

Fred Glover is generally regarded as the originator of Tabu Search metaheuristics. Glover's search name "Tabu" is aptly named because the memory attributes "forces the search to explore new areas of the search space (Michalewicz et al, 1998)."

Glover and Laguna (1997) presented one of the earliest comprehensive looks at Tabu search. Given the re-occurrence of Tabu-search in other literature this work was reviewed to gain insight into this meta-heuristic approach and its application to problem solving and decision making.

Glover (1990) examined the characteristics of heuristic procedures used as frameworks for analyzing difficult optimization problems. While the research included the review of several types of heuristics the author focused specific attention on Tabu search heuristics. Glover (1990) discusses four major heuristic methods (e.g., neural networks, simulated annealing, genetic algorithms, and Tabu search). The author also discussed target analysis as a method for determining good decision rules as a means to

improve heuristic effectiveness. Markland (1990) summarized glovers work relative to these four major areas.

Punnen and Aneja (1995) studied a resource-constrained assignment problem and developed a Tabu search heuristic. The primary utility of this work to this dissertation was in expansion of heuristic test method understanding. The authors used computational results to demonstrate the effectiveness of their method from other algorithms.

Gendreau, Hertz, Laporte (1996) developed a Tabu search heuristic for a stochastic vehicle routing problem with random demands and probabilities. Tabu search heuristics proposed were compared against a known optimal solution. The authors provided a model confidence factor and average deviation to an optimal solution (e.g., "good" vs. optimal). Similarly, Gendreau, Hertz and Laporte (1994) described a Tabu search heuristic for vehicle routing problem with various restrictions. The heuristic utilized a generalized procedure and performed numerical test on a set of benchmark problems to demonstrate the viability of their heuristic.

Logendran and Sonthinen (1997) developed a Tabu search heuristics and statistical experimentation to present a "good" solution for solving a problem within a flexible manufacturing system. In their work they identify a six part Tabu-search heuristic. The application of this study to this literature review was primarily focused on heuristic development and application overview in the area of flexible manufacturing systems.

Dell'Amico (1996) analyzed the performance of lower and upper bounds for a flow-shop problem with two machines. This study used a Tabu search algorithm and

proved the effectiveness of the proposed bounds through computational results.

Although this study was focused on machine scheduling the applications relevance was targeted toward the understanding of knowledge gaps related to assemblies.

Moccellin and Nagano (1998) evaluated the relative performance of Tabu search procedures. Their focus was in the area of flow shop sequencing (which has application to assemblies). Moccellin et al. (1998) presented methods to improve heuristics by obtaining an initial solution using the traveling salesman problem and then Tabu search methods to improve the initial solution.

Consiglio and Zenios (1999) presented a multimodal Tabu search procedure with empirical results.

2.4.7 Additional Techniques

Finite-Element and Difference Methods were investigated for applicability and references such as Grieme (2011), Simpson (2008), and [96] Asvadurov, Druskin, Guddati and Knizhnerman (2003) were explored for further relevance to this dissertation.

Brown and Spillane (1989) described a knowledge-based design aid for fabrication of a low-cost boiler component. Of particular interest in this study was that the design approach they used was a pseudo-random search technique to improve the design cost (Brown et al, 1989). Application to this research was focused on the heuristics and their use of "applications" as part of testing their design aid.

Bracker and Pearson (1986) developed a planning process with comparison to a specified area of interest. The authors used multivariate analysis of variance in their

determinations. The primary use of this study in this dissertation was relative to gaining insight into approaches and hypothesis testing examples.

Kozan (2000) developed an analytical framework for the examination of inventory strategies for an assembly plant. The model addressed minimization strategy along with material management efficiency. Kozan (2000) leveraged this work off of prior work in the area of vehicle routing problems and used a genetic algorithm in its implementation. Historical data was used to measure the heuristic efficiency.

Phoomboplab and Ceglarek (2007) proposed a design synthesis framework for dimensional management of a multi-stage assembly system. Applications from this work included tolerance optimization, fixture layout, and part-to-part joint design. Of note, this work presented a methodology to illustrate a subassembly design configuration and framework (e.g., heuristic for part assembly).

2.5 Research Hypotheses

The null and alternate hypotheses for this research are:

H₀: No relationship/correlation exists to assess the additive relationship of a truncated standard normal distribution with another identical distribution.

H₁: Analysis of the relationships between additive truncated standard normal distributions and a given truncated standard normal distribution will provide meaningful correlation data.

H₂: Regression analysis between an additive truncated standard normal distributions and a given truncated standard normal distribution will provide meaningful data regarding the relationship between these distributions.

H₃: A heuristic based approach for the analysis of a truncated standard normal distributions using its characteristic function and inversion factor can produce

results equivalent to
$$f(z)dz = \int_{z_1}^{z_2} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}+z^2\right)} dz$$
.

These hypotheses will be tested in a later chapter along with the establishment of a heuristic framework/approach for the assembly of truncated normal distributions, and compilation of a comparative analysis of the subject matter. In addition to these research hypotheses, a comparative review will be performed to identify the dominant methods identified in the literature review along with relevant research gaps.

CHAPTER 3

METHODOLOGY

3.1 Research Method Overview

The research approach for this dissertation employs a literature review, comparative analysis, truncated standard normal distribution analysis, application demonstrations, heuristic development and hypotheses testing. An overview of the process employed for this research is depicted in Figure 2.

In this dissertation the literature review follows the initial development of the research questions. These reviews aid in the development of the research hypotheses identified in Chapter 2. Further analysis/comparative reviews aid in the identification of knowledge gaps to substantiate the research hypotheses. Mathematical formulations, correlation and regression analysis tests, along with observation and inspection provide insight into the research questions posed by this dissertation.

This research provides an alternative approach and techniques for solving single doubly truncated standard normal distributions through use of its characteristic function.

Mathematical formulations of this phenomenon using an inversion factor are presented in Appendix A. This approach provides new evidence and performs empirical analysis not previously identified by prior work.

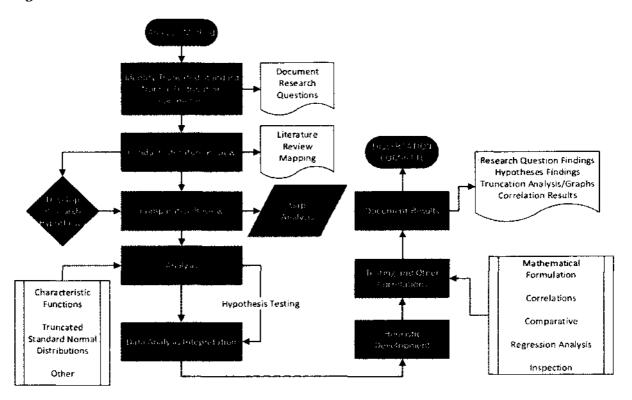


Figure 2: Research Process Overview

Eighty-one combinations of a single doubly truncated normal distribution will be evaluated and a baseline inversion factor will be developed to baseline the analysis results to methods identified by Khasawneh, et al. (2005). These combinations were evaluated in 0.1 increments ranging from an USL = 4 to a LSL = -4. Combinations for the assembly of identical doubly truncated standard normal distributions will use the same range with an overall assembly USL =8 and LSL = -8 (i.e. two assembled distributions each with an USL =4 and LSL =-4).

The analysis results are evaluated mathematically and compared against known

TSND baselines using correlation and regression analysis. Mathematical inspection and

analysis observations provide further quantitative and qualitative data. The results of the analysis will be documented in Appendix B through H, as applicable.

Testing of the research hypotheses is performed following the data analysis. The heuristics and data analysis results serve to "reject" or "fail to reject" the null hypothesis of this research. Alternate hypotheses evaluations were also conducted to determine if there was sufficient or insufficient data to "support" the final conclusions for each hypothesis.

Specifically, this research investigates analysis methods and heuristics for a truncated standard normal distributions' characteristic function and seeks to provide an approach to test the results. The research hypothesis test approach is addressed further in Section 3.4.

The research approach employed by this dissertation primarily utilized a quantitative research along with deductive and inductive modes of reasoning to investigate TSNDs. Creswell (2003) identifies that elements of a quantitative approach involve "reduction to specific variables and hypotheses and questions" in addition to "measurement and observation, and the test of theories." Creswell (2003) also identifies the characteristics associated with deductive and inductive modes of reasoning. The quantitative data analysis techniques utilized in this research include mathematical formulations and their associated statistical analysis. Example data was also generated and evaluated as part of this approach using various analysis techniques. Other evaluations included comparative reviews, data interpretation, and heuristic development. Refer to Sections 3.2, 3.3 and 3.4 for additional details related to research gap identification, TSND analysis and hypothesis testing.

3.2 Comparative Review and Research Gaps

A comparative review was performed of a sample of more than 100 relevant scholarly works in the areas pertaining to assembly, truncated standard normal distributions, heuristics, EVT and other applicable subsets of this dissertation. A comprehensive review of these results is shown in Appendices F and G.

The comparative review aided in classifying and categorizing a representative sample of scholarly works for the purpose of identify truncation methods, heuristics and analysis methods relevant to TSND within the body of knowledge. In general the categorization of comparative review was based on the judgment of the author. Attempts were made to group and categorize literature as objectively as practical. Appendix E categorization information aided in the review and comparative analysis of the literature reviewed. Scholarly works were categorized and grouped based on concepts presented explicitly and implicitly. For example, in some cases a scholarly work may have addressed heuristic steps without explicitly sighting a procedure or approach as a heuristic. As a result, those instances were categorized using good judgment with objective intentions. A primary focus of this review was to identify research and knowledge gaps in this engineering management discipline. The following general areas were analyzed:

- Comparative Review Selective Assembly/Heuristics/Truncation with specific categorization based on data source.
- Comparative Review Heuristics/Benchmarking/Truncation with specific categorization based on a benchmarking emphasis.

- Comparative Review Heuristic Type with specific emphasis toward testing methods.
- Comparative Review Testing Methods & Truncated Assembly.
- Comparative Review Heuristic Data Sources of Truncated Assembly
 The results shown in Figures 3 through 7 and Appendices F and G identify
 observations of various data partitions for the review variables evaluated. The following
 observations are made from the data:
 - Heuristic procedures represent a knowledge generation method (28% from Appendix G, Table G.1) and widely used problem solving/approach techniques used to expand the body of knowledge. Beyond heuristic procedures, examples/case studies also serve as a widely used and accepted methods for knowledge creation. Of the benchmarking methods identified in Appendix G, Table G.1, 43% were involved heuristics in a broader level of review.
 - Statistical means to benchmark quantitative and/or qualitative results (e.g., correlation), and efficiency improvements all represent examples for testing problems in this knowledge area.
 - Appendix G, Tables G.2 and G.4 identify that the majority of testing methods
 identified in the literature review was performed using some form of
 mathematical computations/model and/or via comparative analysis. Table G.6
 identifies heuristics and models as primary analysis techniques for the research.
 - Appendix G, Table G.3 reinforces the knowledge gap relative to truncation/selective assembly and heuristics and although data is limited data sources leveraged "example" data as a means of analysis.

 Simulation, historical data, or example data are also widely used data sources for analyses (i.e. Appendix G, Table G.5).

A review of Appendices F and G also shows that in the area of truncated standard normal distribution analysis that there is little data related to heuristics, analysis for truncation of assemblies, and alternative methods for truncated standard normal distribution using characteristic functions. Figures 3 through 7 provide results for comparative review compilations for select areas of focus in this dissertation.

Figure 3: Comparative Review - Selective Assembly/Heuristics/Truncation

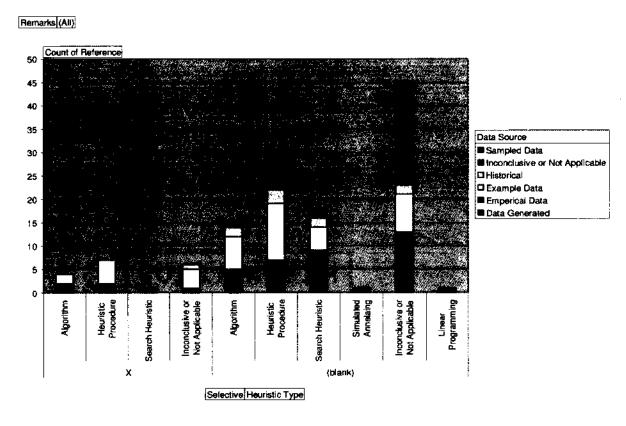


Figure 4: Comparative Review Heuristics/Benchmarking/Truncation

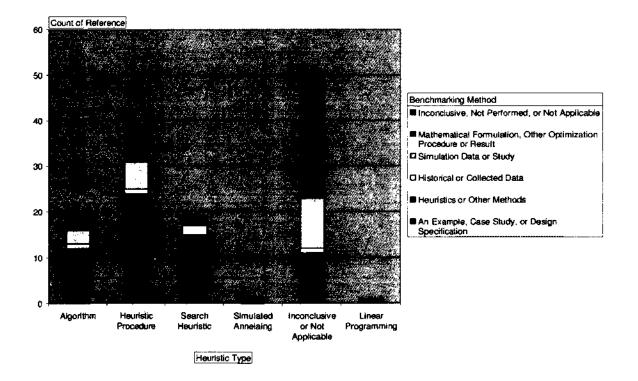


Figure 5: Comparative Review - Heuristic Type & Testing Methods

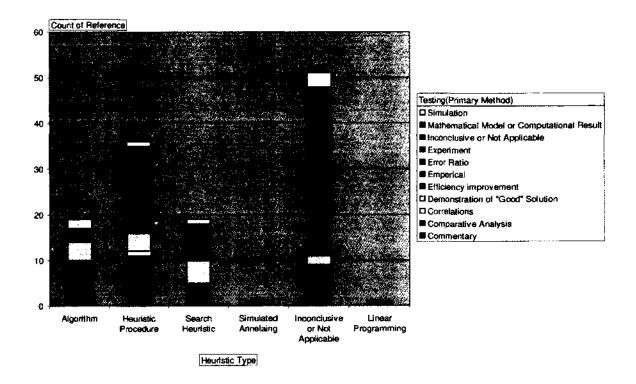


Figure 6: Comparative Review - Testing Methods & Truncated Assembly

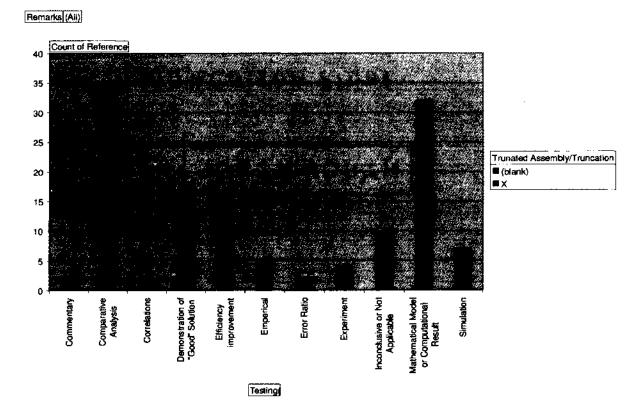
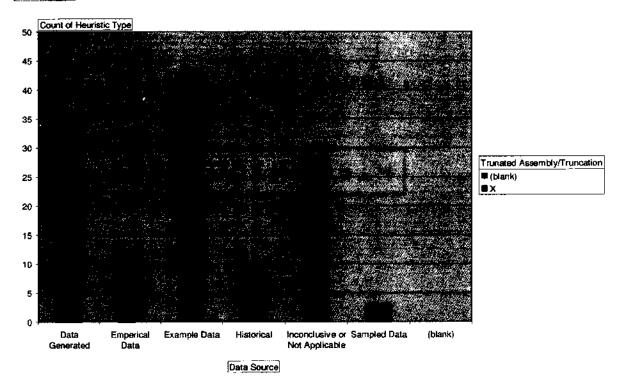


Figure 7: Comparative Review -- Heuristic Data Sources of Truncated Assembly

Reference (All)



3.3 Truncated Standard Normal Distribution Analysis

One facet of this dissertation research focuses on the analysis of truncated standard normal distributions. As part of this research the literature mapping identified a gap in analytical approaches for the computation of a truncated distribution using a distributions characteristic function. Original work presented by this dissertation provides an empirical basis for the proposed approximation of a truncated standard normal distribution assembly using an inversion factor. Heuristic procedures are developed by this research and documented in Appendices I and J. A summary-level of these heuristics are shown in Figures 8 and 10.

Unique aspects of a distributions characteristic function are leveraged by this research in the analysis of truncated standard normal distributions. P. Billingsley (1995) identifies that for a given "characteristic function ϕ uniquely determines the measure of μ it comes from." Therefore, it can be inferred that an inversion formula can be used to identify the result of two doubly truncated normal distributions. This research uniquely identifies a means to obtain the result of such an inversion of a truncated standard normal distribution and provides inversion factors for this inversion with a baseline against known truncated standard normal distributions. This research also proposes an evaluation method to compute the result of two assembled truncated standard normal distributions through the use of the inversion of the combination of their respective characteristic functions and proposes the use of inversion factors established for a given truncated standard normal distribution upper and lower specification limit.

Appendix I documents a baseline inversion heuristic for a truncated standard normal distribution from a characteristic function. Appendix J expands Appendix I

heuristic at the assembly level (for identical distributions). Figure 9 provides a simplified visual representation of two assemblies with a given upper and lower specification.

Equations and relevant calculations are found in Appendix A. Examples of computational results are found in Appendix D. Analysis results for single and assembled TSND parameters are identified in Appendix B. Section 3.4 addresses the analysis testing (e.g. correlation and regression analysis) that was investigated beyond observations and inspections from the mathematical results.

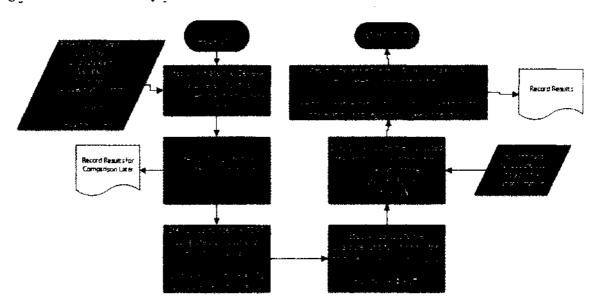


Figure 8: Heuristic - Analysis for Truncated Standard Normal Distribution

Figure 9: Truncation Assembly-level Example (Simplified)

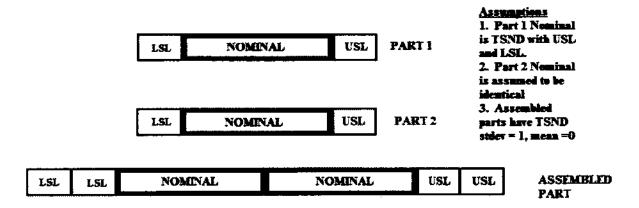
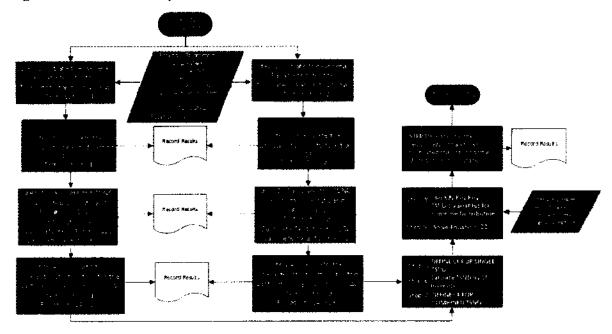


Figure 10: TSND Assembly CF Inversion Heuristic



3.4 Hypothesis Testing

This section outlines the hypothesis testing steps performed as part of this dissertation for each research hypothesis. Various elements of the analysis of the truncated standard normal distributions are performed mathematically and serve as a logical axiom and baseline for this research (i.e., Appendix I heuristic logic). For example, the analysis testing in Appendix H for truncated standard normal distributions (single distribution) using inversion techniques for its characteristic function was established using a known TSND baseline. Logically this method is applied to assemblies by expanding on the mathematical formulations in Appendix A.

This dissertation indentified null and alternative hypotheses to be tested.

Mathematical formulation in addition to the structure hypothesis tests aid in the investigation into the analysis of truncated standard normal distributions. This dissertation uses National Institute of Standards and Technology (NIST) 2014 guidance that identifies "the p-value is the probability of the test statistic being at least as extreme as the one observed given that the null hypothesis is true."

Hypothesis tests will be performed for each hypothesis as follows:

H₀ will be tested by developing identical distributions for combinations of
distributions with specification limits ranging from -4 to 4. Distributions
combinations increments will be analyzed at increments of 0.1 per distributions
(i.e., 81 combinations of two identical distributions). The assembled distributions
will be analyzed in increments of 0.2 for specification limits ranging from -8 to 8.
 The Appendix A equations were used to identify the characteristic function and
other equation inputs and results. Correlation analysis (i.e. Pearson's correlation

coefficient) and regression analysis will be performed to assess the relationship and linear relationship between variables. P-values were also analyzed as part of statistical testing. Statistical testing will be performed with commonly accepted statistical software (Minitab® et al.). The final assessment of this hypothesis will be made following evaluation of the alternative hypotheses. In addition the correlation analysis and regression analysis from those tests would serve to "reject" or "fail to reject" this null hypothesis.

- a. NIST (2014) identifies that "The choice of α is somewhat arbitrary, although in practice values of 0.1, 0.05, and 0.01 are common." As a result, a significance level of $\alpha = 0.05$ was assumed for the analysis performed in this dissertation.
- b. Data results will be reviewed against the evaluation criteria in addition to the results of the alternate hypotheses to evaluate the hypothesis test results.
- 2. H₁ will be tested by following the generation of identical distributions for combinations of distributions with specification limits ranging from -4 to 4. The distributions combination increments will be analyzed at increments of 0.1 per distributions (i.e., 81 combinations of two identical distributions). Assembled distributions will be analyzed in increments of 0.2 for specification limits ranging from -8 to 8. This hypothesis will be tested by generating the distributions for a TSND (with adjusted standard deviation) and TSND (using Khasawneh et al. 2005 methods) and evaluating these distributions using TSNDs assemblies (using

characteristic function inversion). These distributions will be compared as follows:

- a. Direct comparison by correlation between a TSND (e.g., fT(z) adjustdev) and TSND assembly based on its characteristic function.
 Evaluations will be performed using Pearson's correlation coefficient, regression analysis, p-value, and via mathematical formulation and observation/inspection.
- b. Correlations will also be performed between Ratio 1 and Ratio 2 as shown in Appendices B and C. Correlations will also be performed between Ratio 3 and Ratio 4 as shown in Appendices B and C. The ratios represent ratios between TSND assembly-level truncated distributions (with a standard deviation of 1 and an alternative which utilizes a standard deviation of square root of the sum of the squares of each distributions standard deviation).
- c. A significance level of $\alpha = 0.05$ was assumed based on NIST (2014) guidance.
- d. Data results will be reviewed against the evaluation criteria to evaluate the hypothesis test results.
- 3. H₂ will be tested by following the generation of identical distributions for combinations of distributions with specification limits ranging from -4 to 4. The distributions combination increments will be analyzed at increments of 0.1 per distributions (i.e., 81 combinations of two identical distributions). Assembled distributions will be analyzed in increments of 0.2 for specification limits ranging

from -8 to 8. This hypothesis will be tested by generating the distributions for a TSND (with adjusted standard deviation) and TSND (using Khasawneh et al. 2005 methods) and a evaluating these distributions using TSNDs assemblies (using characteristic function inversion). These distributions will be evaluated as follows:

- a. Regression analysis between a TSND (e.g., fT(z) adju stdev) and TSND
 (e.g., fT(z) assy) assembly based on its characteristic function.
- b. Regression analysis between a TSND (e.g., fT(z) standard) and TSND
 (e.g., fT(z) assy) assembly based on its characteristic function.
- c. A significance level of $\alpha = 0.05$ was assumed based on NIST (2014) guidance.
- d. Data results will be reviewed against the evaluation criteria to evaluate the hypothesis test results.
- 4. H₃: A heuristic based approach for the analysis of a truncated standard normal distributions using its characteristic function and inversion factor can produce results equivalent to $f(z)dz = \int_{z_0}^{z_0} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}*z^2\right)} dz$.
 - a. This research hypothesis will be verified by demonstrating the results are equivalent. Correlation and regression analysis will further confirm that the values have a strong correlation. Regression models will confirm that the data model equations are equivalent.
 - b. A significance level of $\alpha = 0.05$ was assumed based on NIST (2014) guidance.

CHAPTER 4

RESULTS

This chapter will discuss the results of the mathematical formulations, correlations, regression analysis and heuristics developed as part of this research.

4.1 TSND Analysis Results and Heuristics

Appendix A provides a summary of the equations utilized as part of this research to investigate the analysis of truncated standard normal distributions. Appendices I and J provide the final heuristics developed as part of this research. Mathematical axioms are leveraged as part of the formulation applications to truncated standard normal distribution assemblies. Correlation analysis and regression analysis identify relationships between various distributions. These methods of evaluation only aid in identifying distribution relationships between the alternative analysis formulation presented and other methods for a single doubly truncated normal distributions.

4.2 Hypothesis Testing Results

Mathematical formulation and observation along with statistical analysis software (Minitab® et al.) were used to test the research hypotheses of this dissertation. Correlations were used as a means to compare different distribution results and to gain insight into any observations between distributions. Regression analysis was used to provide additional insight the relationship between distribution analysis methods. Hypothesis testing was performed using a significance value of $\alpha = 0.05$ along in

conjunction with mathematical formulations, observation, and inspection. While an $\alpha = 0.05$ was specified for analysis testing the results of this dissertation generally indicate that the results were significant to the 0.01 level (e.g., p < 0.001).

The testing of each research hypothesis involved data analysis, observation, and interpretation. Hypothesis testing results are documented in an Appendix C, D, and H. The research hypotheses were tested as follows:

H₀: No relationship/correlation exists to assess the additive relationship of a truncated standard normal distribution with another identical distribution.

This null hypothesis is rejected. Mathematical formulation along with correlation and regression analysis performed as part of alternate hypothesis analysis generally indicate a statistically significant and strong positive relationship (p < 0.001) for all distributions analyzed (where a p-value could be calculated). Additionally, observations and inspections of mathematical formulations support this conclusion. Regression analysis provides further insight into the relationship between assembly-level truncation analysis (using two different methods). R-values ranging from 99.13% to 100% for cubic line model plots further support this conclusion. Appendices B and C document the results and other corresponding analysis.

H₁: Analysis of the relationships between additive truncated standard normal distributions and a given truncated standard normal distribution will provide meaningful correlation data.

Mathematical formulations presented in Appendix A along with correlation analysis testing results support alternate hypothesis H_1 . Correlation data generally indicates a statistically significant and strong positive relationship (p < 0.001) for all analyzed distributions (where a p-value could be calculated). Meaningful results are defined as either a statistically significant relationship, positive correlation/relationship, or any other observed, calculated, or identified parameter which provides data or indications not previously understood by the body of knowledge. Additionally, observations and inspections of mathematical formulations support this conclusion. Appendices B and C document the results and other corresponding analysis.

H₂: Regression analysis between additive truncated standard normal distributions and a given truncated standard normal distribution will provide meaningful data regarding the relationship between these distributions.

Mathematical formulations presented in Appendix A along with regression analysis testing results support alternate hypothesis H_2 . Regression analysis generally indicates a statistically significant and strong positive relationship (p < 0.001) for all analyzed distributions (where a p-value could be calculated). Meaningful results are defined as either a statistically significant relationship, positive correlation/relationship, or any other observed, calculated, or identified parameter which provides data or indications not previously understood by the body of knowledge. Additionally, observations and inspections of mathematical formulations support this conclusion. Appendices B and C document the results and other corresponding analysis.

H₃: A heuristic based approach for the analysis of a truncated standard normal distributions using its characteristic function and inversion factor can produce results equivalent to $f(z)dz = \int_{z_1}^{z_2} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}\star z^2\right)} dz$.

Mathematical formulations presented in Appendix A along with Appendix H analysis support alternate hypothesis H4. Appendix H results confirm that the baseline mathematical formulations via correlation and regression analysis. Appendix H regression results confirm that the results of the equations for a given X value are equivalent. This is confirmed graphically as well as through the examination of the fitted line plot equation for cubic model from the regression analysis. In addition to these results the correlation and regression analysis generally indicates a statistically significant and strong positive relationship (p < 0.001) for the distributions analyzed (i.e., -1 to 1, -2 to 2, -3 to 3, and -4 to 4). Additionally, observations and inspections of mathematical formulations support this conclusion. Appendix H documents the results and other corresponding analysis.

4.3 Simulation Examples

Examples of mathematical formulations used in this dissertation were developed using industry software (i.e., NtRand). This industry software was utilized for the purpose of generating three examples of random data sets with a population of 10,000 samples for a given USL, LSL, standard deviation, and mean. These data sets were then analyzed using mathematical formulations presented in Appendix A and using statistical software (Minitab® et al.).

The simulations performed were for sample distributions generated from -4 to 4, -3 to 3, and -2 to 2. Identical truncated standard normal distribution assemblies were used for each analysis of assemblies. Combination of these assemblies was performed using the distributions characteristic function. Results of this analysis are found in Appendix D. A summary of the results is also identified below in Tables D.1-D.9.

CHAPTER 5

CONCLUSIONS AND RECOMMENDATIONS

For engineering managers, risk managers and quality practitioners, the use of the standard normal distribution and truncated standard normal distribution have particular relevance when bounding data sets, evaluating manufacturing and assembly tolerances, and identifying measures of quality. In particular, truncated standard normal distributions are used in areas such as component assemblies to bound upper and lower process specification limits. This research provided an alternative approach to the analysis of TSNDs using an inversion factor and applied that insight to address the relationship of truncated distributions.

Heuristic procedures were developed to characterize the approach of this dissertation along with mathematical formulation and data analysis. The heuristics, correlations, regression analysis and other investigations performed provided additional insight into these distributions. Appendix A also documents the equations that form a part of the heuristic procedures in Appendices I and J. Additionally, truncation assembly data was provided in Appendix B to address two pair TSND combinations.

This dissertation presents a heuristic approach for the analysis of assembly-level truncated standard normal distributions. Specifically, this dissertation utilized the unique properties of a distributions characteristic function as method for the analysis of truncated assemblies. A comparative review was performed to aid in the identification of traditionally accepted analysis and evaluation methods dealing with part truncation.

In addition to the mathematical formulations for TSND assemblies in this dissertation practical application of the theory was also presented. Three examples of varying specification limits for a sample size of n = 10,000 were developed to reinforce the research framework presented. The analysis results for these examples are presented in Appendix D.

In general, the mathematical formulations performed in conjunction with the correlation and regression analysis results support the alternate hypotheses of this research. The approach presented also provides a framework and baseline for future efficiency and heuristic improvements along with conceptual expansion toward the potential application to other distributions.

5.1 Research Question Conclusions

The research questions, literature review, comparative analysis, TSND analysis, hypothesis testing, and other evaluations assisted with interrogatory review. The following statements and conclusions are provided:

Research Question 1: What are the research gaps relative to truncated standard normal distribution analysis and is there an opportunity to address a portion of these gaps?

This question poses a contextual question aimed at addressing TSND research
gaps. The question was posed as a means to narrow the focus of this research
(relative to assemblies) and to initiate a framework for future expansion of this
work. The literature review and comparative analysis results confirmed the

existence of research gaps as compared to the sample population of scholarly works reviewed.

Research Question 2: Does the analysis of two truncated standard normal distributions (i.e., assemblies) provide a quality indicator and/or an enhanced understanding of characteristics of truncated distributions with respect to assemblies?

• This research question focused on the analysis of two truncated standard normal distributions as a means to gain insight into assemblies. An assembly in its simplest form contains at least two pieces. This is important to engineering managers and other decision makers as it serves as the foundation for understanding more elaborate assemblies. Baseline and assembly level TSND mathematical formulations along with correlation and regression analysis provide insight into the relationships analyzed.

Research Question 3: To what extent can heuristic techniques be employed to aid in truncated standard normal distribution analysis? What relationships can be inferred from the analysis of truncated standard normal distributions?

As identified earlier in this dissertation a heuristic serves as an aid for learning,
discovery and problem-solving. The use of heuristics was considered as a method
of knowledge generation. Development of a "heuristic" provides a method for
which analysis of truncated standard normal distributions could be performed by
the practitioner. Heuristics provide a method of solving problems.

Understanding the TSND analysis relationships also serves as a benchmark for future efficiency improvement or expanded evaluations and comparisons.

Research Question 4: Can qualitative or quantitative data sets be developed to assist decision makers and/or quality practitioners with an enhanced understanding of truncated standard normal distributions (single and assemblies)?

 This question was initially focused on capturing a framework of assemblies and single truncated analysis using CF. Qualitative data would come from a "comparative review" or possible graphs whereas quantitative data is apparent in the analytical portions of the Appendices in this dissertation. Both of these approaches provide practical methods of enhancing TSND knowledge by a practitioner.

Research Question 5: Will correlations, goodness-of-fit or other testing methods provide meaningful data from truncated standard normal distribution (single and/or assemblies) and other known distributions?

Correlation and regression analysis testing was performed in addition to the
mathematical formulations, observations, and data inspections of TSNDs.
 Statistically significant strong positive relationships were identified in analyses
performed. Regression analysis and correlation analysis for various ratios of
assembly distributions were also evaluated for normal distributions. The test
methods presented (e.g. regression analysis) aid in identifying relationships
between distributions analyzed. Further evaluations beyond TSND distributions

were considered outside the scope of this work and provide an avenue for future research in this area.

5.2 Research Assumptions and Limitations

This research includes various assumptions and limitations that form an integral part of the research. The following assumptions and/or limitations apply to this research:

- This research focuses on truncated standard normal distributions. While this phenomenon generally exists in many engineering, financial and related industries it is important to also understand that that sample distributions may be normal even though the population as a whole may be better characterized by another distribution. This limitation could also be the focus of future research in this field.
- General statistical analysis tools were utilized in this research (e.g., Minitab®,
 NtRand, etc.); however, this software is assumed to be a reliable tool used within industry that provides consistent and repeatable results.
- This research scope was limited to the evaluation of identical doubly truncated standard normal distributions.
- Sample size evaluations were limited and represent a future research opportunity
 to provide additional research fidelity and improved accuracy through focused
 sample sizes in specific truncation areas of evaluation (e.g. sample sizes with
 increments smaller than 0.1 or 0.2).
- Statistical Significance values assumed an α = 0.05 as a generally accepted significance level per NIST (2014).

- For the purposes of evaluating " $f_T(z)$ adj. stdev", a $\sigma = \sqrt{{\sigma_1}^2 + {\sigma_2}^2} = 1.414214$ was assumed based on similar guidance by Weisstein, E.W (1994-2014).
- The research analysis was limited to mathematical formulation, correlation
 analysis, and regression analysis. As a result statistical analysis and significance
 (e.g., p < 0.001) does not imply that x causes y.
- It is not the intent of this research to attempt to characterize the population or variations, permutations or other circumstances that may exist in nature.
- Mathematical formulations assumptions were based on mathematical axioms concerning the baseline inversion of a CF using a typical TSND and its application.

5.3 Future Research Opportunities

Elements of this dissertation research provide various opportunities for continued or further research in the area of truncated distribution analysis. While this research focused on the analysis of truncated standard normal distributions expansion of this work toward the evaluation of other distributions could be considered. This research could also be further expanded by:

- Enhancement and improvement of the heuristics developed by this work.
- Refinement of the data as a function of sample size.
- Evaluation of the application of normalization concepts to concepts presented.
- Investigation into the inversion factors for alternative distributions (e.g., Weibull).

- The research analysis was limited to mathematical formulation, correlation analysis, and regression analysis. Alternative analysis methods could be considered to further investigate the analysis of TSNDs.
- Expansion to part binning and storage assembly of truncated piece parts.
- Further expansion into mathematical inversion of CF beyond the concepts presented in this research.
- Expansion of heuristic approach to include search techniques such as Tabu,
 beam, and/or other heuristic techniques.
- Expansion of comparative reviews to identify interrelationships between various methods (e.g. benchmarking, testing, heuristic type, etc).

REFERENCES

- Abadir, K., & Magdalinos., T. (2002). The characteristic function from a family of truncated normal distributions. *Econometric Theory*, 18(5). 1276-1287.
- Abate, J., & Whitt, W. (1991). The Fourier-Series Method for Inverting Transforms of Probability Distributions. Retrieved from the Pennsylvania State University,

 CiteSeer^X_f Website:

 http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.94.9058&rep=rep1&type=pdf
- Abe, S., Murayama, T., Oba, F., & Narutaki, N. (1999). Stability check and reorientation of subassemblies in assembly planning. Systems, Man, and Cybernetics, 1999. IEEE SMC '99 Conference Proceedings. 1999 IEEE International Conference on, 2, 486-491.
- Agard, B., & Kusiak, A. (2004). Data mining for subassembly selection. *Journal of Manufacturing Science and Engineering*, 126, 627-631.
- Aggarwal, C.C., Orlin, J.B., & Tai, R.P. (1997). Optimized crossover for the independent set problem. *Operations Research*, 45(2), 226-234.

- Asvadurov, S., Druskin, V., Guddati, M., & Knizhnerman, L. (2003). On optimal finite-difference approximation of PML. Siam Journal of Numerical Analysis, 41(1), 283-305.
- Bai, H., & Kwong, C.K. (2003). Inexact genetic algorithm approach to target values setting of engineering requirements in QFD. International Journal of Production Research, 41(16), 3861-3881.
- Barish, N.N. (1963). Operations research and industrial engineering: the applied science and its engineering. *Operations Research*, 11(3), 387-398.
- Bastes, R.A., Buck, R.J., Riccomagno, E., & Wynn, H.P. (1996). Experimental design and observation for large systems. *Journal of the Royal Statistical Society*, 59(1), 77-94.
- Baykasoğlu, A. (2001). Goal programming using multiple objective Tabu search.

