# Design Of The Layout Of A Manufacturing Facility With A Closed Loop Conveyor With Shortcuts Using Queueing Theory And Genetic Algorithms 

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# DESIGN OF THE LAYOUT OF A MANUFACTURING FACILITY WITH A CLOSED LOOP CONVEYOR WITH SHORTCUTS USING QUEUEING THEORY AND GENETIC ALGORITHMS 

by

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A dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy<br>in the Department of Industrial Engineering \& Management Systems<br>in the College of Engineering \& Computer Science at the University of Central Florida Orlando, Florida

## Fall Term

2011
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## ABSTRACT

With the ongoing technology battles and price wars in today's competitive economy, every company is looking for an advantage over its peers. A particular choice of facility layout can have a significant impact on the ability of a company to maintain lower operational expenses under uncertain economic conditions. It is known that systems with less congestion have lower operational costs. Traditionally, manufacturing facility layout problem methods aim at minimizing the total distance traveled, the material handling cost, or the time in the system (based on distance traveled at a specific speed).

The proposed methodology solves the looped layout design problem for a looped layout manufacturing facility with a looped conveyor material handling system with shortcuts using a system performance metric, i.e. the work in process (WIP) on the conveyor and at the input stations to the conveyor, as a factor in the minimizing function for the facility layout optimization problem which is solved heuristically using a permutation genetic algorithm. The proposed methodology also presents the case for determining the shortcut locations across the conveyor simultaneously (while determining the layout of the stations around the loop) versus the traditional method which determines the shortcuts sequentially (after the layout of the stations has iii
been determined). The proposed methodology also presents an analytical estimate for the work in process at the input stations to the closed looped conveyor.

It is contended that the proposed methodology (using the WIP as a factor in the minimizing function for the facility layout while simultaneously solving for the shortcuts) will yield a facility layout which is less congested than a facility layout generated by the traditional methods (using the total distance traveled as a factor of the minimizing function for the facility layout while sequentially solving for the shortcuts). The proposed methodology is tested on a virtual 300 mm Semiconductor Wafer Fabrication Facility with a looped conveyor material handling system with shortcuts. The results show that the facility layouts generated by the proposed methodology have significantly less congestion than facility layouts generated by traditional methods. The validation of the developed analytical estimate of the work in process at the input stations reveals that the proposed methodology works extremely well for systems with Markovian Arrival Processes.

This work is dedicated to Capt. Valerian Lasrado, Merlyn Lasrado, Morgan Lasrado, Felix Pinto, Helen Pinto, Monthie Lasrado, Raymond Lasrado, and the rest of my family.

Without your constant support and encouragement none of this would be possible.

## ACKNOWLEDGMENTS

I would like to acknowledge the various institutions $I$ have attended (in order of attendance): Don Bosco High School, St. Stanislaus High School, R.D. National College, Georgia Institute of Technology, and University of Central Florida. I am grateful for the knowledge, values, professionalism, and ethics that were imparted onto me by these institutions.

Much of what $I$ have accomplished in life is built on the support of others. I am grateful for the moral support I have received from my family, teachers, and friends that has enabled me to complete this work. Furthermore, I am grateful for the financial support $I$ have received without which this work would not be possible. I would like to acknowledge (in order or receipt of funds / grants) Capt. Valerian and Merlyn Lasrado, Paul Lasrado, and University of Central Florida (IEMS Department, Graduate Studies, Dr. Yang Wang, Dr. Dima Nazzal, and Dr. Thomas O'Neal) for their generous support through the years.

Finally, I am grateful for the immense support and direction provided to me by my PhD committee: Dr. Dima Nazzal, Dr. Robert Armacost, Dr. Ivan Garibay, Dr. Mansooreh Mollaghasemi, Dr. Charles Reilly, and Dr. Stephen Sivo. Thank you so much for your time, patience, and guidance which enabled an idea to metamorphose into the work that is presented henceforth.

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## LIST OF ACRONYMS / ABBREVIATIONS

| Abbreviation | Meaning |
| :--- | :--- |
| ANOVA | Analysis of Variance |
| CLC | Closed looped conveyor |
| FLP | facility layout problem |
| GA | Genetic algorithm |
| GLM | Generalized Linear Model |
| LCMHS | Looped conveyor material handling system |
| LLDP | Looped layout design problem |
| LLMF | Looped layout manufacturing facility |
| MF | Manufacturing facility |
| MFLP | Manufacturing facility layout problem |
| MHS | Material handling system |
| PS | Production System |
| QAP | Quadratic assignment problem |
| QNA | Queueing network analyzer |
| SA | Simulated annealing |
| SCV | Squared coefficient of variation |

## 1 INTRODUCTION

With the ongoing technology battles and price wars in today's competitive economy, every company is looking for an advantage over its peers; an important practical question is, how do companies create this competitive advantage in terms of creating value (Hitt, Ireland, Camp, \& Sexton, 2001, 2002; Meyer, 1991)? A sustainable competitive advantage could be provided for by being an efficient business (Peteraf, 1993). As per Tompkins, White, and Bozer (2010), companies in the US spend around 8\% of the gross national product annually on new facilities. The authors point out that effective facility planning can reduce operational expenses by $10 \%$ to $30 \%$ annually. Apple (1977) indicates that a good facility layout design incorporates the material handling decisions at the development stage. Tompkins et al. (2010) indicate that material handling and facility planning cost can attribute around $20 \%$ to $50 \%$ of a facility's operating expense. Hence, a particular choice of facility Layout can have a significant impact on the ability of a company to maintain lower operational expenses under uncertain economic conditions. Furthermore, a poor Layout can result in high material handling costs, excessive work-in-process (WIP), and low or unbalanced equipment utilization (Heragu, 2006).

In general, the manufacturing facility (MF) consists of a production system (PS) and a material handling system (MHS). The PS consists of numerous operational cells henceforth referred to as a cell or cells. In the literature, a cell in the $P S$ is referred to as a machine, a facility, a station, a collection of stations, a department, a bay, etc. The manufactured units, henceforth referred to as loads or jobs, are transferred from one cell to another by the MHS. As seen in Figure 1.1, there are various types of MF layouts with respect to material handling systems design: single row, multi row, closed loop layout (Kusiak \& Heragu, 1987), and open field layout (Loiola, de Abreu, Boaventura-Netto, Hahn, \& Querido, 2007).


Figure 1.1: Types of facility layouts w. r. t. material handling design

This research will focus on the layout of a MF, i.e., the manufacturing facility layout problem (MFLP) for a closed loop layout. This special case of the MF will henceforth be referred to as the looped layout MF (LLMF). This special case of MFLP will henceforth be referred to as the looped layout design problem (LLDP), using the nomenclature introduced in Nearchou (2006).

The subsequent discussion will first introduce the MFLP, the LLMF and LLDP will be discussed in great detail in § 2.2.1.

The MFLP can be defined as an optimization problem whose solution determines the most efficient physical organization of the cells in a PS with regards to an objective. The most common objectives aim to minimize the material handling cost (MHC), the traveled distance traveled, or the total time in system (Benjaafar, Heragu, \& Irani, 2002). Previous MFLP formulations tend to ignore the impact of the facility layout on the operational performance of the MF i.e. the work-in-process (WIP), the throughput, or the cycle time. Benjaafar (2002) shows that traditional MF design criteria can be a poor indicator of the operational performance of the MF. Bozer and Hsieh (2005) too support this argument. Kouvelis, Kurawarwala, and Gutierrez (1992) state, "the use of 'optimality" with respect to a design objective, such as the minimization of the material handling cost, is discriminating." Benjaafar (2002) argues that the operational performance of the MF is contingent on the congestion in the MF . The congestion in the $M F$ is a function of its capacity and variability. Hence, it is imperative that the objective of the MFLP captures the impact of the facility layout on the operational performance of the MF. This can be achieved, for example, by setting the objective of the MFLP to minimize the WIP in the MF
(Benjaafar, 2002; Fu \& Kaku, 1997; Kouvelis \& Kiran, 1991; Raman, Nagalingam, \& Gurd, 2008). However, despite the presence of conveyor systems in high volume manufacturing facilities, there are no methods that generate the Layout by minimizing the WIP in a LLMF with a closed loop conveyor (CLC) as the MHS.

This research proposes a solution methodology that addresses the development of a facility layout for a LLMF with a looped conveyor material handling system (LCMHS) that can have shortcuts across it using a system performance metric, i.e. the work in process (WIP) on the conveyor and at the input stations to the conveyor, as a factor in the minimizing function for the facility layout optimization problem which is solved heuristically using a permutation genetic algorithm. It can be argued that there is no difference in the optimal layout as generated by minimizing the WIP versus the distance or cost, Fu and Kaku (1997) support this claim. Benjaafar (2002) proposes that there is a difference and adds that $F u$ and Kaku (1997) did not capture this as a result of the simplistic queueing model used to model the MF. Benjaafar (2002) proposes that under certain conditions both approaches will yield the same facility layout, these restricting conditions are:

1. The flow rates between the cells, machines, stations, departments, facilities, or bays are balanced
2. The cells, machines, stations, departments, facilities, or bays are equidistance
3. The demand and process time variability are low

The first condition is practically unrealistic and applies if and only if all the loads visit all the machines the same number of times. Also, modern MFs manufacture a multitude of products and this situation is rarely encountered. As mentioned, this research will focus on MF that have a LCMHS, therefore the second condition in inherently impossible given the MHS is a loop. The third condition is plausible but there are many situations in practice that have high demand variability, high process variability, or both.

Traditionally for the MFLP, the optimal layout of a facility is first determined. After some time of operation, usually if needed, the best set of shortcuts is determined to alleviate congestion in the LLMF as described by Hong, Johnson, Carlo, Nazzal, and Jimenez (2011). It is the contention of the proposed research that the aforementioned two-step process yields a suboptimal solution. The proposed research aims at determining the best set of shortcuts while simultaneously determining the facility layout, thereby ensuring at worst an equivalent solution to the two-step process.

The computational complexity of the algorithms required to solve the proposed formulation of the MFLP is to be considered. The proposed formulation is a NP-Hard problem as proved by Leung (1992). It has been shown that the computation time required to reach an optimal solution increases exponentially as the number of machines to be arranged increases when using exact solution methods (Foulds, 1983). James, Rego, and Glover (2008) and Loiola, de Abreu, Boaventura-Netto, Hahn, and Querido (2007) supplement this claim with detailed discussions on the computational complexity and the required computation time to reach an optimal solution using exact solution methods. This research proposes the use of genetic algorithms (GA) to solve the formulation as further discussed in $\$ 3.3 .1$ and $\$ 4$.

The rest of this chapter is organized as follows: § 1.1 will provide a description of the LLMF; and $\$ 1.2$ will present the research statement.

### 1.1 Description of the LLMF

A brief description of the LLMF is given below. This description entails the assumptions, definitions and characteristics of the LLMF.

It is assumed that the number of machines required and their groupings are predetermined. The machines may be used individu-
ally or as a group; in either case, they will be referred to as cells. There will be $M$ cells $(i=1,2,3, \ldots, M)$ assigned to $N$ locations $(j=1,2,3, \ldots, N)$ where $M \leq N . \operatorname{If} M<N$ dummy cells $(M+1, M+2, \ldots, N)$ are introduced as recommended by Hillier and Connors (1966). There is one entry point (loading cell) and one exit point (shipping cell) to the LLMF. At the entry point (i=0) products are delivered/loaded into the plant and at the exit point (i=N+1) products are shipped/unloaded out of the plant.

There are $K$ products $(k=1,2,3, \ldots, K)$ flowing through the LLMF each characterized by an independently distributed random variable with an average demand $\left(D_{k}\right)$ and a squared coefficient of variation $\left(C_{k}{ }^{2}\right)$.

The routing for each product through the LLMF is known and is deterministic. Products may visit each cell more than once. The decomposition method as presented in Whitt (1983) is used to determine the internal flows between the cells. The internal flow between cells for each product will be represented by $\lambda_{i j}$, where the product travels from cell $i \quad(i=1,2,3, \ldots, N)$ to cell $j$ $(j=1,2,3, \ldots, N)$ using a LCMHS and $\lambda_{i i}=0$.

The LLMF is a job shop with interconnected bays/cells that each consists of a group of machines or individual machines, an automated material handling system (AMHS) which is a LCMHS with no load recirculation i.e. infinite buffer at unloading station
from the conveyor, an input station (where new jobs are introduced to the LLMF) and an output station (where completed jobs are moved away from the LLMF), and shortcuts as shown in Figure 1.2.

The MF has a variable demand, a regular shape with fixed dimensions. The loads can backtrack to cells, i.e. revisit facilities, and bypass cells in the MF. Each cell has a loading / unloading station where loads are loaded to / unloaded from the conveyor.


Figure 1.2: Layout of the Facility

The arrival process to cell $i$ is characterized by an independently distributed random variable with an average interarrival time $\left(1 / \lambda_{i}\right)$ and a squared coefficient of variation ( $\left.C_{a i}{ }^{2}\right)$, while the service process at each cell is characterized by an independently distributed random variable with a mean service time $\left(\tau_{i}\right)$ and a squared coefficient of variation ( $\left.c_{s i}{ }^{2}\right)$.

In the LLMF, a shortcut can be placed after each cell i in the direction of flow such that it is before the next cell i+1 and
before the corresponding shortcut from the opposite side of the conveyor.

As illustrated by Figure 1.3, two sides of the conveyor are shown. Cell $p$ and cell $q$ are on one side of the conveyor, while cell $r$ and cell $s$ are on the other (opposite) side of the conveyor. The shortcut $p$ (arc 'eh') after cell p is placed in the direction of flow before cell $q$ and before the corresponding shortcut $r$ (arc 'gf') from cell r opposite side of the conveyor.