 Journal of the Operational Research Society, 52, 1359-1369.
- Bermudez, P.D.Z, & Kotz, S. (2010). Parameter estimation of the generalized Pareto distribution Part I. *Journal of Statistical Planning and Inference*, 140, 1353-1373.
- Bermudez, P.D.Z, & Kotz, S. (2010). Parameter estimation of the generalized Pareto distribution Part II. *Journal of Statistical Planning and Inference*, 140, 1374-1388.

- Bernadic, M., & Candel, J. (2012). The doubly truncated function of indices on discrete distributions. *Stat Papers*, 53, 177-193.
- Billingsley, P. (1995). *Probability and Measure* (3rd ed.). New York, NY: John Wiley and Sons, Inc.
- Bisgaard, S. (1997). Designing experiments for tolerancing assembled products.

 Technometrics, 39(2), 142-152.
- Blanchet, J., & Liu, J. (2012). Efficient simulation and conditional functional limit theorems for ruinous heavy-tailed random walks. Stochastic Processes and their Applications, 122, 2994-3031.
- Bohachevsky, I.O., Johnson, M.E., & Stein, M.L. (1986). Generalized simulated annealing for function optimization. *Technometrics*, 28(3), 209-217.
- Bouchard, B., Elie, R., & Imbert, C. (2010). Optimal control under stochastic target constraints. Siam Journal on Controls and Optimization, 48(5), 3501-3531.
- Bracker, J.S., & Pearson, J.N. (1986). Planning and Financial Performance of Small, Mature Firms. Strategic Management Journal, 7, 503-522.

- Bradley, D. M., & Gupta, R.C. (2002). On the distribution of the sum of n Non-Identically Distributed Uniform Random Variables. *Annals of the Institute of Statistical Mathematics*, 54(3), 689-700.
- Brazauskas, V., & Kleefeld, A. (2009). Robust and efficient fitting of the generalized Pareto distribution with actuarial applications in view. *Insurance: Mathematics and Economics*, 45, 424-435.
- Breedis, J.B. (2001). Monte Carlo tolerance analysis of a passively aligned silicon waferboard package. *Electronic Components and Technology Conference*, 2001. *Proceedings.*, 51st, 247-254.
- Brooks, C., Clare, A.D., Dalle Molle, J.W., & Persand, G. (2005). A comparison of extreme value theory approach for determining value at risk. *Journal of Empirical Finance*, 12, 339-352.
- Brown, D.E., & Spillane, A.R. (1989). A Knowledge-based design aid for superheaters employing pseudo-random search. *Journal of the Operational Research Society*, 40(6), 539-550.
- Caleb Li, M.H. (2004). Optimal target selection for unbalanced tolerance design. The International Journal of Advanced Manufacturing Technology, 23, 743-749.

- Caleb Li, M.-H., & Chou, C.-Y.(2001). Target selection for an indirectly measurable characteristic in unbalanced tolerance design. *The International Journal of Advanced Manufacturing Technology*, 17, 516-522.
- Cao, X., & Ho, Y. (1987). Sensitivity analysis and optimization of throughput in a production line with blocking. *IEEE Transactions on Automatic Control*, AC-32(11), 959-967
- Carlson, J.M., & Doyle, J. (2002). Complexity and robustness. Proceedings of the National Academy of Sciences of the United States of America, 99(1), 2538-2545.
- Carpinteri, A., Cornetti, P., & Puzzi, S. (2005). Scale effects on strength and toughness of grained materials: an extreme value theory approach. *Strength and Fracture Complexity*, 3, 175-188.
- Castillo, E., Hadi, A., Balakrishnan, N., Sarabia, J. (2005). Extreme Value and Related Models with Applications in Engineering and Science. Hoboken, NJ: John Wiley & Sons, Inc.
- Chavez-Demoulin, V., & Roehral, A. (2004). Extreme Value Theory can save your neck.

 Retrieved from approximity.com Website:

 http://www.approximity.com/papers/evt_wp.pdf

- Chiang, W-C., Kouvelis, P., & Urban, T.L. (2002). Incorporating workflow interference in facility layout design: the quartic assignment problem. *Management Science*, 48(4), 584-590.
- Cittolin, A. (1997). Selection of assembly sequences using universal filtering methods.

 Emerging Technologies and Factory Automation Proceedings, 1997. ETFA '97., 1997

 6th International Conference on, 195-200.
- Consiglio, A., & Zenios, S. (1999). Designing portfolios of financial products via integrated simulation and optimization models. *Operations Research*, 47(2), 195-208.
- Cooper, A.B., Georgiopoulos, P., Kim H.M., & Papalambros, P. Y. (2006). Analytic target setting: an enterprise context in optimal product design. *Transactions of the ASME*, 128(4), 4-13.
- Coverdale, I., & Wharton, F. (1976). An improved heuristic procedure for a nonlinear cutting stock problem. *Management Science*, 23(1), 78-86.
- Creswell, J. (2003). Research design qualitative quantitative and mixed methods approaches. Thousand Oaks, CA: Sage Publications, Inc.
- Das, S.K., & Sarin, S.C. (1988). Selection of a set of part delivery dates in a multi-job stochastic assembly system. *IIE Transactions*, 20(1), 4-11.

- De Fazio, T.L., Rhee, S.J., & Whitney, D.E. (1999). Design-specific approach to design for assembly (DFA) for complex mechanical assemblies. *IEEE Transactions on Robotics and Automation*, 15(5), 869-881.
- Dell'Amico, M. (1996). Shop problems with two machines and time lags. *Operations*Research, 44(5), 777-787.
- Desmond, D. J., & Setty, C.A. (1961). Simplification of selective assembly.

 International Journal of Production Research, 1(3), 3-18.
- Dhrymes, P. J. (2005). *Moments of truncated (normal) distributions*. Retrieved from the Columbia University, Department of Economics Web site:

 http://www.columbia.edu/~pjd1/mypapers/mycurrentpapers/dummytruncated.pdf
- Diebolt, J., Guillou, A., & Rached, I. (2005). Approximation of the distribution of excess using a generalized probability weighted moment method. *C. R. Acad. Sci. Paris*, *I* 340, 383-388.
- Drees, H., de Haan, L., & Li, D. (2006). Approximations to the tail empirical distribution function with application to testing extreme value conditions. *Journal of Statistical Planning and Inference*, 136, 3498-3538.

- Gendreau, M., Hertz, A., & Laporte, G. (1994). A Tabu search heuristic for the vehicle routing problem. *Management Science*, 40(10), 1276-1290.
- Gendreau, M., Laporte, G., & Séguin, R. (1996). A Tabu search heuristic for the vehicle routing problem with stochastic demands and customers. *Operations Research*, 44(3), 469-477.
- Glover, F. (1990). Artificial intelligence, heuristic frameworks and Tabu search.

 Managerial and Decision Economics, 11, 365-375.
- Glover, F., & Laguna, M (undated). *Tabu Search*. Retrieved from the Pennsylvania State

 University, CiteSeer^X_β Website:

 http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.69.7798&rep=rep1&type=

 pdf
- Grieme, N. (2011). Derivation, general solution, and application of the Finite-Element Method. Retrieved from the University of Minnesota, Mathematics Discipline's Web site: http://facultypages.morris.umn.edu/math/Ma4901/Sp2011/Near/NickGriemenear.pdf
- Grüne-Yanoff, T., & Weirich, P. (2010). The philosophy and epistemology of simulation: a review. *Simulation and Gaming*, 41(1), 20-50.

- Guffin, J. (2010). The Characteristic Function. Retrieved from the Pennsylvania State

 University, Website:

 http://www.math.upenn.edu/~guffin/teaching/fall10/lectures/lecture-25.pdf
- Gutierrez, G.J., Hausman, W.H., & Lee, H.L. (1995). Dynamic control of imperfect component production for assembly operations. *IIE Transactions*, 27, 669-678.
- Hart, C. (2005), Doing a Literature Review. Thousand Oaks, CA: Sage Publications, Inc.
- Heuristic. (2014). In Merriam-Webster.com. Retrieved January 20, 2014, from http://www.merriam-webster.com/dictionary/heuristic
- Horrace, W.C. (2005). Some Results on the Multivariate Truncated Normal Distribution.

 Retrieved from Syracuse University, Surface Website:

 http://surface.syr.edu/cgi/viewcontent.cgi?article=1149&context=ecn
- Huang, G.Q., Qu, T., Cheung, D. W.L., & Liang, L. (2006). Extensible multi-agent system for optimal design of complex systems using analytical target cascading. *The International Journal of Advanced Manufacturing Technology*, 30, 917-926.
- Huang, S.H., Liu, Q., & Musa, R. (2004). Tolerance-based process plan evaluating using Monte Carlo simulation. *International Journal of Production Research*, 42(23), 4871-4891.

- Johnson, A., & Thomopoulos, N.T. (undated). Characteristics and Tables of the LeftTruncated Normal Distribution. Retrieved from the Illinois Institute of Technology,
 Faculty Whitepapers Website:
 http://business.iit.edu/shared/shared_stuartfaculty/whitepapers/thomopoulos_charleft.pdf
- Johnson, A.C., & Thomopoulos, N.T. (undated). Characteristics and tables of the doubly-truncated normal distribution. Retrieved from Illinois Institute of Technology,

 Website:

 http://business.iit.edu/shared/shared_stuartfaculty/whitepapers/thomopoulos_chardoubly.pdf
- Jun, J.B., Jacobson, S.H., & Swisher, J.R. (1999). Application of discrete-event simulation in health care clinics: a survey. *Journal of the Operational Research Society*, 50, 109-123.
- Kannan, SM., & Jayabalan, V. (2001). A new grouping method to minimize surplus parts in selective assembly for complex assemblies. *International Journal of Production Research*, 39(9), 1851-1863.
- Kannan, SM., Jayabalan, V., & Jeevanantham, K. (2003). Genetic algorithm for minimizing assembly variation in selective assembly. *International Journal of Production Research*, 41(14), 3301-3313.

- Kawata, T. (1969). On the inversion formula for the characteristic function. *Pacific Journal of Mathematics*, 31, 81-85.
- Khasawneh, M.T., Bowling, S. R., Kaewkuekool, S., & Cho, B.R. (2005). Tables of a truncated standard normal distribution: a singly truncated case. *Quality Engineering*, 17, 33-50.
- Khasawneh, M.T., Bowling, S.R., Kaewkuekool, S., & Cho, B.R. (2005). Tables of a truncated standard normal distribution: a doubly truncated case. *Quality Engineering*, 17, 1-15.
- Kim, H.M., Michelena, N.F., & Papalambros, P.Y (2003). Target Cascading in Optimal System Design. *Transactions of the ASME*, 125, 474-480.
- Klincewicz, J.G. (1990). Solving a freight transport problem using facility location techniques. *Operations Research*, 38(1), 99-109.
- Klum, G. (1977). Teaching problem-solving heuristics a critique of two studies. *Journal* for Research in Mathematics Education, 8(2), 153-155.
- Kosfeld, M.A., & Quinn, T.D. (1999). Use of dynamic simulation to analyze storage and retrieval strategies. *Proceedings of the 1999 Winter Simulation Conference*, 736-741.

- Kozan, E. (2000). An integrated material handling system for a truck assembly plant.

 Journal of the Operational Research Society, 51, 263-271.
- Krzysztofowicz, R. (1990). Target-setting problem with exponential utility. *IEEE Transactions on Systems, Man, and Cybernetics*, 20(3), 687-688.
- Kuwahara, H., & Mura, I. (2008). An efficient and exact stochastic simulation method to analyze rare events in biochemical systems. The Journal of Chemical Physics, 129(165101), 1-10.
- Kwok, K.S., Driessen, B.J., & Phillips, C.A. (2002). Analyzing the multiple-target-agent scenario using optimal assignment algorithms. *Journal of Intelligent Robotic Systems*, 35, 111-122.
- Kwon, H-M, Kim, K-J, & Chandra, M. J. (1999). An economic selective assembly procedure for two mating components with equal variance. *Naval Research Logistics*, 46, 809-821.
- Lee, B., & Saitou, K. (2007). Assembly synthesis with subassembly partitioning for optimal in-process dimensional adjustability. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing*, 21, 31-43.

- Lee, S. (1994). Subassembly identification and evaluation for assembly planning. *IEEE Transactions on Systems, Man, and Cybernetics*, 24(3): 493-503.
- Lee, S., & Shin, Y.G. (1990). Assembly Planning Based on Subassembly Extraction.

 Robotics and Automation, 1990. Proceedings., 1990 IEEE International

 Conference on, 3, 1606-1611.
- Liu, L., & Cheng, K.L. (1997). Service constrained inventory models with random lifetimes and lead times. *Journal of the Operational Research Society*, 48, 1022-1028.
- Logendran, R., & Sonthinen, A. (1997). A Tabu search-based approach for scheduling job-shop type flexible manufacturing systems. *Journal of the Operational Research Society*, 48, 264-277.
- Lozano, S., Adenso-Diaz, B., Eguia, I., & Onieva, L. (1999). A one-step Tabu search algorithm for manufacturing cell design. *Journal of the Operational Research Society*, 50, 509-516.
- Malakooti, B.B. (1994). Assembly line balancing with buffers by multiple criteria optimization. *International Journal of Production Research*, 32(9), 2159-2178.
- Mansoor, E.M. (1961). Selective assembly it's analysis and applications. *International Journal of Production Research*, *I*(1) 13-24.

- Markland, R.E. (1990). Commentary discussant's comments: 'artificial intelligence, heuristic frameworks and Tabu search. *Managerial and Decision Economics*. 11, 377-378.
- Mazzola, J.B., & Schantz, R.H. (1995). Single-facility resource allocation under capacity-based economies and diseconomies of scope. *Management Science*, 41(4), 669-689.
- Mease, D., Nair, V., & Sudjianto, A. (2004). Selective assembly in manufacturing: statistical issues and optimal binning strategies. *Technometrics*, 46(2), 165-175.
- Meller, R.D., & Bozer, Y.A. (1996). A new simulated annealing algorithm for the facility layout problem. *International Journal of Production Research*, 34(6), 1675-1692.
- Michalewicz, Z., & Fogel, D. (1998). How to Solve it: Modern Heuristics (2nd ed.). New York, NY: Springer.
- Moccellin, J.V., & Nagano, M.S. (1998). Evaluating the performance of Tabu search procedures for flow shop sequencing. *Journal of the Operational Research Society*, 49, 1296-1302.
- Moorhead, P.R., & Wu, C.F.J. (1998). Cost-driven parameter design. *Technometrics*, 40(2), 111-119.

- Musa, R. (2007). New Strategic and Dynamic Variation Reduction Techniques for Assembly Lines (Doctoral dissertation). Available from: http://scholar.lib.vt.edu/theses/available/etd-04192007-114716/unrestricted/DissRMusa3.pdf
- Musa, R., & Chen, F.F. (2008). Simulated annealing and ant colony optimization algorithms for the dynamic throughput maximization problem. *International Journal of Advanced Manufacturing Technology*, 37, 837-850.
- Musa, R., & Chen, F.F. (undated). Hybrid implementation of agile inspection planning and dynamic throughput maximization. *Virginia Polytechnic Institute and State University*, 1-12.
- Musa, R., Chen, F.F., & Ghoniem, A. S. (undated). Dynamic variation reduction and throughput maximization in assembly lines after batch inspection. *Virginia Polytechnic Institute and State University*, 1-6.
- Musa, R., Sturges, R. H., & Chen, F. F. (2006). Agile inspection planning based on CAD-data. Computer-Aided Design & Applications, 3(1-4), 69-78.
- Naddor, E. (1975). Optimal heuristic decisions for the s, s inventory policy. *Management Science*, 21(9), 1071-1072.

- Nair, S.K., Thakur, L.S., & Wen, K-W (1995). Near optimal solutions for product line design and selection: beam search heuristics. *Management Science*, 41(5), 767-785.
- NIST/SEMATECH e-Handbook of Statistical Methods. (2014). Product and Process

 Comparisons. Retrieved from:

 http://www.itl.nist.gov/div898/handbook/toolaids/pff/prc.pdf
- Nussbaum, M., Sepúlveda, M., Singer, M., & LavalFE. (1998). An architecture for solving sequencing and resource allocation problems using approximation methods.

 **Journal of the Operational Research Society, 49, 52-65.
- Ohlemüller, M. (1997). Tabu search of large location-allocation problems. *Journal of the Operational Research Society*, 48, 745-750.
- Ohtsubo, Y. (2004). Optimal threshold probability is undiscounted markov decision processes with a target set. *Applied Mathematics and Computation*, 149, 519-532.
- Ostermeier, M. (2003). Theoretical distribution of truncation lengths in incremental truncation libraries. *Biotechnology and Bioengineering*, 82(5), 565-577.
- Park M.W., & Kim Y.D. (1999). A heuristic algorithm for a production planning problem in an assembly system. *Journal of the Operational Research Society*, 50, 138-147.

- Park, K., Kang, S., & Park, S. (1996). An Integer Programming Approach to the Bandwidth Packing Problem. *Management Science*, 42(9), 1277-1291.
- Patterson, R.A., & Rolland, E. (2002). Hybrid Fiber Coaxial Network Design. *Operations Research*, 50(3), 538-551.
- Peng, L., & Qi, Y. (2009). Maximum likelihood estimation of extreme value index for irregular cases. *Journal of Statistical Planning and Inference*, 139, 3361-3376.
- Phoomboplab, T., & Ceglarek, D. (2007). Design synthesis framework for dimensional management in multistage assembly system. *CIRP ANNALS-Manufacturing*Technology, 56(1), 153-158.
- Ponnambalam, S.G., Aravindan, P., & Rao, M.S. (2003). Genetic Algorithms for sequencing problems in mixed model assembly lines. *Computer & Industrial Engineering*, 45, 669-690.
- Pourbabai, B. (1989). Optimal selection of the local storage sizes of an assembly system.

 International Journal of Production Research, 27(9), 1625-1636.
- Pourbabai, B. (1992). Minimum required local storages of an automated assembly system. *Journal of the Operational Research Society*, 43(2), 95-109.

- Puelz, A.V. (2002). A stochastic convergence model for portfolio selection. *Operations Research*, 50(3), 462-476.
- Pugh, G.A. (1986). Partitioning for selective assembly. Computers & Industrial Engineering, 11 (1-4), 175-179.
- Pugh, G.A. (1992). Selective assembly with components of dissimilar variance.

 Computers and Industrial Engineering, 21(1-4), 487-491.
- Punnen, A.P., & Aneja, Y.P. (1995). A Tabu search algorithm for the resource constrained assignment problem. *Journal of the Operational Research Society*, 46, 214-220.
- Ramirez-Beltran, N.D. (1995). Integer programming to minimize labour costs. *Journal of the Operational Research Society*, 46, 139-146.
- Raschke, M. (2012). Inference for the truncated exponential distribution. *Stochastic Environmental Research and Risk Assessment*, 26, 127-138.
- Rochat, Y., & Semet, F. (1994). A Tabu search approach for delivering pet food and flour in Switzerland. *Journal of Operational Research Society*, 45(11), 1233-1246.

- Rubin, P.A. (1990). Heuristic solution procedures for a mixed-integer programming discriminant model. *Managerial and Decision Economics*, 11, 255-266.
- Salhi, S. (1997). A perturbation heuristic for a class of location problems. *Journal of the Operational Research Society*, 48, 1233-1240.
- Sanderson, A.C. (1997). Assemblability based on maximum likelihood configuration of tolerances. *IEEE Transactions on Robotics & Automation*, 15(3), 568-572.
- Seidmann, A., & Tenenbaum, A. (1994). Throughput maximization in flexible manufacturing systems. *IIE Transactions*, 26(1), 90-100.
- Sheffield, S. (2011). MIT Open Courseware, 18.440, Lecture 27, Moment Generating

 Functions and Characteristic Functions. Retrieved from MIT, Website:

 http://ocw.mit.edu/courses/mathematics/18-440-probability-and-random-variablesspring-2011/lecture-notes/MIT18_440S11_Lecture27.pdf
- Shephard, N.G. (1992). From characteristic function to distribution function: a simple framework for the Theory. *Econometric Theory*, 7, 519-529.

- Simpson, D. P. (2008). Krylov subspace methods for approximating functions of symmetric positive definite matrices with applications to applied statistics and anomalous diffusion (Doctoral dissertation). Available from http://eprints.qut.edu.au/29751/
- So, K.C., & Scott, C.H. (1994). Optimal production sequence for a product with matching components. *Operations Research*, 42(4), 694-708.
- Stinivasa Varadhan, S.R. (2000). Characteristic Functions. Retrieved from New York
 University, Mathematics Department Website:

 http://www.math.nyu.edu/faculty/varadhan/course/PROB.ch2.pdf
- Stoyanov, S., & Rachev, S. (2008). Asymptotic distribution of the sample average valueat-risk. *Journal of Applied Functional Analysis*, 3(4), 443-460.
- Thakur, L.S., Nair, S.K., Wen, K-W, & Tarasewich, P. (2000). A new model and solution method for product line design with pricing. *Journal of the Operational Research Society*, 51, 90-101.
- Weisstein, E.W. (1999-2014). Normal Sum Distribution. Retrieved from MathWorld--A
 Wolfram Website: http://mathworld.wolfram.com/NormalSumDistribution.html

- Whitney, D. E. (2004), *Mechanical Assemblies*. New York, NY: Oxford University Press, Inc.
- Whitney, D. E. (2006). The role of key characteristics in the design of mechanical assemblies. *Assembly Automation*, 26(4), 315-322.
- Wilson, I.D., & Roach, P.A. (2000). Container stowage planning: a methodology for generating computerized solutions. *Journal of Operational Research Society*, 51, 1248-1255.
- Xiaoping, B. & Jingjing, M. (2009). Research on availability model and algorithm of complex storage bin belt transportation system. Electronic Commerce and Business Intelligence, 2009. ECBI 2009. International Conference on, 180-183.
- Xiaoping, B. & Jingjing, M. (2009). Study of Control Optimization Methodologies for Storage Bin Capacity in Transport System. *Industrial Mechatronics and Automation*, 2009. ICIMA 2009. International Conference on, 72-75.
- Yang, C., Gui, W., Kong, L., & Wang, Y. (2009). Modeling and optimal-setting control of blending process in a metallurgical industry. Computers and Chemical Engineering, 33, 1289-1297.

- Zhang, W.Z., Wang, G.X., Cheok, B.T., & Nee, A.Y.C. (2003). A functional approach for standard component reuse. *International Journal of Advanced Manufacturing Technology*, 22, 141-149.
- Zhu, Q., & Oommen, J. (1997). On the optimal search problem: the case when the target distribution is unknown. Computer Science Society, 1997. Proceedings., XVII

 International Conference of the Chilean, 268-277.

APPENDICES

APPENDIX A: EQUATIONS

This appendix documents the equations utilized as part of the truncated standard normal distribution analysis used by the research. This section provides general and specific equations used for the evaluation of truncated standard normal distributions and corresponding assemblies. The following equations were generally or specifically applied in this dissertation and heuristic procedures documented in Appendices I and J.

General Equations:

$$f_T(z) = \int_{z_L}^{z} \frac{f(z)}{\left(\int_{z_L}^{z_U} f(z)dz\right)} dz, \ z_L \le z \le z_u$$
 (EQUATION I)

Equation 1 Reference: Khasawneh et al. (2005)

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}*z^2\right)}$$
 (EQUATION 2)

Equation 2 Reference: Khasawneh et al. (2005)
$$f(z)dz = \int_{z_{L}}^{z_{C}} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2} + z^{2}\right)} dz$$

$$f(z)dz = \int_{z_{L}}^{z_{C}} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2} + z^{2}\right)} dz$$
(EQUATION 3)

Equation 3 Reference: Khasawneh et al. (2005)

$$z = \frac{x - \mu}{\sigma}$$
 (EQUATION 4)

Equation 4 Reference: Khasawneh et al. (2005)

$$\mu_{T_1}(z) = \int_{z_{t_1}}^{z_{t_1}} z f_{T_1}(z) dz$$
 (EQUATION 5)

Equation 5 Reference: Khasawneh et al. (2005)

$$f(x;\mu,\sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\left(\frac{(x-\mu)^2}{2\sigma^2}\right)}$$
 (EQUATION 6)

Equation 6 Reference: Johnson et al. (undated) and Billingsley (1995), adapted

$$\varphi(t) = \varphi_x(t) := E[e^{itX}] = \int_{-\infty}^{\infty} e^{itx} \mu(dx)$$
 (EQUATION 7)

Equation 7 Reference: Billingsley (1995)

$$[e^{itX}] = \cos(t) + i\sin(t)$$
 (EQUATION 8)

Equation 8 Reference: Sheffield (2011)

$$\varphi_{y}(\tau) := \frac{1}{F_{x}(b) - F_{x}(a)} \int_{a}^{b} f_{x}(u)e^{iu\tau} du$$
 (EQUATION 9)

Equation 9 Reference: Abadir et al. (2002)

$$\boldsymbol{\varphi}_{X+Y} = \boldsymbol{\varphi}_X \boldsymbol{\varphi}_Y$$
 (EQUATION 10)

Equation 10 Reference: Sheffield (2011) and Billingsley (1995), adapted

$$\varphi(t) = \int_{a}^{b} f_x(u)e^{iu\tau}du = e^{iu\tau - \frac{\sigma^2r^2}{2}}$$
(EQUATION 11)

Equation 14 Reference: Srinivasa Varadhan (2000)

CF Inversion Equations:

$$\varphi(\tau) = \frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du$$
 (EQUATION 12)

Equation 15 Reference: Adapted from Equation 9 with slight nomenclature change

$$\varphi(\tau) = \frac{e^{iu\tau - \frac{\sigma^2 t^2}{2}}}{F_x(b) - F_x(a)}$$
(EQUATION 13)

Equation 16 Reference: By inspection a combination of Equations 11 and 12

$$f_t(x) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \varphi(\tau) dt$$
 (EQUATION 14)

Equation 17 Reference: Billingsley (1995)

$$f_{t}(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left(\frac{e^{ia\tau - \frac{\sigma^{2}t^{2}}{2}}}{F_{x}(b) - F_{x}(a)} \right) dt$$
(EQUATION 15)

Equation 18 Reference: By inspection the incorporation of Equation 13 into Equation 14

$$f_t(x) \approx \frac{1}{2\pi} \left(C_{\tau_c} \right) \left(\frac{e^{\frac{-\sigma^2 x^2}{2}}}{F_x(b) - F_x(a)} \right)$$
, where $C_{TC} = \frac{1}{\sqrt{2\pi}}$ (EQUATION 16)

Equation 16 Reference: Solved by the author by setting Equation 1 equal to Equation 15. C_{TC} = Equation 15 results/ Equation 1 results for a given z value. See Equation 17

$$f_{t}(z) \approx \frac{1}{2\pi} \left(C_{Tc} \right) \left(\frac{e^{-\frac{\sigma^{2}z^{2}}{2}}}{F_{x}(b) - F_{x}(a)} \right) \approx \int_{z_{L}}^{z} \frac{f(z)}{\int_{z_{L}}^{z_{U}} f(z) dz} dz$$
(EQUATION 17)

, where
$$C_{TC} = \frac{1}{\sqrt{2\pi}}$$

Equation 17 Reference: Set Equation 16 equal to Equation 1. This baselines this equation by this author and identifies C_{TC}

For an Assembly:

Given Equation 14

And
$$\varphi_z(\tau) := \left(\frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du\right) \left(\frac{1}{F_y(b) - F_y(a)} \int_a^b f_y(u) e^{iu\tau} du\right)$$
 (EQUATION 18)

Equation 18 Reference: Solved by applying equation 10 and 12 and via inspection. $\varphi_z = \varphi_x + \varphi_y$

Then
$$f_t(z)_{assy} = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left[\left(\frac{e^{iu\tau - \frac{\sigma^2 z^2}{2}}}{F_x(b) - F_x(a)} \right)_{d1} \left(\frac{e^{iu\tau - \frac{\sigma^2 z^2}{2}}}{F_x(b) - F_x(a)} \right)_{d2} \right] dt$$
 (EQUATION 19)

Equation 19 Reference: Solved by applying Equations 14 and 21 and via inspection. Where d1 is distribution one and d2 is distribution two.

$$\therefore f_t(z)_{assy} = \frac{1}{2\pi} \left(\frac{1}{(F_x(b) - F_x(a))_{d1} * (F_x(b) - F_x(a))_{d2}} \right) \int_{-\infty}^{\infty} e^{-itx} \left[e^{iux - \frac{\sigma^2 t^2}{2}} \right]_{t0} \left(e^{iux - \frac{\sigma^2 t^2}{2}} \right)_{t0} dt \qquad \text{(EQUATION 20)}$$

Equation 20 Reference: Continuation of Equation 19

Where
$$f(x) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left[e^{iu\tau - \frac{\sigma^2 t^2}{2}} \right] dt = e^{-\frac{\sigma^2 t^2}{2}}$$
 (EQUATION 21)

Equation 21 Reference: Applied from Billingsley (1995), Equation 11, and Equation 14. For comparison $\sigma=1$ would result in a inversion of CF similar to Billingsley (1995) Equation 26.21. Adjust for z.

$$\therefore f_{t}(z)_{assy} \approx \frac{1}{2\pi} \left(C_{TC}\right) \left(\frac{\left(\frac{\sigma^{2}r^{2}}{e^{-\frac{r^{2}}{2}}}\right) \left(\frac{\sigma^{2}r^{2}}{e^{-\frac{r^{2}}{2}}}\right)}{\left(F_{x}(b) - F_{x}(a)\right)_{d1} * \left(F_{x}(b) - F_{x}(a)\right)_{d2}}\right), \text{ where } C_{TC} = \frac{1}{\sqrt{2\pi}}$$
 (EQUATION 22)

Equation 22 Reference: Solved by this author by applying the Equation 17 approach with Equation 20 and 21. Assumes C_{TC} remains constant given Equations 10 and 11. Given the values for $\sigma = 1$, $\mu = 0$ the values of x and z and therefore are interchangeable in the notation for this example.

Appendix B, Table B.1 identifies the following variables not cited in the Nomenclature Section of this work. They following calculated variables are identified:

- "f_I(z) Standard" is identified as a truncated standard normal distribution where (σ = 1, μ = 0).
 Results in this column reflect calculations using Equations 1-5 in Appendix A.
- "ft(z) ASSY" is identified as a truncated standard normal distribution assembly, where ($\sigma = 1$, $\mu = 0$)
- " $f_T(z)$ adj. stdev" is identified as a truncated standard normal distribution assembly where ($\sigma = \sqrt{{\sigma_1}^2 + {\sigma_2}^2} = 1.414214$, $\mu = 0$)
- "NORMPDFASSY" is identified as a normal distribution (i.e., Equation 2), where $(\sigma = 1, \mu = 0)$.
- "PDFASSY" is identified as a normal distribution (i.e., Equation 2), where $(\sigma = \sqrt{{\sigma_1}^2 + {\sigma_2}^2} = 1.414214, \mu = 0)$.
- "Ratio 1" is identified as ft(z) ASSY/NORMPDFASSY
- "Ratio 2" is identified as fT(z)/NORMPDFASSY
- "Ratio 3" is identified as fT(z)/ft(z) ASSY
- "Ratio 4" is identified as ft(z) ASSY/PDFASSY
- "Ratio 5" is identified as fT(z)/PDFASSY

APPENDIX B: TSND ANALYSIS RESULTS

This appendix documents the results summary for TSND analysis performed as part of this dissertation. The results include mathematical results and also evaluate various ratios generated using the equations and research steps from Appendix A.

Tabular results include the combinatorial rang of assemblies for identical truncated standard normal distribution combinations ranging from specification limits of -4 to 4.

Table B.1 summarizes the TSND results of this research.

Table B.1 – TSND Analysis Results

Range	DISTRIBUTION 1 µ = 0, o=1, Ctc = 0.39694228, USLASE (unless otherwise noted)				Ctc # 0.39694228,				ASSY \[\mu = 0, \pi = 1, \text{Ctc} = 0.3989422\$\$, USL/LSL (unless otherwise noted)					RATIOS						
Sumilation Number	λ	pdf	φ.(w· μιδα)	ft(z)	X	palf	p(n µ&a)	ft(x)	х	9-(w µ&б)	ft(z) ~ ASSY	f _H z) - ad _t . stdev μ = 0. σ=1 4142	f ₁ (z) Standard	NORMPDF ASSY	PDFASSY	Rano t fi(z) - ASSY NORM PDFASSY	Ratio 2 ff(z) NORMPDFA SSY	Ratio 3 ff(z) ft(x) = ASSY	Rano 4 ft(z) - ASSY PDI-ASSY	Rano 5 fVc) PDFASSU
ı	-4	0 00013383	0.00033548	0 00013384	-4	0.00013383	0.00033548	0.00013384	-8	1 1255E-07	4.49E-08	3 1746E-08	5.05E-15	5.05227E-15	3.1746E-08	1.12521E-07	1.59149E-07	1 12521E-07	1 \$9149E-07	0 99999985
2	-) 9	0 00019866	0.00049799	0 00019867	-3.9	0.00019866	D 00049799	0 00019867	-7.B	2.4799E-07	9.89332-08	6 9948E-08	2.45E-14	2.45286E-14	6 9948E-08	2 47928E-07	3.506688-07	2.47928E-07	3 50668E-07	0.999999985
3	-38	0 00029195	0.00073185	0 00029197	-38	0.00029195	0.00073185	0.00029197	-76	5 356E-07	2 137E-07	1.5107E-07	1.14E-13	1.14416E-13	1.5107E-07	5 35467E-07	7.573o1E-07	5.35467E-07	7 57361E-07	0.999999985
4	-3.7	0.00042478	0.00106483	0.00042481	-3.7	0.00042478	0.00106483	0.00042481	-74	1.1339E-06	4.523E-07	3 1982E-07	5.13E-13	5 12775E-13	3 1982E-07	1.1335 8E-0 6	1.60133E-06	1,13358E-06	1.60333E-06	0.999999985
5	-3.6	0.0006119	0.00153391	0.00061194	-3.6	0.0006119	0 00153391	0.00061194	-72	2.3529E-06	9 387E-07	6 6365E-07	2 21E-12	2 20799E-12	6 6365E-07	2.35228E-06	3 32704E-06	2 35228E-06	3 32704E-06	0.999999985
6	-3.5	0.00087268	0.00218763	0 00087274	-3.5	0 00087268	0.00218763	0.00087274	-7	4 7857E-06	1 909E-06	1.3499E-06	9.13E-12	9 13472E-12	1 3499E-06	4.78451E-06	6 76718E-06	4.78451E-06	6 7671 8 F-06	0 999999985
7	-3.4	0 00123222	0.00308891	0 0012323	-3.4	0 00123222	0 00308891	0.0012323	-68	9.5414E-06	3 806E-06	2 6912E-06	3 63E-11	3 63096E-11	2 6912E-06	9 53895E-06	1.34918E-05	9 53895E-06	1 34918E-05	0.99999985
8	-33	0 00172257	0 00431811	0.00172268	-3.3	0 00172257	0.00431811	0.00172268	-66	1.8646E-05	7 439E-06	5 2593E-06	1 39E-10	1.38668E-10	5 2593E-06	1 86414E-05	2.63662E-05	1.86414E-05	2 63662E-05	0.999999985
ò	-3.2	0 00238409	0.0059764	0.00238424	-32	0 00238409	0.0059764	0.00238424	-6.4	3.5717E-05	1 425E-05	1.0074E-05	5 09E-10	5 08814E-10	1.0074E+05	3 57083E-05	5.05056E-05	3 57083E-05	5 05056E-05	0.999999985
10	-3.1	0 00326682	0.00818922	0 00326703	-3 1	0.00326682	0.00818922	0.00326703	-6.2	6.7063E-05	2 675E-05	1.8916E-05	1 79E-09	1 79378E-09	1 8916E-05	6 70463E-05	9.48298E-05	6.70463E-05	9 48298E-05	0.999999985
	-3	0.00443185	0.0111097	0 00443213	-3	0 00443185	0.0111097	D 00443213	-6	0.00012,343	4.924E-05	3 4813E-05	6.08E-09	6.07588E-09	3.4813E-05	0 000123394	0.000174528	0 000123394	0.000174528	0 999999985
12	-2.9	0.00595253	0.01492173	0 00595291	-29	0 00595253	0 01492173	0.00595291	-58	0.00022266	8 883E-05	6.2803E-05	1 98E-08	1.97732E-08	6 2803E-05	0 000222602	0 000314846	0.000222602	0.000314846	0 999999985
13	-2 8	0.00791545	0,01984235	0 00791595	-28	0.00791545	0.01984235	0 00791595	-5 b	0 00039372	0 0001571	0.00011105	6 18E-08	6.18262E-08	0.00011105	0.000393619	0.00055e732	0 000393619	0 000556732	0.999999985
14	-2.7	0.01042091	0.02612306	0.01042159	-27	0.01042093	0.02612306	0.01042159	-5.4	0.00068241	0 0002722	0.00019248	1 86E-07	1.85736E-07	0 00019248	0 000682242	0 000964958	0 000682242	0 000964958	0.999999985
15	-2.6	0.01358297	0.03404961	0.01358383	-2.6	0,01358297	0.03404961	0 01358383	-5.2	0.00115938	0.0004625	0.00032701	5 36E-07	5.36104E-07	0.00032701	0 001159082	0.001639398	0.001159082	0.001639398	0.999999985
16	-2.5	0.0175283	0.04393972	0.01752941	-2.5	0.0175283	0.04393972	0.01752941	-5	0.0019307	0 0007702	0.00054457	t 49E-06	1 48672E-06	0 00054457	0.00193021	0 002730074	0.00193021	0.002730074	0 999999985
17	-2 4	0 02239453	0.05613832	0.02239595	-24	0.02239453	0.05613832	0.02239595	-48	0.00315151	0 0012573	0.00088891	3 96E-06	3 9613E-06	0.00088891	0 003150712	0 004456345	0 003 150712	0 004456345	0 999999985
18	-2.3	0.02832704	0.07100985	0.02832883	-2 3	0.02832704	0.07100985	0 02832883	-46	0 0050424	0.0020116	0.00142225	1 01E-05	1 01409E-05	0 00142325	0 005041122	0 007130126	0.005041122	0.007130126	0 999999985
19	-2.2	0.03547459	0.08892725	0 03547684	-2.2	0,03547459	0.08892725	0.03547684	-44	0 00790806	0031549	0.00223054	2 49E-05	2 49425E-05	0.00223054	0.007906052	0.011182263	0.007906052	0 011182263	0 999999985
20	2	0 (1439836	0 11025751	U 04398638	-2.1	0.6439836	0.11025751	0.04398638	-4.2	0.01215672	0.0048498	0 00342891	5.89E-05	5 89431E-05	0 00342891	0.012153639	0.017190018	0 012153639	0.017190018	0 999999985
21	?	0.05399097	0.13534386	0.05399439	-2	0.05399097	0 13534386	0.05399439	-4	0.01831796	0 0073078	0 005 16675	0.000134	0.00013383	0.00516675	0 018313319	0 025902225	0 018313319	0 025902225	0 999999985
22	-19	0.06561581	0.16448488	0.06561997	-19	0.06561581	0 16448488	0.06561997	-3 8	0.02705527	0 0107935	0.00763119	0.000292	0 000291947	0.00763119	0.02704842	0.038257088	0.02704842	0.038257088	0 999999985
23	-1.8	0 0789501ь	0.19791124	0 07895516	-1.8	0.07895016	0.19791124	0.07895516	-36	0.03916886	0,0156261	0.01104793	0.000612	0 000611902	0.01104793	0 039158934	0.055386111	0 039158934	0,055386111	0 999999985
24	-1.7	0.09404908	0.23576101	0.09405504	-17	0.09404908	0.23576101	0 09405504	-3 4	0.05558325	0.0221745	0.01567776	0 001232	0 001232219	0.01567776	0.055569172	0.078596632	0 055569172	0.078596632	0.999999985
25	-1.6	0.11092083	0.27805491	0.11092786	-1.6	0.11092083	0.27805491	0.11092786	-3.2	0.07731453	0.030844	0.02180726	0.002384	0.002384088	0.02180726	0 077294947	0 109325411	0 077294947	0 109325411	0 999999985
26	-1.5	0 1295176	0.32467303	0 1295258	-15	0 1295176	0.32467303	0.1295258	-3	0 10541258	0 0420535	0.02973257	0 004432	0.004431848	0.02973257	0.105385872		0.105385872	0 149057011	0 99999985
27	-1.4	0.14972747	0.37533487	0.14973695	-14	0.14972747	0.37533487	0.14973695	-2.8	0 14087627	0.0562015	0.03973543	0.007915	0.007915452	0 03973543	0 140840577	0 199203886	0 140840577	0.199203886	
28	-13	0 17136859	0 42958457	0 17137945	-13	0.17136859	0.42958457	0 17137945	-2.6	0 1845429	0 073622	0.052052	0.013583	0.013582969	0.052052	0 184496149	0 260950009	0.184496149	0 260950009	0.99999985
29	-12	0 19418605	0 48678309	0 19419836	-12	0 19418605	0 48678309	0 19419836	-2.4	0.23695778	0 0945325	0 06683609	0.022395	0 02239453	0.06683609	0.236897744		0 236897744		U.99999985
30	-11	0.21785218	0 54610902	0 21786598	-11	0 21785218	0 54610902	0.21786598	-2.2	0.29823506	0 1189786	0.0841199	~~~~	0 035474593	0.0841199	0.298159504	0 42171463	0.298159504	0 42171463	0 999999985
31	-	0.24197072	0.60656908	0 24198605	-1	0.24197072	0 60656908	0.24198605	-2	0.36792605	0 1467813	0 10377688	0.053991	0.053990967	0 10377687	0.367832838	0 520260087	0,367832838		0.99999985
32	-0.9	0.26608525	0.66701906	0.26610211	-09	0 26608525	0 66701906	0.26610211	-1.8	0.44491443	0 1774952	0 12549235	0 07895	0.078950158	0.12549214	0.444801711	0.629124301	0.444801711	0.629124301	0 999999985
33	-0. 8	0.28969155	0.72619504	0 2897099	-0.8	0.28969155	0 72619504	0.2897099	-1.6	0.52735923	0 2103859	0 14874645		0.110920835	0.14874645	0.527225626	0 745704086	0.527225626	0 745704086	
34	-0.7	0 31225393	0 78275412	0.31227371	-07	0.31225393	0.78275412	0.31227371	-1.4	0.61270401	0.2444335	0 17281872	₩	0 149727466	0.17281872	0 612548786	0.866384542	0.612548786	0 866384542	
35	-0.6	0 3332246	0.83532312	0 33324571	-0.6	0 3332246	0.83532312	0.33324571	-1.2	0.69776472	0.2783678		0.194186	0.194186055	0.19681086	0 697587944		0.697587944		0.999999985
36	-05	0.35206533	0 88255281	0 35208763	-0.5	0.35206533	0.88255281	0 35208763	-!	0.77889945	0.3107359	0.21969565	0.241971	0.241970725	0.21969564	0 778702124	+	0 778702124		0.99999985
37	-0.4	0.36827014	0.92317482	0.36829347	-04	0.36827014	0.92317482	0 36829347	-0.8	0.85225175	0.3399993	0.24038533	0 289692	0 289691553	0.24038532	0 852035839	1 205113285	0 852035839	1 205113285	0.99999985
38	-0.3	0.38138782	0.95605804	0 38141198	-03	0.38138782	0.95605804	0.38141198	-0.6	0.91404698	0 364652	0.25781523	0.333225	0.333224603	0.25781523	0 913815408		0.913815408		0.99999985
39	-0.2	0.39104269	0 98026077	0 39106747	-02	0.39104269	0,98026077	0 39106747	-D 4	0.96091117	0.3833481	0 2710337	0.36827	0.36827014	0.2710337	0 960667725	1 358761434	0 960667725	1 358761434	0 999999985

40	-01	0.39695255	0 99507551	0.39697769	-0.1	0.39695255	0.99507551	0.39697769	-0.2	0.99017527	0 3950228	0.27928791	0 391043	0.391042694	D 2792879	0 989924413	1 400141881	0 989924413	1 40014 (88)	0 999999985
41	Û	0.39894228	1 00006335	0 39896755	0	0.39894228	1 00006335	0.39896755	Ω	1 0001267	0 3989928	0 2820948	0 398942	0 39894228	0.28209479	0 999873319	1 414213541	0 999873319	1 414213541	0 999999985
42	ÐΙ	U 39695255	0 99507551	0 39697769	0.1	0 39695255	0.99507551	0.39697769	0.2	0.99017527	0 3950228	0 27928791	0.391043	0 391042694	0 2792879	0 989924413	1 400141881	0.989924413	1 400141881	0 999999985
43	02	0 39104269	0 98026077	0 39106747	0.2	0 39104269	0 98026077	0 39106747	0.4	0 96091117	0.3833481	0 2710337	0 36827	0.36827014	B 2710337	0 960667725	1 358761434	0.960667725	1 358761434	0 999999985
44	0.3	0 38138782	0 95605804	0 38141198	0.3	0 38138782	0.95605804	0 38141198	0.6	0 91404698	0.364652	0 25781523	0.333225	0 333224603	0.25781523	0 913815408	1 292493857	0 913815408	1 292493857	0 999999985
45	0.4	0.36827014	0 92317482	0 36829347	04	0.36827014	0.92317482	0.36829347	0.8	0.85225175	0.3399993	0 24038533	0 289692	0 289691553	0 24038532	0 852035839	1 205110285	0 852015839	1 205113285	0 999999985
46	0.5	0.35206533	0 88255281	0.35208763	0.5	0 35206533	0 88255281	0 35208763	1	0 77889945	0 3107359	0.21969565	0 24 1971	0 241970725	0.21969564	0 778702124	1 101390613	0.778702124	1 101390613	0 999999985
47	0.6	0 3332246	0 83532312	0.33324571	06	0 3332246	0 83532312	0 33324571	1.2	0.69776472	0 2783678	0.19681086	0 194186	0 194186055	0 19681086	0 697587944	0 986663307	0.697587944	0 986663307	0 999999985
48	07	0.31225393	0 78275412	0 31227371	0.7	0.31225393	0.78275412	0.31227371	1.4	0,61270401	0 2444335	0 17281872	0 149727	0 149727466	0 17281872	0.612548786	0.866384542	0 612548786	0 866384542	-
49	0.8	0.28969155	0.72619504	0 2897099	0.8	0 28969155	0 72619504	0 2897099	16	0 52735923	0 2103859	D.14874645	0.110921	0 110920835	0 14874645		0 745704086	0 527225626	0 745704086	
50	0.9	0.26608525	0.66701906	0.26610211	0.9	0.26608525	0 66701906	0.26610211	18	0.44491443	0 1774952	0 12549215	0.07895	0 078950158			0 629124301	0 444801711		0 999999985
- 51	1	0.24197072	0.60656968	0 24198605	1	D 24197072	0 60656908	0 24198605	2	0.36792605	0 1467813	0 10377688	0 053991	0.053990967	0.10377687	0.367832838	0.520260087	0 367832838		-0 999999985
52	11	0 21785218	0 54610902	0.21786598	11	0 21785218	0.54610902	0.21786598	22	0 29823506	0 1189786	0.0841199	0 035475	0.035474593	0.0841199	0.298159504	0.42171463	0 298159504	0.42171463	0 999999985
53	12	0 19418605	0 48678309	0 19419836	12	0 19418605	0.48678109	0 19419836	24	0 23695778	0.0945325	0 06683609	0 022395	0 02239453			0.335066444	_		
54	13	0 17136859	0 42958457	0 17 37945	13	0 17136859	0.42958457	0 (7137945	2.6	0 1845429	0 073622	0.052052	0 013583	0 013582969	0.052052		0,260950009	0 184496149		
55	14	0 14972747	0 37533487	0 14973695	14	0 14972747	0 37533487	0 14973695	28	0 14087627	0 0562015	0 03973543	0.007915	0 007915452	0 03973543		0 199203886			
. 56	1.5	0.1295176	0 32467303	0 1295258	1.5	0 1295176	0 32467303	0.1295258	3	0 10541258	0.0420535	0.02973257	0.004432	0 004431848			0 149057011		0 149057011	
57	16	0 11092083	0 27805491	0 11092786	16	0.11092083	0 27805491	0 11092786	3 2	0 07731453	0 030844	0.02180726	0.002384	0.002384088	0.02180726	0.077294947	0 109325411	0 077294947	0 1093254)1	
58	17	0.09404908	0.23576101	0.09405504	17	0 09404908	0.23576101	0.09405504	34	0.05558325	0 0221745	0.01567776	0.001232	0 001232219	0.01567776	0.055569172	0 078596632	0.055569172	0.078596632	
59	18	0 07895016	0 19791124	0.07895516	1.8	0.07895016	0 19791124	0.07895516	36	0 03916886	0.0156261	0.01104793	0.000612	0.000611902	0.01104793	0.039158914		0 039158934		
60	1.9	0.06561581	0.1644848B	0.06561997	1.9	0 06561581	0 16448488	0.06561997	38	0.02705527	0.0107935	0.00763119	0 000292	0.000291947	0.00763119	0 02704842	0 038257088	0.02704842	0.038257088	
٥l	2	0.05399097	0 13534386	0.05399439	2	0,05399097	0 13534386	0.05399439	4	0.01831796	0.007307B	0.00516675	0.000134	0 00013383	0.00516675	0.018313319	0.025902225	0 018313319	0.025902225	0.999999985
62	21	0 0439836	0 11025751	0.04398638	2.1	0.0439836	0.11025751	0.04398638	42	0.01215672	0 0048498	0.00342891	5.89E-05	5 8943 (E-05	0,00342891	0.012153639	0.017190018	0.012153639	0.017190018	0 999999985
63	2.2	0 03547459	0.08892725	0.03547684	2.2	0.03547459	0.08892725	0.03547684	4.4	0 00790806	0.0031549	0 00223054	2.49E-05	2 49425E-05	0,00223054	D 007906052	0 011182263	0.007906052	0 011182263	0.999999985
64	2.3	0 02832704	0.07100985	0.02832883	23	0.02832704	0.07100985	0.02832883	4.6	0 0050424	0 0020116	0.00142225	1.01E-05	1 01409E-05	0.00142225	0 005041122	0 007130126	0.005041122		
65	24	0 02239453	0.05613832	0.02239595	24	0.02239453	0 05613832	0 02239595	4.8	0.00315151	0 0012573	0 00088891	3 96E-06	3 9613E-06	0 00088891	0 003150712	0 004456345	0 003150712	0.004456345	n 9999999B5
66	2.5	0.0175283	0.04393972	0 01752941	2.5	0.0175283	0 04391971	0.01752941	5	0.0019307	0.0007702	0.00054457	I 49E-06	1 48672E-06	0 00054457	0 00193021	0 002730074	0.00193021		
67	26	0.01358297	0.03404961	0.01358383	2.6	0.01358297	0 03404961	0.01358383	5.2	0.00115938	0 0004625	0.00032701	5 36E-07	5 36104E-07	0.00032701	0.001159082	0.001639398	0.001159082	0 001639398	0 999999985
68	2.7	0.01042093	0 02612306	0.01042159	2.7	0.01042093	0 02612306	0.01042159	54	0.00068241	0 0002722	0 00019248	1 86E-07	1 85736E-07	0 00019248	0 000682242	0.000964958	0 000682242	0 000964958	0 999999985
69	28	0.00791545	0.01984235	0.00791595	2.8	0.00791545	0.01984235	0.00791595	5,6	0 00039372	0 0001571	0.00011105	o 18E-08	6 18262E-08	0.00011105	0.000393619	0.000556732			
70	2.9	0.00595253	0 01492173	0.00595291	2.9	0 00595253	0.01492173	0.00595291	5.8	0.00022266	8.883E-05	6.2803E-05	1 98E-08	1 97732E-08	6 2803E-05		0 000314846		0 000314846	
71	-3	0.00443185	0.0111097	0.00443211	3	0.00443185	0.0111097	0.00443213	ė	0 00012343	4.924E-05	3.4813E-05	6 08E-09	6.07588E-09	3.4813E-05	0.000123394			0.000174528	+
72	3.1	0.00326682	0.00818922	0.00326703	31	0.00326682	0.00818922	0 00326703	6.2	6,7063E-05	2.675E-05	1.8916E-05	1 79E-09	1 79378E-09	1.8916E-05	6.70463E-05		6 704n3E-05		0.999999985
73	3.2	0.00238409	0.0059764	0 00238424	3.2	0.00238409	0.0059764	0 00238424	6.4	3.5717E-05	1.425E-05	1.0074E-05	5 09E-10	5.08814F-10	1 0074E-05	3 57081E-05	5.05056E-05	3.57083E-05	5.05056E-05	0,999999985
74	3.3	0.00172257	0.00431811	0.00172268	3.3	0.00172257	0 00431811	0.00172268	6.6	1 8646E- 05	7.439E-06	5.2593E-06	1 39E-10	1.38668E-10	5.2593E-06		2 63662E-05	1 86414E-05		0.99999985
75	3.4	0 00123222	0.00308891	0.0012323	3.4	0.00123222	0.00308891	0.0012323	6,8	9 5414E-06		2.6912 E- 06	1 63E-11	3.63096E-11	2.6912E-06		1 34918E-05	9 53 895E-0 6		
76	3.5	0.00087268	0.00218763	0 00087274	3.5	0 00087268	0 00218763	0 00087274	7	4.7857E-06	1.909E-06	1.3499E-06	9 13E-12	9.13472E-12	1.3499E-06	4 78451E-06	6 7671 8E- 06	4.78451E-06	o 76718E-06	0 999999985
77	36	0 0006119	0.00153391	0.00061194	3.6	0.0006119	0 00153391	0.00061194	7.2	2 3529E-06	9.387E-07	6.6365E-07	2 21E-12	2.20799F-12	6 63659-07	2,35228E-06	3.32704E-06	2.35228E-06	3 32704E-06	0 999999985
78	37	0 00042478	0.00106483	0 00042481	3,7	0 00042478	0.00106483	0.00042481	7.4	1 1339E-06	4.523E-07	3.1982E-07	5 I3E-13	5.12775E-13	3 19825-07	1 13358E-06	1 60333E-06	1.13358E-06	1 60333E-06	0 999999985
79	38	0 00029195	0.00073185	0 00029197	3.8	0 00029195	0 00073185	0 00029197	7.6	5 356E-07	2.137E-07	1.5107E-07	1 148-13	1.14416E-13	1 5107E-07	5 35467E-07	7 57361E-07	5.35467E-07		
80	39	0 00019866	0.00049799	0.00019867	3.9	0 00019866	0 00049799	0.00019867	7.8	2 4799E-07	9 893 É-08	6 9948E-08	2.45E-14	2.45286E-14	6 9948E-08	2 47928E-07	3.50668E-07	2 47928E-07	3.50668E-07	0 999999985
81	4	0.00013383	0.00033548	0.00013384	4	0 00013383	0.00033548	0 00013384	Ħ	1 1255E-07	4 49E-08	3 1746E-08	5 05E-15	5 05227E-15	3.1746E-08	1.12521E+07	1 59149E-07	1.12521E-07	1 59149E-07	0 999999985

APPENDIX C: CORRELATION AND REGRESSION ANALYSIS

This appendix documents the correlation testing and regression analysis performed as part of the scope of this dissertation. Tables C.1 through C.5 summarize the correlation and regression results identified in Figures C.1 through C.120. The results are as follows.

Table C.1 - Pearson Correlation for ft(z) - ASSY, fT(z) - standard

$\sigma = 1$	$\mu = 0$	Correla	
	n = 81	ft(z) - ASSY, fT	(z) - standard
USL	LSL	Pearson correlation of ft(z) - ASSY and fT(z) - adju stdev	P-Value
8	-8	0.968	p < 0.001
7.8	-7.8	0.968	p < 0.001
7.6	-7.6	0.968	p < 0.001
7.4	-7.4	0.968	p < 0.001
7.2	-7.2	0.968	p < 0.001
7		0.967	p < 0.001
6.8	-6.8	0.967	p < 0.001
6.6	-6.6	0.967	p < 0.001
6.4	-6.4	0.967	p < 0.001
6.2	-6.2	0.967	p < 0.001
6	-6	0.967	p < 0.001
5.8	-5.8	0.968	p < 0.001
5.6	-5.6	0.968	p < 0.001
5.4	-5.4	0.968	p < 0.001
5.2	-5.2	0.968	p < 0.001
5	-5	0,968	p < 0.001
4.8	-4.8	0.968	p < 0.001
4.6	-4.6	0.969	p < 0.001
4.4	-4.4	0.969	p < 0.001
4.2	-4.2	0.970	p < 0.001
. 4	-4	0.971	p < 0.001
3.8	-3.8	0,972	p < 0.001
3.6	-3.6	0.974	p < 0.001
3.4	-3.4	0.976	p < 0.001
3.2	-3.2	0,978	p < 0.001
3	-3	0.980	p < 0.001
2.8	-2.8	0.983	p < 0.001
2.6	-2.6_	0.985	p < 0.001
2.4	-2.4	0.988	p < 0.001
2.2	-2.2	0.991	p < 0.001
2	-2	0.993	p < 0.001
1.8	-1.8	0.995	p < 0.001
1.6	-1.6	0.997	p < 0.001
1.4	-1.4	0.998	p < 0.001
1.2	-1.2	0.999	p < 0.001
1	-1	0.999	p < 0.001
0.8	-0.8	1.000	p < 0.001
0.6	-0.6	1.000	p < 0.001
0.4	-0.4	1.000	p < 0.001
0.2	-0.2	1.000	Note 1

Note 1: For values referencing this note the p-value could not be calculated

Note 2: Standard deviation is 1, unless otherwise noted in Appendix B

Table C.2 - Pearson Correlation for ft(z) - ASSY, fT(z) - adju stdev

σ = 1	$\mu = 0$ $n = 81$	Correlati ft(z) - ASSY, fT(z	
USL	LSL	Pearson correlation of ft(z) - ASSY and fT(z) - standard	P-Value
8	-8	1	Note 1
7.8	-7.8	1	Note 1
7.6	-7.6	1	Note 1
7.4	-7.4	1	Note 1
7.2	-7.2	1	Note I
7	-7	1	Note 1
6.8	-6.8	1	Note 1
6.6	-6.6	-	Note 1
6.4	-6.4	1	Note I
6.2	-6.2	1	Note 1
6	-6	1	Note 1
5.8	-5.8	1 .	Note I
5.6	-5.6	1	Note i
5.4	-5.4	1	Note 1
5.2	-5.2	1	Note 1
5	-5	1	Note I
4.8	-4.8	l	Note 1
4.6	-4.6	1	Note 1
4.4	-4.4	1	Note 1
4.2	-4.2	<u>l</u>	· Note 1
4	-4		Note 1
3.8	-3.8	1	Note 1
3.6	-3.6	1	Note 1
3.4	-3.4	1	Note 1
3.2	-3.2	1	Note 1
3	-3	1	Note 1
2.8	-2.8	1	Note 1
2.6	-2.6	1	Note 1
2.4	-2.4	1	Note 1
2.2	-2.2	1	Note 1
2	-2	. 1	Note 1
1.8	-1.8	1	Note 1
1.6	-1.6	1	Note 1
1.4	-1.4	1	Note 1
1.2	-1.2	1	Note 1
1	-1	1	Note 1
0.8	-0.8	1	Note 1
0.6	-0.6	1	Note 1
0.4	-0.4	1	Note 1
0.2	-0.2	1	Note I

Note 1: For values referencing this note the p-value could not be calculated Note 2: Standard deviation is 1, unless otherwise noted in Appendix B

Table C.3 - Pearson Correlation of Analysis Ratios

	M = 0	Correlations:		Correlations:	
$\sigma = 1$	n = 81	RATIO 1, RATIO	2	RATIO 3, RATIO) 4
TICI	LCI	Pearson correlation of	P-	Pearson correlation of	P-Value
USL	LSL	RATIO 1 and RATIO 2	Value	RATIO 3 and RATIO 4	P-value
8	-8	1	Note 1		Note 1
7.8	-7.8	1	Note 1	J	Note 1
7.6	-7.6	1	Note 1	1	Note 1
7.4	-7.4	1	Note 1	j i	Note 1
7.2	-7.2	1	Note 1	1	Note 1
7	-7	1	Note 1	1	Note 1
6.8	-6.8	1	Note 1	1	Note 1
6.6	-6.6	1	Note 1	1	Note 1
6.4	-6.4	Ī	Note 1	1	Note 1
6.2	-6.2	1	Note 1	1	Note 1
6	-6	<u> </u>	Note 1	1	Note i
5.8	-5.8	1	Note 1	1	Note 1
5.6	-5.6	l	Note 1	1	Note 1
5.4	-5.4	1	Note 1	1	Note 1
5.2	-5.2	1	Note 1	1	Note 1
5	-5	1	Note 1	1	Note 1
4.8	-4.8	1	Note 1	1	Note 1
4.6	-4.6	1	Note 1	1	Note 1
4.4	-4.4	1	Note 1	1	Note 1
4.2	-4.2	1	Note 1	1	Note 1
4	-4	1	Note 1	1	Note 1
3.8	-3.8	1	Note 1	1	Note 1
3.6	-3.6	1	Note 1	1	Note 1
3.4	-3.4	1	Note 1	11	Note 1
3.2	-3.2	1	Note 1	1	Note 1
3	-3	1	Note 1	1	Note 1
2.8	-2.8	<u> </u>	Note 1	1	Note 1
2.6	-2.6	1	Note 1	<u> </u>	Note 1
2.4	-2.4	1	Note 1	1	Note 1
2.2	-2.2	l	Note 1	<u>l</u>	Note 1
2	-2	1	Note 1	1	Note 1
1.8	-1.8	<u>l</u>	Note 1	1	Note 1
1.6	-1.6	1	Note I	1	Note 1
1.4	-1.4	1	Note 1	11	Note 1
1.2	-1.2	1	Note 1	1	Note 1
1	-l	1	Note 1	1	Note 1
0.8	-0.8	1	Note 1	<u> </u>	Note 1
0.6	-0.6	1	Note I	1	Note 1
0.4	-0.4	1	Note 1	1	Note 1
0.2	-0.2	1	Note 1	1	Note 1

Note 1: For values referencing this note the p-value could not be calculated Note 2: Standard deviation is 1, unless otherwise noted in Appendix B

Table C.4 – Regression Analysis for ft(z) - ASSY, fT(z) - standard

$\sigma = 1$	$\mu = 0$			Regression for:
Note 2	n = 81		<u> </u>	ft(z) - ASSY, fT(z) - standard
USL	LSL	R∗sq . (adj)	P-Value	Fitted Line Plot Equation for Cubic Model
8	-8	99.14%	p < 0.001	Y = 0.007522 + 2.915 X - 10.14 X**2 + 13.46 X**3
7.8	-7.8	99.14%	p < 0.001	$Y = 0.007806 + 2.908 X - 10.10 X^{**}2 + 13.41 X^{**}3$
7.6	-7.6	99.14%	p < 0.001	$Y = 0.008111 + 2.901 X - 10.06 X^{**}2 + 13.35 X^{**}3$
7.4	-7.4	99.13%	p < 0.001	$Y = 0.008441 + 2.893 X - 10.02 \bar{X}^{**}2 + 13.29 X^{**}3$
7.2	-7.2	99.13%	p < 0.001	Y = 0.008800 + 2.885 X - 9.973 X**2 + 13.22 X**3
7	-7	99.13%	p < 0.001	$Y = 0.009190 + 2.876 X - 9.923 X^{**}2 + 13.14 X^{**}3$
6.8	-6.8	99.13%	p < 0.001	$Y = 0.009616 + 2.865 X - 9.869 X^{**}2 + 13.06 X^{**}3$
6.6	-6.6	99.13%	p < 0.001	$Y = 0.01008 + 2.854 X - 9.810 X^{**}2 + 12.97 X^{**}3$
6.4	-6.4	99.13%	p < 0.001	$Y = 0.01060 + 2.842 X - 9.744 X^{**}2 + 12.88 X^{**}3$
6.2	-6.2	99.13%	p < 0.001	Y = 0.01117 + 2.829 X - 9.671 X**2 + 12.77 X**3
6	-6	99.14%	p < 0.001	Y = 0.01180 + 2.814 X - 9.590 X**2 + 12.65 X**3
5.8	-5.8	99.14%	p < 0.001	Y = 0.01251 + 2.797 X - 9.500 X**2 + 12.51 X**3
5.6	-5.6	99.15%	p < 0.001	$Y = 0.01331 + 2.778 X - 9.398 X^{**}2 + 12.36 X^{**}3$
5.4	-5.4	99.16%	p < 0.001	Y = 0.01422 + 2.757 X - 9.283 X**2 + 12.19 X**3
5.2	-5.2	99.17%	p < 0.001	Y = 0.01525 + 2.732 X - 9.152 X**2 + 11.99 X**3
5	-5	99.19%	p < 0.001	$Y = 0.01642 + 2.705 X - 9.002 X^{**}2 + 11.77 X^{**}3$
4.8	-4.8	99.21%	p < 0.001	$Y = 0.01778 + 2.672 X - 8.830 X^{**}2 + 11.51 X^{**}3$
4.6	-4.6	99.24%	p < 0.001	$Y = 0.01934 + 2.635 X - 8.630 X^{**}2 + 11.21 X^{**}3$
4.4	-4.4	99.28%	p < 0.001	$Y = 0.02116 + 2.593 X - 8.399 X^{**}2 + 10.87 X^{**}3$
4.2	-4.2	99.33%	p < 0.001	$Y = 0.02327 + 2.543 X - 8.131 X^{**}2 + 10.47 X^{**}3$
4	-4	99.39%	p < 0.001	$Y = 0.02572 + 2.485 X - 7.820 X^{**}2 + 10.00 X^{**}3$
3.8	-3.8	99.46%	p < 0.001	Y = 0.02857 + 2.418 X - 7.460 X**2 + 9.468 X**3
3.6	-3.6	99.54%	p < 0.001	$Y = 0.03186 + 2.341 X - 7.048 X^{**}2 + 8.855 X^{**}3$
3.4	-3.4	99.62%	p < 0.001	$Y = 0.03564 + 2.254 X - 6.581 X^{**2} + 8.161 X^{**3}$
3.2	-3.2	99.71%	p < 0.001	Y = 0.03994 + 2.156 X - 6.061 X**2 + 7.390 X**3
3	-3	99.79%	p < 0.001	$Y = 0.04478 + 2.048 X - 5.496 X^{**2} + 6.558 X^{**3}$
2.8	-2.8	99.86%	p < 0.001	Y = 0.05017 + 1.933 X - 4.899 X**2 + 5.685 X**3
2.6	-2.6	99.92%	p < 0.001	Y = 0.05607 + 1.813 X - 4.291 X**2 + 4.807 X**3
2.4	+2,4	99.95%	p < 0.001	$Y = 0.06244 + 1.692 X - 3.696 X^{**2} + 3.962 X^{**3}$ $Y = 0.06919 + 1.574 X - 3.137 X^{**2} + 3.186 X^{**3}$
2.2	-2.2 -2	99.98% 99.99%	p < 0.001	Y = 0.07622 + 1.462 X - 2.633 X**2 + 2.508 X**3
1.8	-1.8	100.00%	100.0 p < 0.001	$Y = 0.07622 + 1.462 \times -2.033 \times^{++}2 + 2.308 \times^{++}3$ $Y = 0.08339 + 1.359 \times -2.196 \times^{++}2 + 1.942 \times^{++}3$
1.6	-1.8	100.00%	p < 0.001	Y = 0.09056 + 1.266 X - 1.829 X**2 + 1.490 X**3
1.4	-1.6	100.00%	p < 0.001 p < 0.001	$Y = 0.09036 + 1.266 \text{ A} - 1.829 \text{ A}^{-1}2 + 1.490 \text{ A}^{-1}3$ $Y = 0.09755 + 1.185 \text{ X} - 1.532 \text{ X}^{++}2 + 1.142 \text{ X}^{++}3$
1.4	-1.4	100.00%	p < 0.001	Y = 0.1042 + 1.115 X - 1.295 X**2 + 0.8829 X**3
1.2	-1.2 -1	100.00%	p < 0.001 p < 0.001	Y = 0.1103 + 1.057 X - 1.112 X**2 + 0.6629 X**3
0.8	-0.8	100.00%	p < 0.001	$Y = 0.1157 + 1.009 X - 0.9725 X^{**2} + 0.5600 X^{**3}$
0.6	-0.6	100.00%	p < 0.001	$Y = 0.1203 + 0.9714 \times -0.8702 \times *2 + 0.3660 \times *3$
0.4	-0.4	100.00%	p < 0.001	$Y = 0.1471 + 0.7627 \times -0.3293 \times **2$
0.2	-0.4	100.00%	p < 0.001	Y = 0.1985 + 0.5026 X
0.2	-0.4	100.00%	p < 0.001	4 - 0.1763 7 0.3020 A

Note 1: For values referencing this note the p-value could not be calculated Note 2: Standard deviation is 1, unless otherwise noted in Appendix B

Table C.5 - Regression Analysis for ft(z) - ASSY, $f\Gamma(z)$ – adju stdev

$\sigma = 1$ Note 2	μ = 0 n = 81		fr(z)	Regression for: - ASSY vs. fT(z) - adju stdev
Note 2	11 - 61		11(Z)	- A331 vs. 11(2) - adju stdev
USL	LSL	R-sq (adj)	P-Value	Fitted Line Plot Equation for Cubic Model
8	-8	100.00%	Note 1	$Y = -0.000000 + 1.414 X + 0.000000 X^{**2}$
7.8	-7.8	100.00%	Note I	Y = -0.000000 + 1.414 X + 0.000000 X**2
7.6	-7.6	100.00%	Note I	$Y = 0.0000000 + 1.414 X + 0.0000000 X^{**2}$
7.4	-7.4	100.00%	Note I	Y = 0.0000000 + 1.414 X + 0.0000000 X**2
7.2	-7. <u>2</u>	100.00%	Note 1	Y = -0.0000000 + 1.414 X
7	-7	100.00%	p < 0.001	Y = -0.0000000 + 1.414 X
6.8	-6.8	100.00%	Note 1	Y = 0.000000 + 1.414 X - 0.000000 X**2
6.6	-6.6	100.00%	Note 1	Y = 0.0000000 + 1.414 X
6.4	-6.4	100.00%	Note 1	Y = -0.0000000 + 1.414 X - 0.0000000 X**2
6.2	-6.2	100.00%	Note 1	Y = -0.000000 + 1.414 X
6	-6	100.00%	Note 1	Y = 0.000000 + 1.414 X
5.8	-5.8	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
5.6	-5.6	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
5.4	-5.4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
5.2	-5.2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
5	-5	100.00%	p < 0.001	Y = -0.000000 + 1.414 X
4.8	-4.8	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
4.6	-4.6	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
4.4	-4.4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
4.2	-4.2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
4	-4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
3.8	-3.8	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
3.6	-3.6	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
3.4	-3.4	100.00%	p < 0.001	$\dot{Y} = 0.000000 + 1.414 X$
3.2	-3.2	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
3	-3	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
2.8	-2.8	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
2.6	-2.6	100.00%	p < 0.001	Y = 0.0000000 + 1.414 X
2.4	-2.4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
2.2	-2.2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
2	-2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
1.8	-1.8	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
1.6	-1.6	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
1.4	-1.4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
1.2	-1.2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
1	-1	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
0.8	-0.8	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
0.6	-0.6	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
0.4	-0.4	100.00%	p < 0.001	Y = 0.000000 + 1.414 X
0.2	-0.2	100.00%	p < 0.001	Y = 0.000000 + 1.414 X

Note 1: For values referencing this note the p-value could not be calculated

Note 2: Standard deviation is 1, unless otherwise noted in Appendix B



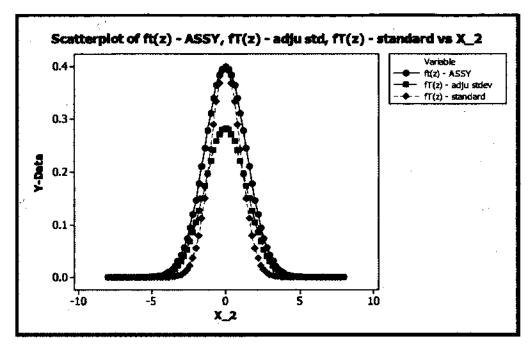
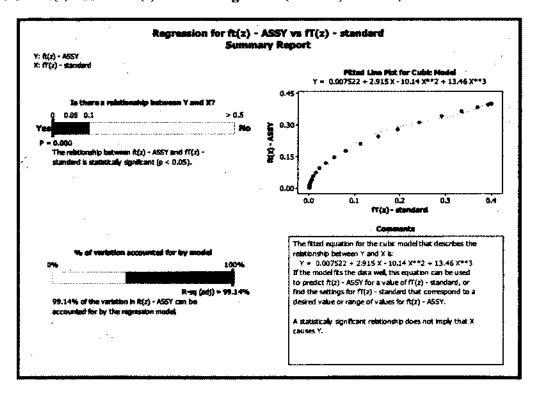


Figure C.2 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 8, LSL = -8)



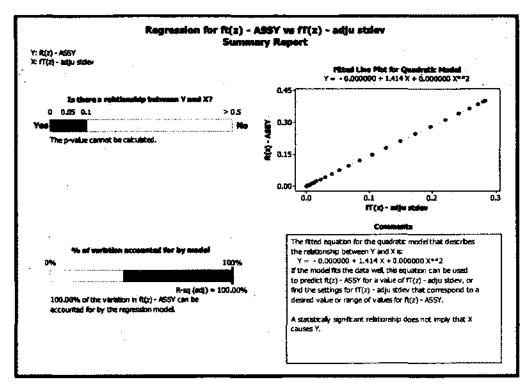
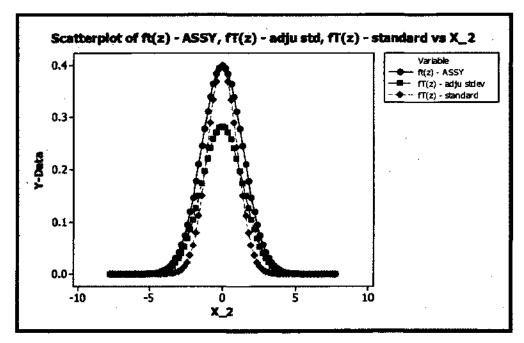


Figure C.3 • ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 8, LSL = -8)





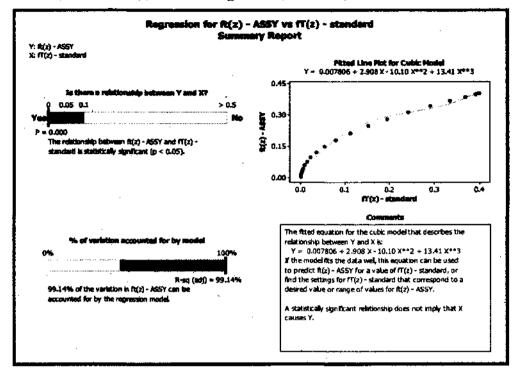
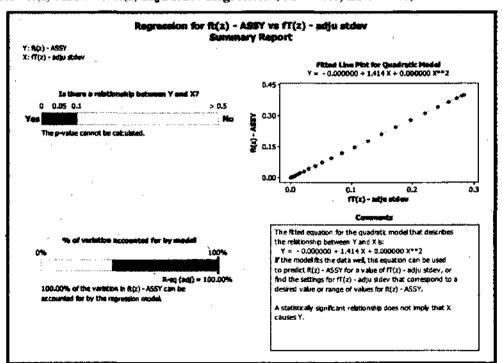


Figure C. 5 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 7.8, LSL = -7.8)