Figure 1.3: Shortcut diagram

If a cell is the last cell on its side of the conveyor in the direction of flow, then a shortcut is always placed after that cell (the short wall of the conveyor that connects the two sides.)

### 1.2 Research Statement

For a LLMF, the proposed methodology will aim to solve the LLDP for a LCMHS with shortcuts, using a system performance metric, i.e. the work in process (WIP) on the conveyor and at the input
stations to the conveyor, as a factor in the minimizing function for the facility layout optimization problem which is solved heuristically using a permutation genetic algorithm.using an operational performance metric, i.e. the work in process on the conveyor and the input stations in a MF, as the minimizing function of the design criteria. Bozer \& Hsieh (2005) suggests that for a LLMF, the most appropriate design criterion for the LLDP would be to minimize the total WIP on the conveyor and the input stations for all the cells in the LLMF. Benjaafar (2002) shows that using the total WIP in the system (WIP in the production system, the unloading and unloading stations, and the MHS) as a design criterion for a MF with automated vehicles as the MHS can have a significant impact on the layout of the $M F$.

As described earlier, most traditional MFLP methods aim at minimizing the total distance traveled, the material handling cost, or the time in the system (based on distance traveled at a specific speed). However, Bozer \& Hsieh (2005) suggest that one or more loading stations in the LLMF might become unstable as a result of the traditional layouts creating too much flow over certain segments of the conveyor. Also, one of the outcomes of the proposed research is that the traditional optimal layout, i.e., the layout with the minimum distance may not have the minimum WIP for the LLMF.

Further, as described earlier, the two step process of first determining the optimal Layout and then determining the best set of shortcuts will yield a sub optimal solution. The proposed research addresses this issue by determining the set of shortcuts and the layout simultaneously and iteratively, thereby ensuring at worst an equivalent solution to the two-step process.

The remainder of the document is organized as follows: $\$ 2$ will present the literature review with regards to the proposed methodology; § 3 will present the research design; $£ 4$ will present the proposed implementation; and $\$ 5.2 .9$ will discuss the concluding statements and future work.

## 2 LITERATURE REVIEW

The amount of research done on the manufacturing facility layout problem (MFLP) is very vast. Due to its broad applicability and solution complexity it has been the subject of active research over the last 50 years. Koopmans and Beckmann (1957) are the first to discuss the FLP. They define the FLP as a quadratic assignment problem (QAP) that determines the layout of facilities so that the material handling cost between the facilities is minimized. Sahni and Gonzalez (1976) prove the computational complexity and the difficulty involved in solving QAP problems by showing the QAP is NP-Complete.

Figure 2.1 on page 14 as presented in (Drira, Pierreval, \& Hajri-Gabouj, 2007) illustrates the broad nature of the MFLP. This literature review will focus on the facility layout procedures for a static MF with (refer to

Figure 2.2 on page 15): available data, a variable (stochastic?) demand, a regular shape with fixed dimensions, a looped conveyor based MHS with no load recirculation i.e. infinite buffer at unloading station from the conveyor, with backtracking and bypassing enabled, formulated as a QAP that minimizes material handling cost by minimizing the congestion in the system i.e. the WIP in the manufacturing facility.

The rest of this chapter is organized as follows: § 2.1 will present a list of review papers related to the proposed methodology; § 2.2 will present a review of the MFLP; § 2.3 will present a review of the solution methods for the MLFP; § 2.4 will present a review of conveyor systems and methods of analysis for such systems.

### 2.1 Review Papers on Research Topic

There have been numerous review and survey papers that have tracked the research on $\operatorname{FLP}$ and other research subjects related to the FLP over time pertaining to the current research topic of a LLDP with a LCMHS.

- Wilson (1964) presents a review of various FLP's with regards to fixed designs, material flow networks, and communication networks
- El-Rayah and Hollier (1970) present a review of various FLP while also reviewing optimal and suboptimal algorithms for solving a QAP
- Pierce and Crowston (1971) present a review of algorithms for solving the QAP using tree-search algorithms


Figure 2.1: Manufacturing Facility Layout Problem Outline


Figure 2.2: Manufacturing Facility Layout Problem Research Focus

- Hanan and Kurtzberg (1972) present a survey of algorithms for solving applications of the QAP to a variety of industries
- Moore (1974) presents a review of the, then, current state of $F L P$ research in Europe and North America based on responses to a survey sent to authors of various FLP algorithms
- Francis and Goldstein (1974) present a list of papers published in between 1960 to 1973 on location theory, however, many of these references allude to the FLP and algorithms used to solve the QAP
- Burkard and Stratmann (1978) present a review that extends the work performed by Pierce and Crowston (1971) by comparing the efficacy of various suboptimal algorithms
- Muth and White (1979) discuss deterministic, probabilistic, descriptive and normative approaches used to model conveyor systems
- Foulds (1983) presents a review of optimal and sub optimal algorithms for the QAP highlighting the application of graph theory to solve the FLP
- Levary and Kalchik (1985) present a review that compares and contrasts several sub optimal algorithms used to solve the QAP
- Buzacott and Yao (1986) present a review that compares and contrasts several analytical models of flexible manufacturing systems by evaluating the strengths and weaknesses of each model
- Finke, Burkard, and Rendl (1987) present a survey of the theory and solution procedures (exact and approximate) for the QAP with special interest devotes to integer programming equivalents to the QAP
- Hassan and Hogg (1987) present a review and evaluation of algorithms that apply graph theory to solve the FLP
- Kusiak and Heragu (1987) present a review that evaluates the, then, current state of optimal and suboptimal algorithms to solve the FLP
- Bitran and Dasu (1992) present a review of manufacturing systems modeled as open queueing networks
- Pardalos, Rendl, and Wolkowicz (1994) present a survey of the, then, current state of QAP research covering QAP formulations, solution methods and applications
- Meller and Gau (1996) present a survey that compares and contrasts the, then, current $F L P$ software to the FLP research
- Mavridou and Pardalos (1997) present a survey of simulated annealing algorithms and genetic algorithms used for generating approximate solutions for the FLP
- Balakrishnan and Cheng (1998) present a review of the algorithms to solve the FLP based on multiple periods planning horizons (Dynamic $\mathrm{FLP}^{1}$ ) as opposed to static unchanging layouts
- Govil and Fu (1999) present a survey of queueing network models for the analysis of various manufacturing systems by identifying the main factors affecting the models as well as variations of the models
- Pierreval et al. (2003) present a review of manufacturing facility layout where evolutionary principles have been applied to optimize the MFLP
- Haupt and Haupt (2004) present a detailed review and analysis of GAs and the practical application of GAs with examples of executable Matlab and Fortran code.

1 The current research will focus on static facility layouts although future work will extend the static facility layout model to a dynamic facility layout model

- Asef-Vaziri and Laporte (2005) present a review of loop based facility planning methodologies for $M F$ with trip based MHS i.e. automated guided vehicles (AGV)
- Agrawal and Heragu (2006) present a review of automated material handling systems (AMHS) used in Semiconductor Fabs
- Singh and Sharma (2006) present an exhaustive survey of various algorithms as well as computerized facility layout software developed since 1980 for the FLP
- Drira, Pierreval, and Hajri-Gabouj (2007) present a review of algorithms for the FLP along with a generalized framework for the analysis of literature with regards to FLP as shown in Figure 2.1 on page 14
- Loiola et al. (2007) present a survey of QAP and associated procedures by discussing the most influential QAP formulations and QAP solutions procedures
- Nazzal and El-Nashar (2007) present a survey of models of conveyor systems in semiconductor fabs and an overview of the corresponding simulation based models.
- Shanthikumar, Ding, \& Zhang (2007) present a survey of the application of queueing theory literature to semiconductor manufacturing systems


### 2.2 Manufacturing Facility Layout Problem

This section first presents a review of the general MFLP formulations where $M$ facilities / cells are assigned to $N$ locations with regards to a certain objective. The most common objectives aim to minimize the material handling cost (MHC), the distance traveled, or the total time in system (Benjaafar, Heragu, \& Irani, 2002). The proposed research will formulate the LLDP as a QAP to generate an optimal layout for a LLMF. Second, a review of the LLDP is presented in $\$ 2.2 .1$ on page 22. Third, a review of MFLP formulations with that minimize the WIP in the MF is presented in $\$ 2.2 .2$ on page 28.

The MFLP is formulated as a QAP by Koopmans and Beckmann (1957). Sahni and Gonzalez (1976) show that the QAP is NPComplete. Given that there are $M$ cells and $N$ locations, if $M<N$ dummy cells $(M+1, M+2, \ldots, N)$ are introduced as stated in Hillier and Connors (1966). The following notation is used where $x_{i j}$ is the decision variable:

$$
\begin{align*}
& \lambda_{i k}-\text { flow of loads from cell } i \text { to cell } k \\
& C_{j i}-\text { cost of transporting load from location } j \text { to location } l \\
& x_{i j}-1 \text { if cell i is at location } j ; 0 \text { otherwise } \\
& \operatorname{Min} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N} \sum_{l=1}^{N} \lambda_{i k} c_{j l} x_{i j} x_{k l} \tag{1}
\end{align*}
$$

$$
\begin{array}{ll}
\text { s.t. } & \sum_{i=1}^{N} x_{i j}=1 \\
& \forall j, 1 \leq j \leq N \\
\sum_{j=1}^{N} x_{i j}=1 & \forall i, 1 \leq i \leq N  \tag{4}\\
& x_{i j} \in\{0,1\} \\
1 \leq i, j \leq N
\end{array}
$$

The formulation as presented in (1)-(4) minimizes the transportation cost of a MF. Given that $d_{j i}$ is the distance between location $j$ and location $l$; (1) can be restated as follows to generate a layout that minimizes the total distance traveled by the loads in a MF.

$$
\begin{equation*}
\operatorname{Min} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N} \sum_{l=1}^{N} \lambda_{i k} d_{j l} x_{i j} x_{k l} \tag{5}
\end{equation*}
$$

s.t. (2) - (4)

As indicated by Loiola et al. (2007), there are various formulations of the FLP; all of these formulations can be traced back to the QAP. Examples of such formulations include: quadratic set covering problem (QSP) formulation (Bazaraa, 1975), linear integer programming formulation (Lawler, 1963), mixed integer programming formulation (Bazaraa \& Sherali, 1980; Kaufman \& Broeckx, 1978), graph theoretic formulation (Foulds \& Robinson,
1976), formulations by permutations (Hillier \& Connors, 1966), and trace formulations (Edwards, 1980).

The proposed research will focus on the formulation by permutations as it is the most commonly used formulation and extends itself well to formulations with very complicated objective functions. According to Hillier and Connors (1966) and Loiola et al. (2007) if $S_{N}$ is the set of all permutations of $N$ variables, $\pi \epsilon S_{N}$ and $\mathrm{C}_{\pi(i) \pi(j)}$ is the cost of transporting load from location $\pi(i)$ to location $\pi(j)$. Then, given that each permutation ( $\pi$ ) represents a unique layout of the MF , i.e. a unique assignment $M$ cells to $N$ locations, the MFLP that minimizes the transportation costs in the MF reduces to:

$$
\begin{equation*}
\underset{\pi \in S_{N}}{\operatorname{Min}} \sum_{i=1}^{N} \sum_{j=1}^{N} \lambda_{i j} c_{\pi(i) \pi(j)} \tag{6}
\end{equation*}
$$

Loiola et al. (2007) state that the above formulation is equivalent to (1)-(4), as (2) and (3) define a matrix $\boldsymbol{X}=\left[x_{i j}\right]$ for each $\pi$ related to $S_{N}$ as in (6), where for all $1 \leq i, j \leq N$,

$$
x_{i j}= \begin{cases}1, & \text { if } \pi(i)=j  \tag{7}\\ 0, & \text { if } \pi(i) \neq j\end{cases}
$$

### 2.2.1 Looped Layout Design Problem (LLDP)

The LLDP is a special case of the MFLP applied to LLMF. LLMF's are attractive due to their low setup costs as the LLMF requires
minimal material handling resources to link the various cells to each other (Afentakis, 1989). By design, in a LLMF all the cells are easily accessible (Afentakis, 1989). There are two types of layout patterns: the closed loop layout that has a predetermined pattern and the open field type layout that has no predetermined pattern. Chae and Peters (2006) indicate that the latter is more difficult to solve and may result in less desirable solutions as a result of the lack of modularity and/or structure in the prescribed layout of the LLMF.

As in the case of the MFLP, the LLDP aims to determine the most effective arrangement of $M$ cells to $N$ locations (around a loop) with regards to a certain objective. The most common objective for the LLDP is to minimize the material handling cost (Asef-Vaziri \& Laporte, 2005). Most of the current research of the LLDP is geared towards LLMF's with AGV's as the MHS (AsefVaziri \& Laporte, 2005; Nearchou, 2006), Bozer and Hsieh (2005) present a solution to the LLDP for a LLMF with a closed loop conveyor as the MHS. Kouvelis and Kim (1992) and Leung (1992) show the LLDP is NP-Complete. As in the case of MFLP, metaheuristic solution approaches are most effective to solve LLDP with greater than 20 cells (Asef-Vaziri \& Laporte, 2005).