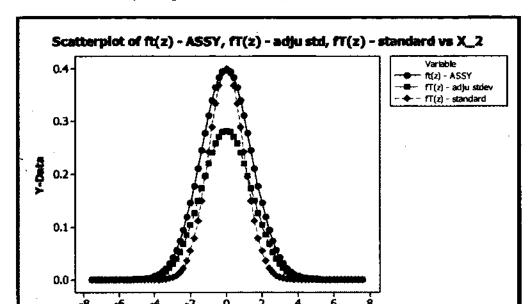
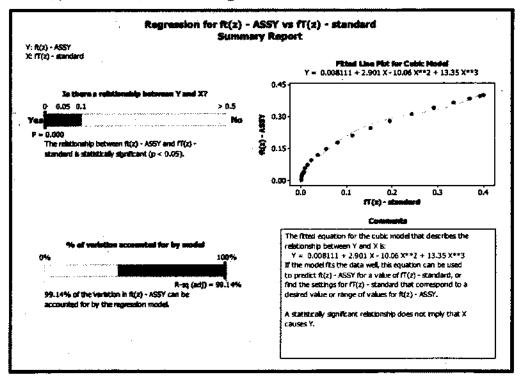


Figure C.7 - TSND Assembly Comparison (USL = 7.6, LSL = -7.6)

Figure C. 8 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 7.6, LSL = -7.6)

X_2



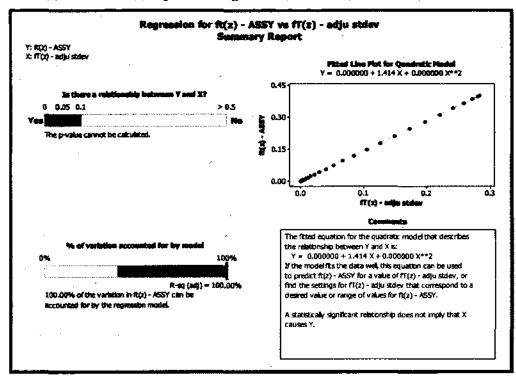
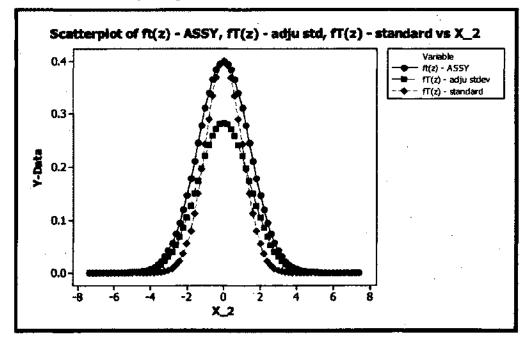


Figure C.9 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 7.6, LSL = -7.6)





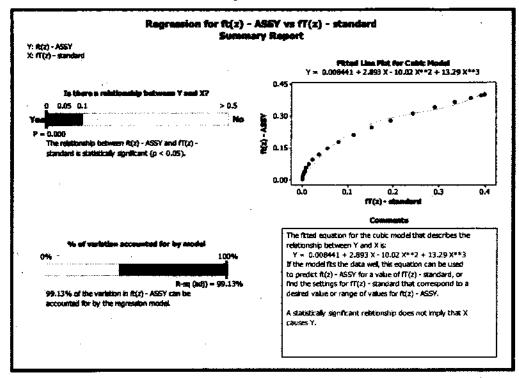
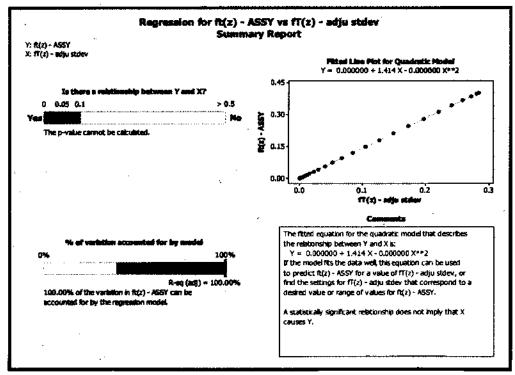


Figure C.11 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 7.4, LSL = -7.4)





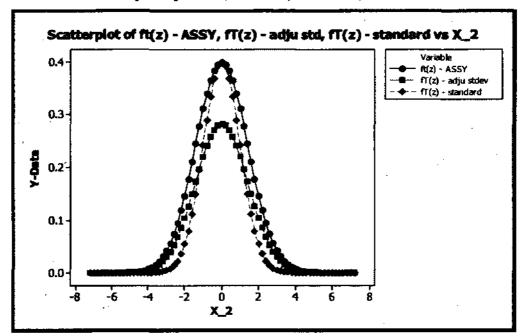
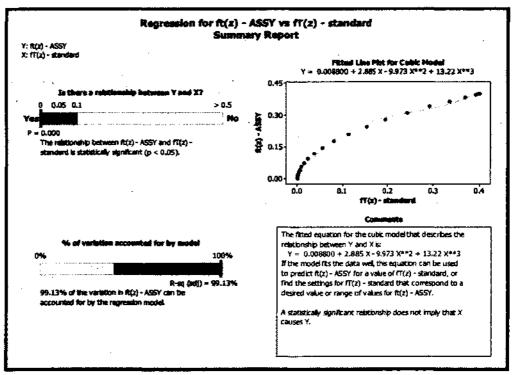


Figure C.13 - TSND Assembly Comparison (USL = 7.2, LSL = -7.2)





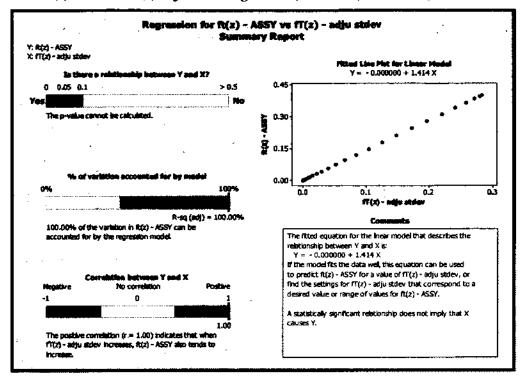
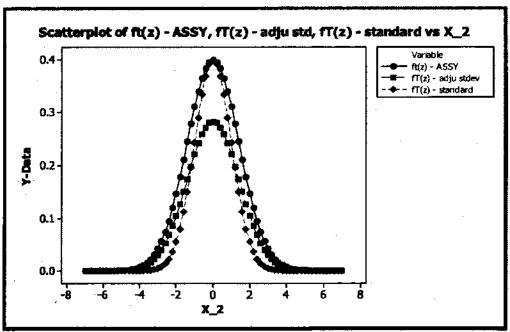


Figure C.15 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 7.2, LSL = -7.2)





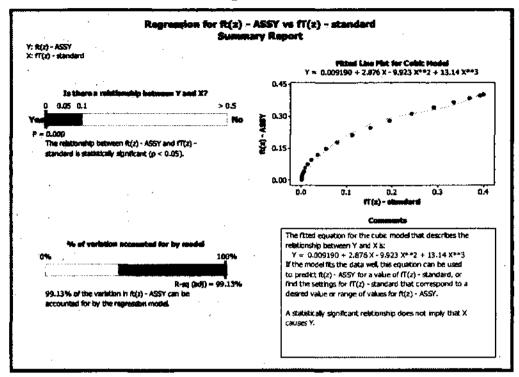
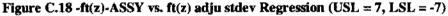
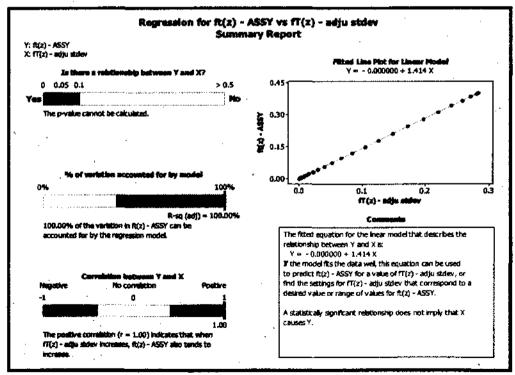


Figure C.17 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 7, LSL = -7)





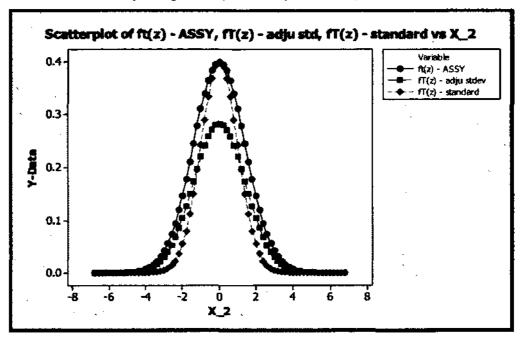
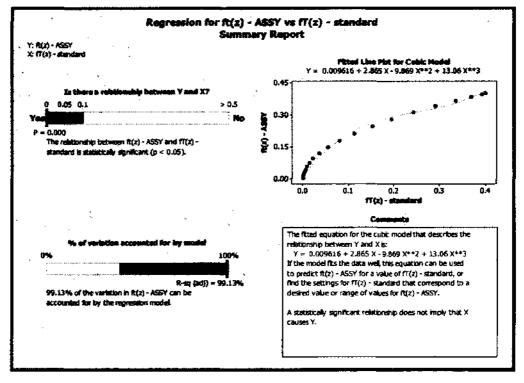


Figure C.19 - TSND Assembly Comparison (USL = 6.8, LSL = -6.8)





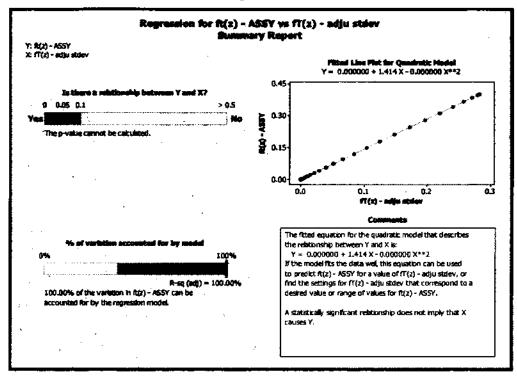
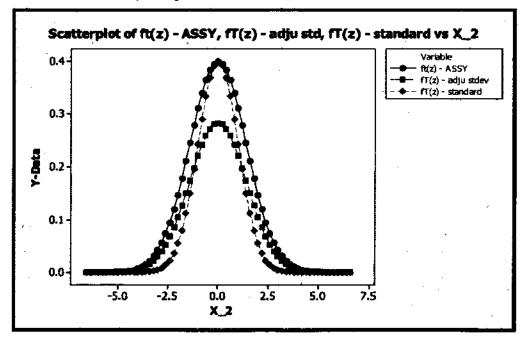


Figure C.21 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 6.8, LSL = -6.8)





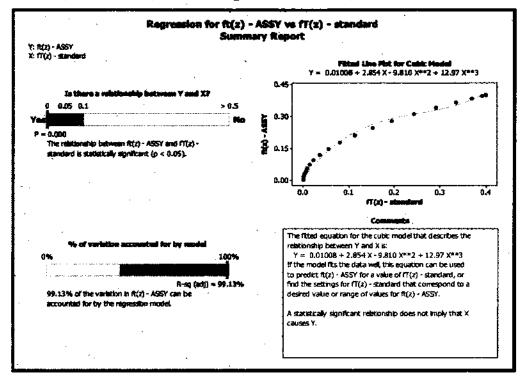
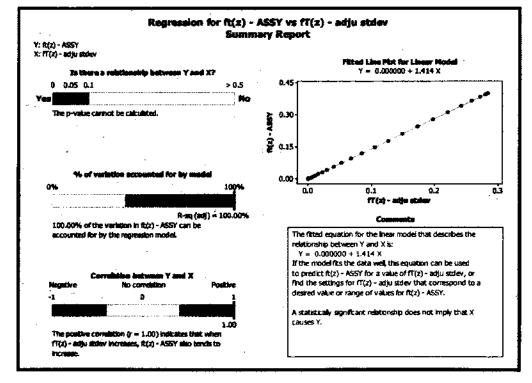


Figure C.23 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 6.6, LSL = -6.6)





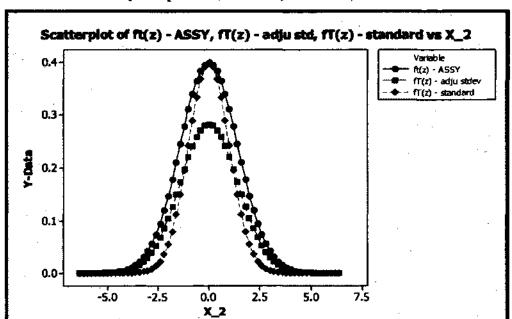
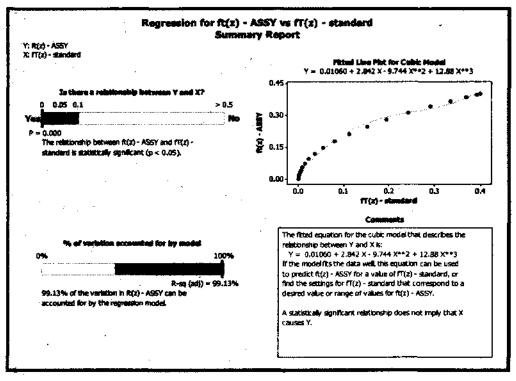


Figure C.25 - TSND Assembly Comparison (USL = 6.4, LSL = -6.4)

Figure C.26 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 6.4, LSL = -6.4)



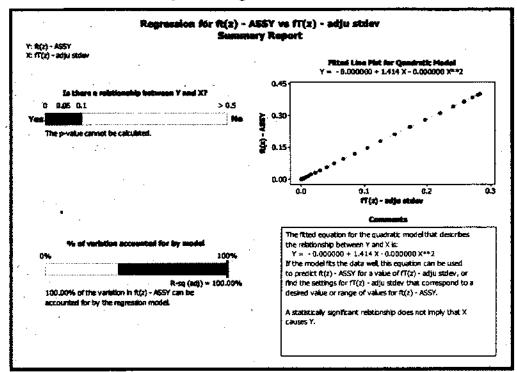
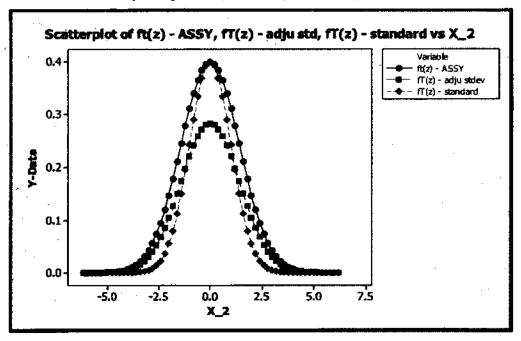


Figure C.27 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 6.4, LSL = -6.4)





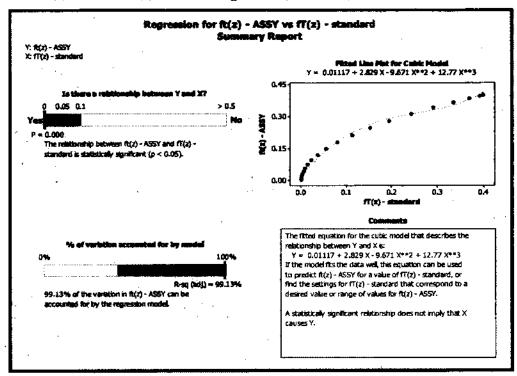
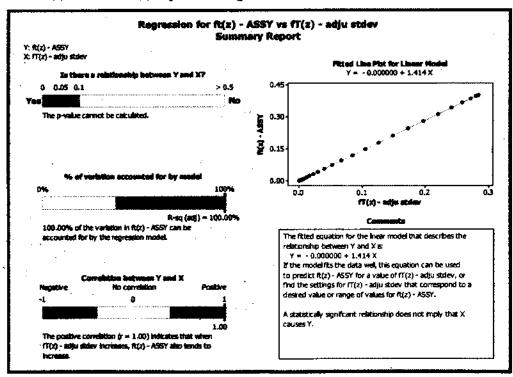


Figure C.29 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 6.2, LSL = -6.2)





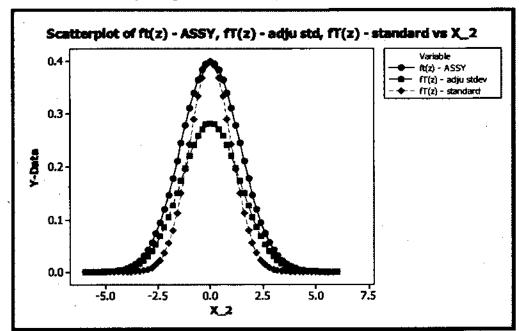
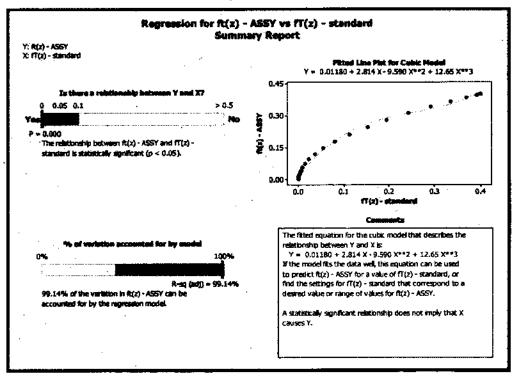


Figure C.31 - TSND Assembly Comparison (USL = 6, LSL = -6)

Figure C.32 • ft(z)-ASSY vs. ft(z) standard Regression (USL = 6, LSL = -6)



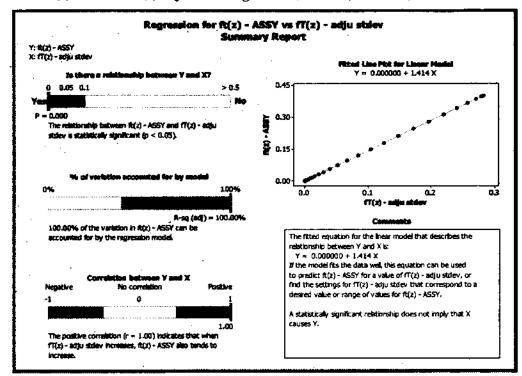
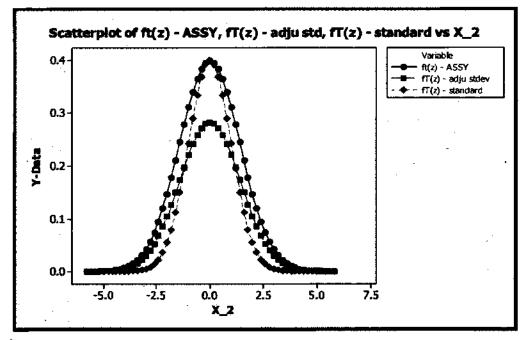


Figure C.33 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 6, LSL = -6)





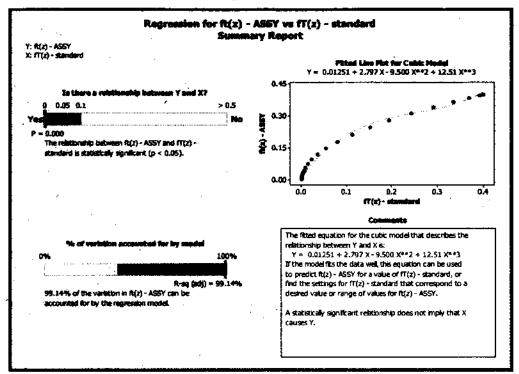
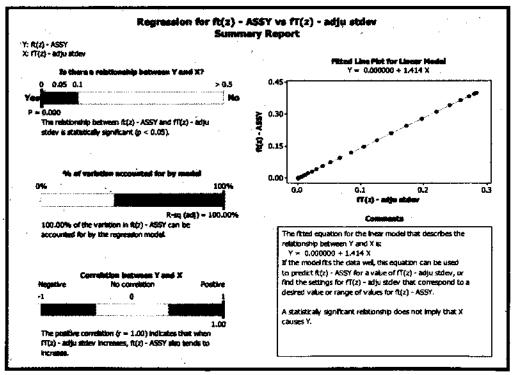


Figure C.35 • ft(z)-ASSY vs. ft(z) standard Regression (USL = 5.8, LSL = -5.8)





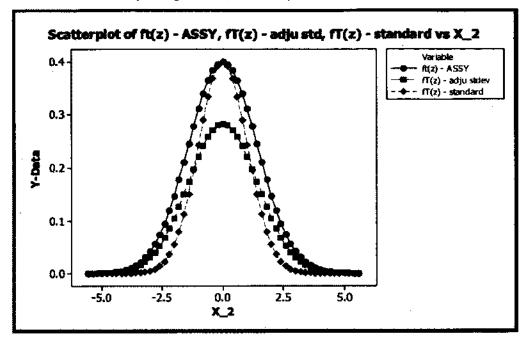
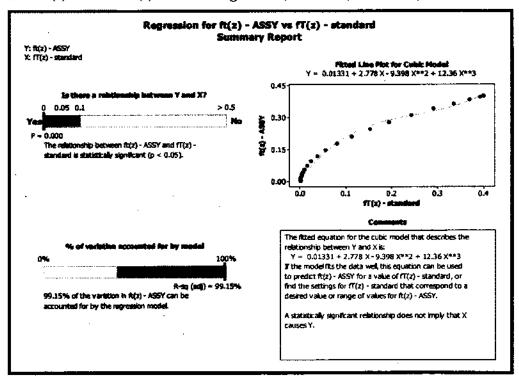


Figure C.37 - TSND Assembly Comparison (USL = 5.6, LSL = -5.6)

Figure C.38 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 5.6, LSL = -5.6)



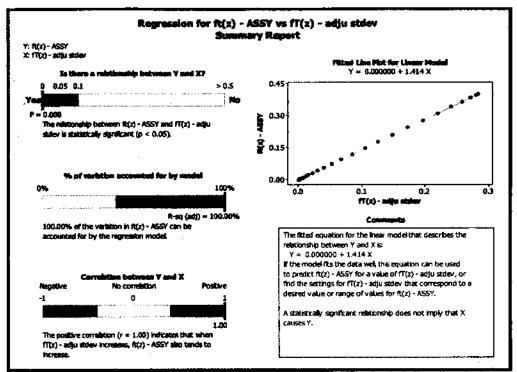
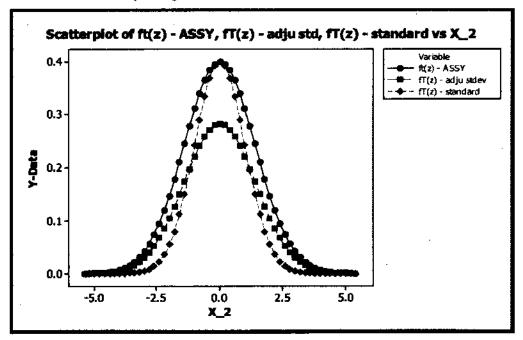


Figure C.39 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 5.6, LSL = -5.6)





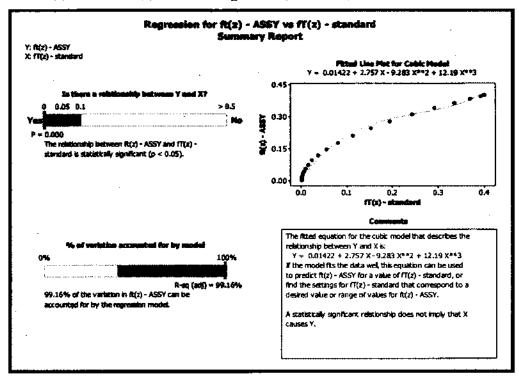
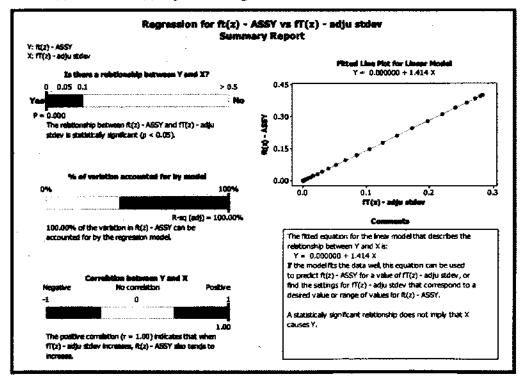


Figure C.41 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 5.4, LSL = -5.4)





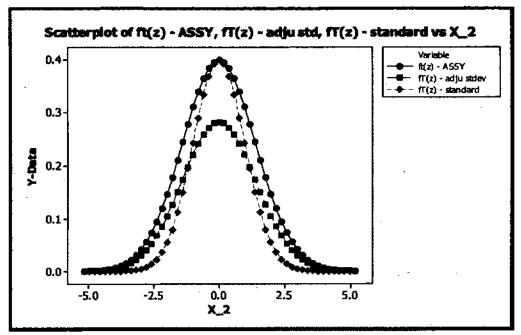
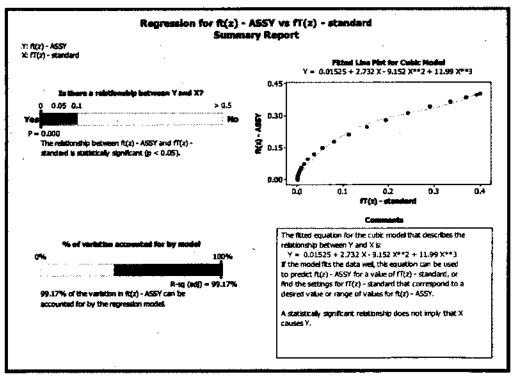


Figure C.43 · TSND Assembly Comparison (USL = 5.2, LSL = -5.2)





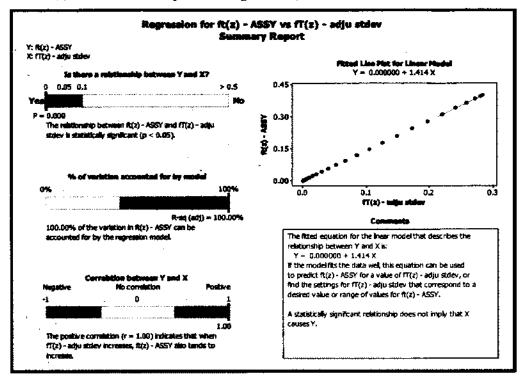
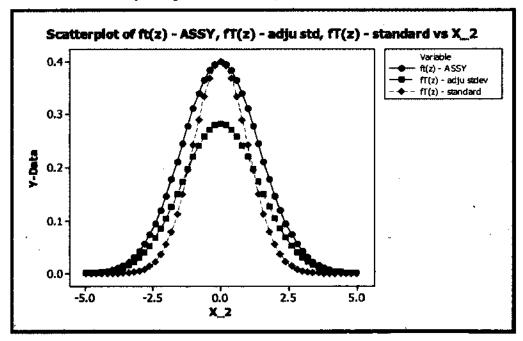


Figure C.45 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 5.2, LSL = -5.2)





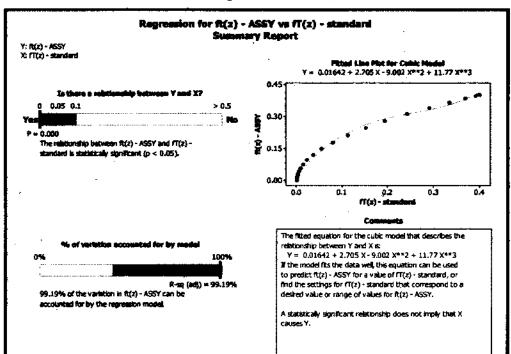
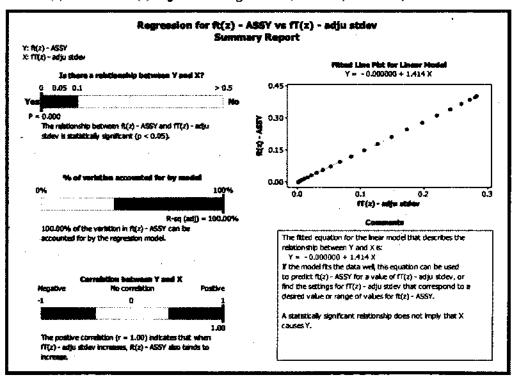


Figure C.47 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 5, LSL = -5)

Figure C.48 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 5, LSL = -5)



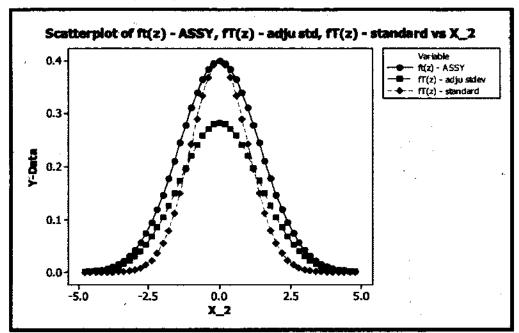
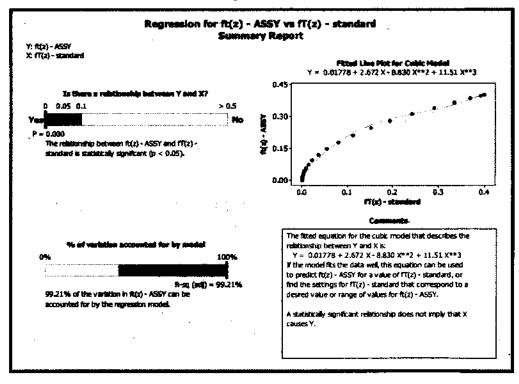


Figure C.49 · TSND Assembly Comparison (USL = 4.8, LSL = -4.8)





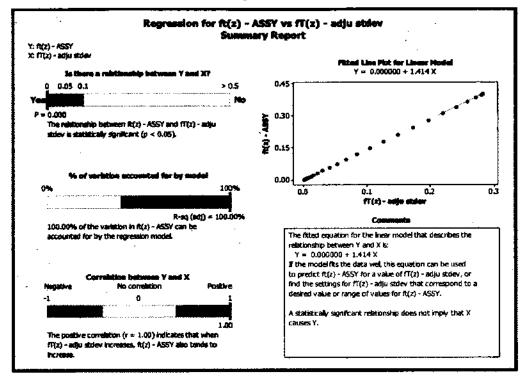
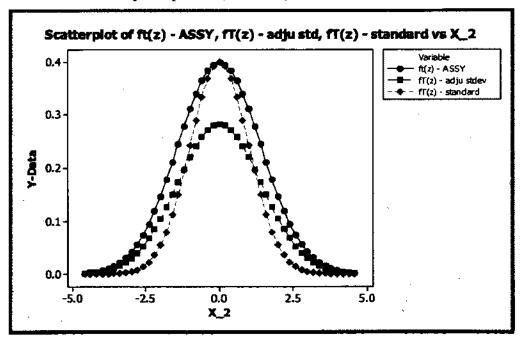


Figure C.51 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 4.8, LSL = -4.8)





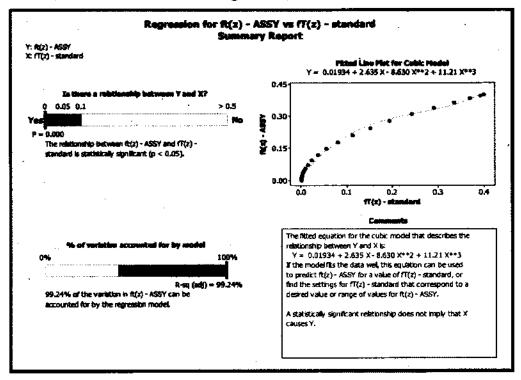
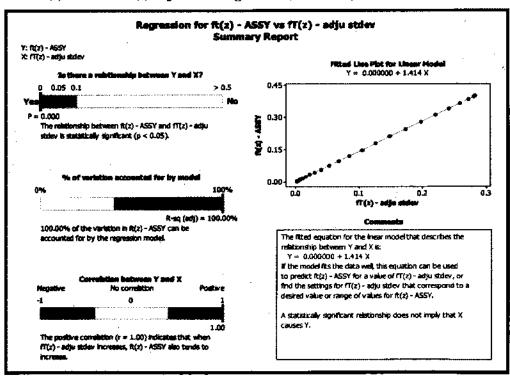


Figure C.53 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 4.6, LSL = -4.6)





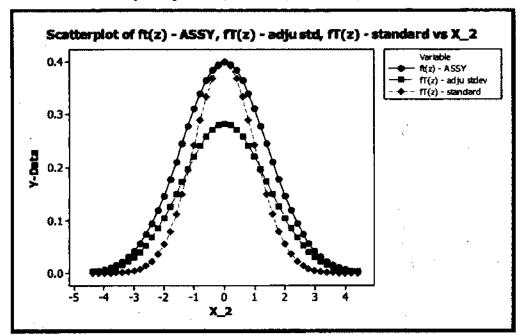
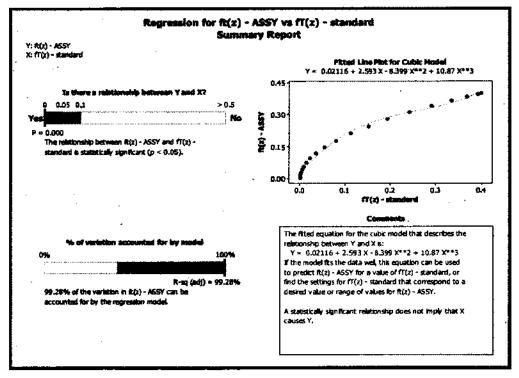


Figure C.55 - TSND Assembly Comparison (USL = 4.4, LSL = -4.4)





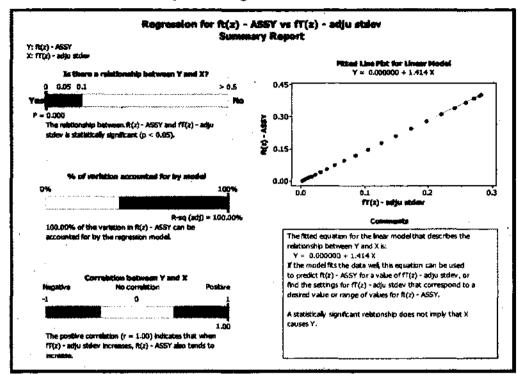
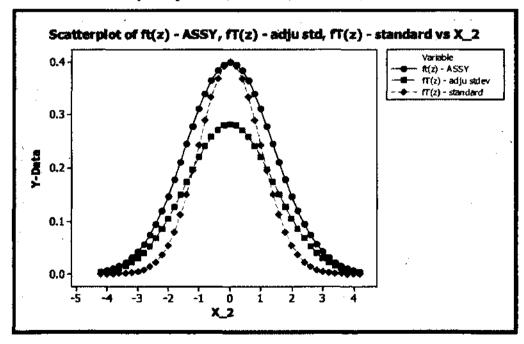


Figure C.57 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 4.4, LSL = -4.4)





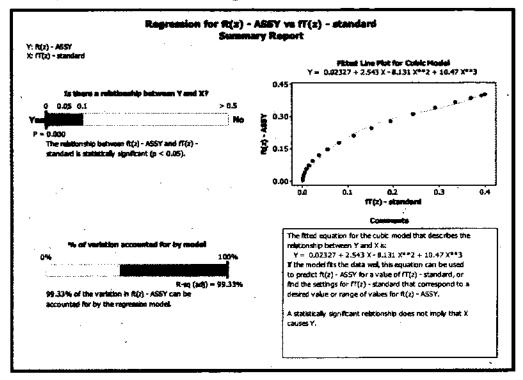
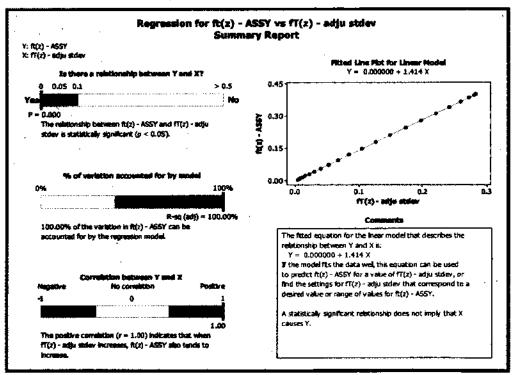


Figure C.59 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 4.2, LSL = -4.2)





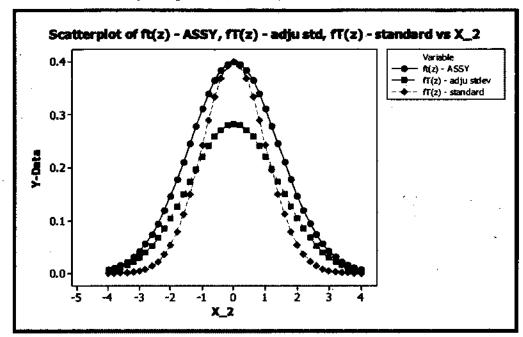
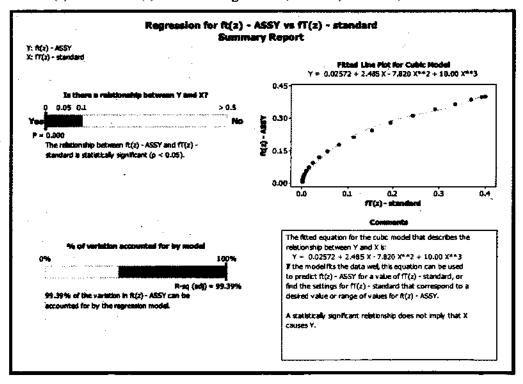


Figure C.61 - TSND Assembly Comparison (USL = 4, LSL = -4)





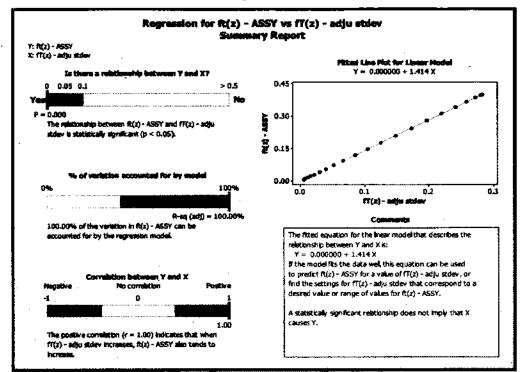
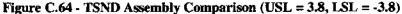
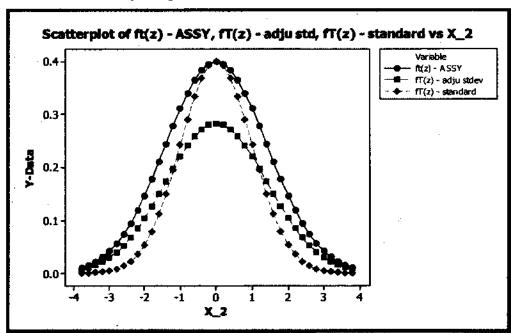