Afentakis (1989) is the first to propose an algorithm to explicitly design the layout of LLMF. Afentakis (1989) proposes to
minimize the traffic congestion, which can be defined as the number of times a load traverses the loop before it departs from the system. Afentakis (1989) proposes a heuristic based on a graph theoretic approach to minimize the traffic congestion of all the loads (also referred to as MIN-SUM). The heuristic constructs a layout from the dual of a linear programming (LP) relaxation of the problem. Afentakis (1989) was able to solve a LLDP with up to 12 cells.

Leung (1992) builds on Afentakis (1989) by proposing a heuristic based on a graph theoretic approach to minimize the maximum traffic congestion of all the loads (also referred to as MINMAX) . Kaku and Rachamadugu (1992) model the LLDP as a QAP and find optimal and near optimal solutions for smaller problems.

Millen, Solomon, and Afentakis (1992) analyze the impact of the number of loading and unloading stations on the material handling requirements for a LLDP using simulation. They point out that having a single loading and unloading station for the LLDP increases the material handling requirements by as much as $200 \%$ versus having a loading and unloading station at each cell.

Kouvelis and Kim (1992) propose an algorithm to solve the LLDP. By using the formulation as described by (6), they develop dominance relationships to easily identify local optimal solutions thereby reducing the solution space. They develop and ap-
ply a branch-and-bound procedure and heuristic methods successfully to a LLDP with 12 cells.

Kiran and Karabati (1993) present a branch-and-bound procedure and heuristic methods for a LLDP. As in Kouvelis and Kim (1992), Kiran and Karabati (1993) too present dominance rules based on a special distance metric to identify local solutions. They present a special case of the LLDP / QAP that is solvable in polynomial time. When all the cells in a LLMF interact with only one cell, the LLDP can be solve in $O\left(n^{2} \operatorname{logn}\right)$ time.

Das (1993) presents a four step heuristic procedure for solving the LLDP that combines variable partitioning and integer programming to minimize the total projected travel time between cells. Each cell is represented by its special coordinate, its orientation with respect to the layout (horizontal or vertical), and the location of its loading or unloading station. The heuristic becomes computationally inefficient for problems with greater than 12 cells.

Banerjee and Zhou (1995) present a formulation of the LLDP as a specialization of the flow network based MFLP proposed by Montreuil (1990). The method as proposed by Montreuil (1990) is more complicated as the physical considerations of the cells are taken into account (Afentakis (1989) and related methods ignore the dimensional characteristics of a cell and its relationship
to the locations it is assigned to.) The cells are assumed to be rectangular and the dimensions are the decision variables.

Cheng, Gent, and Tosawa (1996) and Cheng and Gen (1998) extend Afentakis (1989) by applying a genetic algorithm with a modified mutation process to solve the LLDP by investigating its performance on both MIN-SUM and MIN-MAX congestion measures. A nearest neighbor local search is used to determine the best genes to mutate.

Tansel and Bilen (1998) present a solution to the LLDP by proposing a heuristic that applies positional moves and local improvement algorithms based on k-way interchanges or swaps between cells in a particular layout so as to determine the best layout for the LLMF.

Bennell, Potts, and Whitehead (2002) present a local search and a randomized insertion algorithm for the MIN-MAX LLDP. The proposed method is an extension of Leung (1992) that overcomes the implementation difficulties, computational requirements, and generates better solutions with respect to Leung (1992).

Bozer and Hsieh (2005) analyze the performance of a LCMHS with fixed windows. A stability factor (SF) for the LCMHS is derived by determining the maximum utilization of the loading stations along the LCMHS. The utilization at each loading station is characterized by the speed of the LCMHS, the arrival rate to the
loading stations, and the flow rate on the conveyor segment leading up to each loading station. The system is the stable if $S F<1$. A methodology is presented to estimate the WIP on the LCMHS. A proof is provided to show that minimizing the WIP on the LCMHS is equivalent to minimizing the distance traveled by the loads. Using this result, a methodology is presented to generate the optimal layout of stations around the LCMHS by minimizing only the WIP on the LCMHS with maximum value the $S F$ as a user defined constraint. Their research does not address the WIP at the loading station of the LCMHS.

Yang, Peters, and Tu (2005) propose a two-step heuristic procedure to solve the LLDP. The first step of the solution methodology determines the Layout as proposed by Montreuil (1990) to minimize the material handling costs by using a combined space filling curve and simulated annealing algorithm. Then, the output from the first step is used to solve the LLDP using a mixed integer programming formulation.

Chae and Peters (2006) propose a simulated annealing heuristic for the LLDP that build on an earlier method proposed by Das (1993). They apply an open field type layout method to generate a closed loop layout, thereby generating much better solutions in terms of minimizing material movement while maintaining layout modularity and structure.

Öncan and AltInel (2008) present two exact solution approaches for LLDP: a dynamic programming algorithm and a branch and bound scheme. They also present new upper and lower bound procedures for the QAP using the branch and bound scheme.

Ozcelik and Islier (2011) present a methodology for optimizing the number of loading and unloading stations while determining the layout the LLDP. However, the proposed methodology uses the traditional decision criterion for the objective function, i.e. aims to generate a layout that minimizes the total distance travelled.

### 2.2.2 Formulations with Minimum WIP design objective

There is extensive literature for the MFLP with the design objective of minimizing the material handling cost, the travel time in system, or the total distance traveled by the loads in the system. There are numerous literature review and survey papers as presented in $\S 2.1$ on page 16 on this subject matter. However, these traditional criteria for design can be poor predictors of the operational performance of a MF. The papers presented in this section are the few approaches that propose to solve the MFLP using the operational performance of a MF as the design criteria, this approach will be utilized by the proposed research.

Solberg and Nof (1980) present a mathematical model based on queueing network theory for the analysis of various Layout configurations for a MF. The method presented is not a MFLP but rather an attempt to explicitly develop an alternative design criterion for the MFLP.

Kouvelis and Kiran (1991a, 1991b) and Kouvelis et al. (1992) present the MFLP formulated as a QAP with the objective of minimizing the material handling cost and the WIP holding cost for a MF with AGV's as the MHS over single and multiple periods.

Fu and Kaku (1997a, 1997b) present a MFLP with the objective on minimizing the average WIP for the MF. The objective function is similar to that used in Kouvelis and Kiran (1991a, 1991b), i.e., minimizing the material handling cost and the WIP holding cost for a MF with $A G V^{\prime} s$ as the $M H S$ over a single period. They made numerous simplifying assumptions to model the queueing network as a Jackson network so as to obtain a closed form expression of the average WIP. They show that there is no difference between the traditional facility design objective and the tested objective that take the operational performance as the design criteria.

Benjaafar (2002) extends Fu and Kaku (1997a, 1997b) by relaxing several assumptions and using the queueing network analyzer as presented by Whitt (1983a). Benjaafar (2002) shows that when
some of the assumptions made by $F u$ and Kaku (1997a, 1997b) are relaxed, the claim of equivalent outcomes between the two formulations is not always valid. Benjaafar (2002) shows that under general conditions the layouts generated by the two formulations can be very different. The key difference between Benjaafar (2002) and Fu and Kaku (1997a, 1997b) is that as a result of using the QNA, Benjaafar (2002) is able to capture the interaction between the various systems in the MF that were absent in $F u$ and Kaku (1997a, 1997b). Raman et al. (2008) extend Benjaafar (2002) for $\mathrm{MF}^{\prime}$ s with unequal area cells.

Johnson, Carlo, Jimenez, Nazzal, and Lasrado (2009) present a greedy heuristic for determining the best set of shortcuts for a LLMF with a LCMHS.

Hong et al. (2011) extend Johnson et al. (2009) and present a methodology for determining the location of shortcuts for a LLMF with a LCMHS using WIP as the decision criterion.

### 2.3 Solution Methods

The various algorithms used to revolve MFLP formulated as a QAP can be categorized into: exact algorithms, heuristic algorithms, and meta-heuristic algorithms. As a result of the choice of design objective, i.e. generate a layout that minimizes the average WIP in the MF/LLMF, the exact and heuristic solution methods
cannot be used to solve the proposed LLDP as further discussed in § 3.3.1 on page 70.

Two recent review papers (Drira et al., 2007; Loiola et al., 2007) indicate that meta-heuristic approaches are the most popular solution methods. These methods are able to cope with large problem sizes and are able to effectively solve an optimal or near optimal solution. The proposed research will utilize the meta-heuristic approach to solve the LLDP formulated as a QAP, more specifically, genetic algorithms (GA) to solve the LLDP. However, for sake of completeness, a brief overview of other methods and algorithms used to solve the MFLP will be presented in the subsequent sections.

Exact solution algorithms are limited as a result of computational inefficiencies and computer memory issues. As discussed earlier, Foulds (1983) show that when using exact solution methods the computation time required to reach an optimal solution increases exponentially as the number of cells to be arranged increases. This outcome is reiterated by James, Rego, and Glover (2008) and Loiola, de Abreu, Boaventura-Netto, Hahn, and Querido (2007) who present detailed discussions on the computation complexity and the required computation time to reach an optimal solution using exact solution methods. This shortcoming of the exact algorithms has led to the development of many heuristic
approaches to solve the MFLP. With the development of sophisticated generally applicable meta-heuristic algorithms, the older problem specific heuristic algorithms have lost favor with practitioners.

### 2.3.1 Exact Algorithms

There are two types of exact solution algorithms used to determine the global optimum for the MFLP formulated as a QAP: branch and bound algorithms and cutting plane algorithms (Kusiak \& Heragu, 1987). In general, exact solution methods implement controlled enumeration as a means to obtain the optimal solution while not enumerating through all the possible solutions (including infeasible solutions) i.e. total enumeration. The examination of the lower bounds for the QAP is crucial to the development of efficient and expeditious controlled enumeration based exact solution methods. A good lower bound procedure will yield values close to the optimal value for the QAP (Loiola et al., 2007).

The branch and bound algorithm is the most commonly implemented and most researched exact solution algorithm. This algorithm is first presented independently by both Gilmore (1962) and Lawler (1963), the algorithms differ in the computation of the lower bound used to eliminate undesired solutions. The lower bound procedures as presented by Gilmore (1962) and Lawler
(1963) are the most popular procedures due to their simplicity and efficiency in terms of computational requirements. These lower bound procedures are limited in that for larger problems they provide weak lower bounds.

Bazaraa and Sherali (1980) present the cutting plane algorithm. This algorithm is computationally inefficient and requires a large amount of computer memory and works well only for small problem sizes.

### 2.3.2 Heuristics Algorithms

Problem specific heuristic algorithms have lost favor to more generally applicable meta-heuristic algorithms. The following discussion provides a brief overview of heuristic algorithms, more detailed description of the heuristic algorithms is provided by Kusiak and Heragu (1987). There are two broad categories of heuristic algorithms in the literature: Construction algorithms, and improvement algorithms.

In construction algorithms each cell is assigned to a location individually until the layout is obtained, i.e. the solution is constructed ab initio. Improvement algorithms begin with a randomly generated initial solution and try to improve it by systematic assigning cells to locations. The assignment yielding the best solution is retained and the process is repeated until
no further improvement is possible or a stopping criterion is met.

### 2.3.3 Meta-Heuristic Algorithms

Meta-heuristic algorithms have gained much traction since 1980 and have been applied to a wide variety of optimization problems. In general, meta-heuristic algorithms build on the theory and application of natural process to the resolution of the QAP by iterating until a stopping criterion is satisfied. A very important step for all these algorithms is parameter selection at the initialization of the algorithm. By effectively varying the parameters, convergence to poor local minima can be avoided. This feature makes meta-heuristic algorithms very attractive as they usually generate optimal or near optimal solutions for very complicated problems that cannot be solved by exact and heuristic algorithms.

This review will focus on the application of meta-heuristc algorithms to the MFLP/LLDP formulated as a QAP. Drira et al. (2007) and Singh and Sharma (2006) indicate that genetic algorithms are the most popular meta-heuristic algorithms used to solve the MFLP formulated as a QAP. The proposed research will implement a genetic algorithm based solution procedure to solve the LLDP. However, for completeness, other meta-heuristic algo-
rithms such as simulated annealing and Particle Swarm Optimization will be briefly discussed.

### 2.3.3.1 Genetic Algorithms

Genetic algorithm methodology (GA) is introduced by Holland (1975) and popularized by Goldberg (1989). Since its introduction, GA's have greatly influenced many solution procedures for complex optimization problems.

GA is a selection and optimization technique that solves an optimization problem by adopting the principles of natural selection and genetics to traverse through the search space to find the global optimal solution. There are two broad categories of GAs: discrete GAs and continuous GAs. The proposed research will implement a discrete GA; hence this review will focus on presenting a broad overview of discrete GAs and their applications to the QAP. There have been numerous applications of the GA to solve the FLP (Balakrishnan \& Cheng, 2000; Balakrishnan, Cheng, Conway, \& Lau, 2003; Benjaafar, 2002; Chan \& Tansri, 1994; Cheng \& Gen, 1998; Cheng et al., 1996; Cheng, Gent, \& Tozawa, 1995; El-Baz, 2004; Ficko, Brezocnik, \& Balic, 2004; Islier, 1998; Kochhar, Foster, \& $S$ Heragu, 1998; Lee, Han, \& Roh, 2003; Mak, Wong, \& Chan, 1998; Rajasekharan, Peters, \& Yang, 1998; Raman et al., 2008; Suresh, Vinod, \& Sahu, 1995; Tam, 1992; Tate \& Smith, 1995; Tavakkoli-Moghaddain \& Shayan, 1998;
M. Wang, Hu, \& Ku, 2005; Wu, Chu, Wang, \& Yan, 2007). In general, these methods follow the framework as presented in Figure 2.3; hence, to avoid redundancy, a general detailed overview of GA is presented.