Figure C.63 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 4, LSL = -4)





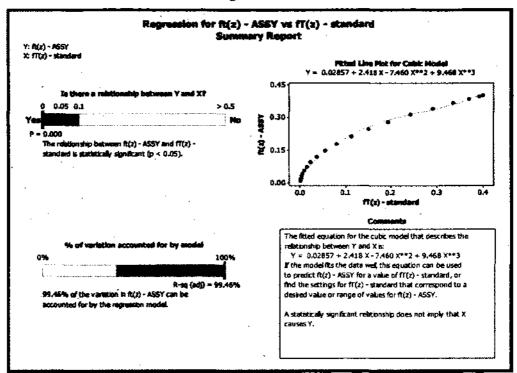
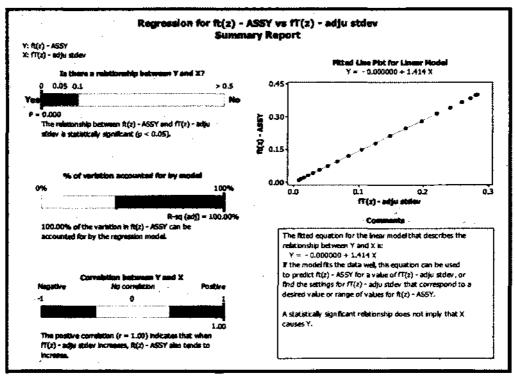


Figure C.65 · ft(z)-ASSY vs. ft(z) standard Regression (USL = 3.8, LSL = -3.8)





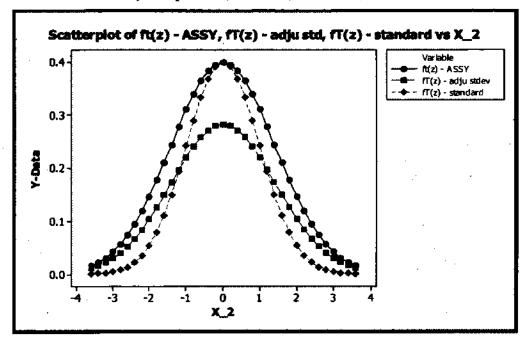
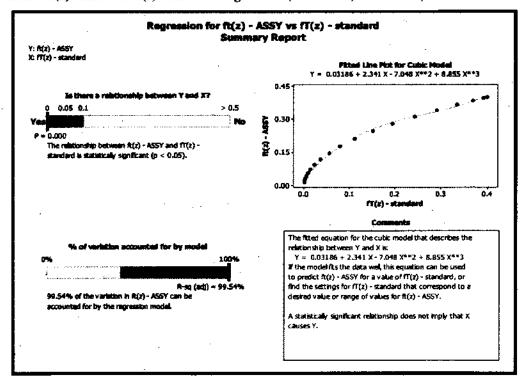


Figure C.67 • TSND Assembly Comparison (USL = 3.6, LSL = -3.6)





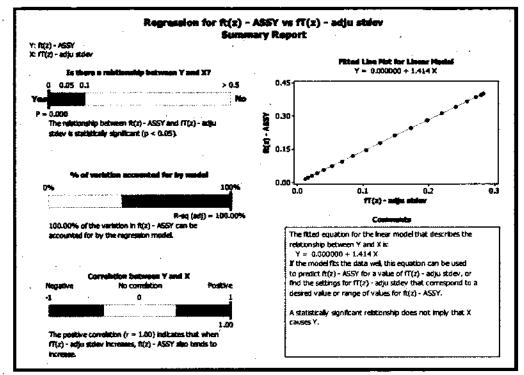
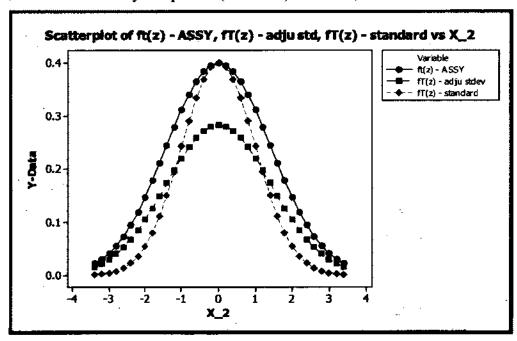


Figure C.69 • ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 3.6, LSL = -3.6)





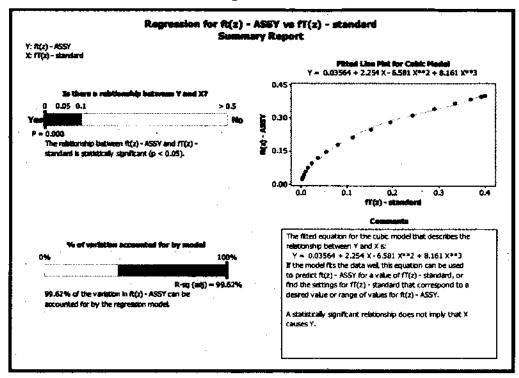
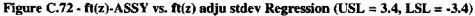
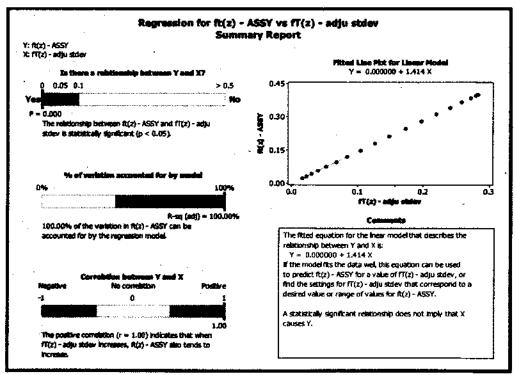


Figure C.71 • ft(z)-ASSY vs. ft(z) standard Regression (USL = 3.4, LSL = -3.4)





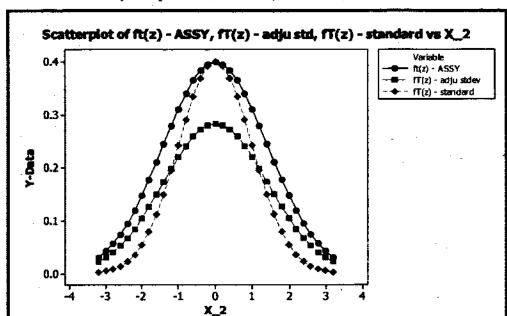
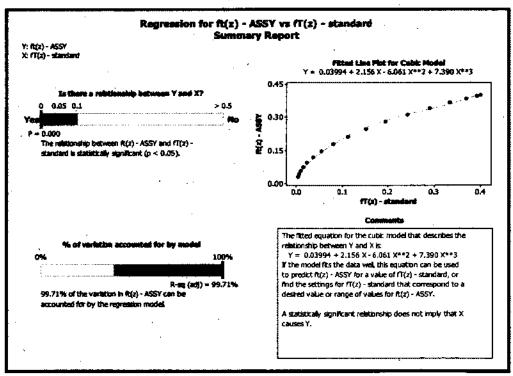


Figure C.73 TSND Assembly Comparison (USL = 3.2, LSL = -3.2)





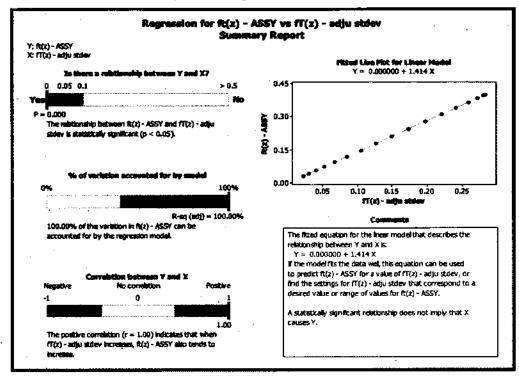
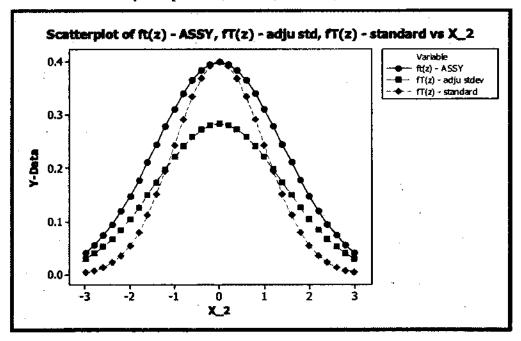


Figure C.75 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 3.2, LSL = -3.2)





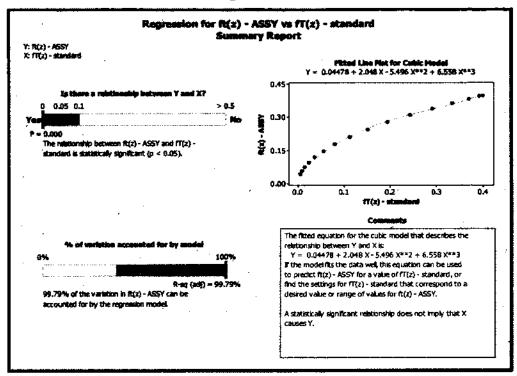
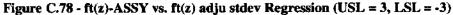
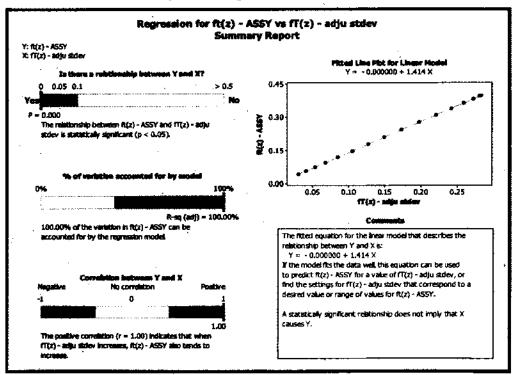


Figure C.77 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 3, LSL = -3)





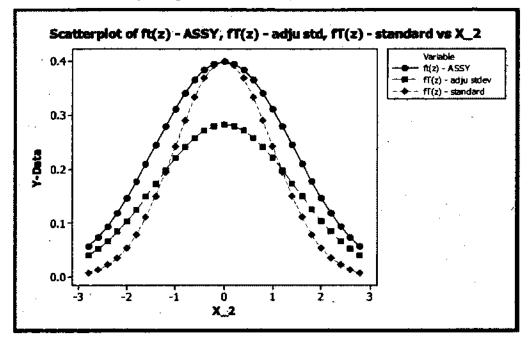
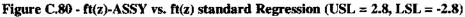
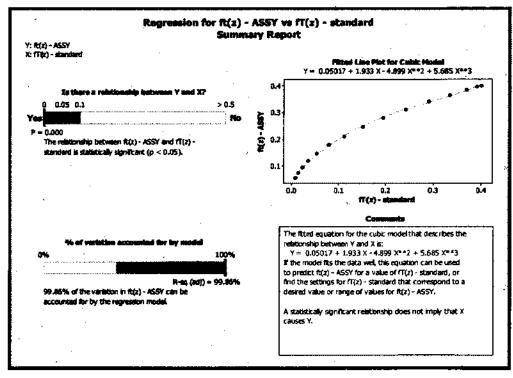


Figure C.79 - TSND Assembly Comparison (USL = 2.8, LSL = -2.8)





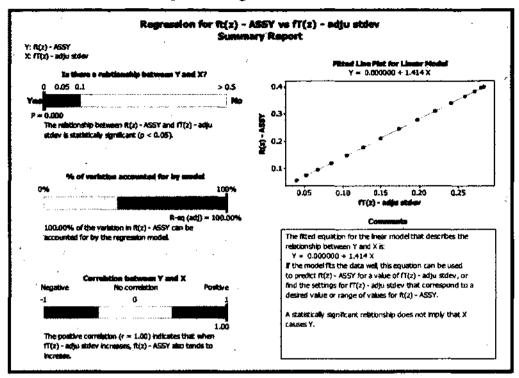
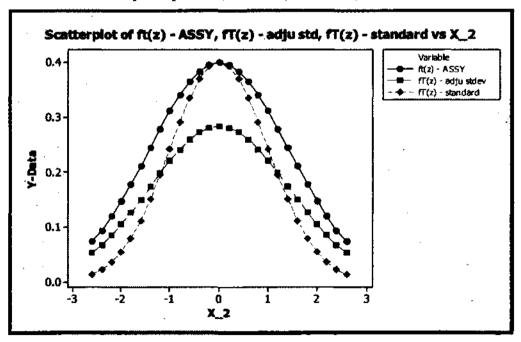


Figure C.81 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 2.8, LSL = -2.8)





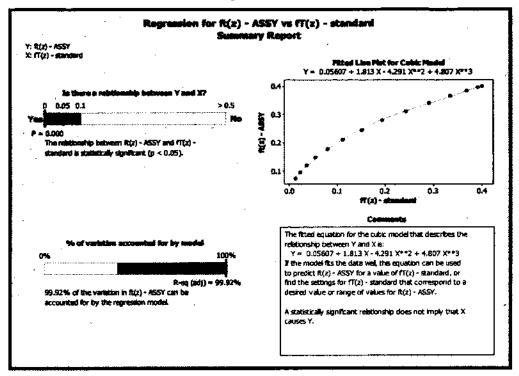
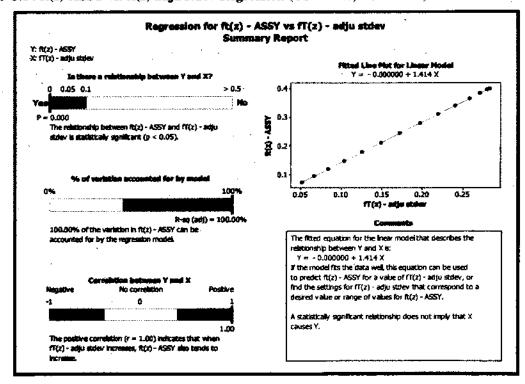


Figure C.83 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 2.6, LSL = -2.6)





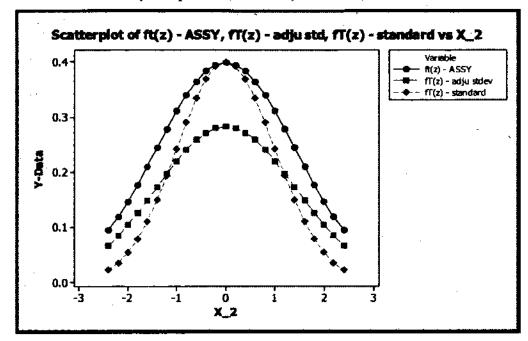
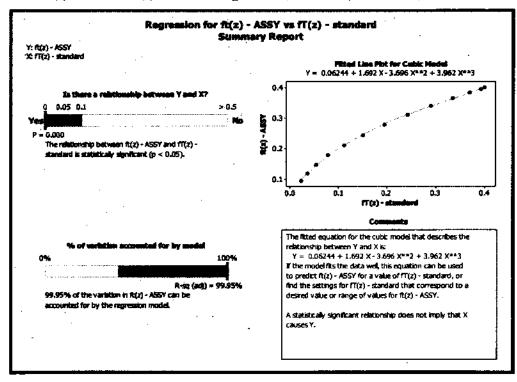


Figure C.85 · TSND Assembly Comparison (USL = 2.4, LSL = -2.4)





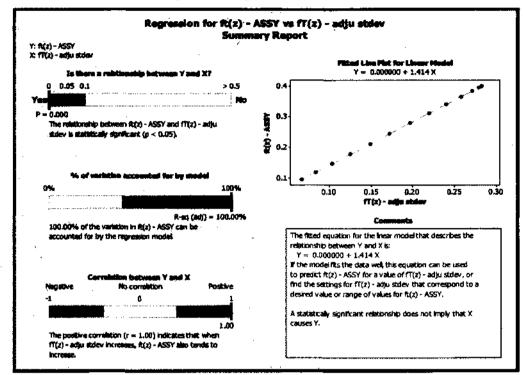
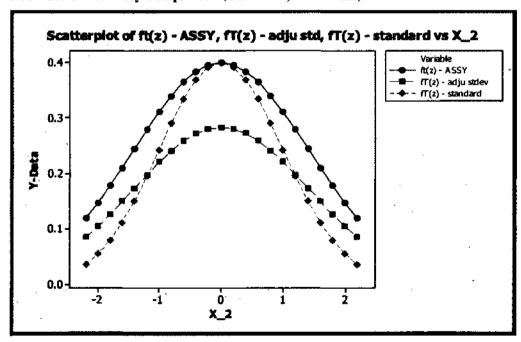


Figure C.87 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 2.4, LSL = -2.4)





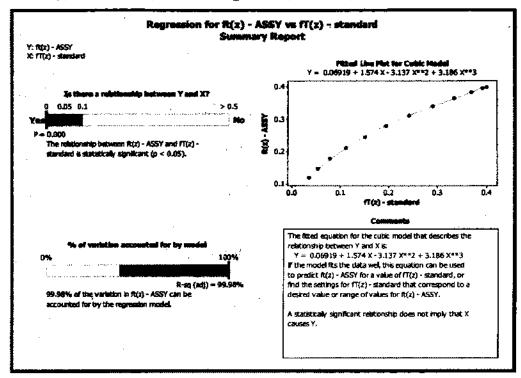
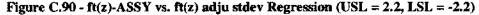
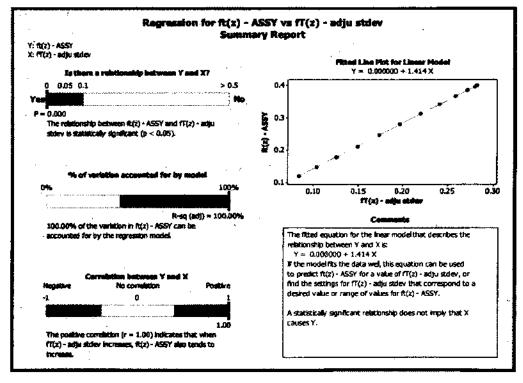


Figure C.89 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 2.2, LSL = -2.2)





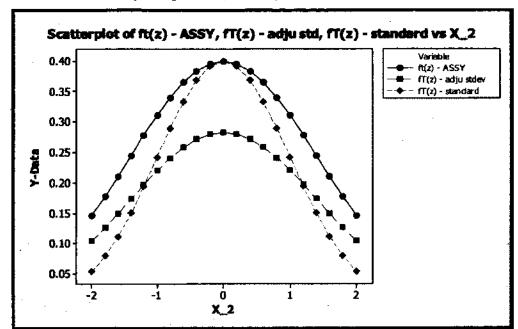
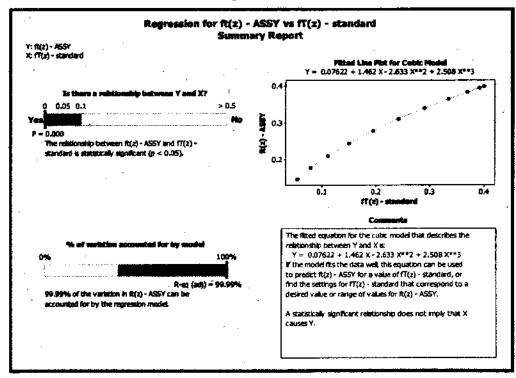


Figure C.91 - TSND Assembly Comparison (USL = 2, LSL = -2)





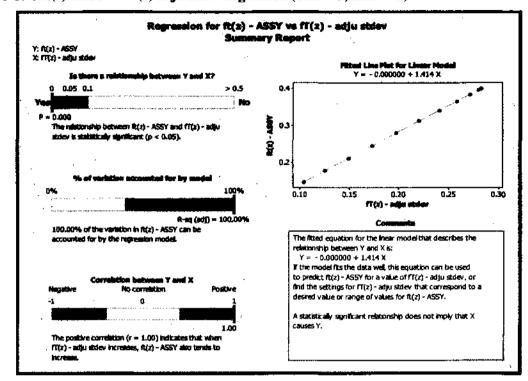
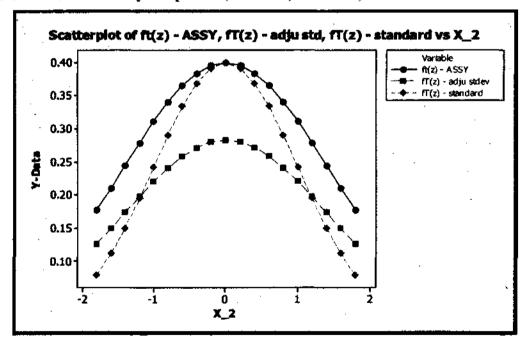


Figure C.93 ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 2, LSL = -2)





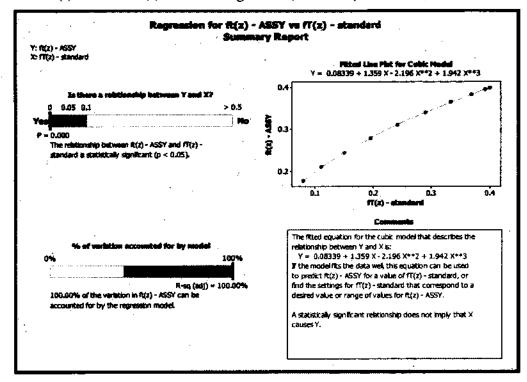
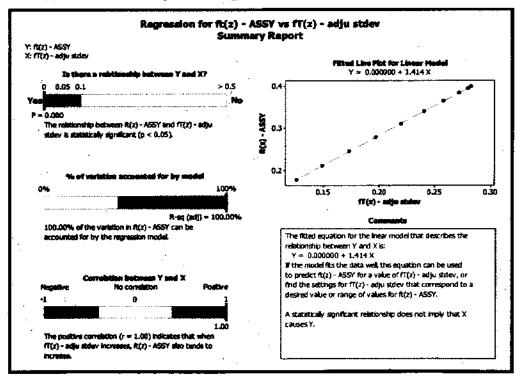


Figure C.95 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 1.8, LSL = -1.8)





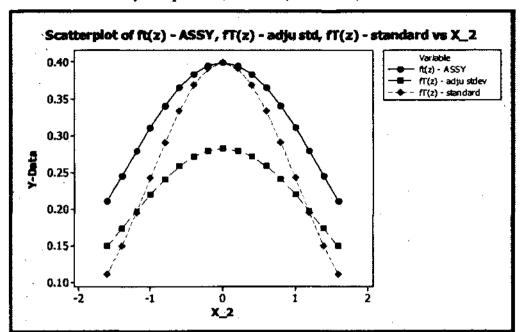
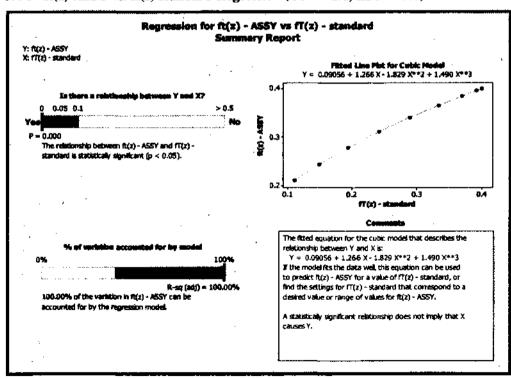


Figure C.97 - TSND Assembly Comparison (USL = 1.6, LSL = -1.6)





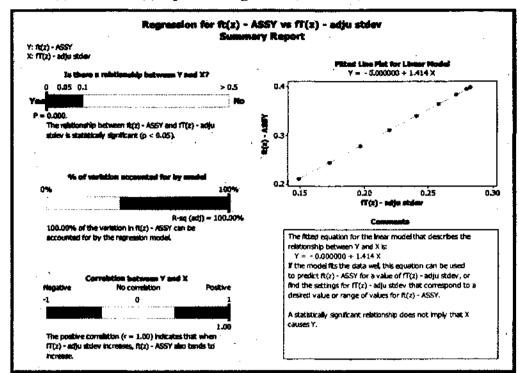
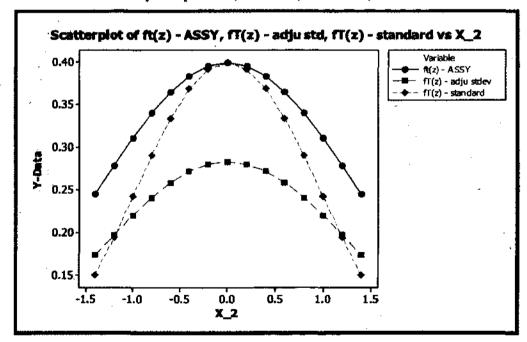


Figure C.99 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 1.6, LSL = -1.6)





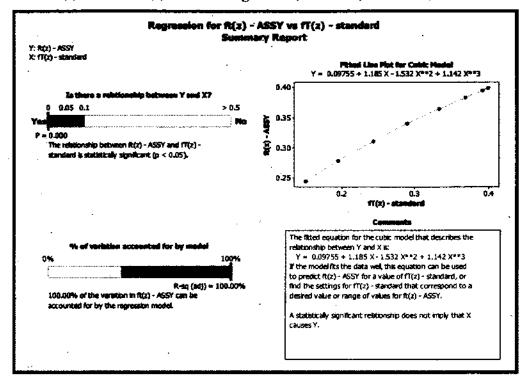
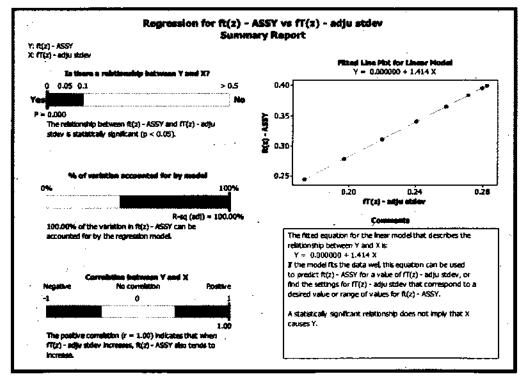


Figure C.101 · ft(z)-ASSY vs. ft(z) standard Regression (USL = 1.4, LSL = -1.4)





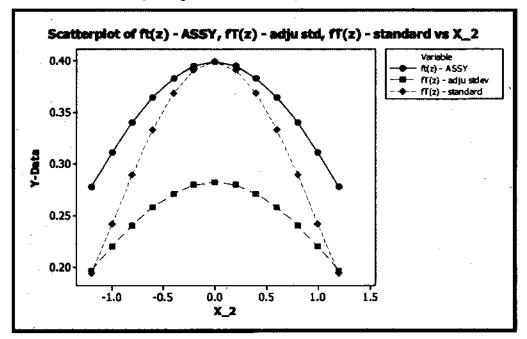
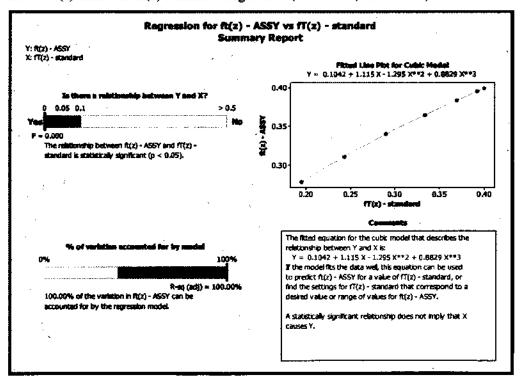


Figure C.103 - TSND Assembly Comparison (USL = 1.2, LSL = -1.2)

Figure C.104 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 1.2, LSL = -1.2)



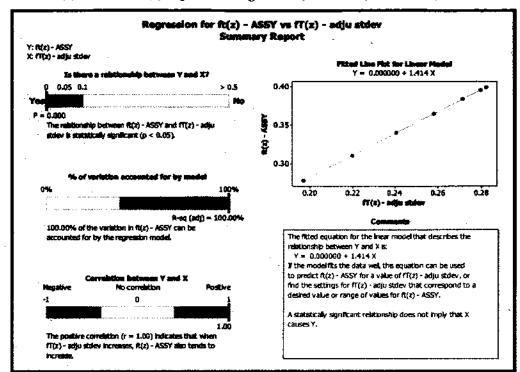
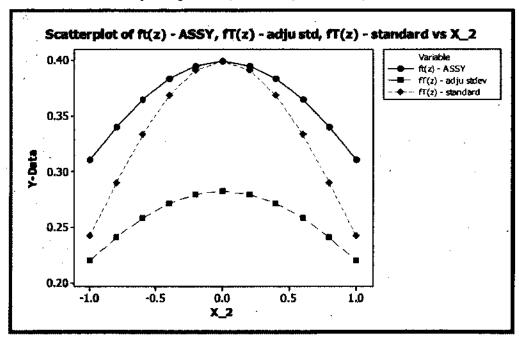


Figure C.105 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 1.2, LSL = -1.2)





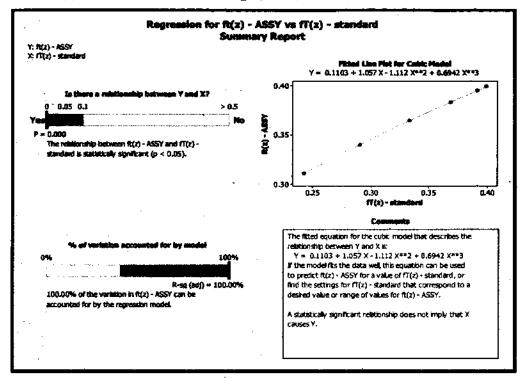
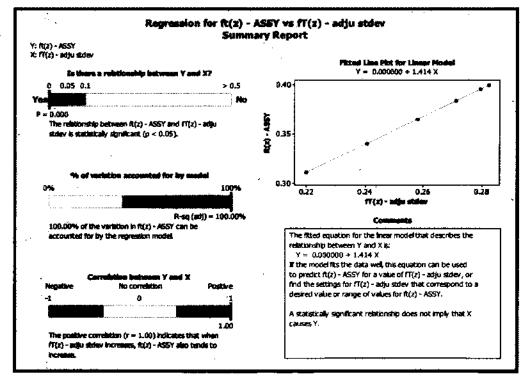


Figure C.107 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 1, LSL = -1)





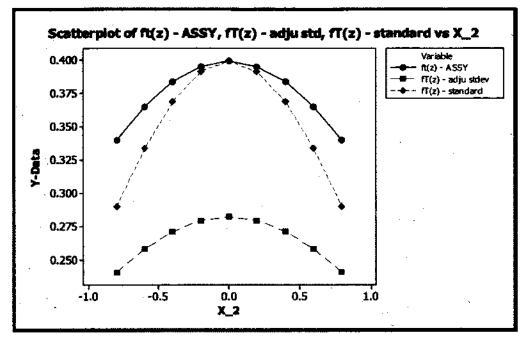
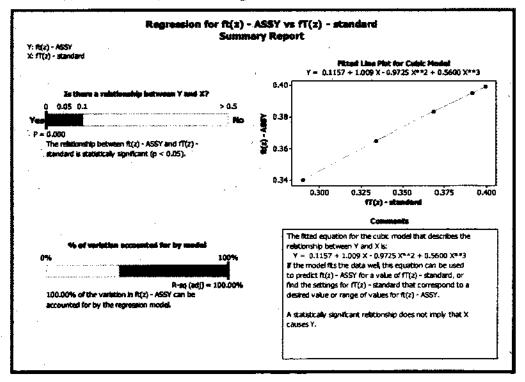


Figure C.109 - TSND Assembly Comparison (USL = 0.8, LSL = -0.8)





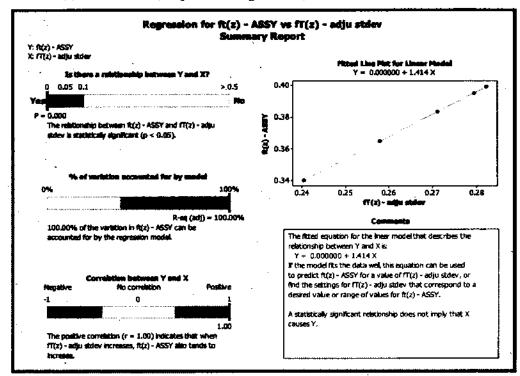
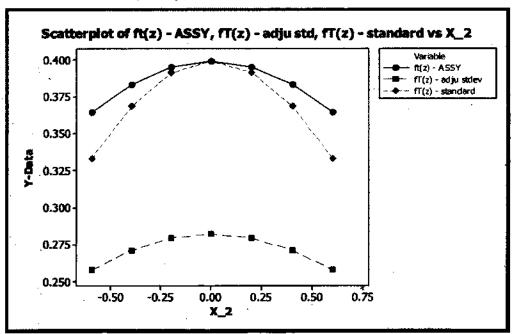


Figure C.111 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 0.8, LSL = -0.8)





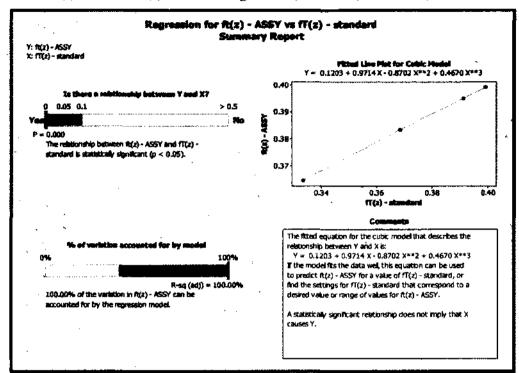
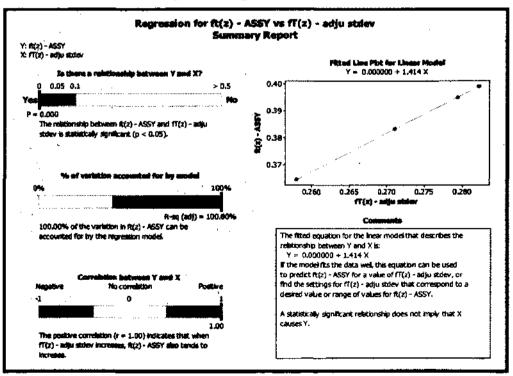


Figure C.113 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 0.6, LSL = -0.6)





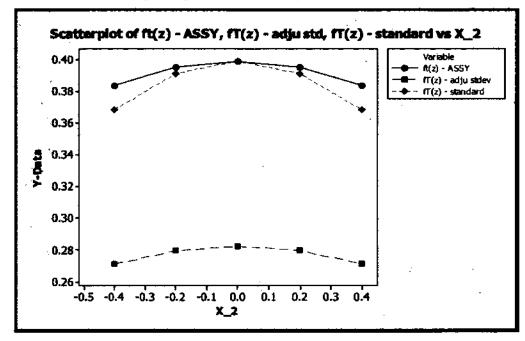
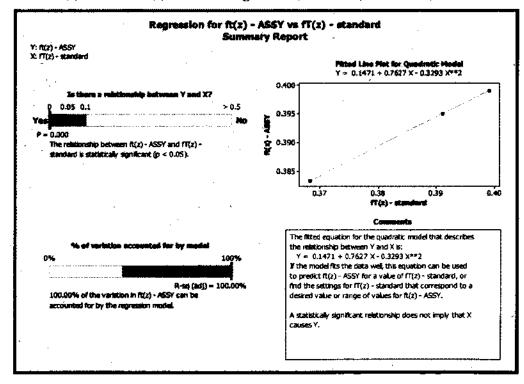


Figure C.115 - TSND Assembly Comparison (USL = 0.4, LSL = -0.4)





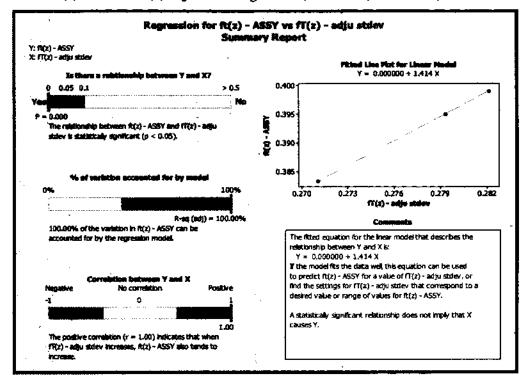
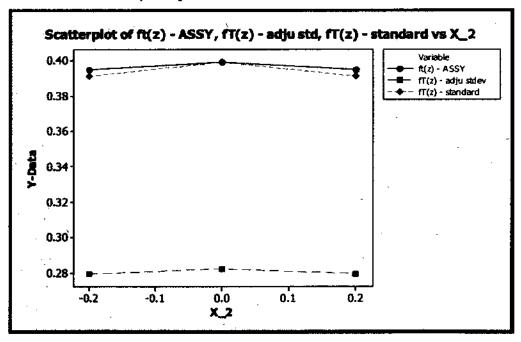


Figure C.117 - ft(z)-ASSY vs. ft(z) adju stdev Regression (USL = 0.4, LSL = -0.4)





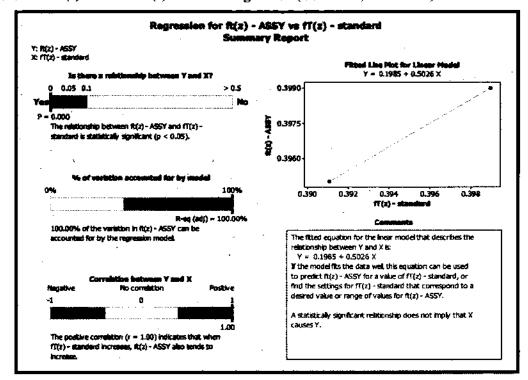
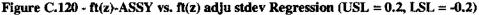
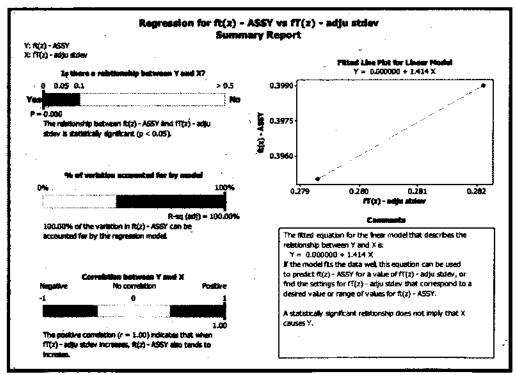


Figure C.119 - ft(z)-ASSY vs. ft(z) standard Regression (USL = 0.2, LSL = -0.2)





APPENDIX D: TSND ANALYSIS EXAMPLES

This appendix documents the analysis results for three simulated truncated standard normal distribution assemblies. Various examples and their results demonstrate the application of a truncated standard normal distribution characteristic function inversion using an inversion factor. This example has been baselined against calculation methods which employ methods found in References [104] and [105].

The three examples identified use the inversion factor verified from a single truncated standard normal distribution. Inversion factors for truncated standard normal distributions will be established for various combinations (i.e., USL = 8 to LSL = -8). For the purpose of this example, identical combinations will be used due to the multitude of combinations and to maintain simplicity in the calculations presented within the framework for this research.

Refer to Section 4 for additional information.

Example 1:

Simulation Input Parameters: $\mu = 0$, $\sigma = 1$, LSL = -2, USL = 2, n = 10,000 (sample size)

Table D.1 Truncated Distribution Simulation Range, 10,000 Samples (-2 to 2)

Bin	Frequency	Bin	Frequency		Bin	Frequency	Bin	Frequency
-4	0	-1.9	120		0.1	313	2.1	0
-3.9	0	-1.8	136		0.2	316	2.2	0
-3.8	0	-1.7	118		0.3	352	2.3	0
-3.7	0	-1.6	150		0.4	340	2,4	0
-3.6	0	-1.5	197		0.5	352	2.5	0
-3.5	0	-1.4	189		0.6	331	2.6	0
-3.4	0	-1.3	202		0.7	328	2.7	0
-3.3	0	-1.2	212		0.8	282	2.8	0
-3.2	0	-1.1	238		0.9	298	2.9	0
-3.1	0	-1	241		1	290	3	0
-3	0	-0.9	256		1.1	261	3.1	0
-2.9	0	-0.8	309		1.2	226	3.2	0
-2.8	0	-0.7	304		1.3	230	3.3	0
-2.7	0	-0.6	300		1.4	223	3.4	0
-2.6	0	-0.5	277		1.5	169	3.5	0
-2.5	0	-0.4	337		1.6	192	3.6	0
-2.4	0	-0.3	306		1.7	164	3.7	0
-2.3	0	-0.2	340_		1.8	160	3.8	0
-2.2	0	-0.1	307		1.9	140	3.9	0
-2.1	0	-9.91E- 15	365		2	129	4	0
-2	0	•		' '			More	0

Table D.2 - Pearson Correlation of Example 1

	Pearson correlation of ft(z) a- ASSY and	Pearson correlation of ft(z) a- ASSY and		
TSND RANGE	f(z) - standard	ft(z) – adju stdev		
USL = 2, $LSL = -2$.973	1		

Table D.3 - Regression Analysis of Example 1

TSND	R-sq		Fitted Line Plot Equation for Cubic
(USL = 2, LSL = -2)	(adj)	P-Value	Model
ft(z) a- ASSY and			Y = 0.03426 + 2.546 X - 7.524
ft(z) – standard	99.55%	p < 0.001	X**2 + 9.334 X**3
ft(z) a- ASSY and			
ft(z) – adju stdev	100%	p < 0.001	Y = 0.000000 + 1.545 X

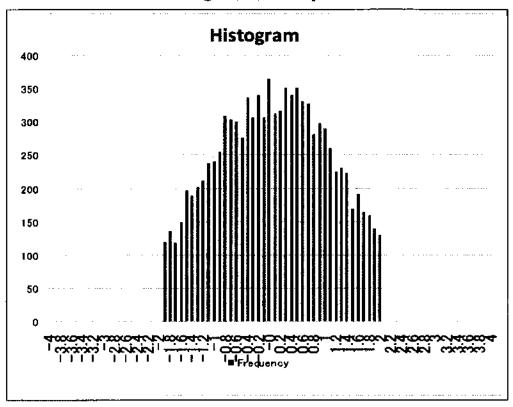
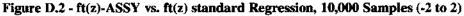
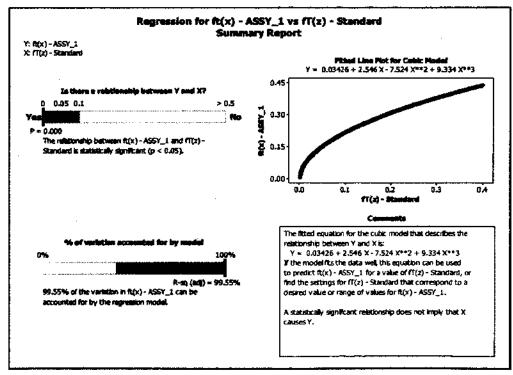


Figure D.1 - Truncated Distribution Histogram, 10,000 Samples (-2 to 2)





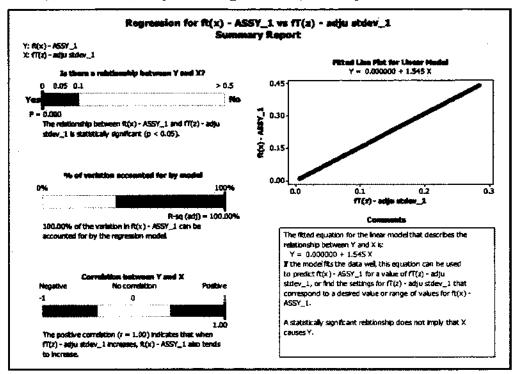


Figure D.3 - ft(z)-ASSY vs. ft(z) adju stdev Regression, 10,000 Samples (-2 to 2)

Example 2:

Simulation Input Parameters: $\mu = 0$, $\sigma = 1$, LSL = -3, USL = 3, n = 10,000 (sample size)

Table D.4 Truncated Distribution Simulation Range, 10,000 Samples (-3 to 3)

Bin	Frequency	Bin	Frequency		Bin	Frequency	Bin	Frequency
-4	0	-1.9	57		0.1	365	2.1	57
-3.9	0	-1.8	67		0.2	386	2.2	39
-3.8	0	-1.7	60		0.3	401	2.3	37
-3.7	0	-1.6	100		0.4	392	2.4	29
-3.6	0	-1.5	129		0.5	371	2.5	18
-3.5	0	-1.4	156		0.6	365	2.6	14
-3.4	0	-1.3	153		0.7	315	2.7	18
-3.3	0	-1.2	186		0.8	321	2.8	11
-3.2	0	-1.1	192	[0.9	303	2.9	7
-3.1	0	-1	228	[I	259	3	6
-3	0	-0.9	242	[1.1	221	3.1	0
-2.9	9	-0.8	266	[1.2	215	3.2	0
-2.8	6	-0.7	326	[1.3	188	3.3	0
-2.7	10	-0.6	337		1.4	138	3.4	0
-2.6	13	-0.5	338	[1.5	156	3.5	0
-2.5	17	-0.4	321	[1.6	123	3.6	0
-2.4	20	-0.3	374	i [1.7	106	3.7	0
-2.3	23	-0.2	361	i [1.8	88	3.8	0
-2.2	36	-0.1	392		1.9	89	3.9	0
-2.1	31	-9.9E-15	400		2	58	4	0
-2	54			•			More	0

Table D.5 - Pearson Correlation of Example 2

	Pearson correlation of ft(z) a- ASSY and	Pearson correlation of ft(z) a- ASSY and
TSND RANGE	ft(z) - standard	ft(z) – adju stdev
USL = 3, LSL = -3	.972	1

Table D.6 - Regression Analysis of Example 2

TSND	R-sq		
(USL = 3, LSL = -3)	(adj)	P-Value	Fitted Line Plot Equation for Cubic Model
ft(z) a- ASSY and ft(z) -			Y = 0.02832 + 2.369 X - 7.014 X**2 +
standard	99.45%	p < 0.001	8.675 X**3
ft(z) a- ASSY and ft(z) - adju			Y = -0.000000+1.422 X+0.000000 X**2 -
stdev	100%	Note 1	0.000000 X**3

Note 1: For values referencing this note the p-value could not be calculated

Note 2: Standard deviation is 1, unless otherwise noted in Appendix B



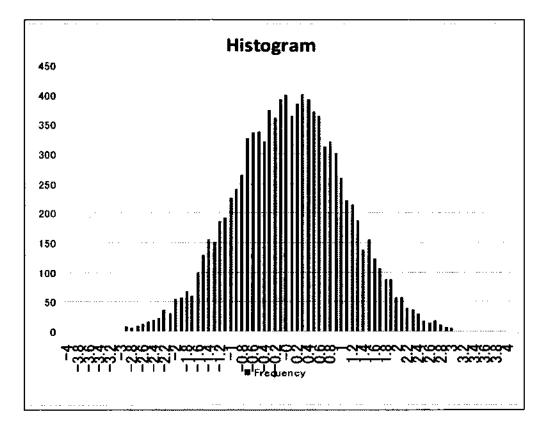
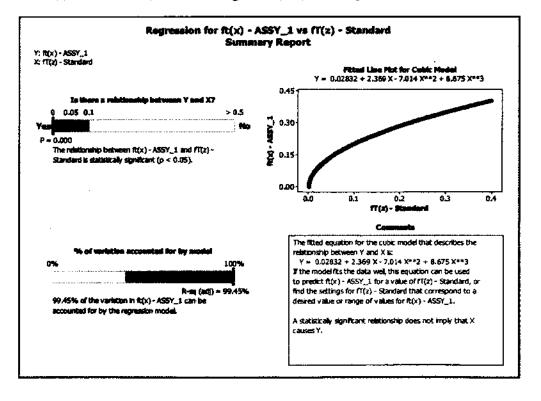


Figure D.5 - ft(z)-ASSY vs. ft(z) standard Regression, 10,000 Samples (-3 to 3)



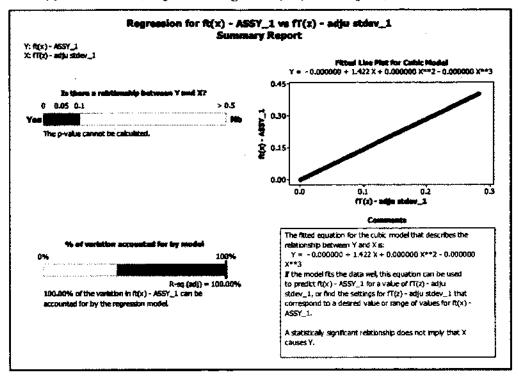


Figure D.6 - ft(z)-ASSY vs. ft(z) adju stdev Regression, 10,000 Samples (-3 to 3)

Example 3:

Simulation Input Parameters: $\mu = 0$, $\sigma = 1$, LSL = -4, USL = 4, n = 10,000 (sample size),

Table D.7 Truncated Distribution Simulation Range, 10,000 Samples (-4 to 4)

Bin	Frequency	Bin	Frequency	Bin	Frequency	Bin	Frequency
-4	0	-1.9	57	0.1	369	2.1	52
-3.9	0	-1.8	61	0.2	388	2.2	37
-3.8	0	-1.7	59	0.3	411	2.3	38
-3.7	0	-1.6	90	0.4	398	2.4	25
-3.6	2	-1.5	123	0.5	372	2.5	14
-3.5	2	-1.4	158	0.6	370	2.6	19
-3.4	0	-1.3	156	0.7	315	2.7	11
-3.3	3	-1,2	182	0.8	317	2.8	12
-3.2	3	-1.1	191	0.9	301	2.9	6
-3.1	1	-1	221	1	253	3	7
-3	3	-0.9	241	1.1	223	3.1	3
-2.9	6	-0.8	274	1.2	221	3.2	4
-2.8	7	-0.7	326	1.3	188	3.3	3
-2.7	8	-0.6	337	1.4	143	3.4	2
-2.6	11	-0.5	344	1.5	142	3.5	0
-2.5	14	-0.4	330	1.6	122	3.6	0
-2.4	21	-0.3	371	1.7	101	3.7	0
-2.3	21	-0.2	363	1.8	85	3.8	1
-2.2	36	-0.1	399	1.9	87	3.9	0
-2.1	28	-9.91E- 15	403	2	56	4	0
-2	52					More	0

Table D.8 - Pearson Correlation of Example 3

	Pearson correlation of	Pearson correlation of
	ft(z) a- ASSY and	ft(z) a- ASSY and
TSND RANGE	ft(z) - standard	ft(z) – adju stdev
USL = 4, LSL = -4	.972	1

Table D.9 - Regression Analysis of Example 3

TSND	R-sq	P-	
(USL = 4, LSL = -4)	(adj)	Value	Fitted Line Plot Equation for Cubic Model
ft(z) a- ASSY and ft(z) -		p <	$Y = 0.02827 + 2.352 X - 6.955 X^{**}2 + 8.593$
standard	99.45%	0.001	X**3
ft(z) a- ASSY and ft(z) - adju		Note	$\dot{Y} = 0.0000000 + 1.414 \text{X} - 0.0000000 \text{X}^{**2} +$
stdev	100%	1	0.000000 X**3

Note 1: For values referencing this note the p-value could not be calculated

Note 2: Standard deviation is 1, unless otherwise noted in Appendix B



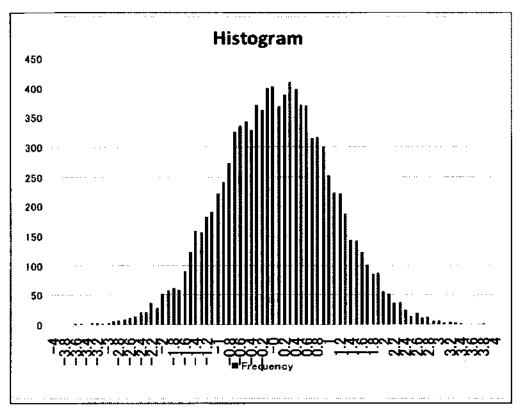
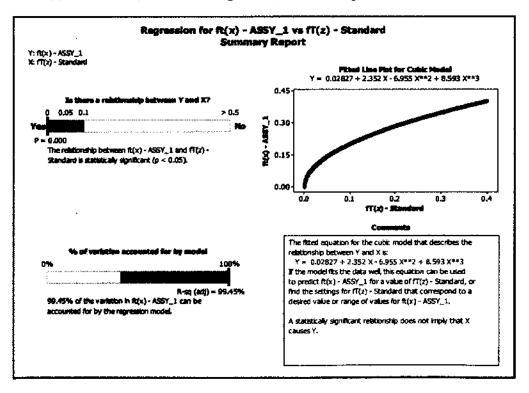


Figure D.8 - ft(z)-ASSY vs. ft(z) standard Regression, 10,000 Samples (-4 to 4)



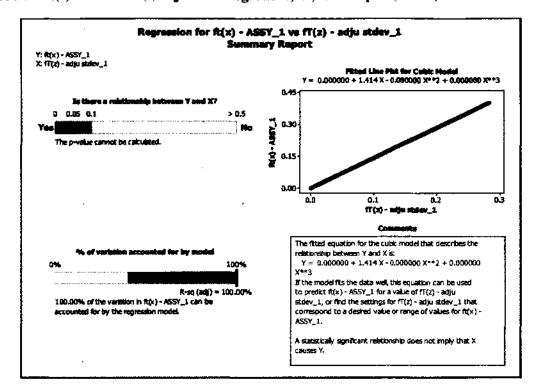


Figure D.9 - ft(z)-ASSY vs. ft(z) adju stdev Regression, 10,000 Samples (-4 to 4)

APPENDIX E: CATEGORIZATION INFORMATION

This appendix provides grouping information related to the comparative review and literature review conducted as part of this research. Categorizations generally focused on the primary method identified by the research in each field of categorization. The analysis results for the comparative reviews performed are identified in Appendices F and G. It is not the intent of this dissertation to define the general concepts presented in this appendix. Refer to relevant references for insight into that level of evaluation which is outside the scope of this dissertation. In order to reduce the degree of analysis subjectivity, the following serves to contextualize the groupings performed in this research:

<u>Search Heuristics</u>: Search Heuristic generally included beam search, pseudo random search, and tab search heuristics. Refer to Michalewicz and Fogel (1998) for additional heuristic summary information outside the scope of this work.

Heuristic Procedure: Heuristic procedures were generally grouped to include explicitly identified heuristic procedure, knowledge based procedure, Taguchi procedures, and other step by step instructions that are generally representative of a heuristic as defined above.

Algorithm: Algorithm groupings generally included the references to assignment algorithms, greedy algorithms, genetic algorithms, network based algorithms, and other general reference to mathematical steps and formulations. Refer to Michalewicz and Fogel (1998) for algorithm information which is outside the scope of this work.

Optimization: The grouping and identification of optimization techniques was identified if any of the following optimization methods were identified:

- Any Colony Optimization
- Perturbation Techniques
- Keifer-Wolfwitz Optimization Procedure
- Operations Research
- Highly Optimized Tolerance (HOT)
- Utility Maximization through Criteria Weighting
- Optimization Model
- Simplex Method (or variant)
- Pattern Enumeration
- Mixed Integer Programming
- Attribute Level Driven
- Linear
- Policy Space Procedure
- Mathematical formulation
- Analytical Target Cascading
- Simulated Annealing
- Heuristic Based
- Weighting
- Function

Benchmarking Methods:

- An Example, Case Study, Design Specification, and Case Study Compared to design specification: This benchmarking method was identified if the literature generally or specifically involved examples, case studies, or design specifications as part of the literature evaluations.
- Heuristics or Other Methods: This grouping was identified if heuristic performance or computational experiment comparisons were identified by the literature.
- Historical or Collected Data Comparisons
- Simulation Data or Study: Results of examples compared with simulation study or other simulation/study comparison
- Mathematical Formulation: Identified if the primary benchmarking method observed dealt with mathematical formulations and related comparisons.
- Inconclusive or Not Performed: No experimental comparisons were performed.

Data Source/Simulation:

- Historical: Historical data was generally grouped or identified as data that was used
 for analysis based on previously collected or possibly even analyzed data. Historical
 data was pre-existing data. In some cases historical data was used to compare an
 existing state with a proposed future or improved condition.
- Data Generated: Any reference to data that was simulated, generated, randomly
 created or proposed as part of a scholarly work. Example of data generation could
 include such data as Monte Carlo Simulation or random number generation.

- Empirical data: Empirical data was generally identified as data which may have involved real time results or other industry related data.
- Sampled Data: Sample data groups consisted of those groups pulled from identified sample data from a given process.
- Example Data: Example data was grouped as that data which was used for demonstration purposes. This field differs from data generation or historical data.
- Inconclusive Identified when the data source was not easily or readily identifiable.

<u>Test Methods</u>: Test methods were generally grouped into one of the following categories:

- Efficiency Improvement: Methods in which tests were performed to show an improvement in efficiency over a given value, process, heuristic, or other measured result.
- Demonstration of "Good" Solution: This grouping included results which focused not on optimization but on obtaining reasonably accurate or balanced solutions.
- Comparative Analysis: Direct or interpreted tests by comparison
- Simulation: A test method in which data may have been generated or developed as a means to produce a data set or solve a solution.
- Correlations: Statistical analysis such a Pearson's Correlation Coefficient or other general method of comparing the relationships of one variable to another.
- Experiment: Test methods done by physical or theoretical method.
- Error Ratio: Regression or other analysis in which error ratios were evaluated

- Mathematical Model: A test method involving the evaluation or utilization of a mathematical or analytical model.
- Commentary: Qualitative testing focused on interpretation and judgment

"Meaningful results" are defined as: either a statistically significant relationship, positive correlation/relationship, or any other observed, calculated, or identified parameter which provides data or indications not previously understood by the body of knowledge.

APPENDIX F: LITERATURE REVIEW VARIABLES

This appendix provides variables utilized in the gap analysis of the subject dissertation. Refer to Chapter 2 for the literature review variables reviewed (e.g., truncation, Selective assembly, etc.). It should be noted that not all references were utilized in this review. An "X" denotes that the literature identified an explicit or implied identification of the literature review variable. Additionally, general calculation references, definitions, duplicative or other references were excluded from this review. All review variables analyzed are included in Table F.1. Refer to Chapter 2 for additional information.

Table F. 1 – Literature Review Table

					Literature Re	Literature Review Variables	at the				
Réses	Trancated Assembly Trancates	S. de Chr.	Parago Design	Hanrishes/ Francesches/ Estatishe Selutions	Optimal Target Setting Optimization/Mar- Minimization	Invatory Margaret System Storige Defreey	Assembly Systems Freshin Freshin Membershin Freshin Freshin Supercing	Kaerledge Abergenne	Complexity Robert Design Smallerity Anadysis	Dynamic Simuladina Simuladina	Estre Volte Plant
***			X	×					×	-	
Malakoot, B.B. (1994)					I		X				
Park M.W., & Kan Y.D. (1939)				X	X		X				
Pourtsbui, B. (1992)				X	X	X	X				
Pourbabai, B. (1989)			X		X	X	X				
Can, X, & Ha, Y. (1987)			X	ĸ	ĸ	ĸ	X		×	ж	
Seidham, A., & Tenenbaum, A. (1994)		ï	x	×	X		M		ĸ	K	
Kosfeld, M.A.,& Quinn, T.D. (1999)					×	X			×	×	
Bown DE, & Spilene, A.R. (1989)				H	×			н			
Thelon, L.S., Neig S.K., Wen, K.W., & Tennewich P. (2000)				M	М				X	×	
Coverbie, I., & Whanton, F. (1976)			X	X	×	X					
Rubin P.A. (1990)			×	X	¥					×	

					Literature Re	Literature Review Variables	-				:
Press	Transfer Average	S de die	Telemacy Present Continue	Heurisfest Franceschy Heurisfe Schfens	Optimal Target Selling Optimization Men- Minimalian	Investory Management Systems Starnger Definery	Assembly Systemy Florible Membedering Production Supercing	Kranide Margani	Control Parties	Dynask Salake Salake	Extrase Volte Theory (EVT)
Klum, G. (1977)				x				-			
Nais, S.K., Thakue, L.S., & Wen, K.W. (1995)		X	ĸ	М	ĸ			M	H	×	
Barish, NN (1963)								x			
Naddor, B. (1975)				x	X	×					
Sq. K.C., & Soot, C.H. (1994)			X	X	x	X	X			×	
Klinowicz, 1 G. (1990)				X	×	X					
Bai, H., & Kwong, C.K. (2003)			x	X	X						
Cooper AB, Georgiopodos P., Kim H.M., & Pepalembers, P. Y. (2006)		×		×	¥	The second section of the section of					
Kwol, K.S., Driesen, B.I., & Philips, C.A. (2002)				×	X				×		
Hanner, G.Q., Qa, T., Channer, D. W.L., & Linner, L. (2006)					×						×
Cale 14, M.H (2004)	X		X		X		X		X		

					Literature Ber	Literature Review Variables					
Bafores.ce	Trancated Assembly/ Trancates	Salaufire Assembly	Tolermood Parameter Beriga Quality Confed	Henristes Frameworks Hanriste Schtims	Optimal Target Setting Optimization Man- Minimization	Inventory Menogenent Systemy Sternger Definery	Assembly Systems Fraches Fraches Membership Fraches Sequencing	Kamiséga Mangamat	Complexity/ Redext Design/ Servicity/ Analysis	Dynamic Similbrim Si milbrim	Extruse Value Theory (EVT)
Obsrabo, Y. (2004)				×	×						
Kim, HM, Michelene, NF., & Papelemben, P.Y (2003)		·	ĸ	· "	×					×	
Krayamafawicz, R. (1990)					×				×		
Moothead, P.R., & Wh. C.F.I. (1998)			x	X	x				×		
Muss, R., Starges, R. H., & Chen, F. F. (2006)			K	Ħ	Ħ		X			×	
Minne, R., & Chen, F.F. (undered)		×		Ħ	ĸ					X	
Muss, R., Chen, F.F., & Groesen, A. S. (undered)				×	X		X			x	
Mass, R., & Chen, F.F. (2008)		X	X	X	X					ĸ	
Russe, S.H., Lin, Q., & Musse, R. (2004)		X	x	X	X		X			×	
Zhang, W.Z., Wang, G.X., Check, B.T., & Nee, A.Y.C. (2003)				X			×	ж			
Meller, R.D., & Boner, Y.A. (1996)				×	×						

					Literature Re	wien Verinbles					
Reference	Truncated Assembly/ Truncation	Selective Amendiy	Tolerance/ Parameter Design/ Quality Control	Heuritica Francusche Heuritic Solutions	Optimal Target Setting Optimisation/Mex-	Inventory Management Systems Storage Delivery	Amendaly Systems/ Flexible Missoficturing/ Production Sequencing	Knowledge Management	Complimity/ Robust Design/ Sensitivity Analysis	Dynamic Simulation Simulation	Extreme Value Theory (EVI)
Kwon, H-M, Kim, K-J, & Chandra, M J. (1999)	X	X	x		x			x			<u>.</u>
De Fanio, T.L., Rhee, S.J., & Whitney, D.E. (1999)				x			x				
Kaman, SM., Jayabalan, V., & Jeevmanhan, K. (2003)		X		x	x						
Pomembeles. S.G., Astrinden. P., & Rao, M.S. (2003)				X	x		x				
Kaman, SM., & Inyabalan, V. (2001)	х	X		x					х		
Pught, G.A. (1986)	x	x					X				
Das, S.K., & Serie. S.C. (1988)				x		X	X			x	
Cittoliz, A. (1997)				x			х				
Puph, G.A. (1992)	X	X								x	
Massoor, E.M. (1961)		x	x				x				
Desmond, D. I., & Setty, C.A. (1961)		X	x	X						į	

	Extreme Value Theory (EVT)											
	Dymonic Standation/ Simelation			X						X	×	×
	Complexity Robert Bengal Semilirity Analysis	X		X				×				
	Krawladge Mangement				×							
	Assembly Systemy Flexible Manufacturing Production Sequencing	Х	X	X	X	×	Х		X	×	×	
Literature Kerien Variables	Lavondary Management Systems Serape Defenry									×		
Literature Ka	Optional Target Section Optional military Marinette		X	X	X	×	×	×	×		×	×
	Heuristica/ Francuscha/ Heuristic Scheipen		×	X	х	Ħ		×		X	×	
	Telemacs Parameter Danga Quality Control	X						×	X	×	X	X
	Selective Assembly				X	X	X			X		
	Truncated Amunhty/ Truncation											
_	Reference	Whitney, D. E. (2006)	Lee, S., & Shin Y.G. (1990)	Lee, B., & Saiton, K. (2007)	Aged, B. & Kusisk, A. (2004)	Abe, S., Mongeme, T., Obe, F., & Montaki, N. (1999)	Lee, S. (1994)	Bohardawsky, I.O., Johnson, M.E., & Swin, M.E. (1996)	Sanderson, A.C. (1997)	Phoendopleb, T. & Caplack, D. (2007)	Gutierre, G.I., Haumer, W.H., & Lee, H.L. (1995)	Brankis, J.B. (2001)

				X	X		X				Park, K. Kang. S. & Park, S. (1996)
	X					X	X				M.zerbenna, M., Seculyaber, M., & Singer, M., & Laval, E. (1998)
				X	X	X	X	X			Logandem, R., & Sommen, A., Southern, A. (1991)
					X		X			X	Gendreau, M., Hertz, A., & Leporte, G. (1994)
					X	X	X		,		Cendram, M., Legorie, G., & Sécuin R. (1996)
					X	X	X				Rochet Y., & Semet F. (1994)
							X				Pummen, A.P., & Ameje, Y.P. (1995)
	Х					X					Pasiz, A.V. (2002)
						X	X				(T99T) . E .idla.2
							X				Lozzon, S., Adenso-Dizer, B., Eunia I., & Oniara I. (1999)
Marting Value Times (T/3)	immered Simulated Simulated seineliste	Venques?) Sealing Sealing Sealing in Sealing	sgbalwarii stampanii/	'pidmont'. 'amour?? sidizof? gainers densité asiraber? gainense?	Inventory Management Systems Stenges Stenges	ingraT ismitqO Sprints? -rahAssinchmitqO gattashminthf	'erinine.H 'erinem:1 'erine.H 'alakwiH endmis?	Tolerance Parameter Design Occupi	svitzelo? ¿śdanach	Trescated Amenda Seinomrif	saratañ
					naldaira'i mir	aff sustanstal					

					Literature Re	Literature Review Variables					
Reference	I Village	Selective Aucubly	Tolerance Parameter Donica Quality Control	Bearities/ Francosta/ Bearitie Solution	Optimal Target Setting/ Optimization/for-	Inventory Management Systems Serges Deferry	Assembly Systems Farable Manufacturing Production Sequencing	Knethije Mangemen	Complacty/ Robust Design/ Scenitivity Analysis	Dynamic Stands (to a) Stands (to a)	Extreme Value Theory (EVT)
Kozm, E. (2000)				X	X	×					
Glover, F. (1990)				X	X						
Madeland, R.E. (1990)				X							
Grine Yesuff, T., & Westch, P. (2010)								X			X
Wilson, I.D., & Roach, P.A. (2000)				X	X	X	×				
Consiglio, A., & Zenies, S. (1999)	· •		X	×	×					×	
Mooralie, IV, & Nageno, M.S. (1998)				X	X		X			X	
Basna, R.A., Buck, R.J., Riccomanno. E., & Wigon, H.P. (1996)				×					M	,	
Bevbasoëh. A. (2001)				Х				X			
Dell'Amico, M (1996)	X			X			X		×		
Patterson, R.A., & Rolland, E. (2002)				×				X		×	

					Literature Re	Literature Review Variables					:
Reference	Transmind Assembly/ Tymenties	Salective Assembly	Talenaese Panaese Daniga Quality Cantral	Remissies Francenthy Hemitic Solutions	Option Target Setting Option of Max.	Inventory Management Systems Storger	Assembly System Flexible Manufacturing Production Sequencing	Karalahe Mangemet	Complexity/ Robert Dunigs/ Somitivity Analysis	Dynamic Stanbilina Stanbilina	Extrane Value Theory (EVT)
Chieng, W.C., Konvelis P., & Urber, TL. (2002)				H	×	×	×				
Remiser-Baltum, N.D. (1995)				I	X						
Arrack C.C., Orlin J.B. & Tai, R.P. (1997)				×	×			X	X		
Bracker, J.S., & Paserson, J.N. (1986)				×					X		
hm, JB, Jambsen, S.H., & Swither, JR. (1999)				×	X		X	X		×	
Liu, L., & Chang. K.L. (1997)			×	-	X	×					
Marrole IB, & Schertz R.H. (1995)				X	X	X					
Oblemiller, M. (1997)				X	X						
Bisguard, S. (1997)		X	X				X				
Ostumeier, M. (2003)	×										
Bradley, D. M., & Gapta, R.C. (2002)	X										

					Literature Re	wiew Variables					
Reference	Truncated Amenaly/ Truncation	Soloctive Assembly	Tolerance/ Parameter Design/ Quality Control	Hamistica Francesocka Hamistic Salations	Optimal Target Setting/ Optimalstins/Max- Minimization	Inventory Management Systems Storage Delivery	Amenably Systems Flexible Manufacturing Production Sequencing	Knowledge Managament	Complicity/ Robust Dusign/ Sensitivity Analysis	Dynamie Simulation/ Simulation	Extreme Value Theory (EVI)
Dhryman, P. J. (2005)	x		x		X					X	
Yang, C., Gui, W., Kong, L., & Wang, Y. (2009)				X	x			X .		x	
Griesse, N. (2011)											
Zhu, Q., & Oommen, J. (1997)				X	x	x	Х	x			
Bouchard, B., Elie. R., & Imbert C. (2010)			·	x	x					x	
Simpson, D. P. (2008)	x		X	x	x					x	
Asvadurov, S., Druskin, V., Goddati, M., & Knishnaman, L. (2003)	x			x	x						
Xisoping, B. & Ringing, M. (2009)				X		X	x		X	X	
Messe, D., Neir, V., & Sadilanto, A. (2004)		X		x	X	x				x	
Xinoping, B. & Finstine, M. (2009)					X	x	-				X
Glover, F., & Laguna, M (undeted)				X	X						

					Literatur Ka	Literatur Resiss Variables	: : 				
	Trensceed Amenday Transcettes	Salective Amenal &	Tolerance Parameter Opality Control	Paris Services	Optimal Target Setting Optimization	Enventory Management System Stange Delivery	Amenda System Franka Mandalan Production Superior	Kurkip. Karkip.	Complexity Release Design Sessitivity Analysis	Dynamic Simulation	Extrema Value Theory (EVI)
4 .6	×		X	X	X			X			
Johns on, A., & Themopoules, N.T. (unched)	X		W		×						
Khararash, M.T., Bowling, S.R., Kaswkushool, S., & Cho, B.R. (1005)	×										
Johns on, A.C., & Thermopoules, N.T. (modeled)	×										
Khasarash M.T., Bowling S.R., Karatuskool S., & Cho, B.R. (2005)	×										
Resolde, M. (2012)	X									X	×
Bimaket, I., & Litt., J. (2012)										Х	×
Kuvesber, H., & Mere, I. (2008)										x	×
Dress, H., de Hass. L., & Li, D. (2006)											×
Stoymov, S. & Rachev, S. (2008)	×			- · · · ·						×	×

:					Literatum Re	wiew Variables					
Reference	Truncated Amendy/ Truncation	Selective Amembly	Tolerance/ Parameter Design/ Quality Control	Hauristica/ Frameworks/ Heuristic Salations	Optimal Target Setting/ Optimization/Max- Minimization	Inventory Management Systems/ Storage/ Dolivery	Amembly Systems/ Flexible Minufecturing/ Production Sequencing	Knowledge Management	Camplicity/ Robust Design/ Sensitivity Analysis	Dynamic Simulation/ Simulation	Extreme Value Theory (EVT)
Chavez-Dessoulin, V., & Rouhmi. A. (2004)											X
Peng, L., & Qi, Y. (2009)	X						, ,				x
Bermudex, P.D.Z., & Kotz, S. (2010)	X										X
Bermudez, P.D.Z., & Kotz, S. (2010)	X		x					:			<u> </u>
Hosrace, W.C. (2005)	X					·			!		
Brazenskas, V., & Kleefeld, A. (2009)			X						X	x	x
Carpinteri, A., Cometti. P., & Puzzi. S. (2005)	x		x							;	x
Brooks, C., Clam, A.D., Delle Molle, J.W., & Persand, G. (2005)			x							x	X
Diebolt, J., Guilleu, A., & Rached, I. (2005)			x				X				х
Castillo, E., Hadi A., Balakrishnan. N., Sarabia. J. (2005)	X		X							X	X

					Literature Ro	Literature Review Variables					
Reference	Truncated Amenaby/ Truncation	Salactiva Assembly	Tokenace Parameter Dunkey Quality Central	Hominica Francustal Heminic Solution	Optional Taxgat Setting/ Optionisation/Ant- Minimization	Laventery Management Systems/ Storage/ Delivery	Assembly System Flexible Manufacturing/ Production Sequencing	Kawledge Mangemen	Complexy/ Robust Bosine/ Semitivity Analysis	Dymanic Stands (fin) Stands (fin)	Errene Value Theory (EVI)
Michelewicz, Z., & Fogel, D. (1998)				x	X						
Whitney, D. E. (2006)			X				Х				
Billings Lev. P. (1995)											i
Sheffseld, S. (2011)											
Abadir, K., & Magrialinos., T. (2602)	X										
Shephard, N.G. (1992)	X	_									
Kawata, T. (1969)											
Bernedic, M., & Candal, I (2012)	X			-							 .

APPENDIX G: CATEGORIZATION AND COMPARATIVE ANALYSIS

This appendix provides a categorization and comparative analysis of the literature review variables for a sample set of data for the subject dissertation. It should be noted that not all references were utilized in this review. For example, general calculation references, definitions, duplicative or other references were excluded from this review. All review variables analyzed are included in Table G.7. Refer to Chapter 2 and Appendix E for additional information.