The material discussed henceforth is from Haupt and Haupt (2004), unless stated otherwise. Figure 2.3 illustrates the general flowchart for $a$ GA. The cost function, or as it is sometimes referred to as the fitness function, is the function over which the GA attempts to solve the optimization problem. The cost function could be a mathematical function, an experiment, etc. There are several user defined parameters (in between 0 and 1) in the GA: the selection rate, the crossover rate, and the mutation rate. These parameters are introduced and described in the following description of the GA.

The proposed research uses the average WIP on the LLMF as the cost function. The GA begins by defining a chromosome as an array of the decision variable values to be optimized. For the FLP, the chromosome is represented by a string of values that indicate if a particular cell is at a particular location as described by the decision variable. Each chromosome is a unique Layout configuration of the MF i.e. candidate solution to the FLP.

The GA starts with an initial set of randomly generated chromosomes (initial solutions). Next, the cost for each chromosome is evaluated. At this stage, the idea of 'survival of the fittest' is applied, in that; the best solutions (chromosomes) are selected to be mated according to a selection rate.


Figure 2.3: Flowchart of a GA

From the set of selected chromosomes a predefined number of chromosomes (parents) are selected to be mated according to:
a) Pairing the best with the worst
b) Random pairing
c) Weighted random pairing: where the best chromosomes are assigned higher mating probabilities which give them the best likelihood of mating
d) Tournament selection: It mimics mating competition in nature; a small subset of two to three chromosomes is randomly selected. From this subset, the best chromosome is selected. The process is repeated until the required number of parents is reached.

Weighted random pairing and tournament selection are the most commonly used selection schemes used to determine the set of parents to be mated. The most common form of mating involves a pair of parents producing a pair of offspring. For each parent a crossover point is determined by multiplying the length of the chromosome (the number of characters / bits in the string of decision variables) by the crossover rate. In some mating / crossover schemes multiple crossover points are determined. Therefore, for each parent there could be two of more chromosomes ready for mating. The offspring generated have one or more parts of each parent's chromosome to form a new chromosome i.e. a new unique solution. This is one way in which the GA traverses through the problem space.

This operation is better illustrated with an example. Let P1 and P2 be the two parents with offspring O1 and O2. The chromo-
somes for each parent are $P 1=[111111]$ and $P 2=[000000]$. As it can be seen the length of the chromosome is 6 (as each chromosome characterized by 6 bits). In this case, the parent chromosome is split into two parts as determined by the crossover point that is derived by applying the crossover rate over the number of bits in the chromosome. If the crossover rate is 0.4 , the crossover point is at $0.4 * 6=2.4$ bits which is rounded down to 2 bits. The chromosomes for parents can be rewritten as $\mathrm{P} 1=[11$ 1111] and $P 2=[00$ 0000]. The offspring are given as follows $\mathrm{O} 1=[110000]$ and $\mathrm{O} 2=[001111]$.

Mutations alter a certain portion of the chromosome. Mutation is another operation by which the GA traverses through the problem space. As a result of mutation, the new population has traits not inherent to the original population. Hence, by introducing the mutation operation the GA is prevented from converging too quickly to a local solution prior to sampling the problem space. At this point an elitist methodology is recommended. The previous best solution is retained in memory, if none of the mutations improve upon this solution it is re-introduced into the population set. This method of keeping track of the best solution, i.e. the elitist methodology, inadvertently enables the GA to converge to the global optimal solution after a certain number of iterations. In the illustrated example, a mutation to
the offspring 02 could be $O 2=[101011]$ as indicated by the numbers that are bold and italic in 02 . The mutation is brought about by changing the 0 to 1 , and a 1 to 0 .

The next step is to check for the stopping criteria. If the stopping criterion is not met, the processes are repeated as shown in Figure 2.3 on page 37. In general, there are two stopping criteria most commonly used in the literature:
a) No statistically significant improvement in $X$ number of iterations
b) A certain number of iterations have been completed One may question whether the solution generated by the GA is the global optimal solution, or if there exists a proof of convergence for the GA. Holland (1975) presents a loose proof of convergence for the $G A$ called the schema theorem which a logical argument that states: by design the GA favors the best chromosomes and as a result of the selection process the GA will eventually converge to the global optimal solution. Greenhalgh and Marshall (2000) present $t(\delta)$ as a lower bound for the number of iterations (a large number) required to assure the GA converges to the global optimal solution with an associated probability $\delta$. Rudolph (2002) supports this claim and further adds that, "convergence to the global optimum is not an inherent property of the GA but rather is a consequence of the algorithmic trick of
keeping track of the best solution (the elitist methodology) found over time." Rudolph (2002) proves that if the mutation operation is unchanged the GA will have a chance of converging to the global optimal if and only if the selection operation is changed i.e. varied as the iterations progress. Rudolph (2002) also proves that the GA could possibly converge to the global optimal solution by the introduction of time variant, i.e. after a certain number of iterations, mutation, crossover, and selection rates. As with the other meta-heuristic approaches proper initial parameter selection can ensure the quality of the solution. De Jong (1975) presents the following observations on choice of initial parameters:
a) Small population sizes improve initial performance
b) Large population sizes improve long-term performance
c) High mutation rates are good for offline performance, where offline performance is the running average of the best cost solution found in each generation
d) Low mutation rates are good for online performance, where online performance is the running average of all cost solutions up to the current generation
e) Crossover rate should be around 0.60

### 2.3.3.2 Particle Swarm Optimization

Eberhart and Kennedy (1995) and Kennedy and Eberhart (1995) introduce particle swarm optimization (PSO). This algorithm is inspired by the flocking behavior of flocking animals. The PSO is similar to the GA; it begins with a randomly selected population of possible solutions referred to as particles. However, there are no evolutionary operations such crossover and mutation as in the case of the GA.

The PSO algorithm adjusts the trajectories of a population of "particles" through a problem space on the basis of information about each particle's previous best performance and the best previous performance of its neighbors (Kennedy \& Eberhart, 1995). The performance of the PSO algorithm is impacted by choice of the initial parameters as further discussed by Shi and Eberhart (1998). Kennedy and Eberhart (1997) present a discrete version of PSO where particles take on zero or one values.

### 2.3.3.3 Simulated Annealing

Simulated annealing is introduced by Kirkpatrick (1984). Burkard and Rendl (1984) present an application of simulated annealing for the QAP. This algorithm simulates the annealing of solids. The algorithm associates the objective function values of feasible solutions of the optimization problem to energy states of a physical system. In nature, a stable system is the system with
global minimum energy state. The simulated annealing algorithm attempts to simulate the process of attaining the global minimum of the specified problem. As in the physical world, a system moves to more stable if the energy of the current state is lower than the previous state, likewise in simulated annealing a new preferred solution is accepted if it improves on an existing solution. More specifically, a solution that is a neighboring solution to the current one is generated with a probability. This probability depends on the difference between the functions of the two solutions and a temperature; a gradually decreased parameter. This process is repeated iteratively until no further improvement is possible or a stopping criterion is reached. Several initial parameters must be specified as recommended by Laarhoven and Aarts (1987), the choice of which determines the quality of the solution.

### 2.3.3.4 Tabu Search Algorithm

Tabu search (TS) algorithm is introduced by Glover (1989, 1990). It is an evolutionary algorithm that maintains and updates a list (tabu list) of best solutions, each receiving a priority value, found via the search process. A methodology is presented to accept or reject new solutions in the neighborhood of older solutions based on the tabu list information and the priorities. In many ways, the $T S$ algorithm is a randomized local optimiza-
tion algorithm that iteratively traverses through the search space to find the global optimal solution by maintaining a tabu list of previously evaluated solutions.

### 2.4 Conveyor Analysis

Conveyor Systems have been studied over the last half century as a MHS in MF's with the combined purpose of transferring and storing manufacturing units (loads). This research will focus on MF's with LCMHS as the MHS i.e. a LCMHS. The LCMHS operates at a constant conveyor speed with fixed windows and no load recirculation. The loading and unloading stations to and from the LCMHS are assumed to have infinite capacity. Research papers that cover the load recirculation problem (Bastani, 1988; Bastani \& Elsayed, 1986; Hsieh \& Bozer, 2005; Pourbabai \& Sonderman, 1985; Schmidt \& Jackman, 2000; Sonderman, 1982) are not currently considered, however, future extensions of the proposed methodology will be explored to include the load recirculation problem.

Kwo (1958) is the first to analyze LCMHSs. He develops a deterministic model of loads traveling between two stations on a LCMHS. He proposes three intuitive yet fundamental principles to ensure the LCMHS operates satisfactorily: (1) The speed of the LCMHS must operate within its permissible range (speed rule); (2) The LCMHS must have enough capacity to meet the manufactur-
ing systems demands (capacity must have enough capacity to meet the manufacturing systems demands (capacity rule); (3) The LCMHS must be loaded and unloaded uniformly i.e. the number of loads loaded on the LCMHS must equal the number of loads unloaded from the LCMHS (uniformity principle). However, this paper does not present work on estimating performance measures for LCMHSs.

Kwo's work is analytically modeled by Muth (1972) for LCMHSs with continuous loads and by Muth (1974) for LCMHSs with discrete spaced loads. (Muth, 1974) presents an analytical model, for a system with deterministic flow rates, whose solution yields the stable operating conditions of LCMHSs (determines the minimum number of bins required) with one loading and one unloading station.

In Muth (1975), he extends his previous work for the case of multiple loading and unloading stations by solving a difference equation that reflects the dynamics of the multi-station system with deterministic flow rates.

Muth (1977) presents an analytical solution for the probability distribution of the material flow leaving the unloading station for a LCMHS with one loading and one unloading station is considered. The results show that the LCMHS reduces the random fluctuations in the input flow. This smoothing effect is quantified by a variance reduction factor which is the ratio of the
variances of output flow and input flow. However, this study is limited to systems with one loading and one unloading station.

Mayer (1960) presents the first probabilistic model of a LCMHS system with one loading and one unloading station that describe the functional aspect of transferring loads to and from a loading station while enabling the windows to hold multiple loads.

Morris (1962) extends Mayer's work to include multiple grouped loading stations followed by multiple grouped unloading stations. The separate grouping of loading and unloading stations is not very conducive to most real world settings.

Coffman Jr, Gelenbe, and Gilbert (1986) develop an analytical model of a LCMHS system with one loading and one unloading station with the aim of determining the optimal distance, in terms of number of windows, between the loading and unloading station on the conveyor. The solution is mathematically intense and can often lead to very complicated unsolvable expressions for the moment generating function for the number of windows. However, their work highlights the importance of the location of the loading and unloading stations that is often overlooked in both research and practice.

Pourbabai (1986) analyzes the effect of external variability of the flow rates on the performance of a LCMHS system with one loading, one unloading station, and recirculation of loads. The
production system is modeled as G/G/1/0 queuing system with retrials, stationary counting arrival process, generally distributed service times, and no waiting room. The flow of load within the manufacturing facility is recursively estimated using a renewal process. One of the key outcomes of this research is that a streamlined loading process aids in reducing the congestion on the MHS. Most of the loading stations at LCMHS's in modern manufacturing facilities have robots that have a deterministic service time which is less that the cycle time (the time it takes one window to pass) of the conveyor (Nazzal \& El-Nashar, 2007).

Atmaca (1994) analyzes the performance of a manufacturing system with unreliable machines and a LCMHS with fixed windows. An approximate method is presented that calculates the total time in system for the loads, and the WIP for the manufacturing system with a LCMHS with multiple loading and unloading stations. The system is decomposed into individual sections which are then analyzed in isolation. The loading stations and unloading stations to the conveyor are equipped with a queue hence there is no load recirculation or loads lost to the LCMHS system. It is the first work that approximates number in queue (WIP) and time in queue at the loading stations by modeling the loading stations as a G/G/1 queue.

Bozer and Hsieh (2004) propose an approximate method to estimate the waiting times at the loading stations in a LCMHS. The setup of loading and unloading stations is similar to that proposed by Atmaca (1994). Atmaca (1994) assumes adjacent windows on the conveyor are independent, however, the authors propose that a better estimate of the expected wait times at the loading stations can be achieved by considering correlated adjacent windows.

Nazzal, Johnson, Carlo, and Jimenez (2008) presented a model that approximates the $W I P$ on a LCMHS with multiple loading station and turntables. The LCMHS can be thought of as being 4 straight line conveyors in a rectangle each connected to the other by a turntable. This model is catered to semiconductor wafer fabs (Nazzal \& El-Nashar, 2007). The LCMHS is divided into segments, the WIP on each segment is calculated as prescribed by Bozer and Hsieh (2005) while the WIP at the turntables estimated by modeling the turntables as M/D/1 queue (Buzacott \& Shanthikumar, 1993).

Nazzal et al. (2010) extend Nazzal et al. (2008) by approximating the WIP on a LCMHS with shortcuts. The LCMHS is decomposed into sets of cells. Each set of cells is formed using adjacent and opposite cells. The WIP for each cell is then estimated using standard queueing procedures. The total WIP is

This chapter has presented a review of the literature dealing with the proposed research. The next chapter will present the research design.

## 3 RESEARCH DESIGN

The proposed methodology will aim to solve the LLDP for a LLMF with a LCMHS with shortcuts, using an operational performance metric, i.e. the work in process on the conveyor and the input stations in a manufacturing facility, as the minimizing function of the design criteria.