Table G.1 - Comparative Review Results Heuristic Type/Benchmark Method

Benchmark Method Henristic Type	An Kxample, Case Study, or Design Spec.	To natinity or Other or Indicate or Indica	Historical or Collected Data	Simulation Data or Study	olisemedie le le robatumedi other orminatio ormosedure rosedure	evindenoedl to V. , Performed, to V. ro eldseilgqA	Grand Total
Algorithm	46%	%9	1%	2%	2%	% 0	15%
Heuristic Procedure	10%	%6 6	1%	%5	1%	3%	28%
Search Heuristic	2%	%6	2%	%0	% 0	2%	15%
Simulated Annealing	%0	%0	%0	%0	1%	%0	1%
Inconclusive or Not Applicable	%9	2%	1%	%6	10%	12%	40%
Linear Programming	%0	%1	% 0	0%0	%0	0%	1%
Grand Total	23%	27%	46%	16%	14%	17%	127

Table G. 2 - Comparative Review Results Heuristic Type/Test Method

Testing (PM)	nmentary	parative yeis	elation	ood" utions	iciency alustion	pirical alysis	or Ratio	riment	or Inc.	n Model putation	ulation	id Total
Heuristic Type	Com	Comp. Analy	Corr	"Gor Solut	Effic Eval	Empi Analy	Erro	Experim	N/A	Math er Comp	Simu	Grand
Algorithm	0%	8%	0%	3%	1%	0%	0%	1%	0%	1%	2%	15%
Heuristic Procedure	2%	7%	1%	3%	5%	0%	0%	2%	1%	7%	1%	28%
Search Heuristic	0%	4%	0%	4%	4%	0%	1%	0%	0%	2%	1%	15%
Simulated Annealing	0%	0%	0%	0%	1%	0%	0%	0%	0%	0%	0%	1%
Inconclusive or Not Applicable	0%	7%	0%	2%	2%	4%	1%	0%	7%	16%	2%	40%
Linear Programming	0%	1%	0%	0%	0%	. 0%	0%	0%	0%	0%	0%	1%
Grand Total	2%	27%	1%	12%	12%	4%	2%	3%	8%	25%	6%	127

Table G.3 - Comparative Review Results Sel. Assy, Heuristic Type, Data Source

					Data Source	urce.		
Selective Assembly:	Heuristic	Data	Enpirical Data	Example Data	Heterital	Inconclusive or	Sampled	Crand Total
	Algorithm	2%	%0	2%	%0	%0	%0	3%
	Heuristic Procedure	1%	1%	4%	%0	%0	%	%9
Selective	Search Heuristic	1%	%0	%0	%0	%0	%0	1%
Identified	Inconclusive or Not Applicable	%1	%0	% E	%1	% 0	%0	59%
	Total	4%	1%	%6	%1	%0	%0	14%
	Algorithm	3%	1%	%9	2%	1%	%0	12%
	Heuristic Procedure	3%	2%	%6	2%	4%	2%	23%
	Search Heuristic	4%	3%	4%	2%	1%	%1	14%
Selective Assembly	Simulated Amealing	1%	%0	%0	%0	%0	%0	1%
Not Identified	Inconclusive or Not Applicable	%65	2%	%9	7%	17%	%0	35%
	Linear Programming	1%	%0	%0	% 0	%0	%0	1%
	Total	20%	%8	25%	%L	%27	7%	86%
Grand Total		24%	%6	34%	%8	%82	7%	127

Table G.4 - Comparative Review Results Test Method

Testing (Primary Method)	Truncation Assy / Truncation	No Truncation Assy /Truncation	Grand Total
Commentary	0%	2%	2%
Comparative Analysis	5%	22%	27%
Correlations	0%	1%	1%
Demonstration of "Good" Solution	1%	11%	12%
Efficiency improvement	1%	11%	12%
Empirical	3%	1%	4%
Error Ratio	1%	1%	2%
Experiment	0%	3%	3%
Inconclusive or Not Applicable	2%	6%	8%
Mathematical Model or Computational Result	9%	16%	25%
Simulation	1%	5%	6%
Grand Total	22%	78%	127

Table G.5 - Comparative Review Truncation and Data Source w/Heuristic

Truncation & & Data Source	Heuristic Identified	Heuristic Type Not Identified	Grand Total
Data Generated	5%	20%	24%
Empirical Data	1%	8%	9%
Example Data	7%	27%	34%
Historical	0%_	8%	8%
Inconclusive or Not Applicable	9%	13%	23%
Sampled Data	0%	2%	2%
Grand Total	22%	78%	127

Table G.6 - Comparative Review Optimization Techniques

Optimization	
Technique	Total
Analytical Target Cascading	1%
Analytical Target Setting	1%
Attribute Level Driven	1%
Function	1%
Heuristic Based	11%
Highly Optimized Tolerance	
(HOT)	1%
Inconclusive	2%
Keifer-Wolfowitz Optimization Procedure	1%
Linear	1%
Markovian queuing network	1 12
model	1%
Mathematical Formulation	4%
Mixed Integer Programming	1%
Not Applicable	43%
Optimization Model	1%
Optimization Model	23%
Partitioned Decision Making	
Model	1%
Pattern Enumeration	2%
Semi-Markovian model	
generating such an optimal	
(deterministic) routing scheme	1%
Simplex Method (or variant)	1%
Simulated Annealing	
Optimization	1%
Stochastic Model	1%
Target Setting	1%
Utility Maximization through	:
Criteria Weighting	1%
Value iteration and policy	
improvement methods	1%
Weighting	1%
(blank)	1%
Grand Total	127

Table G.7 - Categorization Table from Comparative Review

			Coffee	Catagorization & Other Speeding	The Co.			
Reference	Hauristic Type	Optimization Technique	Fects	Perchanting Meked	Data Searce	00	Tasifug (Primary Maked)	Results
Carlem, J.M., & Doyle, J. (2002)	Algorism	Highty Optimized Tolerance (HOT)	Her Method	Historical or Collected Data	Historical	Not Applicable	Service	Review. Approach Déves Options Companion Algorithm (similar to)
Matalmoni, B.B. (1994)	Deconductive or Not Applicable	Optomomore Model	Assembly Line Buffering	Heuristics or Other Methods	Hasterical	9 Ters Date was not	Efficiency	Compand with other methods using Computational Experiments
Park M. W., & Kien Y.D. (1999)	Algoriden	Uhliky Matipianion Omogh Criteria Weghting	Assembly syntems operating on males-to- entine heats	Hearings or Other Methods	Den Generated	Used an Additive Utility Prancion	Companive Analysis	Network Based Algorithm Compand with other methods using Companishment Experiments
Poutballe, B. (1992)	Agoritan	Optimisation Model	Admicification of strainman anquing local stranges.	Signilation Data or Study	Den	'Appearinged Solution',	Companie	Review: Approach Deven for Solution Algorithm and Application Solution Algorithm
Pourbabai, B. (1989)	Inconclusive or Not Applicable	нроги хронали Экспонов инськуютуу	Design of m essenthly system, linked by a transporter for just-to-time (III) and stoodge statemen	Sinvalution Date. or Study	Data Generated	'Approximated Solution'	Sicrolation	Review: Approach Divum for Solution Algorithm and Application
Can, X, at Biq Y: (1987)	Alexifes	Kathe Wolfowitz Optionita Procedure	Observations sated as part of the aimstakes render. Asplice another variable dependencies. Stochastic another another another stochastic	Mathematical Formulation, Orbits Optionstion Procedure or Rent	Des	Crude Mone Carlo Baranete	Compactive	Review: Agranach Deven for Solution Algorithm and Application Perturbation analysis of discrete event dynamic gystem Compenions to Kiefler Wolfswerz Optimization Proceeding
Seitham, A. & Teacham, A. & (1994)	Bernink Prostite	<u>ु</u>	Evaluates specialing apprendues to part- systing policies	Mathematical Formulation Other Optimization Procedure or Respli	Incontraire or Not Auxiliable	New optimal FMS performance secults	Companie	Review: Approuch Daven for Solution Algorifum and Application Closed Loop Hemistic Policies Probabilistic Shottest Quane (\$5(3) \$chechling Hemistic.

			Catago	rization & Other S	pecifics			
Reference	Henrisic Type	Optimization Technique	Pecas .	Benchmarking Mached	Data Searce	Other	Testing (Primary Method)	Romarks
Nadder, E. (1975)	Hauristic Procedure	Mathemetical Formulation	Heuristic ducision roles in probabilistic inventory systems requiring only the knowledge of the mean and standard deviation of demand, probability of no demand, carrying and replantating costs, dusing availability, and lead-time.	An Example Case Study, or Design Specification	Parample Data	Not Applicable	Mathematical Model or Computational Result	Henriatic Decision Policy for probabilistic inventory systems Numerical ments are given to illustrate the application of the rules.
So, K.C., & Scott, C.H. (1994)	Algorithm	Optimization Model	Studied a production control model for a product comprised of matching composition	Heuristics or Other Methods	Respirical Data	Not Applicable	Companitive Analysis	Greatly Handstic Sequencing Rule
Klinowicz, J.G. (1990)	Hawistic Procedure	Linear	Hauriatic Mathods to solve freight transport problem and cost Strikty location problem.	Henristics or Other Methods	Historical	Temsport Problem	Demonstration of 'Good' Solution	Empirical Testing. Compared with other methods using Computational Experiments
Bai, H., & Kweng, C.K. (2003)	Algorithm	Optimization Model	An "insuser" genetic algorithm approach and model were used for determination of target values for engineering requirements in Quality Function Deployment.	Heucistica or Other Methods	Example Deta	Not Applicable	Mathematical Model or Computational Result	Review: Approach Daiven Genetic Algorithm Interactive approach to obtain inexest optim target values
Cooper, A.R., Georgiopoulos, P., Kim. H.M., & Papalambros, P. Y. (2006)	Hauristic Procedure	Partitional Decision Making Model	A partitioned decision-making process is smodeled to desconstrate how decisions at the top-level of the hierarchy analysical target asting are supercled results from the lower level analysic target cascading	An Rumple Case Study, or Design Specification	Example Data	Measures of Resciveness of Analysical Target Setting	Companive Analysis	Example of deployment related to decision making and product development Heuristic Procedural Francework
Kwok, K.S., Drianen, B.J., &			Focus is on a maximum utilization problem of a set of mobile robots with limited sensor-range capabilities and	Mathematical Formulation, Other Optimization		Темиросі		Network Optimization Model Assignment Algorithm
Phillips, C.A. (2002)	Alsocitum	Optimization Model	limited travel distances (initially at sundom positions).	Procedure or Result	Example Data	Problem Max Oct.	Computative Applyzia	Compared with other optimization procedu

			Coto	rization & Other S	encifics			
Reference	Henrisis Type	Optinization Technique	Facus	Beachmarking Mathod	Data Searce	Offer	Testing (Primary Mothod)	Romarks
				An Example		Set targets to extraone lower and upper bounds (normality 0 and or) for testing the boundaries of decision variables in		
Hunng, G.Q., Qu, T., Cheung D. W.L., & Liang L. (2006)	Inconclusive or Not Applicable	Analytical Target Cascading	Utilized a study-agent system to active for optimal design using analytical target cascading	Case Study, or Design Specification	Example Data	minimization and maximization	Demonstration of "Good" Solution	Hierarchical system modeling Arnibute Level Driven
Calab Li, M.H. (2004)	Inconclusive or Not Applicable	Optimization Model	On optimal manufacturing actings to minimize quality loss for the identified production system	An Example Case Study, or Design Specification	Example Data	Not Applicable	Bevor Ratio	Truncated argumentrical quadratic loss function. Minimize aspected quality loss
Ohmuha, Y. (2004)	Elementic Procedure	Value iteration and policy improvement methods	Evaluation of risk minimizing problems in undiscounted Markov decisions procuses with a target set. Also utilizes infinite horizon cases to show that an optimal value function is a unique solution to an optimality equation.	An Example Case Study, or Design Specification	Example Data	Min Opt	Mathematical Model or Computational Result	Rink Minimization Policy Improvement Methods Policy Space Procedure Optimal Value Punction is unique to optimality
Kira, H.M., Michelma, N.F., & Papalambers, P.Y(2029)	Inconclusive or Not Applicable	Optimizațian Model	Used target cascading to model a smitt- level optimization problem using design targets (cascaded to lower levels) by partitioning freit problem into small sub- problems	An Example, Case Study, or Design Specification	Example Dua	Analytical Example and Application	Comparative Analyzis	Model Using Analytical Target Catcading
Kazysztofirwicz, R. (1990)	Inconchasive or Not Applicable	Target Setting	Provides an critique and application extension of a decision model	Inconclusive, Not Performed, or Not Applicable	Inconclusive or Not Applicable	Exp. Utility Function	Mathematical Model or Computational Result	Decision Model Critique
Moodand, P.R., & Wu C.F.I. (1998)	Eleoristic Procedure	Optimizațios Model	Developed a modeling and data-malysis strategy for a general loss function, in which the quality characteristic follows a location-scale model.	Heuristics or Other Metsods	Empirical Daya	Min Opt	Exerinent	Extends a nominal-the-best parameter design to include loss finations of a much more general nature Taguchi Procedure Compand with other methods using Computational Experiments

			Catag	erization & Other !	pecifics			
Reference	Henrisic Type	Optimization Technique	Fecus	Reachmerking Mathed	Data Segre	Other	Terting (Primary Mathed)	Remarks
Musa, R., Stargea, R. H., & Chea, F. F. (2006)	Algorithm.	Optimization Model	Develops a methodology for impection planning for a new product based on CAD data and ainstanton.	Hearistics or Other Methods	Data Generated	Inspertion Plans	Simplation	Methodology for inspection planning for a ne- product based on CAD data Genetic Algorithm
Musa, R., & Chen, F.F. (undated)	Algorifes	Optimization Model	Revision of a previous model for importion planning in agile production environment using Dynamic Throughput Maximization (DTM).	Simulation Duta or Study	Data Generated	Solve Nomerical Examples	Companive Analysis	Meta-heuristic Algorithm Simulated Ameeting Algorithm Compares results with and without implementation of the purposed integration
Minna, R., Chen, F.F., & Choniera, A. S. (undated)	Henristic Procedure	Optimization Model	Development of a mathematical part matching model for variation reduction	Simulation Data or Study	Data Generated	impection Plana	Mathematical Model or Computational Result	Mathematical Model to match path to achiev minimal variation using 3-role heuristic procedure
Mussa, R., & Chen, F.F. (2008)	Algoritus	Optimization Model	Exploits data of measured features of a batch of subsessmbly data to reduce variation in the final assembly to maximize the rolled yield throughput.	Simulation Data or Study	Data Generated	Maximum Optimization used commercial optimization solvers (e.g. opt.models)	Demonstration of "Good" Solution	Five Algorithms (simple gready, simulated amesting, set colony optimization) Gready Algorithm Simulated Amesting
Husing, S.H., Liu, Q., & Muss, R. (2004)	Heuristic Procudence	Patteen Encomparing	Proposed a method for process plan evaluation to provide rapid evaluation for process plan decision making	Simulation Data or Study	Empirical Data	Assignment of Production Tolerances as part of heuristic procedural approach	Companitive Analysia	Monte Carlo Simulation by prediction of mathining tolerances

			Catego	rization & Other S	pedio			· · · · · · · · · · · · · · · · · ·
Reference	Henristic Type	Optionistics Technique	Fecas	Benchmarking Method	Data Saurce	Ofter	Testing (Primary Mathed)	Results
Zhang, W.Z., Wang, G.X., Chaok, B.T., & Nas, A.Y.C. (2003)	Heuristic Procedure	Not Applicable	Proposed a knowledge-based selection procedurerules (e.g., henriatic) to provide a usique name based search mechanism geand toward component muse (i.e. respektation)	Inconclusive Not Performed, or Not Applicable	Inonachusive or Not Applicable	Not Applicable	Inconclusive or Not Applicable	Rules based selection procedure Knowledge Based Selection Procedure
Meller, R.D., dr Bosse, Y.A (1996)	Algorithm	Simulated Amending Optimization	Presented a henciatic 4.e sinzulated:	Heucistics or Other Methods	Historical	Ransuples of real life facility layout problems Min Opt	Demonstration of "Good" Solution	limprovement type layout algorithm Simulated Armesling Algorithm
Kwon, H-M, Kim, K-I, & Chandes, M. J. (1999)	Inconclusive or Not Applicable	Optimization Model	On product clearance the focus of this meanth dealt with component characteristics of a nomial distribution with equal variance	Mathematical Formulation, Other Optimization Procedure or Result	Exemple Data	Cost Model	Mathematical Model or Computational Rands	Component characteristics. Assumed to be normally distributed Formulae for rejection and making
De Fazio, T.L., Rhee, S.I., & Whitney, D.R. (1999)	Algoritus	Not Applicable	Detailed subassembly partitioning based on criterion based searches and identified genetic algorithm search techniques for us in assembly sequencing	An Rumple Case Study, or Design Specification	Example Data	Sourch Henriatic	Efficiency improvement	Design For Assembly Method Assembly Sequence Analysis Criterion Based Searches Genetic Algorithm
Kaman, SM., Inyahalan, V., & Januarahan, K. (2003)	Algorithm	Henristic Resed	Utilized genetic algorithms to find the best combination of the selective assembly groups necessary to minimize assembly variation and formed on linear assembly	Mathematical Formulation, Other Optimization Procedure or Result	Example Data	Genetic Algoritums Min Opt	Demonstration of "Good" Solution	Method for selective grouping Genetic Algorithm

			California	rizadine & Other S	ectic.			
Bafarago:	Henristic Type	Optimization Technique	Focus	Benchmarking Michael	Data Saurce	Other	Testing (Primary Maked)	Reserts.
								Harristic Comparison
Promorabalara, S.G., Azavindan, P., & Ran, M.S.		Hauristic	Investigation of genetic algorithms and also performed a comparison of enting va- yeopoosed GA's by consideration of variation at multiple assembly levels (e.g.	Henristics or	Example	Genetic		Sequencing Problem for Mixed Model Assembly Lines
(2003)	Algorithm.	Breed	zaw materiala product subassembly, etc.)	Other Methods	Data	Algorithma	Experiment	Genetic Algorithm
Kaupin, SM, & Jayabalan, V. (2001)	Hearistic Procedure	Not Applicable	Proposed a method for lot partitioning using selective assembly groups	Henristics or Other Methods	Example Data	Lot Partisoning to aid in selective assembly	Comparative Analysis	Complex sasy's with 3 mating parts Compared with other methods using Computational Experiments
Pugh, G.A. (1926)	Inconclusive or Not Applicable	Not Applicable	Introduces the idea of partitioning a component population into groups paior to made a seembly	Inconclusive, Not Performed, or Not Applicable	Example Data	George Partitioning	Inconclusive or Not Applicable	Early initial framework of method
Des., S.K., & Satin, S.C. (1988)	Heuristic Procedure	Not Applicable	Used a dynamic programming approach along with a heuristic procedure to address part arrival dates in a smiti-job stockastic assembly system.	Henristics or Other Methods	Data Generated	Algoritan	Compensive Analysia	Hencistic Procedure Stochastic va. Deterministic
Cistolin, A. (1997)	Heuristic Procedure	Not Applicable	Used filter and assembly sequencing methods to group and sequence assembly combination	Heuristics or Other Methods	Example Data	Anny Sequencing and used filtering methods	Experiment	Method Costopicion
Pugh, G.A (1992)	Inconclusive or Not Applicable	Not Applicable	Discusses the systematical truncation and normal distributions in addressing component distributions	Simulation Data or Study	Data Generated	Assembly Procedure	Simulation	Truncation based on variances for selective
Manaoor, E.M. (1961)	Inconclusive or Not Applicable	Not Applicable	Selective Assembly focus with application to a case history of a piston-cylinder fit and problem solving for a mis-matching inste	An Example, Case Study, or Design Specification	Example Data	Example of a piston	Mathematical Model or Computational Result	An application of selective assembly

		·	Cates	erization & Other	Specifics			
Reference	Hauristic Type	Optinization Technique	Forms	Benchmarking Maked	Dain Source	Other	Testing (Primary Minhod)	Romerks
Dustricted, D. J., & Setty, C.A. (1961)	Heuristic Procedure	Not Applicable	Proposed a method such that components should be balanced by quantifies subset than by size.	An Example Case Study, or Design Specification	Example Data	Numerical Example	Mathematical Model or Computational Result	Method proposed belancing quantities by quantities rather then by size
Whitney, D. R. (2006)	Inconclusive to: Not Applicable	Not Applicable	Identifies key characteristics associated with mechanical assemblies, data flow chains and tolerance analysis. This smeach focuses on utilizing key characteristics for conveying design intent.	Inconclusive Not Performed, or Not Applicable	Inconclusive or Not Applicable	Whitney covers meembly techniques and research supports the gap analysis and application of this dissertation focus.	Inconclusive or Not Applicable	Role of Key Characteristics in Mach Assy's
Lee, S., & Shin, Y.G. (1990)	Heuristic Procedure	Mathematical Formulation	Presented a method for the automatic desensions of sesembly partial orders from a linium graph representation	An Example Case Study, or Design Specification	Example Data	Method provides a new approach to any via temp relationships Max opt	Experiment	Method for extensitic determination of any partial order from a linium graph up of an any through ext. of preferred any
Lee, B., & Saiton, K. (2007)	Alzaritum	Optimization Model	Presents a systematic method that decomposes product geometry at an early stage of design, selects joint types, and generates submentably partitioning to achieve the adjustment of the critical denomicons during assembly processes	An Example Case Study, or Design Specification	Example Data	Key Characteristics used in Opt. Model	Companitive Analysis	Genetic Algorithm generates candidate joint assemblies based on joint library specific for an application domain. Genetic Algorithm.
Agard, B., & Konisk, A. (2004)	Heuristic Procedure	Optimization Model	Data mining was emplemented at part of the subsessibly selection process and utilized and integer programming model and applied a heuristic algorithm for the selection of the optimal subsessmily structure.	An Example, Case Study, or Daviga Specification	Example Data	Example and automotive case study	Mathematical Model or Computational Result	Data mining elgorithm
Abe, S., Murayama, T., Oba, F., & Narutaki, N.	:		Focus on benefitics to aid in the	An Example, Case Study, or Design	Example	GA and hearistics to select the excedient	Demonstration of "Good"	Mathod for adaction of verification time
(1999)	Alsocifica	Inconclusive	remeration of assembly successing	Specification	Data	candidates	Solution	Genetic Algorithm

			Cang	erization & Other	Specifics			
Récue	Henristic Type	Optimization Technique	Focus	Benchmurking Michod	Data Source	Other	Testing (Primary Mothod)	X-Ads
Lee, S. (1994)	Inconclusive or Not Applicable	Weighting	Presents a method for the automatic generation of seembly sequences from a listing gush representation of an assembly strongh the security decreasonattics of assembly into subsequencies	An Example Case Study, or Design Specification	Historical	Correspondence	Compactive Analysis	Data Source: CAD database
Bohachevaky, 1.O., Johnson, M.E., & Stein, M.L. (1986)	Simulated Assessing	Francica	Described generalized simulated amening for the "optimization of fractions laving many local extense" and methods for improved optimizes of other problems.	Mathematical Formulation, Other Optimisation Procedure or Result	Data Generated	Semeitivity Analysia	Recency	Generalismi Simulated America
Sandarson, A.C. (1997)	Algorithm.	Optimization Model	Used a tolerance model to estimate part configurations based on maximum likelihood using filter algorithm.	An Example Case Study, or Design Specification	Example Data	Tolerance Model: Max Opt	Comparative Analysis	App. Of each to set subsessenblise med to evaluate sary spec steps and discriminate at any seq. plans Filter Algorithm
Phoembepiab, T., & Cegiarsk, D. (2007)	Heuristic Procedure	Not Applicable	Proposed a design synthesis framework for dimensional management of a stulki- stage assembly system	Simulation Data or Study	Data Generated	Moste Cado Simulation	Simulation	Dimensional Mgast Method for process design configuration
Curieres, G.I., Hereman, W.H., & Lee, H.L. (1995)	Heuristic Procedure	Optimization Model	Identified a computationally infineible dynamic programming formulation along with a myopic control procedure for general application to sorting and matching problems	Heuristics or Other Methods	Rmpirical Data	Mathematical Model	Efficiency improvement	Hearistic for noting comp into class sizes Compared with other methods using Computational Experiments
Bruedia, IB. (2001)	Inconclusive or Not Applicable	Optimization Model	Presented a simplified approach to submeasably design using Moste Carlo Analysis	Signalation Data or Study	Deta Generated	Monte Carlo Simulation	Significa	Monte Carlo Anglysis

			Catego	rization & Other S	pecifics			
Reference	Hanristic Type	Optinization Technique	Fecus	Buckmerking Method	Date Searce	Officer	Testing (Primary Method)	Panack;
Lozmo, S., Adumo-Diaz, B., Egnia, I., & Omiesa, L. (1999)	Search Henristic	Not Applicable	Used a Tabu search hemistic in a cellular manufacturing design and proposed systematically explored familie machine cell configurations in part family determinations	Heneistics or Other Methods	Requirical Data	Benchmarked against 2 simulated amealing approaches	Demonstration of "Good" Solution	Tabo Search for manufacturing cell design
Salbi, S. (1997)	Heuristic Procedure	Houristic Based	Developed a constructive heuristic for a location problem. The author tested the proposed heuristic against other location problem methods	Henristics or Other Methods	Data Generated	Perturbation hemistic	Efficiency intercovernment	Tested against septiable methods on a class location problems Parturbation hausinic and heuristic procedure
Puniz, A.V. (2002)	Inconclusive or Not Applicable	Stochastic Model	Presented selection techniques for a dynamic model framework for decision makes	Simulation Data or Study	Deta Generated	Max Opt	Empirical	Primarily Financial but provided relative information on a stochastic convergence mode for consideration.
Pumm, A.P., & Aneja, Y.P. (1995)	South Hamistic	Not Applicable	Studied a resource-constrained assignment problem and developed a Tabu search heuristic	Historical or Collected Data	Example Deta	Resource Commined Assignment Problem	Efficiency improvement	Tabu Search uses strategic oscillation, randomized short-term memory and stablishe start as a season of search diversification
Rochet, Y., &	Sourch	Optimization	Evaluated a vehicle routing problem using two purposed heuristics to find a "good"	Hauristics or	Example	Vehicle Roving	Demonstration of "Good"	2 henriches methods. Fast straightforward insertion procedure and a method based on Tabu search techniques. Tabu Search henriches Compared with other methods using
Sesset, F. (1994) Gendress, M., Luporte, G., &	Heuristic Search	Model Heuristic	Developed a Tabu search heuristic for a stochastic vehicle routing problem with	Other Methods Henristics or	Data	Problem Comparisons against known optimal	Solution	Computational Experiments Tabu Search Compared with other methods using
Seguin, R. (1996) Gendreen, M., Hertz, A., & Laporte, G. (1994)	Heuristic Search Heuristic	Based Heuristic Based	andon demands and probabilities Described a Taku search heuristic for vehicle routing problem with various restrictions	Other Methods Henristics or Other Methods	Historical Example Data	Numerical tests on a set of benchmark problems	Error Ratio Companitive Analysis	Computational Experiments Tabu Search - Tabu route. A search heuristic for the vehicle routing problem with capacity and route legath reprictions

			Cotog	rimtion & Other S	pedio			
Reference	Henrisic Type	Optinization Technique	Focus	Benchmarking Method	Deta Saurce	Other	Testing (Primary Mished)	Ramarks
Markland, R. R. (1990)	Heuristic Procedure	Not Applicable	Commentary on Henristic procedure presented by glover in [68]	Heuristics or Other Methods	Prompte Data	Negati networks, aissuinted amouling, GA, and Tabu Search	Commentary	Discussion of {62}
Grime-Yamoff, T., & Weirich, P. (2010)	Inconctusive or Not Applicable	Not Applicable	Discourse the philosophical and quintum clogical implications of aimminion, aimminion representation, and policy decinion. The paper argued that aimminion is "an important new tool for the social acianous"	Inconclusive, Not Performed, or Not Applicable	Inconclusive or Not Applicable	Philosophical approach to atzategic methodology. Historical Analysis	Inconclusive or Not Applicable	Application of strategy security to easy strategy
Wilson, I.D., & Roach, P.A. (2000)	Henristic Procedure	Optimization Model	Presents a methodology for automatic generation of computerized solutions to the container stowage problem.	An Example Case Study, or Design Specification	Example Data	Heuristic cules were developed	Demonstration of "Good" Solution	Optimization using Tabu Search
Consiglio, A., & Zenica, S. (1999)	Search Henristic	Optimization Model	Formulates a hierarchical optimization model	An Example Case Study, or Design Specification	Empirical Data	Respirical results	Rificiency improvement	Design spacification meaning the portfolio results Tabu Search
Moorelin, J.V., & Nagano, M.S. (1998)	Search Heuristic	Mathematical Formulation	Formed on flow simp sequencing (which has application to assembly sequencing). Methods to improve huminica by obtaining an initial solution using the traveling selection perblem and then Tabu search methods to improve the initial solution.	An Example Case Study, or Design Specification	Respirical Data	Evaluates the relative performance of the procedures	Demonstration of "Good" Solution	Tabu Search
Bastes, R.A., Buck, R.J., Riccomagno, E., & Wyss, H.P. (1996)	Heuristic Procedure	Not Applicable	Identified experimental design and modeling at part of optimization and sensitivity analysis of large systems	An Example, Case Study, or Design Specification	Empirical Data	optimization and sensitivity analysis	Demonstration of "Good" Solution	System decomposition using space matrix method experimental design, and modeling

			Code	erization & Other:	Specifics			
Reference	Hauristic Type	Optimization Technique	Facus.	Benchmurking Mathed	Data Seurce	Other	Testing (Primary Method)	Remorks
Вауктоўн, А (2001)	Search Heuristic	Not Applicable	Used methematical pregramming tools to model multiple objective optimization publishes	Henristics or Other Methods	Example Data	Goal Programming	Compositive Analysis	Trend in kineature is using modern heuristic optimization tach. GA, TS, and SA. Paper user Multi. Obj Tabu Search.
Dell'Amico, M.	Search		Analyzed performance of lower and upper bounds for a flow-shop problem with two marchines. This study used a Tabu search algorithm and proved the effectiveness of the pusposed bounds farough computational	Heuristics or	Deta	FlowShop Problem w2	Reficiency	Transation application using upper lower bounds Tabu Search Compared with other methods using
Patterson, R.A., & Rolland, E. (2002)	Heuristic Heuristic Procedure	Not Applicable	results Explored network design and presented a heuristic with a methodology that utilized an adaptive recogning technique. The authors also generalized their formulation and measured its effectiveness	Other Methods Henristics or Other Methods	Rumple Data	Proposes a formulation and heuristic based on hierarchical decomposition	Mathematical Model or Computational Result	Computational Experiments meta-heuristic over specialized heuristics for sub-problems. Developed 80 test problems to model data
Ching W-C., Konvelia P., & Urbin, T.L. (2002)	Search Heuristic	Heuristic Based	Developed optimal and heuristic achinions methodologies for evaluation of workflow interference. The paper focused on application of these methodologies from a facility layout perspective by examining baseds and bound heuristics along with Tabu search he	Heuristics or Other Methods	Data Generated	Workflow interference from a facility layout pempactive	Efficiency improvement	Optizual and heuristic solution methodologies are developed and evaluated Tabu Search Bunnch and Bound
Ramina-Beltran, N.D. (1995)	Heuristic Procedure	Optimismi to Model	Demonstrated a real-world application of an integer programming problem. The focus of this study was on finfing an optimal solution for a labor cost problem.	An Example Case Study, or Design Specification	Example Data	Real-world application of pure integer programming	Mathematical Model or Computational Result	Branch and bound algorithms are used and a state—space model was used to predict the stochastic behavior of mostily depends
Aggarwai, C.C., Orlin, I.B., & Tni, R.P. (1997)	Algorithm	Henristic Based	Explored applications of genetic algorithms to demonstrate the utility of knowledge based mechanisms	Heuristics or Other Methods	Inconclusive or Not Applicable	Technique used an optimize	Comparative Analysis	Purpose if the paper was to desaminate the power of knowledge based mechanisms in Genetic Alcorithms

			Catego	erization & Other !	ecitio.			
Reference	Hearistic Type	Op ünimün Takkiyue	Focus	Benchmarking Method	Dain Senze	0 f er	Testing (Primary Miched)	Rannaks
Bracker, I.S., & Penson, I.N (1986)	Heuristic Procedure	Net Applicable	Developed a planning process with comparison to a specified uses of interest. The authors used multivariate analysis of variance.	An Example, Case Study, or Design Specification	Sampled Data	Hagristic Procedure	Comparative Analysis	Application is methodological as the study analysms shortomings of prior smearch and strategic planning.
Jun, J.B., Jacobson, S.H., & Swisher, J.R. (1999)	Harristic Procedure	Optimization Model	Used discrete event simulation to improve patient flow and for assource allocation.	An Example Case Study, or Design Specification	Sampled Data	Discussion of discust syust simulation	Kiliciancy improvement	Allocation of monoton. Selected for application of flow sequencing. Sample data in the form of a survey.
Liu, L., & Chang. K.L. (1997)	Inconthuive or Not Applicable	Optimization Model	Studied continuous review investory models and included review of exponentially distributed variables along with other key operating characteristics for the inventory model.	Mathematical Formulation, Other Optimization Procedure or Result	Example Data	Markov process for inventory modela	Comparative Analysis	Application of optimization of systems parameters
Manuala, J.B., & Schenz, R.H. (1995)	Starch Henristic	Hauristic Based	Developed an optimal allocation model of a single facility production environment.	Hauristics or Other Methods	Data Generated	Generalizes an approach to resource application	Companiive Analysis	Research Application: Primarily formed on approach, knowledge area with respect to over- arching dissentation research and approach focus
Oblemilier, M. (1997)	Search Baseistic	Henristic Banad	Used simulated amending for solving a minimum location problem and efficiency of the method was presented along with smults relative to the expected deviation	Henristics or Other Methods	Data Generated	Tabu Search	Demonstration of "Good" Solution	Simulated Armenting, Is a good alt, for minima location. The study compares those prior findings with Tabu search
Biagasod, S. (1997)	Inconclusive or Not Applicable	Not Applicable	Explored the experimental determination of tolerance limits of mating components of an assembled product	Mathematical Formulation, Other Optimization Procedure or Result	Example Data	Design complex provided	Mathematical Model or Computational Result	Outlines theory and methods for exp. Of tolerance limits for mating components Ind. Indirect Application to selective any
Ontermeier, M. (2003)	Inconclusive or	Not Applicable	Key points made in his meenth (not performed) were that "experimental determination of the distributions used world require actuality, cost-probability," sequencing. This lends credence to the use of Monte Carlo simulation presented in this dissectation.	Mathematical Formulation, Other Optimization Procedure or Ramik	Rossople Data	Non-specific. Paper presents incremental transation of DNA	Mathematical Model or Computational Result	Research Application: Primarily focused on approach, knowledge area with suspect to over- arching dissertation research and approach focus

.

			Catego	erization & Other :	Specifics			
Riferace	Henrisik Type	Optimization Technique	Fecus	Benchmarking Maked	Data Source	Other	Testing (Primary Maked)	Ramarks
Bradley, D. M., & Ospia, R.C. (2002)	Inconclusive or Not Applicable	Not Applicable	Analyses data associated with the same of "n" independent non-identically distributed uniform produce variables	inonaclusive Not Performed, or Not Applicable	Inconclusive or Not Applicable	Not truncated but sum of n non- ident uniform sundom var	Mathematical Model or Computational Result	Application considerations
Discysmen, P. J. (2005)	Inconclusive or Not Applicable	Analytical Target Setting	Developed the moments of truncated distributions in density endogenous variable models. An interesting aspect of this study to this research was the approach to normalization of a truncated distribution used wifain the study	An Example Case Study, or Design Specification	Example Data	Presents moments of truncated distributions in variable models	Companiive Analysis	
Yang, C., Gui, W., Kong, L., & Wanz, Y. (2009)	Henristic Procedure	Optimization Model	Present a quality prediction model for optimal-enting control of a manufacturing process in a metallurgical industry. Their approach used a "kind of hismrchical strategy for determination of an optimal set point for new material portioning	Simulation Data	Example Data	Presents a hierarchical inference strategy	Efficiency	Strategy proposed based on bisses to sid in determining an optimal set-point for real-time proportioning
Griegne, N. (2011)	Inconclusive or Not Applicable	Not Applicable	Pixite difference methods	An Example Case Study, or Design Specification	Example Data	Application of Finite element method	Inconclusive or Not Applicable	General colution for FRM
Zhu, Q., & Oceneses, I. (1997) Boucherd, B., Rise, R., &	Sauch Heuristic	Heuristic Based	Binning search philosophy based on detection function. Optimal mechanic control problem under stochastic tartet	Historical or Collected Data	Historical Example	Not Applicable Optimal control	Companitive Analysis	Application consideration as it relates to unknown truncation assys Authors assume that their method is the first use because of unknown target distribution.
Isabert, C. (2010)	Procedure	Optimization Model	constrains	or Study	Data	problem	Correlations	

			Cutus	mintion & Otter	pecifics			
Reference	Henrisis Type	Optimization Tachnique	Fecus	Baselmarking Mathod	Data Source	Office	Testing (Primary Method)	Romerks
Simpson, D.P. (2008)	Heuristic Procedure	Heuristic Based	Finite diffirme methods	Simulation Data or Study	Date Generated	Application	Mathematical Model or Computational Result	Formulates simple sufficient conditions for optimality
Asvadanov, S., Dronkin, V., Guddari, M., dr Knizhostowa, L. (2003)	Heuristic Procedure	Heuristic Resed	Finite difference suchods	Inconclusive, Not Performed, or Not Applicable	Inconclusive or Not Applicable	Not Applicable	Comparative Analysis	Henristic Fosenewode
Xinoping B. & Jingjing M (2009)	Hauristic Procedure	Not Applicable	Presents a system analysis model and application algorithm for calculating availability of complex storage him	Inconclusive, Not Performed, or Not Applicable	Inconclusive or Not Applicable	bins	Companiive Analysis	Application of availability and algorithm for housistic
Minne, D., Neix V., & Sudjiante, A. (2004)	Heuristic Payenton	Mathematical Formulation	Described a statistical formulation for determination of optimal biuming strategies for various loss functions and distributions and compare the results to bississica.	An Example Case Study, or Dusign Specification	Example Data	biomine	Mathematical Model or Computational Result	Statistical formulation and optimal birming under loss function and distributional assumptions
Xiaoping B. & Jinging M (2009)	Inconclusive or Not Applicable	Optimization Model	Reviews optimization methodologies as it relates to binning	Mathematical Formulation, Other Optimization Procedure or Result	Inconclusive or Not Applicable	Not Applicable	Efficiency improvement	
Glover, F., & Laguna, M (underted)	Search Heuristic	Heucistic Based	Exploration of Tabu Search. Application for improved understanding of Tabu Search. mathods	Inconclusive, Not Performed, or Not Applicable	Incomclusive or Not Applicable	Not Applicable	Demonstration of "Good" Solution	Tabu Search
Caleb Li, MH., & Chou, C Y.(2001)	Heuristic Procedure	Optimization Model	Application of process optimization as it relates to quality characteristics. Application to target selection of dissertation and consideration of methods and quality indicators.	An Example, Case Study, or Dusign Spacification	Example Data	Tagrachi losa function	Demonstration of "Good" Solution	
Johnson, A., & Thomopoulos, N.T. (undeted)	Inconclusive or Not Applicable	Not Applicable	Left Truscated Normal Distributions	Inconclusive Not Performed, or Not Applicable	Example Deta	Tables	Mathematical Model or Computational Reput	Transated Dist

			Catag	rintim & Oka !	pecifics		•	
Reference	Houristic Type	Optimization Technique	Fecus	Benchmarking Mithed	Data Saurce	Other	Testing (Primary Mathed)	Zanerks
Khasawaak,			T .					
M.T., Bowing			ŀ			This method		
S.R.,			1	Inconclusive,		aldresses	!	
Karwkuskooi, 5., & Cho, B.R.	• •		Tables of Standard Normal	Not Performed, or Not	Inconclusive or Not	doubly	,	
	Inconclusive or	N1 1:1.	L			truncated	.	Truncated Dist
(2005)	Not Applicable	Not Applicable	Doubly Truncated Distributions	Applicable	Applicable	distribution	Respinced	Innered Dec
						This method		
Tahanam A.C. A			11-1-1-17	Inconchanive	F			
Johnson, A.C., & Thomapouips.	baconclusive or		Methods and Equations for Doubly Truncated Normal	Not Performed, or Not	Inconclusive or Not	doubly truncated		
N.T. (undeted)	Not Applicable	Not Applicable	Distributions	Applicable	Applicable	distribution	Empirical	Transacted Dist
Khanawash,	May ubbranise	INN Apporture	twin.ordene	Approcase	Approxime	This mathed	ecoficient	TL/MUCSINGS TNM1
M.T. Bowling S.				Inconclusive		addresses a		
R., Kaswkunicoel				Not Performed	Inconclusive	singly		
S. & Cho. B.R.	Incomplants or		Tables of Standard Normal Singly	or Not	or Not	truncated		
(2005)	Not Applicable	Not Applicable	Truncated Distributions	Applicable	Applicable	distribution	Empirical	Truncated Dist
(2000)	INA PROPERTY	1401 Librariant	Examined right truncation	sufferience.	Minning	(HIJITANIEM	Estibilitat	11 Personn Pent
			exponential distributions and an					
			estimates for foite sample sizes of					
			transation points. Randake also	1				
			introduced the use of an incurse					
Ranchke, M.	Inconclusive or		ment against error to evaluate the	Simulation Data	Dista	Not	Companies	
(2012)	Not Applicable	Not Applicable	entimentors behavior	or Study	Generated	Applicable	Anelysis	Monte Carlo Simulation
	1441.14		Introduced change of measure	- CALLETON OF THE CALLETON OF	-	rapperoance	1000,700	THINK CALLS CALLED
;			techniques for care-event-analysis					i
			of heavy tailed . Moste Carlo					
			simulations were used by the					
			authors to aid in the attimation of					
		İ	care event probabilities and to					
	i		present a "nood" Markovian				Demonstration	
Blanchet, J., &	Inconclusive or	i	approximation of conditional	Simulation Data	Data	Monte Carlo	of "Good"	•
Liu, J. (2012)	Not Applicable	Not Applicable	distribution	or Structy	Generated	Simulation	Solution	
			Used a weighted stochestic	•				
			aintrilation algorithm (SSA) and a			Weighted		
			Monte Carlo simulation method to			Stochastic		
Kuwahara, H., &	Inconclusive or		malyze care events of biochemical	Simulation Data	Data	Simulation	Comparative	
Mara, I. (2008)	Not Ambicable	Not Applicable	system.	or Study	Generated	method	Analysis	Repristics not specifically discussed

			Catego	erization & Other	Specific.			
Reference	Henristic Type	Optimization Taksinjae	Fecus	Beachmerking Moked	Data Searce	Other	Testing (Primary Mathed)	Remarks
Denne, H., de Hann, L., & Li, D. (2006)	Inconclusive or Not Applicable	Not Applicable	Anderson-Durling type test of the null hypothesis used to demonstrate distribution belongs to EVI domain of attraction	Signalation Data or Study	Data Generated	Anderson- Darling Type Test	Mathematical Model or Computational Result	Weighted approximations of the tail of the distributions and other empirical data
Stoymuov, S., & Rachev, S. (2008)	Inconclusive or Not Applicable	Not Applicable	Effects of tail distributions analyzed with convergence side	Simulation Data or Study	Inconclusive or Not Applicable	Monte Carlo Simulation	Computative Analysis	Approximation Model
Chaves- Demoulin, V., & Roshul, A (2004)	Inconclusive or Not Applicable	Not Applicable	General overview of EVT	Inconclusive Not Performed, or Not Applicable	Inconclusive or Not Applicable	Not Applicable	Inconcinuive or Not Applicable	
Peng, L., & Qi, Y. (2009)	Inconclusive or Not Applicable	Not Applicable	Studied maximum idealized estimates of estreme value indicase between -1 and -1/2. They also generalized irregular cases and cases of an unknown estreme value index.	An Example Case Study, or Dunign Specification	Inconclusive or Not Applicable	Maximum Likelihood	Mathematical Model or Congutational Result	
Bermuder, P.D.Z., & Kotz, S. (2010)	Inconclusive or Not Applicable	Not Applicable	This paper focused on methods such as massimus likelihood (AIL.), method of moments (ASCNI), and probability weighted moments (PWNI).	Heusistics or Other Methods	Data Generated	GPD, ML, MOM	Mathematical Model or Computational Result	Exactional varying methods for the use of the generalized Pareto distribution (CPD) and their application to estimation methods. This literature focused on applications to EVT and its approach was to review and identify options of GPD parameter estimation.
Bernsuder, P.D.Z., & Ketz, S. (2010)	Inconclusive or Not Applicable	Nor Applicable	This focused on the application and methods of [114] to real world data. The others provide close by providing criteria for a decision maker to aid in determination of an appropriate method for their application.	Heuristics or Other Methods	Duta Generated	Application of Real World Data	Mathematical Model or Computational Revolt	Examined varying seetheds for the use of the generalised Pareto distribution (CPD) and fasir application to estimation methods. This literature focused on applications to EVT and its approach was to review and identify options of GPD paretness estimation.

	· -·		Catego	erization & Other !	Specifics			
Reference	Henristic Type	Optimization Technique	Feces	Buschmerbing Mathed	Duta Senzor	Officer	Testing (Primary Method)	Ramarks
Homice, W.C.	Inconthuive or Not Applicable	Not Applicable	Mathematical Formulation	Mathematical Formatistion, Other Optimization Procedure or Result	Inconchaive or Not Applicable	Mathematical Proof	Mathematical Model or Computational Result	
Brizmuskan, V., & Rhesfild, A. (2009)	Inconclusive or Not Applicable	Not Applicable	Proposed a method fix firing GPD associated with trade-offs between robustness and efficiency. Using a "triamed moments" method as a basis the authors used simulations and their method to fit GPD to historical data. Utility was provided fullowing application.	Simulation Data or Study	Data Generated	Large sample sizes used to provide a mean and relative efficiency by various methods	Mathematical Model or Corsputational Result	Microse Carlo, 10,000 assuples
Carpinteri, A., Cornetti, P., & Puzzi, S. (2005)	Inconclusive or Not Applicable	Not Applicable	Used extreme value theory in the form of a statistical model to evaluate materials. Prior compensions using EVI and a Multi-Fractional Scaling Law (MFSL) are used in their evaluation.	Inconclusive Not Performed, or Not Applicable	Empirical Data	MPSL and EVT, Model and Correlations	Enapérical	A model and consilation between for their are of interest in deaver (e.g. fracture energy and crack rurinos parameters)
Brooks, C., Clare, A.D., Delle Molle, J.W., & Persand, G. (2005)	Inconclusive or Not Applicable	Not Applicable	Examined various EVT models for VaR. The authors used GPD, ML and a semi-comparaentic methodology in their reviews.	Simulation Data or Study	Data Generated	Comparative Analysis	Comparative Analysis	Monte Cario
Diebolt, J., Guillou, A., & Rachad, I. (2005)	Inconclusive or Not Applicable	Not Applicable	Used a generalized probability weighted moment method (GPWM) to study the asymptotic behavior of estimation tools presented	Mathematical Formulation, Other Optimization Procedure or Rasult	Empirical Data	Mathematical Proof	Mathematical Model or Computational Result	
Cantillo, E., Hadi, A., Balakvizhom, N., Sarabia, J. (2005)	Inconclusive or	Not Applicable	Not Applicable	Inconclusive, Not Performed, or Not Applicable	Incomming or Not Applicable	Not Applicable	Inconclusive or Not Applicable	Overaching review and application only

Congestization & Other Specifics								
Reference	Henzistic Type	Optimization Tathnique	Fecus	Benchmerking Method	Data Saurce	Other	Testing (Primary Method)	Ramarks
Michelewicz, Z., & Fogel, D. (1998)	Inconclusive or Not Applicable	Not Applicable	Not Applicable	Inconclusive Not Performed, or Not Applicable	Inconclusive or Not Applicable	Not Applicable	Inconclusive or Not Applicable	Overanching review and application only
Whitney, D. E. (2004)	Inconclusive or Not Applicable	Not Applicable	Not Applicable	Inconclusive Not Performed, or Not Applicable	Inconclusive or Not Applicable	Not Applicable	Inconclusive or Not Applicable	Overarching review and application only
Billingsley, P. (1995)	Inconclusive or Not Applicable	Not Applicable	General Probability	Mathematical Formulation, Other Optimization Procedure or Result	Incenclusive or Not Applicable	Not Applicable	Mathematical Model or Computational Rumit	Overarching review and application only
Sheffield, S. (2011)	Inconclusive or Not Applicable	Not Applicable	Cheracteristic Functions	Mathematical Formulation, Other Optimization Procedure or Result	Inconclusive or Net Applicable	Not Applicable	Mathematical Model or Computational Result	Overarching review and application only
Abadir, K., & Magdalima., T. (2002)	Inconclusive or	Not Applicable	Characteristic Punctions	Mathematical Formulations, Other Optimization Procedure or Result	Inconclusive or Not Applicable	Not Applicable	Mathematical Miodal or Computational Result	Characteristic Function of a Truncated Stand

				Categorization & Other Specific	ogge			
Beforesco	Henriste Type	Opfinission Technique	Pects	Bercharthing	Dada Sanze	O B er	Total	Reserts
Shqib al , NG (1992)	Incontraive or Not Applicable	Not Applicable	Chemosecistic Francions	Merhennical Fermitation, Other Optimization Procedure or Restrict	Inconclusive or Not Applicable	Not Applicable	Mathematical Model or Computational Result	
Errorez, I. (1969)	Incondusive or Not Applicable	Not Applicable	Instructions of Chemicaristic	Mathematical Formulation, Other Optimization Procedure or Remit	Increductive or Not Applicable	Not Applicable	Mathematical Model or Compatibilities Reput	
Bernetic, M. & Cantel, J. (2012)	Inconclusive or Not Applicable Not Applicable	Nor Applicable	Transand Nouse! Dambuicas	Mathematical Formulation, Other Optimization Procedure or Result	facourturie or Not Avelicible	Not Applicable	Mathematical Model or Computational Remai	

APPENDIX H: RESEARCH HYPOTHESIS H₃ TESTING RESULTS

This appendix documents the results of research hypothesis H3 testing. Given that the CF inversion methods presented in this dissertation were developed using a single doubly truncated standard normal distribution as a baseline, by logical inference and inspections the results are identical. However, Tables H.1 and H.2 presented below further reinforce this logical inference through correlation and regression analysis under the varying USL and LSL's presented (i.e., Ct = 0.39894228, Fx(b) = 0.9997, Fx(a) = 3.16712 E-05, n = 81). A Pearson's correlation of 1 suggests a statistically significant strong positive correlation. Regression analysis between the two distributions across varying x-values identifies an adjusted R-square value of 100% at a p-value of <.001. The corresponding fitted line plot equation confirms that the values are identical. Table H.3 contains a summary of the hypothesis test table.

Table H.1 - H3 Hypothesis Pearson Correlation of fT(z) and ft(z) - CF

TSND RANGE	Pearson correlation of fT(z) and ft(z) - CF
USL = 4, LSL = -4	1
USL = 3, LSL = -3	1
USL = 2, LSL = -2	J
USL = 1, $LSL = -1$	l

Table H.2 - H3 Hypothesis Regression Results of fT(z) and ft(z) - CF

TSND RANGE	R-sq (adj)	P-Value	Fitted Line Plot Equation for Cubic Model
USL = 4, LSL = -4	100%	p < 0.001	$Y = 0.000000 + 1.000 X - 0.000000 X^{**2}$
USL = 3, LSL = -3	100%	p < 0.001	Y = 0.000000 + 1.000 X
USL = 2, LSL = -2	100%	p < 0.001	Y = 0.000000 + 1.000 X
USL = 1, LSL = -1	100%	p < 0.001	Y = 0.000000 + 1.000 X

Table H.3 - H3 Hypothesis Test Summary Table

X	pdf	fT(z)	φ(w/μ&σ)	ft(z) - CF
-4	0.00013383	0.00013384	0.00033548	0.00013384
-3.9	0.000198655	0.00019867	0.00049799	0.00019867
-3.8	0.000291947	0.00029197	0.00073185	0.00029197
-3.7	0.00042478	0.00042481	0.00106483	0.00042481
-3.6	0.000611902	0.00061194	0.00153391	0.00061194
-3.5	0.000872683	0.00087274	0.00218763	0.00087274
-3.4	0.001232219	0.0012323	0.00308891	0.0012323
-3.3	0.001722569	0.00172268	0.00431811	0.00172268
-3.2	0.002384088	0.00238424	0.0059764	0.00238424
-3.1	0.003266819	0.00326703	0.00818922	0.00326703
-3	0.004431848	0.00443213	0.0111097	0.00443213
-2.9	0.005952532	0.00595291	0.01492173	0.00595291
-2.8	0.007915452	0.00791595	0.01984235	0.00791595
-2.7	0.010420935	0.01042159	0.02612306	0.01042159
-2.6	0.013582969	0.01358383	0.03404961	0.01358383
-2.5	0.0175283	0.01752941	0.04393972	0.01752941
-2.4	0.02239453	0.02239595	0.05613832	0.02239595
-2.3	0.028327038	0.02832883	0.07100985	0.02832883
-2.2	0.035474593	0.03547684	0.08892725	0.03547684
-2.i	0.043983596	0.04398638	0.11025751	0.04398638
-2	0.053990967	0.05399439	0.13534386	0.05399439
-1.9	0.065615815	0.06561997	0.16448488	0.06561997
-1.8	0.078950158	0.07895516	0.19791124	0.07895516
-1.7	0.094049077	0.09405504	0.23576101	0.09405504
-1.6	0.110920835	0.11092786	0.27805491	0.11092786
-1.5	0.129517596	0.1295258	0.32467303	0.1295258
-1.4	0.149727466	0.14973695	0.37533487	0.14973695
-1.3	0.171368592	0.17137945	0.42958457	0.17137945
-1.2	0.194186055	0.19419836	0.48678309	0.19419836
-1.1	0.217852177	0.21786598	0.54610902	0.21786598
-1	0.241970725	0.24198605	0.60656908	0.24198605
-0.9	0.26608525	0.26610211	0.66701906	0.26610211
-0.8	0.289691553	0.2897099	0.72619504	0.2897099
-0.7	0.312253933	0.31227371	0.78275412	0.31227371
-0.6	0.333224603	0.33324571	0.83532312	0.33324571
-0.5	0.352065327	0.35208763	0.88255281	0.35208763
-0.4	0.36827014	0.36829347	0.92317482	0.36829347
-0.3	0.381387815	0.38141198	0.95605804	0.38141198
-0.2	0.391042694	0.39106747	0.98026077	0.39106747
-0.1	0.396952547	0.39697769	0.99507551	0.39697769
0	0.39894228	0.39896755	1.00006335	0.39896755
0.1	0.396952547	0.39697769	0.99507551	0.39697769
0.2	0.391042694	0.39106747	0.98026077	0.39106747
0.3	0.381387815	0.38141198	0.95605804	0.38141198
0.4	0.36827014	0.36829347	0.92317482	0.36829347

X	pdf	fT(z)	φ(w/μ&σ)	ft(z) - CF
0.5	0.352065327	0.35208763	0.88255281	0.35208763
0,6	0.333224603	0.33324571	0.83532312	0.33324571
0.7	0.312253933	0.31227371	0.78275412	0.31227371
0.8	0.289691553	0.2897099	0.72619504	0.2897099
0.9	0.26608525	0.26610211	0.66701906	0.26610211
1	0.241970725	0.24198605	0.60656908	0.24198605
1.1	0.217852177	0.21786598	0.54610902	0.21786598
1.2	0.194186055	0.19419836	0.48678309	0.19419836
1.3	0.171368592	0.17137945	0.42958457	0.17137945
1.4	0.149727466	0.14973695	0.37533487	0.14973695
1.5	0.129517596	0.1295258	0.32467303	0.1295258
1.6	0.110920835	0.11092786	0.27805491	0.11092786
1.7	0.094049077	0.09405504	0.23576101	0.09405504
1.8	0.078950158	0.07895516	0.19791124	0.07895516
1.9	0.065615815	0.06561997	0.16448488	0.06561997
2	0.053990967	0.05399439	0.13534386	0.05399439
2.1	0.043983596	0.04398638	0.11025751	0.04398638
2.2	0.035474593	0.03547684	0.08892725	0.03547684
2.3	0.028327038	0.02832883	0.07100985	0.02832883
2.4	0.02239453	0.02239595	0.05613832	0.02239595
2.5	0.0175283	0.01752941	0.04393972	0.01752941
2.6	0.013582969	0.01358383	0.03404961	0.01358383
2.7	0.010420935	0.01042159	0.02612306	0.01042159
2.8	0.007915452	0.00791595	0.01984235	0.00791595
2.9	0.005952532	0.00595291	0.01492173	0.00595291
3	0.004431848	0.00443213	0.0111097	0.00443213
3.1	0.003266819	0.00326703	0.00818922	0.00326703
3.2	0.002384088	0.00238424	0.0059764	0.00238424
3.3	0.001722569	0.00172268	0.00431811	0.00172268
3.4	0.001232219	0.0012323	0.00308891	0.0012323
3.5	0.000872683	0.00087274	0.00218763	0.00087274
3,6	0.000611902	0.00061194	0.00153391	0.00061194
3.7	0.00042478	0.00042481	0.00106483	0.00042481
3.8	0.000291947	0.00029197	0.00073185	0.00029197
3.9	0.000198655	0.00019867	0.00049799	0.00019867
4	0.00013383	0.00013384	0.00033548	0.00013384

Figure H.1 - TSND Range (-4 to 4)

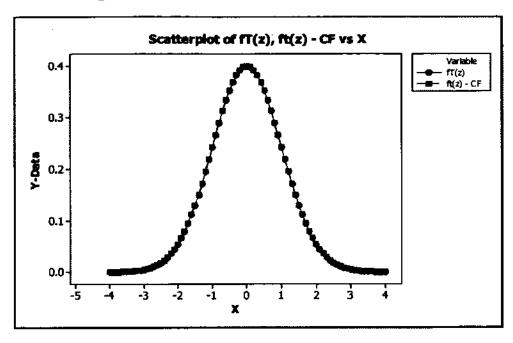


Figure H.2 - TSND Regression (-4 to 4)

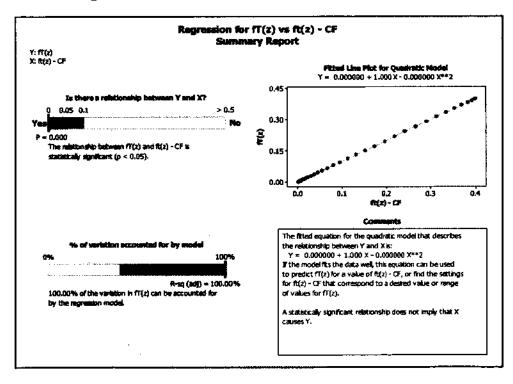


Figure H.3 - TSND Range (-3 to 3)

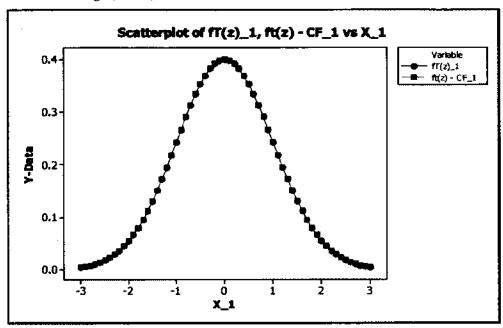


Figure H.4 - TSND Regression (-3 to 3)

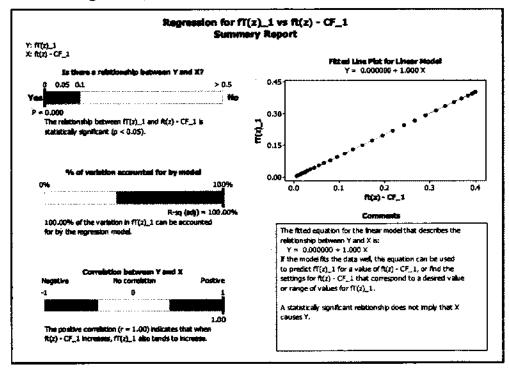


Figure H.5 - TSND Range (-2 to 2)

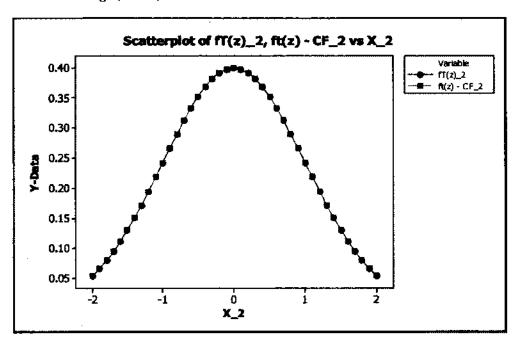


Figure H.6 - TSND Regression (-2 to 2)

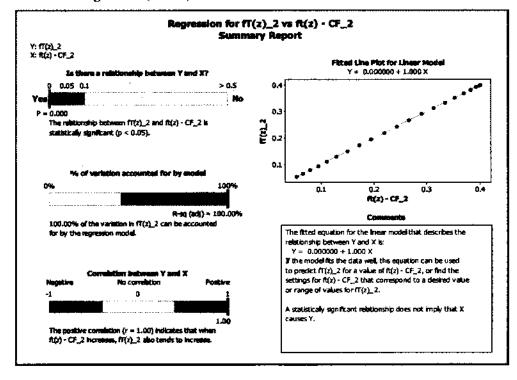


Figure H.7 - TSND Range (-1 to 1)

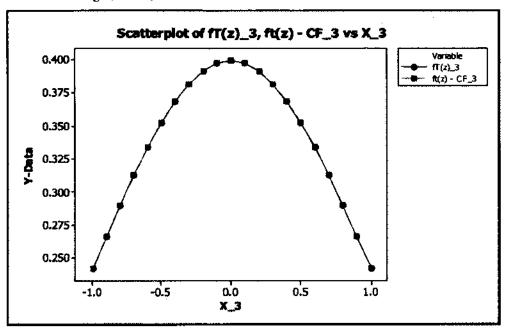
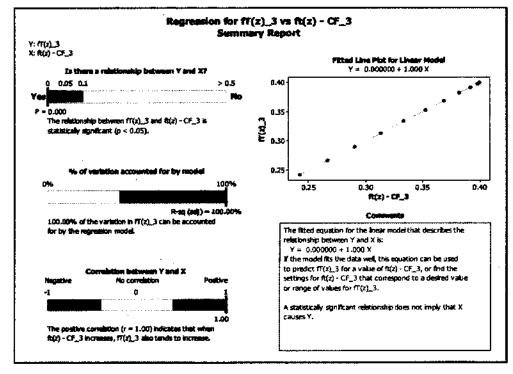


Figure H.8 - TSND Regression (-1 to 1) 1



APPENDIX I: HEURISTIC – TSND BASELINE USING CF INVERSION

This appendix documents the heuristic procedure developed for the baseline inversion of a characteristic function to a truncated standard normal distribution. The general equations are presented in Appendix A. A high-level graphical summary of this heuristic is found in Figure 8. The details for this heuristic are as follows:

Begin Heuristic:

Step 1: Initiate the General Parameters for the Truncated Standard Normal Distribution

- I. Define Parameters $\sigma = 1$, $\mu = 0$, USL, LSL, x, n
- II. Define x as a variable between the USL and LSL
 - a. For a doubly truncated normal distribution (with CF inversion) per Appendix A, Equations 1-5.
 - b. For a probability density function (PDF) refer to Appendix A, Equation (6).
 - c. Calculate Z using Appendix A, Equation (4).

Step 2: Calculate the probability density function (PDF) – (for information)

I. Using Appendix A, Equation (6) from Billingsley (1995), adapted to notation herein:

$$f(x;\mu,\sigma) = \frac{1}{\sqrt{2\pi\sigma}}e^{-\left(\frac{(x-\mu)^2}{2\sigma^2}\right)}$$

Step 3: Calculate the Truncated Standard Normal Distribution

I. Using the defined parameters from step 1 and Appendix A, Equations (1), (2), (3), (4) and (5) from Khasawneh et al. (2005), calculate $f_T(z)$ as follows:

$$f_{T}(z) = \int_{z_{L}}^{z} \frac{f(z)}{\left(\int_{z_{L}}^{z_{U}} f(z)dz\right)} dz \qquad z_{L} \le z \le z_{H} \qquad (APPENDIX A, EQUATION 1)$$

Where
$$f(z) = \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2} \star z^2\right)}$$
 (APPENDIX A. EQUATION 2)

$$f(z)dz = \int_{z_{\perp}}^{z_{\perp}} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2} + z^{2}\right)} dz$$
(APPENDIX A, EQUATION 3)

Given that:

a.
$$z = \frac{x - \mu}{\sigma}$$
 (APPENDIX A, EQUATION 4)

b.
$$\mu_{T_1}(z) = \int_{z_{L_1}}^{z_{U_1}} z f_{T_1}(z) dz \qquad (APPENDIX A, EQUATION 5)$$

This establishes the baseline for the CF inversion. Khasawneh et al. (2005) provides further insight into the calculation of a truncated standard normal distribution using Appendix A, Equations (1) through (5).

- II. Calculate $F_x(b)$ and $F_x(a)$ using Appendix A, Equation (6).
 - a. For $F_x(b)$ the value of X = USL
 - b. For $F_x(a)$ the value of X = LSL
- Step 4: Calculate the CF φ for the given distribution (Appendix A, Equations 2 and 11)
 - I. Since a normal distribution = $\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ has a $\varphi(t) = e^{\frac{iut^2-\frac{\sigma^2t^2}{2}}{2}}$ then

$$\varphi(t) = \int_{a}^{b} f_{x}(u)e^{iu\tau}du = e^{iu\tau - \frac{\sigma^{2}r^{2}}{2}}$$

(Note: for a continuous distribution $b = +\infty$ and $a = -\infty$)

II. Therefore for a truncated standard normal distribution (use Appendix A, Equations 12 and 13)

$$\varphi(\tau) = \frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du = \frac{1}{F_x(b) - F_x(a)} \left(e^{iu\tau - \frac{\sigma^2 r^2}{2}} \right) = \frac{e^{iu\tau - \frac{\sigma^2 r^2}{2}}}{F_x(b) - F_x(a)}$$

III.
$$f_{t}(x) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \varphi(\tau) dt = f_{t}(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left(\frac{e^{iu\tau - \frac{\sigma^{2}t^{2}}{2}}}{F_{x}(b) - F_{x}(a)} \right) dt$$

a. Using Appendix A, Equations 11 and 15

- Step 5: Calculate the truncated standard normal distribution by inversion of the characteristic function using the inversion factor.
 - I. Set the results of Step 3.I (for a given parameter set) equal to step 4.III. The difference equates to the equation and inversion factor (C_{TC}) in Step 5.II.

II.
$$f_r(x) \approx \frac{1}{2\pi} \left(C_{Tc} \right) \left(\frac{e^{\frac{-\sigma^2 x^2}{2}}}{F_x(b) - F_x(a)} \right)$$
, where $C_{TC} = \frac{1}{\sqrt{2\pi}}$

- a. Noted as Appendix A, Equation 16
- b. Where C_{TC} = is a constant for USL and LSL.

Step 6: Baseline the results against a known truncated standard normal distribution

- 1. Generate a given distribution for a range of x value for a given sample size. For the purpose of this dissertation increments of 0.1 were used for a given TSND (e.g. USL/LSL from 4 to -4)
- II. Perform mathematical formulation in addition to correlation and regression analysis. An example is identified in Appendix H.

End Heuristic

Note - Refer to Appendix A for additional information on equations, applications, and references.

APPENDIX J: HEURISTIC - TSND ASSEMBLY USING CF INVERSION

This appendix documents the heuristic procedure developed from the baseline inversion heuristic developed in Appendix B. The general equations utilized by this heuristic are presented in Appendix A. A high-level graphical summary of this heuristic is found in Figure 10. The details for this heuristic are as follows:

Begin Heuristic:

- Step 1: Define the general parameters for the Truncated Standard Normal Distribution
 - 1. Define parameters $\sigma = 1$, $\mu = 0$, USL, LSL, x, n
 - II. Define x as a variable between the USL and LSL
 - d. For a doubly truncated normal distribution (with CF inversion) per Appendix A, Equations 1-5.
 - e. For a probability density function (PDF) refer to Appendix A, Equation (6).
 - f. Calculate Z using Appendix A, Equation (4).
- Step 2: Calculate the probability density function (PDF) (for information)
 - I. Using Appendix A, Equation (6) from Billingsley (1995), adapted to notation herein:

$$f(x;\mu,\sigma) = \frac{1}{\sqrt{2\pi}\sigma}e^{-\left(\frac{(x-\mu)^2}{2\sigma^2}\right)}$$

- Step 3: Calculate the Truncated Standard Normal Distribution
 - I. Using the defined parameters from step 1 and Appendix A, Equations (1), (2), (3), (4) and (5) from Khasawneh et al. (2005), calculate $f_I(z)$ as follows:

$$f_T(z) = \int_{z_L}^{z} \frac{f(z)}{\left(\int_{z_L}^{z_U} f(z)dz\right)} dz \qquad z_L \le z \le z_u \qquad (APPENDIX A. EQUATION 1)$$

Where
$$f(z) = \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}*z^2\right)}$$
 (APPENDIX A, EQUATION 2)

and

$$f(z)dz = \int_{z_{L}}^{z_{c}} \frac{1}{\sqrt{2\pi}} e^{\left(-\frac{1}{2}+z^{2}\right)} dz$$
 (APPENDIX A. EQUATION 3)

Given that:

$$c. \quad z = \frac{x - \mu}{\sigma}$$
 (APPENDIX A, EQUATION 4)

d.
$$\mu_{T_1}(z) = \int_{z_{L_1}}^{z_{U_1}} z f_{T_1}(z) dz$$
 (APPENDIX A, EQUATION 5)

This establishes the baseline for the CF inversion. Khasawneh et al. (2005) provides further insight into the calculation of a truncated standard normal distribution using Appendix A, Equations (1) through (5).

- II. Calculate $F_x(b)$ and $F_x(a)$ using Appendix A, Equation (6).
 - e. For $F_x(b)$ the value of X = USL
 - f. For $F_x(a)$ the value of X = LSL

Step 4: Calculate the CF φ for the given distribution (using Appendix A, Equations 2 and 11):

I. Since a normal distribution =
$$\frac{1}{\sqrt{2\pi\sigma}}e^{-\frac{(x-\mu)^2}{2\sigma^2}} has \ a \ \varphi(t) = e^{\frac{iu\tau - \frac{\sigma^2t^2}{2}}{2}} then$$
$$\varphi(t) = \int_a^b f_x(u)e^{iu\tau} du = e^{\frac{iu\tau - \frac{\sigma^2t^2}{2}}{2}}$$

(Note: for a continuous distribution $b = +\infty$ and $a = -\infty$)

II. Therefore for a truncated standard normal distribution (Appendix 12 and 13):

$$\varphi(\tau) = \frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du = \frac{1}{F_x(b) - F_x(a)} \left(e^{iu\tau - \frac{\sigma^2 r^2}{2}} \right) = \frac{e^{iu\tau - \frac{\sigma^2 r^2}{2}}}{F_x(b) - F_x(a)}$$

III. Given that
$$f_t(x) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \varphi(\tau) dt$$
, then $= f_t(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left(\frac{e^{iu\tau - \frac{\sigma^2 t^2}{2}}}{F_x(b) - F_x(a)} \right) dt$,

(Appendix A. Equations 11 and 12)

Step 5: Define the characteristic function for x as: The characteristic function of a probability measure μ is defined for real t by (repeat for two identical distributions):

1.
$$\varphi(t) = \varphi_x(t) := E[e^{itX}] = \int_{-\infty}^{\infty} e^{itx} \mu(dx)$$
 (Appendix A. Equation 7)

a. where $[e^{itX}] = \cos(t) + i\sin(t)$ (Appendix A. Equation 8)

b. where
$$\varphi_{X+Y} = \varphi_x \varphi_y$$

(Appendix A. Equation 10)

- II. Billingsley (1995) identifies that a Characteristic Function has 3 fundamental properties as follows:
 - i. "If μ_1 and μ_2 have respective characteristic functions $\varphi_1(t)$ and $\varphi_2(t)$ then $\mu_1 * \mu_2$ has characteristic function $\varphi_1(t) * \varphi_2(t)$.

 Billingsley (1995) notes that "although convolution is essential to the study of sums of independent random variables, it is a complicated operation, and its often simpler to study the products of the corresponding characteristic functions.
 - ii. The characteristic function uniquely determines the distribution. This shows that in studying the products in (i), no information is lost.
 - iii. From the pointwise convergence of characteristic functions follows the weak convergence of the corresponding distributions. This makes it possible, for example, to investigate the asymptotic distributions of sums of independent random variables by means of their characteristic functions."
- Step 6: Calculate the truncated standard normal distribution by inversion of the characteristic function using the inversion factor.
 - I. Set the results of Step 3.1 (for a given parameter set) equal to step 4.III. The difference equates to the equation and inversion factor (C_{TC}) in Step 5.II.

II.
$$f_t(x) \approx \frac{1}{2\pi} \left(C_{Tc} \right) \left(\frac{e^{-\frac{\sigma^2 x^2}{2}}}{F_x(b) - F_x(a)} \right)$$
, where $C_{TC} = \frac{1}{\sqrt{2\pi}}$ (Appendix A. Equation 16)

- a. Where C_{TC} = is a constant for USL and LSL
- Step 7: Abadir, K., & Magdalinos., T. (2002) define the characteristic function for a doubly truncated normal distribution as: "the variate where x is doubly truncated to $y \in (a,b)$, where b > a, and its characteristic function is given by the integral (repeat for two identical distributions:

I.
$$\varphi_y(\tau) = \frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du$$
 " (Appendix A, Equation 12)

II. Then logically the sum of the characteristic functions for two doubly truncated normal distributions is given Equation 10 and Step 7.II.a (Appendix A, Equation 18)::

a.
$$\varphi_z(\tau) := \left(\frac{1}{F_x(b) - F_x(a)} \int_a^b f_x(u) e^{iu\tau} du\right) \left(\frac{1}{F_y(b) - F_y(a)} \int_a^b f_y(u) e^{iu\tau} du\right)$$

Step 8: Using an inversion formula the sum of two doubly truncated normal distributions can be used to determine the resulting probability density function for the combined distribution. Given the following:

I. Since
$$f(x) = \frac{1}{2\pi} \int_{0}^{\infty} e^{-itx} \varphi(t) dt$$
 (Appendix A. Equation 14)

II. and Appendix A, Equation 10.

Step 9: Solve for
$$f_{t}(x)_{axxy} = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-itx} \left[\left(\frac{e^{iut - \frac{\sigma^{2}t^{2}}{2}}}{F_{x}(b) - F_{x}(a)} \right)_{d1} \left(\frac{e^{iut - \frac{\sigma^{2}t^{2}}{2}}}{F_{x}(b) - F_{x}(a)} \right)_{d2} \right] dt$$

(Appendix A, Equation 19)

1.
$$f_{t}(x)_{assy} = \frac{1}{2\pi} \left(\frac{1}{(F_{x}(b) - F_{x}(a))_{d1} * (F_{x}(b) - F_{x}(a))_{d2}} \right) \int_{-\infty}^{\infty} e^{-itx} \left[\left(e^{iu\tau - \frac{\sigma^{2}r^{2}}{2}} \right)_{d1} \left(e^{iu\tau - \frac{\sigma^{2}r^{2}}{2}} \right)_{d2} \right] dt$$

(Appendix A, Equation 20)

i. Where
$$\int_{-\infty}^{\infty} e^{-itx} \left[e^{iu\tau - \frac{\sigma^2 t^2}{2}} \right] dt = e^{-\frac{\sigma^2 r^2}{2}}$$
 (Appendix A, Equation 21)

II.
$$f_t(x)_{assy} \approx \frac{1}{2\pi} (C_{Tc}) \left(\frac{\left(e^{-\frac{\sigma^2 t^2}{2}}\right) \left(e^{-\frac{\sigma^2 t^2}{2}}\right)}{\left(F_x(b) - F_x(a)\right)_{d1} * \left(F_x(b) - F_x(a)\right)_{d2}} \right)$$
, where C_{TC} $\frac{1}{\sqrt{2\pi}}$

(Appendix A, Equation 22)

Step 10: Baseline the results against a known truncated standard normal distribution (final state)

- Generate a given distribution for a range of X value for a given sample size. For the purpose of this dissertation increments of 0.2 were used for a given TSND (e.g. USL/LSL from 8 to -8. Two identical distributions with an USL (4) and LSL (-4) were assembled. See Figure 9.
- II. Perform mathematical formulation in addition to correlation and regression analysis. Assembly results are identified in Appendix D, E, and H.

End Heuristic

Note - Refer to Appendix A for additional information on Equations, Applications and References.

VITA

John Walter Ralls

Department of Engineering Management and Systems Engineering Old Dominion University, Norfolk, VA 23529

EDUCATION

- Doctor of Philosophy, Engineering Management, Old Dominion University, 2014 (expected)
- Master of Engineering Management, The George Washington University,
 Washington, D.C., 2005
- Bachelor of Science, Marine Engineering Systems, United States Merchant
 Marine Academy, 2001

WORK EXPERIENCE:

Mr. John Walter Ralls has over 10 years of experience in engineering and management. He has significant project management experience in the area of manufacturing, design, system development, and front line engineering management. As a licensed professional engineer in the Commonwealth of Virginia, Mr. Ralls also holds certifications in project management, refrigeration, and holds a USCG 3rd Assistant Engineers License for Steam, Diesel, and Gas Turbines of Any Horsepower.