### 3.1 Conveyor Analysis

This section presents a queueing-based analytical model to estimate the expected work-in-process (WIP) and the associated delays of the jobs traveling on the LCMHS as presented in Nazzal et al. (2008) in two phases as described in $\$ 3.1 .1$ and $\S 3.1 .2$. The introduction of shortcuts across the LCMHS introduces some delays and congestion into the LLMF as presented in Nazzal et al. (2010) as described in $\$ 3.1 .3$. The value of the proposed model is that it would allow designers to quickly and accurately evaluate the expected performance of LCMHS. One may skip over $\S$ 3.1.2, if turntables are not considered in the design.

Figure 3.1 illustrates the LLMF. The system is composed of a unidirectional LCMHS with four $90^{\circ}$ turntables located at the corners, and $M$ cells. Each cell has an entry (exit) point to (from) it called the loading (unloading) station. It is assumed that no cell is located between the turntables on the shorter
sides of the LMCHS. The turntables are only activated when jobs need to (from) travel along the shorter sides of the conveyor.


Figure 3.1: The LLMF with shortcuts
It is assumed that the loading and unloading stations at each cell have infinite capacity and are never blocked. Jobs in the facility will have associated routes which define the sequence of tools (and cells) a job needs to visit for processing. A job that completes processing in a particular cell is placed in the associated unloading station and waits to be loaded onto the LCMHS. The demand is modeled by using a "From-To" matrix representing the average flow rate of moves between a pair of cells i.e. $\lambda_{i j}$.

The LCMHS is specified in terms of its speed and length. The length can be described in terms of "windows". A window is defined to hold at most one job provided that all jobs have the same dimensions and all windows are of equal size. The conveyor cycle time is the time required for the conveyor to move the length of one window. It is assumed that the LCMHS load/unload
time is constant and less than the conveyor cycle time and therefore the conveyor continues to move while loads are being loaded and unloaded from the load/unload stations.

The turntables are located at the points of intersection between various sections of the conveyor to change the load's traveling direction by 90 degrees. A turntable cycle consists of receiving a load, changing the load's direction, releasing the load, and returning to home position. The time to complete such cycle is assumed to be deterministic. It is also assumed that all turntables operate at the same speed.

It is important to note that if a shortcut is assigned after cell i, the flow of loads after the shortcut on the conveyor should be adjusted to reflect the amount of loads that are diverted on the shortcut i.

### 3.1.1 Phase I: The Traveling WIP on the Conveyor

Phase I analysis provides an estimate for the expected traveling WIP on the conveyor without considering any turntables as described in Bozer and Hsieh (2005). The conveyor travels at a constant speed; move requests follow a Poisson process; loading and unloading stations have unlimited capacity; and the conveyor is continuous with no turning delays (i.e. no turntables).

Consider that the conveyor is a series of nodes with a set of segments ( $S$ ) connecting two nodes to form a network of nodes.

The turntable, loading station for cell 1, the unloading station for cell 1, the loading station for cell 2 , the unloading station for cell 2, etc. are nodes, and only the sections of conveyor between adjacent nodes form the set of segments (S).

As defined earlier, a window (Y) is the length of a conveyor defined to hold at most one job. Therefore, for a segment i with length $d_{i}$, the number of windows $\left(w_{i}\right)$ is given by

$$
\begin{equation*}
w_{i}=\frac{d_{i}}{\Upsilon} . \tag{8}
\end{equation*}
$$

Let $\alpha_{i}$ be the average number of loads per time unit on segment $i$ and $s$ be the distance based speed of the conveyor. The window based speed of the conveyor ( $v$ ) with respect to the window size in terms of windows per time unit is given by

$$
\begin{equation*}
v=\frac{s}{\Upsilon} . \tag{9}
\end{equation*}
$$

This representation of the window speed of the conveyor is general as it account for non-unity window sizes. As long as the conveyor system is stable as described in Bozer and Hsieh (2004); the probability that segment $i$ is occupied ( $q_{i}$ ) is given by

$$
\begin{equation*}
q_{i}=\frac{\alpha_{i}}{v} . \tag{10}
\end{equation*}
$$

The expected traveling WIP ( $W I P_{P I}$ ) on the conveyor is given by

$$
\begin{equation*}
W I P_{P I}=\sum_{i \in S} w_{i} q_{i} . \tag{11}
\end{equation*}
$$

### 3.1.2 Phase II: WIP at the Turntables

In Phase II the turntables are analyzed in pairs by selecting the two corner turntables located at the same side of the conveyor. For each pair of turntables the downstream turntable will never have loads waiting in queue because both turntables have deterministic turning time and are synchronized.


Figure 3.2: Types of Turntables
Queueing effects are only observed in the upstream turntable. Since it is assumed that jobs arrive according to a Poisson process, and the turning time is deterministic, the corner upstream turntable can be analyzed as an $M / D / 1 / b$ system, where $b$ is the number of windows separating the upstream turntable and the last unloading station before the turntable.

Let $\lambda_{C}$ be the arrival rate of loads to the corner turntable, and $t$ be the turning time of the turntable. Buzacott and Shanthikumar (1993) provide a thorough discussion of analyzing general blocking queues. The following approximation, which is
also discussed by Hopp and Spearman (2000) is used to describe the expected WIP at the upstream turntable ( $W I P_{U}$ ) which is given by :

$$
\begin{equation*}
W I P_{U}=\left(\frac{1}{2}\right)\left(\frac{\lambda_{c}^{2} t^{2}}{1-\lambda_{c} t}\right)+\lambda_{c} t . \tag{12}
\end{equation*}
$$

Equation (12) assumes that, on average, the turntable queue does not extend to block the pick-up station immediately upstream of the turntable which is considered as the stability condition. Details on verifying this stability condition are provided in Nazzal et al. (2008).

The expected WIP at the downstream turntable ( $W I P_{D}$ ) would be its utilization and is given by

$$
\begin{equation*}
W I P_{D}=\lambda_{c} t . \tag{13}
\end{equation*}
$$

Let $\lambda_{r c}$ be the arrival rate of loads to the right corner turntable, and $\lambda_{l c}$ be the arrival rate of loads to the left corner turntable. Therefore, the total WIP at the turntables (WIP ${ }_{I I}$ ) on the conveyor is given by

$$
\begin{equation*}
W I P_{P I I}=\left[\left(\frac{1}{2}\right)\left(\frac{\left(\lambda_{r c} t\right)^{2}}{1-\lambda_{r c} t}\right)+2 \lambda_{r c} t\right]+\left[\left(\frac{1}{2}\right)\left(\frac{\left(\lambda_{l c} t\right)^{2}}{1-\lambda_{l c} t}\right)+2 \lambda_{l c} t\right] . \tag{14}
\end{equation*}
$$

### 3.1.3 Phase III: WIP on the Shortcuts

In Phase III, the expected waiting delays and WIP resulting from shortcuts are incorporated. Consider the four stockers $p, q$, r, and $s$ from Figure 3.3, and the shortcut turntables $e, f, g$, and h. A cell in this analysis is determined by four stockers and the insertion of two shortcuts, one in each direction. The reference for the cell is arbitrarily given to the lower left stocker, stocker $p$ in this example. For any balanced system with $N$ bays there will be a maximum of $B-1$ cells as shown in Figure 3.4.


Figure 3.3: Cell p


Figure 3.4: Cells in the LLMHS

The congestion caused by introducing shortcut eh and/or shortcut $g f$ in cell ' $p$ ' is now modeled. This is done by computing the average delays due to turntables. Let, $T_{e}, T_{g}, T_{f}$, and $T_{h}$ be the expected delay at the queues that form due to turntables $e, g, f$, and $h$, respectively. It is assumed that the rate at which loads are picked off the CFT at stockers $s$ and $q$ is greater than the speed of the CFT, and therefore, no queue will form before either stocker. This assumption is consistent with the conveyorbased tool-to-tool model from SEMATECH (2002) as loads are removed from (moved to) the conveyor before being loaded (unloaded). In the SEMATECH Model, FOUPS are delayed due to loading and unloading at the stocker, without impacting the conveyor.

Further, no queue will form on shortcuts eh and $g f$ for two reasons: 1) The deterministic and identical turning time of the turntables will ensure that the interarrival time of loads to segments $g f$ and eh is always larger than the turning time of turntables $f$ and $h$, respectively; 2) Higher priority at turntables $f$ and $h$ is given to the loads coming off shortcuts $g f$ and eh, respectively.

The expressions to derive the mean arrival rate of loads on the shortcuts is first presented, namely $\lambda_{e h}$ and $\lambda_{g f}$, and on other segments within a cell, namely $\lambda_{\text {ef }}$ and $\lambda_{g h}$ given the from-to matrix of move requests. These expressions are necessary before
deriving the analytical model for estimating the average delays and WIP caused by turntables $e$ and $g$, and the model that estimates the average delays and WIP caused by turntables $f$ and $h$.

### 3.1.3.1 Estimating the mean arrival rates of loads

### 3.1.3.1.1 Arrival rates of loads to shortcuts

It is assumed that turning loads arrive at turntables $g$ and $e$ according to a Poisson Process with arrival rate $\lambda_{\text {eh }}$ and $\lambda_{g f}$ respectively. $\lambda_{\text {ef }}$ and $\lambda_{g h}$ are estimated as the average number of loads per time that will require travel on, respectively, shortcuts $g f$ and eh to take the shortest distance path from their origin stocker to their destination stocker. $\lambda_{\text {eh }}$ values can be obtained by observing that the loads traveling on shortcut eh are those that originate from stockers upstream of turntable e for delivery to those downstream of turntable $h$ minus the loads that would be carried on all the preceding cell shortcuts that have the same direction as eh.

$$
\begin{equation*}
\lambda_{e h}=\sum_{i=s+1}^{p} \sum_{j=s}^{i-1} \alpha_{i j}-\sum_{k l \in U_{c h}} \lambda_{k l} y_{k l} . \tag{15}
\end{equation*}
$$

Similarly, values can be obtained by observing that the loads traveling on shortcut $g f$ are those that originate from stockers upstream of turntable $g$ for delivery to those downstream of turntable $f$ minus the loads that would be carried on all the preceding cell shortcuts that have the same direction as $g f$.

$$
\begin{equation*}
\lambda_{g f}=\sum_{i=q+1}^{r} \sum_{j=q}^{i-1} \alpha_{i j}-\sum_{k l \in U_{s f}} \lambda_{k l} y_{k l} . \tag{16}
\end{equation*}
$$

Where $\alpha_{i j}$ is the average rate of loads traveling from stocker i to stocker $j$, stocker $N+1$ is stocker 1, and, and $U_{g f}\left(U_{e h}\right)$ is the set of shortcuts upstream of shortcuts $g f$ (eh) and in the same direction. $y_{k l}$ is an indicator variable that shortcut $k l$ is installed $\left(y_{k 1}=1\right)$, or not $\left(y_{k 1}=0\right)$. Equations (15) and (16) are executed sequentially; equation (15) should be executed starting at cell 1 followed by cell 2 and so forth up to cell B-1. Equation (16) should be executed in the opposite direction; starting at cell B-1 and moving backwards down to cell 1.

### 3.1.3.1.2 Arrival rates of loads to segments between shortcuts

It is assumed that passing loads arrive at turntables $e$ and $g$ according to a Poisson process with arrival rates $\lambda_{e h}$ and $\lambda_{g f}$ respectively. $\lambda_{\text {eh }}$ are estimated as the average number of loads per time that will travel from stockers $s, s+1, \ldots, p$ to stockers $q$, $q+1, \ldots, r . A l s o$, if shortcut $g f$ was not installed- all the loads that would have traveled on shortcut $g f$.

$$
\begin{equation*}
\lambda_{e f}=\sum_{i=s}^{p} \sum_{j=q}^{r} \alpha_{i j}+\lambda_{g f}\left(1-y_{g f}\right) . \tag{17}
\end{equation*}
$$

Similarly, arrival rates $\lambda_{g h}$ are determined by estimating the average number of loads per time that will travel from stockers $q$, $q+1, \ldots, r$ to stockers $s, s+1, \ldots, \underset{59}{p}$. Also, if shortcut eh was not
installed - all the loads that would have traveled on shortcut eh.

$$
\begin{equation*}
\lambda_{g h}=\sum_{i=q}^{r} \sum_{j=s}^{p} \alpha_{i j}+\lambda_{e h}\left(1-y_{e h}\right) \tag{18}
\end{equation*}
$$

### 3.1.3.2 Estimating the average WIP at input turntable of a cell

The congestion delays on segments rg and pe can be modeled as a single-server queue with two types of customers: turning loads and passing loads. The time for turning loads to be "served" at the turntable is modeled as a deterministic delay with mean $t$. Deterministic turning time is a reasonable assumption in a highly automated system and has been verified through consultation with industry collaborators. Passing loads require "no service" at a turntable but must wait to pass until there are no turning loads in front of them.

For turntable $e$, consider an $M / D / l$ queue with arrival rate $\left(\lambda_{p e}\right.$ $\left.=\lambda_{e h}+\lambda_{e f}\right)$ and service time distribution:

$$
\begin{gather*}
\qquad S=\left\{\begin{array}{ll}
t & \text { for a turning load } \\
0 & \text { for a passing load }
\end{array} .\right.  \tag{19}\\
E(S)=E(S \mid \text { load is serviced }) \operatorname{Pr}(\text { load is serviced }) \\
+E(S \mid \text { load is passing }) \operatorname{Pr}(\text { load is passing }) \\
=t \cdot \frac{\lambda_{e h}}{\lambda_{p e}}+0 \cdot \frac{\lambda_{e f}}{\lambda_{p e}} \tag{20}
\end{gather*}
$$

Where $\lambda_{e h} / \lambda_{p e}$ is the steady-state probability that a load arriving at turntable e will turn to go on shortcut eh, $t$ is the time for the turntable to rotate the load 90 degrees, wait for the load to get off the turntable, and turn back 90 degrees to the original position. The variance of $t$ is zero, because turning times are deterministic.

By the Pollaczek-Khintchine formula (Khintchine, 1932; Pollaczek, 1930), the expected WIP, $L_{e}$, due to turntable e, is given by:

$$
\begin{align*}
L_{e} & =\frac{\lambda_{p e}{ }^{2} E\left(S^{2}\right)}{2\left(1-\lambda_{p e} E(S)\right)}+\lambda_{p e} E(S)  \tag{21}\\
& =\frac{\lambda_{p e} \lambda_{e h} t^{2}}{2\left(1-\lambda_{e h} t\right)}+\lambda_{e h} t
\end{align*}
$$

The analysis of turntable $g$ will be identical after replacing pe, ef, and eh in equations (28)-(31) with rg, gh, and $g f$, respectively.

### 3.1.3.3 Estimating the average delays at the exit turntable of a cell

Loads traveling on segments ef and gh are passing loads that will get delayed by the loads coming from shortcuts $g f$ and eh, respectively. Because the turning time of all turntables is deterministic, the minimum interarrival time to turntables $f$ and $h$ from the shortcut (by the turning loads) is $t$, the turning de-
lay. Therefore, the passing loads on segments ef and gh will wait between 0 and $t$ depending on the probability of finding the turntable occupied by a turning load (utilization of the turntable) and the remaining turning time for the load blocking their way. The average remaining service time, $E\left(t_{r}\right)$, of a turning load as seen by a randomly arriving passing load is given by (Kleinrock, 1975):

$$
\begin{equation*}
E\left(t_{r}\right)=\frac{t\left(c_{s}^{2}+1\right)}{2} \tag{22}
\end{equation*}
$$

Where, $c_{s}{ }^{2}$ is the coefficient of variation of turning time. Since turning times are deterministic, $c_{s}{ }^{2}=0$ and thus, $E\left(t_{r}\right)=t / 2$. The expected service (busy) time of turntable $f$, is the proportion of loads that turn multiplied by the turning time. Therefore, the expected delay caused by turntable $f$ is given by:

$$
\begin{align*}
T_{f} & =u_{f} \frac{t}{2}+\frac{\lambda_{g f}}{\lambda_{e f}+\lambda_{g f}} t \\
& =\frac{\lambda_{g f} t^{2}}{2}+\frac{\lambda_{g f}}{\lambda_{e f}+\lambda_{g f}} t \tag{23}
\end{align*}
$$

The first term in expression (9) is the remaining turning time as seen by a load arriving from segment ef. The second term is the expected busy time of turntable $f . U_{f}$ is the utilizations of turntable $f$. Therefore, using Little's law, the expected WIP due to turntable $f$ is given by:

$$
\begin{align*}
L_{f} & =\lambda_{g f} \frac{\lambda_{g f} t^{2}}{2}+u_{f}  \tag{24}\\
& =\frac{\lambda_{g f}^{2} t^{2}}{2}+\lambda_{g f} t
\end{align*}
$$

The analysis of turntable $h$ to estimate $T_{g}$ and $L_{g}$ will be identical after replacing subscripts $g f, e f$, and $f$, in equations and (24) with eh, gh, and $g$, respectively.

### 3.1.4 WIP on the Conveyor

From equation (11) and equation (14) the estimated WIP on the conveyor (WIP ${ }_{\text {CoNV }}$ ) is given by

$$
\begin{align*}
& E\left(W I P_{C O N V}\right)=\underbrace{\sum_{i \in S} w_{i} q_{i}}_{\substack{\text { Phase l: } \\
\text { traveling WIP }}}+\underbrace{\left(\frac{1}{2}\right)\left(\frac{\left(\lambda_{r c} t\right)^{2}}{1-\lambda_{r c} t}\right)+2 \lambda_{r c} t}_{\begin{array}{c}
\text { Phase II: } \\
\text { two righ orner turntables }
\end{array}}+\underbrace{\left(\frac{1}{2}\right)\left(\frac{\left(\lambda_{l c} t\right)^{2}}{1-\lambda_{l c} t}\right)+2 \lambda_{l c} t}_{\begin{array}{c}
\text { Phase II: } \\
\text { two left corner turntables }
\end{array}}  \tag{25}\\
& +\underbrace{\sum_{\forall(p, e, f, g) \in M-1} L_{e} y_{e h}+L_{g} y_{g f}+L_{f} y_{g f}+L_{h} y_{e h}}_{\text {accumulated WIP due to turntables } e, g, f, \text {, in each cell }}
\end{align*}
$$

### 3.1.5 Stability Condition for LLMF

For a LCMHS, the utilization is given by

$$
\begin{equation*}
\rho_{\text {LCMHS }}=\max _{i}\left[\frac{\lambda_{i}+\alpha_{i}}{v}\right] \tag{26}
\end{equation*}
$$

As long as $\rho_{\text {LCMHS }}<1$, the LLMF is stable.

### 3.2 Input Station Analysis

### 3.2.1 Previous Models of WIP at the Input (Loading) Stations

### 3.2.1.1 Method of Atmaca (1994)

For each cell i, the WIP at the input stations is given by

$$
\begin{equation*}
E\left(W I P_{I N P}\right)_{i}=\frac{\left(v-\alpha_{i}\right)\left(v-q_{i} \alpha_{i}+2 \alpha_{i}\right)}{2 v^{2}\left(1-q_{i}\right)\left(v-\alpha_{i}-\lambda_{i}\right)} \tag{27}
\end{equation*}
$$

### 3.2.1.2 Method of Bozer and Hsieh (2004)

For each cell i, let $\gamma_{i}$ represent the event that the queue at loading station is empty, therefore $P\left(\gamma_{i}\right)$ is given by

$$
\begin{equation*}
P\left(\gamma_{i}\right)=\frac{\lambda_{i}}{v-\alpha_{i}} \tag{28}
\end{equation*}
$$

Let $a_{i}$ be the adjusted probability that segment $i$ is occupied taking into account the correlation between the status of adjacent windows, $a_{i}$ is given by

$$
\begin{equation*}
a_{i}=\frac{\bar{a}_{i}}{q_{i}} \tag{29}
\end{equation*}
$$

where

$$
\begin{align*}
\bar{a}_{i+1}= & \bar{a}_{i}+\left(q_{i}-\bar{a}_{i}\right)\left\{P\left(\gamma_{i}\right)+\left(1-P\left(\gamma_{i}\right)\right) F_{i}(1 / v)\right\} \\
& +\left(q_{i}-\bar{a}_{i}\right) P\left(\gamma_{i}\right)  \tag{30}\\
& +\left(\bar{a}_{i}-2 q_{i}+1\right)\left\{P\left(\gamma_{i}\right)-\left(1-P\left(\gamma_{i}\right)\right) F_{i}(1 / v)\right\}
\end{align*}
$$

and, $F_{i}$ is exponentially distributed with rate $\lambda_{i}$. Bozer and Hsieh (2004) utilize the tagged load approach to estimate
 stations with single robots. For each cell $i$, the expected WIP at the loading station is given by

$$
\begin{equation*}
E\left(W I P_{I N P}\right)_{i}=\frac{\left(v-\alpha_{i}\right)\left(v-a_{i} \alpha_{i}+2 \alpha_{i}\right)}{2 v^{2}\left(1-a_{i}\right)\left(v-\alpha_{i}-\lambda_{i}\right)} \tag{31}
\end{equation*}
$$

### 3.2.2 Proposed Methodology for WIP at Input Stations

The proposed methodology models the loading station as a M/G/1 queue. In general, the service time is the amount of time the load waits at the front of the queue, i.e. the head of the line (HOL), before it is loaded on the conveyor. It is assumed that the time the robot takes to transfer the load to the conveyor is negligible in comparison to the conveyor cycle time; defined as the time to move one window. Each load at the loading station will be served for either a Type 1 or a Type 2 service distribution.

### 3.2.2.1 Type 1 Service Distribution

This type of service time is when the load arrives to an empty input station queue

- Event 1: The load waits for the residual conveyor cycle time
- The Uniform Distribution with the range $[0,1 / v]$ is used to model event 1
- Event 2: The load waits for the first unoccupied window
- The Geometric distribution with probability of success 1 - $\phi_{i}\left(\phi_{i}\right.$ further discussed in $\$ 3.2 .2 .4$ on page 68) is used to model the expected number of windows till the first empty window. This multiplied by the conveyor cycle time is used to model event 2

Both the events are assumed to be independent of each other For each cell i, the expected service time for service type 1, $E\left(S T 1_{i}\right)$, is given by

$$
\begin{equation*}
E\left[S T 1_{i}\right]=\frac{1}{2 v}+\frac{\phi_{i}}{1-\phi_{i}} \cdot \frac{1}{v} \tag{32}
\end{equation*}
$$

For each cell i, the variance for service type 1, $\operatorname{Var}\left(S T 1_{i}\right)$, is given by

$$
\begin{equation*}
\operatorname{Var}\left[S T 1_{i}\right]=\frac{1}{12 v^{2}}+\frac{\phi_{i}}{\left(1-\phi_{i}\right)^{2}} \cdot \frac{1}{v^{2}} \tag{33}
\end{equation*}
$$

### 3.2.2.2 Type 2 Service Distribution

This type of service time is when the load arrives to a nonempty input station queue

- Event 1: The load waits for the first unoccupied window
- The Geometric distribution with probability $\phi_{i}$ multiplied by the cycle time is used to model event 1

For each cell i, the expected service time for service type 2 , $E\left(S T 2_{i}\right)$, is given by

$$
\begin{equation*}
E\left[S T 2_{i}\right]=\frac{\phi_{i}}{1-\phi_{i}} \cdot \frac{1}{v} \tag{34}
\end{equation*}
$$

For each cell i, the variance for service type 2, $\operatorname{Var}\left(S T 2_{i}\right)$, is given by

$$
\begin{equation*}
\operatorname{Var}\left[S T 2_{i}\right]=\frac{\phi_{i}}{\left(1-\phi_{i}\right)^{2}} \cdot \frac{1}{v^{2}} \tag{35}
\end{equation*}
$$

### 3.2.2.3 Expected WIP at input stations

For each cell $i$, the WIP at the input stations as per Welch (1964) is given by

$$
\begin{align*}
E(W I P)_{i}= & \frac{\lambda_{i} E\left[S T 2_{i}\right]}{1-\lambda_{i}\left[E\left[S T 2_{i}\right]-E\left[S T 1_{i}\right]\right]} \\
& +\frac{\lambda_{i}^{2}\left[\operatorname{Var}\left[S T 1_{i}\right]+E\left[S T 1_{i}\right]^{2}-\left(\operatorname{Var}\left[S T 2_{i}\right]+E\left[S T 2_{i}\right]^{2}\right)\right]}{2\left\{1-\lambda_{i}\left[E\left[S T 2_{i}\right]-E\left[S T 1_{i}\right]\right]\right\}}  \tag{36}\\
& +\frac{\lambda_{i}^{2}\left[\operatorname{Var}\left[S T 2_{i}\right]+E\left[S T 2_{i}\right]^{2}\right]}{2\left\{1-\lambda_{i} E\left[S T 2_{i}\right]\right\}}
\end{align*}
$$

Substituting equations (32)-(35) in equation (36), we get

$$
\begin{equation*}
E\left(W I P_{I N P}\right)_{i}=\frac{2 \lambda_{i} \phi_{i}}{\left(2 v+\lambda_{i}\right)\left(1-\phi_{i}\right)}+\frac{\lambda_{i}^{2}\left(1+\phi_{i}-2 \phi_{i}^{2}\right)}{3 v\left(2 v+\lambda_{i}\right)\left(1-\phi_{i}\right)^{2}}+\frac{\lambda_{i}^{2}\left(\phi_{i}+\phi_{i}^{2}\right)}{2 v\left[v-\phi_{i}\left(v+\lambda_{i}\right)\right]\left(1-\phi_{i}\right)} \tag{37}
\end{equation*}
$$

### 3.2.2.4 A note on the adjusted probability

The adjusted probability $\phi_{i}$ is the probability that a load arriving to the input station in segment i sees an occupied window. $\phi_{i}$ is developed using numerical experiments, in a manner similar to which the G/G/1 approximation, as presented by Kraemer and Langenbach-Belz (1976) and reported by Shanthikumar and Buzacott (1980), was developed.

It is observed that using the probability that the segment was occupied, i.e. $q_{i}$, as the probability of success for the Geometric distribution underestimated the number of Bernoulli trials until the first success. It is also observed that under high utilization, the adjustment required to $q_{i}$ is minimal, whereas under low utilization the adjustment to $q_{i}$ is significant. Intuitively, under high utilization, since the conveyor is almost completely occupied $q_{i}$ approaches $\phi_{i}$, and theoretically at a utilization of $1, q_{i}=\phi_{i}$. With this in mind, for each cell i, a simple metric for $\phi_{i}$ is given by

$$
\begin{equation*}
\phi_{i}=q_{i}\left(2-\rho_{i}\right) \tag{38}
\end{equation*}
$$

Where, the utilization for each cell i is given by

$$
\begin{equation*}
\rho_{i}=\frac{\lambda_{i}+\alpha_{i}}{v} \tag{39}
\end{equation*}
$$

As it can be seen, equation (38) satisfies all the observances described above: under low utilizations the adjustment factor is significant, under high utilizations the adjustment factor is minimal, and when $\rho_{i}$ is $1, q_{i}=\phi_{i}$.

### 3.2.3 Total WIP at the Input stations

For the LCMHS, given $E\left(W I P_{\text {INP }}\right)_{i}$, the total $W I P E\left(W I P_{I N P}\right)$ at the input stations is given by

$$
\begin{equation*}
E\left(W I P_{I N P}\right)=\sum_{i=1}^{M} E\left(W I P_{I N P}\right)_{i} \tag{40}
\end{equation*}
$$

### 3.3 Optimization Model

If the total WIP is used as the objective function of the LLDP, there is no penalty for adding shortcuts to the LLMF since adding shortcuts always reduces the $W I P$ on the LLMF. Hence, the total cost function is used as the objective function of the LLDP as the total cost function enables the penalization of adding shortcuts to the LLMF. The total cost function is given by

$$
\begin{equation*}
Z=C_{W I P}\left[E\left(W I P_{I N P}\right)+E\left(W I P_{C O N V}\right)\right]+C_{s c} \cdot \# \text { Shortcuts } \tag{41}
\end{equation*}
$$

Let $\Omega$ be the ratio of the cost of installing the shortcut to the cost of a single unit of production. The effective cost per production unit is given by Hong et al. (2011) as follows

$$
\begin{equation*}
x=E\left(W I P_{I N P}\right)+E\left(W I P_{\text {CONV }}\right)+\Omega \cdot \# \text { Shortcuts } \tag{42}
\end{equation*}
$$

This method is employed to bypass the issue of determining the price of a unit of production and the price of installing a shortcut.

For a LLMF, the LLDP with a LCMHS is presented below using the formulation by permutations: the objective function as shown in equation (43) represents the total cost in the system for a permutation $\pi$. Equation (44) is included to ensure only feasible permutations if the LLMF are considered to solve the LLDP.

$$
\begin{array}{ll}
\operatorname{Min}_{\pi \in S_{N}} & C_{\text {WIP }}\left[E\left(\text { WIP }_{I N P}\right)+E\left(\text { WIP }_{\text {CONV }}\right)\right]+C_{s c} \cdot \# \text { Shortcuts }\left.\right|_{\pi} \\
\text { s.t. } & \rho_{\text {LCMHS }_{\pi}}<1 \tag{44}
\end{array}
$$

### 3.3.1 The case for the use of genetic algorithms

Exact solution and heuristic methods cannot be used to solve the LLDP as presented. The lower bound techniques used to efficiently eliminate solutions by selective enumeration are invalid as they are built on the assumption that all the objective coeffi-

```
cients are known and unchanging. The coefficients of the objec-
tive function as presented in equation (43) are not known and
vary stochastically at each iteration, as a result of the proce-
dure used to estimate the WIP as presented in s 3. Therefore,
the GA solution procedure is used to determine the near optimal
(since there is no definite proof for convergence) solutions for
the LLDP. § 4 will present the implementation of the proposed
research design as described in § 3.
```


## 4 SOLUTION ALGORITHM FOR THE LLDP

The section discusses in some detail the implementation of the proposed research. The majority of the section discusses the solution algorithm for the LLDP.

The goals of this implementation are to highlight the benefit of using the WIP as opposed to distance traveled as the design criterion for the LLDP, and to also highlight the benefit of combining the determination of the Layout and the determination of the shortcuts into a single step LLDP as opposed to the twostep process as discussed previously.

A genetic algorithm (GA) is used to solve the LLDP as described in equation (43) and equation (44). Each permutation $\pi$ represents a unique layout. In essence, for each permutation $\pi$, the greedy heuristic as described by Johnson et al. (2009) is used to determine the number of shortcuts. In this manner, the fitness value (equation (43)) for each and every permutation $\pi$ reflects the benefit (if any) of including the shortcuts. The method to pick the best set of shortcuts is discussed in great detail in $\$ 4.2 .3$ on page 83. As a result, the GA returns the solution that reflects the lowest WIP while considering shortcuts. Traditionally, one would first run a solution algorithm to determine the best layout, and then one would run another solution algorithm to determine the best set of shortcuts.

Thereby, the benefits of the shortcuts are only seen for the best layout. However, in the proposed methodology the benefits of the shortcuts are seen for every layout encountered, thereby guaranteeing an equivalent or better solution as compared to the traditional method.

### 4.1 Encoding the Chromosomes

### 4.1.1 Encoding the Cells: cell chromosomes

Haupt and Haupt (2004) is used as a reference for this following discussion. Consider the facility below:


Figure 4.1: Illustrative Facility

There are four locations ( $N=4$ ) and four machines ( $M=4$ ). In the case as shown in Figure 4.1: machine 1 is in location 1 , machine 2 is in location 2, etc. To generalize, each location is fixed while the cells are assigned to different locations. In terms of problem representation, the chromosomes will be encoded in a
similar manner. The choice of the numbering of the locations and cells is arbitrary and selected by the practitioner.

$$
\text { cell chromosome }=\underbrace{m_{1}}_{1} \underbrace{m_{2}}_{2} \underbrace{m_{3}}_{3} \cdots \underbrace{m_{M}}_{N}=\left[m_{1} m_{2} m_{3} \ldots m_{M}\right]
$$

Here, $m_{i}$ indicates a specific cell i represented by a floatingpoint number assign to a specific location (1,2,...,N). The general cell chromosome would read as follows: cell 1 is assigned to location 1, cell 2 is assigned to location 2, etc. Coming back to the illustrative problem, the cell chromosome for the Layout as depicted in Figure 3.1 is [1234].


Figure 4.2: Alternate illustrative Facility
Likewise, the cell chromosome for the facility as shown in Figure 4.2 is [2341]. Hence, it can be seen that the reordering the numbers in a cell chromosome will result in different layouts. For the problem as depicted by Figure 4.1 and Figure 4.2, each cell $i$ is represented by a single bit as $N$ is a single bit. To further generalize, the number of bits for each cell should be derived from the number of bits required to represent $N$. Table
4.1 illustrates the number of bits required to encode each cell with respect to N .

Table 4.1: Number of bits required for different N's

| N | Bits |
| :--- | :--- |
| $1-9$ | 1 |
| $10-99$ | 2 |
| $100-999$ | 3 |
| $1000-9999$ | 4 |
| $\vdots$ | $\vdots$ |

To further illustrate this, consider the facility in the Figure 3.3, machine 1 is in location 1, machine 2 is in location 2, etc. N is in between 10 and 99, therefore two bits will be required to encode each machine.


Figure 4.3: Alternate illustrative Facility

The cell chromosome for the facility in Figure 4.3 is

$$
\text { Chromosome }=[010203040506070809101112]
$$

Likewise, for Figure 4.4 the cell chromosome is [090207060504030801121110]


Figure 4.4: Alternate illustrative Facility

### 4.1.2 Encoding the Shortcuts: shortcut chromosomes

If a shortcut is assigned after a cell i then it will be encoded as 1, else 0. Consider the facility below


Figure 4.5: Illustrative Facility with shortcuts
As illustrated by Figure 4.5, there is a shortcut after cell 1, cell 2, and cell 4. There is no shortcut after cell 3. Therefore, the shortcut chromosome for this Layout can be encoded as follows: [1101]. It is important to note that if a cell is the last cell on its side of the conveyor in the direction of flow, then a shortcut is always placed after that cell (the short wall of the conveyor that connects the two sides.)

### 4.1.3 Encoding a Layout or permutation $\pi$

Combining the method for encoding the cells and the shortcuts, the Layout and shortcut configuration as shown Figure 4.5 can be represented as: [1234][1101]. The first part represents the chromosome for the cells henceforth referred to as the cell chromosome, while the second part represents the chromosome for the shortcuts henceforth referred to as the shortcut chromosome, and both together represent the chromosome for the permutation $\pi$. The method to generate the chromosome for the cell is described in § 4.2.2 on page 83. The method to generate chromosome for the shortcuts is described in $\$ 4.2 .3$ on page 83. This particular configuration will yield its corresponding WIP which will be used as the fitness function for the GA.

### 4.2 High Level Solution Algorithm

The flowchart of the solution algorithm is presented in Figure 4.6. Each sub task is presented subsequently in their respective sections.

In essence, the GA is initialized after which an initial population of cell chromosomes is generated. Next, the fitness value for the permutation $\Pi$ as given by equation (42) is computed. For each permutation $\Pi$, there is a set of shortcuts as represented by the shortcut chromosome that minimizes the WIP for the re-
spective cell chromosome. In this way, the proposed methodology improves on the traditional two-step process of the Layout by finding the best set of shortcuts at each iteration for every Layout arrangement (cell chromosome) visited.


Figure 4.6: Flowchart of Solution Algorithm
After the fitness value is computed for all the permutations, the population is ordered from least fitness value to largest

```
fitness value. A certain number of permutations (selection rate
* population) are retained, the rest are discarded. After this
point the GA loop begins.
    The mates are selected using tournament selection and enough
offspring are generated so that the population size is the same
as before. Next, the cell chromosomes are mutated and then each
permutation }\Pi\mathrm{ is reevaluated just as described earlier. Next the
iteration statistics are collected. The GA loops till the stop-
ping criterion is reached.
```


### 4.2.1 Initializing the $G A$

In this sub-process, all the parameters of the GA are set. The process is fairly straight forward; the user enters the requisite information for the parameters of the GA.

```
START
```

Enter the following information
Number of Facilities (nbay)
Population Size (pop)
Maximum Iterations (maxit)
Terminating Condition (tcond)
Selection Rate (xrate)
Crossover Rate (crate)
Mutation Rate (mrate)
Elitism Criteria (elite)
STOP

Figure 4.7: Flowchart of the Initialize Sub-process

The user also enters information about the LLMF, so as to evaluate the fitness function, viz. the ratio of the cost to install a shortcut to the cost of a unit of production from equation (42), the flow rate multiplier from equation (45), and the speed of the conveyor.

### 4.2.1.1 A note on Initial Parameter selection

Haupt and Haupt (2004) is used as a reference for this discussion. Proper initial parameter selection can ensure the quality of the solution. The approaches discussed obtain their inferences by analyzing a variety of GAs generated by varying $\mu, N_{p o p}, X_{\text {rate }}$, and $G . \mu$ is the mutation rate, $N_{p o p}$ is the number of chromosomes, $X_{\text {rate }}$ is the crossover rate, $G$ is the generation gap and has the bounds $0<G \leq 1$. The generation gap, $G$, is the fraction of the population that changes every generation. A generation gap algorithm picks $G \cdot N_{p o p}$ members for mating. The $G \cdot N_{p o p}$ offspring produced replace $G \cdot N_{p o p}$ chromosomes randomly selected from the population.

De Jong (1975) presents the following observations on choice of initial parameters:
f) Small population sizes improve initial performance
g) Large population sizes improve long-term performance
h) High mutation rates are good for off-line performance, where off-line performance is the running average of the best cost solution found in each generation
i) Low mutation rates are good for on-line performance, where on-line performance is the running average of all cost solutions up to the current generation
j) Crossover rate should be around 0.60

Grefenstette (1986) is uses a meta-genetic algorithm to optimize the on-line and off-line performance of GAs. He suggests that, "while it is possible to optimize GA control parameters, very good performance can be obtained with a range of GA control parameter settings." Schaffer, Caruana, Eshelman, and Das (1989) tests 8400 possible combinations of GAs and report the best online performance resulted for the following parameter settings: $\mu=0.005$ to $0.01, N_{p o p}=20$ to 30 , and $X_{\text {rate }}=0.75$ to 0.95 .

Bäck (1993) shows that the desirable mutation rate $\mu=1 / N_{\text {bits }}$, where $N_{\text {bits }}$ is the number of bits of the chromosome. Gao (1998) computes a theoretical upper bound on convergence rates in terms of $\mu, N_{p o p}$, and $N_{b i t s}$ by developing a Markov chain model for the canonical GA. The resulting theorem shows that GAs converge faster for large $\mu$ and smaller $N_{p o p}$. Cervantes and Stephens (2006)
state that using $1 / N_{\text {bits }}$ too general and that one can generally choose $\mu \ll 1 / N_{\text {bits }}$.

Traditionally large populations have been used to thoroughly explore complicated cost surfaces. Crossover rate is the operator of choice to exploit those solution spaces; the role of mutation is somewhat nebulous. In one sense, greater exploration is achieved if the mutation rate is great enough to take the gene into a different region of solution space. Yet a mutation in the less critical genes may result in further exploiting the current region. Perhaps the larger mutation rates combined with the lower population sizes act to cover both properties without the large number of function evaluations required for large population sizes.

Haupt and Haupt (2004) have performed extensive comparisons of GA performance as a function of population size and mutation rate, as well as some other parameters. The criterion was finding a correct answer with as few evaluations of the cost function as possible. Their conclusions are that the crossover rate, method of selection (roulette wheel, tournament, etc.), and type of crossover are not of much importance. Population size and mutation rate, however, have a significant impact on the ability of the GA to find an acceptable minimum.

### 4.2.2 Generate Initial Population and Cell Chromosome

The initial population of cell chromosomes can be generated using the Fisher-Yates shuffle algorithm (Fisher \& Yates, 1948). The algorithm is as follows:

```
Step 0: Set initial chromosome to a sequential ordering of N fa-
    cilities to current chromosome
Step 1: Set N = number of facilities
Step 2: Set i = N
Step 3: Set j = random integer such that 1\leqj\leqi
Step 4: Swap the values in the i ith and j }\mp@subsup{}{}{\mathrm{ th }}\mathrm{ position of current
    chromosome
Step 5: Set i = i-1 and repeat step 3 until i=2, then STOP
```

This algorithm is applied 'p' number of times (to generate $p$ chromosomes) where p is the desired population.

### 4.2.3 Evaluate Permutation $\pi$

This is the most computationally expensive step of the GA. In an attempt to expedite the evaluation of each permutation $\pi$, a table of solutions is maintained. The table contains three columns of information: Cell chromosome, shortcut chromosome, and fitness value. As the GA progresses, the table is appended with new permutations that are encountered.

For each permutation $\pi$ in the population, the evaluation procedure is as follows: Search for the cell chromosome in first column of the table, if it is found then return the shortcut chromosome and fitness value, else a corresponding shortcut chromosome is generated and in the process the fitness value for
the permutation $\pi$ is computed using equation (42). The table is then updated with the information of the new permutation $\pi$.

### 4.2.3.1 GA applied to solve only the layout problem

If the GA is applied to solve only the layout problem then method as prescribed by $\$ 4.2 .3 .1$ for determining the shortcuts is omitted in the operation of the GA. In this manner, the GA will solve for a system that determines only the layout of the LLMF .

### 4.2.3.2 Generating the shortcut chromosome

Johnson et al. (2009) prescribes a greedy heuristic to identify the best set of shortcuts for a given cell chromosome. The heuristic is as follows:

```
Step 0: Start without any shortcuts
Step 1: Using the equation (42),i.e. the fitness value, evaluate
    the effect of adding each shortcut individually
Step 2: Rank shortcuts according to their impact on fitness val-
    ue (the higher the rank the greater the effect in de-
    creasing the WIP)
Step 3: Add highest ranked remaining shortcut. If the fitness
    value decreases; go to Step 4, otherwise stop
Step 4: Add shortcut to set of best shortcuts, return to Step 3.
```

Use encoding procedure as described in $\$ 4.1 .2$ to generate the shortcut chromosome. Next, record the resulting fitness value for the current permutation $\pi$.

### 4.2.4 Select Cell Chromosomes for Mating

After evaluating the population, the permutations are ranked. The highest rank has the lowest fitness value. A portion of the population (selection rate * population) is selected for mating, the rest are discarded. Tournament selection is used to select the pairs of cell chromosomes from the retained permutations for mating.

### 4.2.5 Mate / Crossover Cell Chromosomes

Two cell chromosomes are mated to create a new offspring. The methodology is best illustrated by example. Consider a facility with 7 cells. The cell chromosomes for permutations are [1234567] and [7351264]. The crossover point (crossover rate * number of facilities) is the position in the cell chromosome over which the permutations swap values. Arbitrarily, the crossover point is determined by rounding up the result of multiplying the crossover rate by the number of facilities by the number of bits required to represent the facilities to the next integer. For the current example: the number of facilities is 7; the number of bits required is $1 ;$ and if the crossover rate is 0.4 , the crossover point is the 3. The first step of the mating results in the following children (the parents are split at the crossover point). The second portion of parent 2 (parent 1) is
appended to the first portion of parent 1 (parent 2) to form Child 1 (child 2) as illustrated below:

$$
\begin{aligned}
& \text { Parent } 1=[123 \mid 4567] \rightarrow \text { Child } 1=[123 \mid 1264] \\
& \text { Parent } 2=[735 \mid 1264] \rightarrow \text { Child } 2=[735 \mid 4567]
\end{aligned}
$$

As it can be seen, Child 1 and Child 2 are not unique permutations. The procedure described henceforth ensures unique offspring are created.

For Child 1 (Child 2), create three ordered sets of values:

- Set $1 \rightarrow$ values from Child 1 (Child 2) that are before the crossover point
- Set $2 \rightarrow$ values from Child 2 (Child 1) that are before the crossover point
- Set $3 \rightarrow$ values from Child 1 (Child 2) that are after the crossover point
- For each value of Set 3
- Check for value in Set 1
- If found then replace value from Set 3 with corresponding value from Set 2 and repeat procedure for replaced value
- If not found is Set 1, then move to next value in Set 3 otherwise restart procedure with current value
- After completion, append Set 3 to Set 1 to get a unique Child 1 (Child 2)

Coming back to the example, the procedure as described above is illustrated below, for Child 1:

Set $1=[123]$
Set $2=[735]$
Set $3=[1264]$
$\rightarrow$ The first value of Set 3 is ' 1 ', it is found in Set 1 . The corresponding value for ' 1 ' from Set 1 in Set 2 is '7', so replace '1' in Set 3 with '7'. Set 3 is now [7264], '7' is not in Set 1, so move to next digit in Set 3.
$\rightarrow$ Next value in Set 3 is ' 2 ', it is found is Set 1 , the corresponding value for ' 2 ' from Set 1 in Set 2 is '3', so replace ' 2 ' in Set 3 with ' 3 '. Set 3 is now [7364], '3' is in Set 1. The corresponding value for ' 3 ' from Set 1 in Set 2 is '5', so replace '3' in Set 1 with '5'. Set 3 is now [7564], '5' is not in Set 1, so move to next digit in Set 3.
$\rightarrow$ Next value in Set 3 is '6', it is not found is Set 1 , so move to next digit in Set 3. Set 3 is now [7564].
$\rightarrow$ Next value in Set 3 is '4', it is not found is Set 1, so move to next digit in Set 3. Set 3 is now [7564].
$\rightarrow$ There are no more digits in set 1 ,

REPEAT PROCEDURE FOR CHILD 2.

### 4.2.6 Mutate Cell Chromosomes

Given the mutation rate, nmut (mutation rate * \{population - 1\} * number of facilities) mutations are performed. The methodology is as described below.

```
Step 1: Set counter to zero
Step 2: if elitism in place: Set i = random integer such that
    2 \leqi \leq pop, otherwise 1\leqi\leq pop
Step 3: Set j = random integer such that 1\leqj\leqnbay
Step 3: Set k = random integer such that 1\leqk\leqnbay
Step 4: Go to row i in the population, swap the jth and k }\mp@subsup{}{}{\mathrm{ th }}\mathrm{ values
    of the cell chromosome, while counter < nmut return to
    step 2 and increment counter by 1, otherwise STOP
```


### 4.2.7 Terminating Condition

As discussed in the previous sections, there is no proof for convergence for a GA, therefore some criteria has to be set on when to terminate the GA: usually referred to as a terminating condition. In the GA implemented, the terminating condition is set to the maximum number of iterations as set by the user. In the test problem, the terminating condition was 1000 iterations.

### 4.2.8 Collect Iteration Statistics

The permutation $\pi$ with the best (lowest) fitness value from each iteration is recorded. These recorded fitness values are then plotted and analyzed to ensure the GA is performing adequately.

## 5 TESTING PROCEDURE

The objectives of this research are to propose the design of a LLMF with a LCMHS with shortcuts by minimizing the WIP in the system while using GAs to solve the LLDP. This chapter presents the tasks that are performed to support the research objectives. The three main tasks are:

1. Validate the proposed analytical approximation for the expected WIP at the input stations as given by equation (37) in § 3.2.2.3.
2. Test and evaluate the overall proposed methodology (LLDP) of Layout and shortcut design for a LLMF.
3. Determine the set of parameters that improve the performance of the genetic algorithm solution procedure by varying the parameters over an initial number of test problems. These parameters once determined will be fixed for all the problems tested.

### 5.1 Testing the Expected Value of WIP at the input Stations

 This section presents the methodology for validating the expected value for the WIP at the input stations to a LCMHS with multiple input and output stations. For the expected WIP at the input stations: each of the system configurations presented will be simulated and the accuracy of the methodology to estimate theWIP at the input stations will be evaluated. The simulation model as presented by SEMATECH (2002) is used to generate the simulation data against which the estimate for the $W I P$ at the input stations will be tested. This simulation model has been tested, validated, and verified by academic and industrial professionals as being representative of a semiconductor manufacturing fab. Finally, various hypotheses are tested that compare the results of the total WIP at the input stations from the simulation against the analytical estimate using the Generalized Linear Model (GLM) analysis procedure with post-hoc analysis that enables the comparison of means from multiple groups while minimizing the Type $I$ and Type II errors.

### 5.1.1 Problem Description

Consider a 24 cell LLMF as shown in Figure 5.1. This LLMF is a simplified depiction of a 300 mm wafer fabrication facility as described in Agrawal and Heragu (2006), Nazzal and El-Nashar (2007), and SEMATECH (2002). The flow rates between the facilities are known and represented in the 'from-to' matrix (further described in $\$ 5.1 .2)$.


Figure 5.1: 300mm Wafer Fabrication Facility

### 5.1.2 Parameters to be varied

The parameters presented in Table 5.1 are varied to generate the different scenarios. As it can be seen, 90 different scenarios are considered. The simulation runs will be performed using Automod Simulation Software from Brooks Automation. Each simulation is warmed up for 2 days (simulation time) and then run for 10 replications of 30 days (simulation time). The total WIP at the input stations is captured for each replication. The speed of the conveyor is set to $3 \mathrm{ft} / \mathrm{sec}$.

Table 5.1: Parameters to vary for testing the Expected total WIP at the Input stations

|  | Level |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Factor | 1 | 2 | 3 | 4 | 5 | 6 |
| Utilization ( $\rho_{\text {LCMHS }}$ ) | 0.15 | 0.3 | 0.45 | 0.6 | 0.75 | 0.9 |
| Job Flow Matrix (Layout) | X | $Y$ | $Z$ |  |  |  |
| Arrival Process $\left(C_{a}{ }^{2}\right)$ | 0.5 | 0.77 | 1 | 1.23 | 1.5 |  |

It is important to notice that the conveyor speed and flow rate multiplier have not been included in the list of parameters to vary. Based on empirical observances, any combination of conveyor speed and flow rates that yields the same conveyor utilization, denoted by $\rho_{\text {LCMHS }}$, will have statistically indifferent results in terms of total WIP on the LCMHS; hence for a given layout it is sufficient to vary the utilization of the conveyor ( $\rho_{\text {LCMHS }}$ ) $\cdot$

Different job flow matrixes are used to test different systems so as to introduce some diversity of flows into the testing procedure. For each flow layout l, at a specified conveyor utilization, the effective flow rates $\left(\lambda_{i j}\right)$ can be generated using an arrival rate multiplier $\left(\vartheta_{1}\right)$ that adjusts the raw flow rate as given by.

$$
\begin{equation*}
\lambda_{l j}=\vartheta_{l} \cdot \tilde{\lambda}_{l j} \tag{45}
\end{equation*}
$$

Three layouts are utilized: Layout $X$, Layout $Y$, and Layout $Z$. The arrival rate multipliers are given in Table 5.2. The base flow rates matrix for Layout $X$ is presented in Appendix $A$ while the base flow rates matrix for Layout $Y$ is presented in Appendix B. For Layout $Z$, all bays send the same number of loads to all other bays; the base flow rates matrix for the uniform layout is given by:

$$
\tilde{\lambda}_{i j}= \begin{cases}0 & \forall i=j  \tag{46}\\ 0.5273 & \forall i \neq j\end{cases}
$$

Table 5.2: Flow Rate Multipliers at different Conveyor Utilizations
$\rho_{\text {LCMHS }}$

|  | 0.45 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 0.15 | 0.30 | 0.45 | 0.60 | 0.75 | 0.90 |
| $\Theta_{\mathrm{X}}$ | 10.6410 | 21.2820 | 31.9230 | 42.5640 | 53.2050 | 63.8460 |
| $\Theta_{\mathrm{Y}}$ | 7.0400 | 14.0790 | 21.1190 | 28.1590 | 35.1980 | 42.2380 |
| $\Theta_{\mathrm{Z}}$ | 11.1320 | 22.2640 | 33.3960 | 44.5280 | 55.6600 | 66.7920 |

Note: The multipliers for the various layouts are selected such that the overall WIP for each layout is approximately the same at each level of utilization given a fixed conveyor speed $3 \mathrm{ft} / \mathrm{sec}$ for the different layouts

The squared coefficient of variation of the arrival process $c_{a}{ }^{2}$ is varied because it is important to check how robust the methodology is with respect to different input arrival processes, so as to prescribe a general approach. The Weibull distribution is used to obtain the required variation in the arrival processes $\left(c_{a}{ }^{2}\right)$ for systems tested. It is represented by Weibull ( $\beta, \alpha$ ) as presented in Walck (2007); where $\boldsymbol{\alpha}$ is the shape parameter, and $\beta$ is the scale parameter. From Walck (2007), the mean (average) of Weibull $(\beta, \alpha)$ is given by

$$
\begin{equation*}
\mu=\frac{\beta}{\alpha} \Gamma\left[\frac{1}{\alpha}\right] \tag{47}
\end{equation*}
$$

Where, $\Gamma[x]$ represents the gamma function. Next, from Walck (2007), the variance of Weibull $(\beta, \alpha)$ is given by

$$
\begin{equation*}
\sigma^{2}=\frac{\beta^{2}}{\alpha}\left[\left(2 \Gamma\left[\frac{2}{\alpha}\right]\right)-\left(\frac{1}{\alpha} \Gamma\left[\frac{1}{\alpha}\right]^{2}\right)\right] \tag{48}
\end{equation*}
$$

Therefore the coefficient of variation for Weibull ( $\beta, \alpha$ ) is given by

$$
\begin{equation*}
c_{a}^{2}=2 \alpha \frac{\Gamma[2 / \alpha]}{\Gamma[1 / \alpha]^{2}} \tag{49}
\end{equation*}
$$

It is imperative that all the test levels have the same average effective flow while reflecting the various levels of variability. In order to achieve this, for each effective flow rate between cell $i$ and cell $j$; the mean of the Weibull Distribution $\left(\mu_{i j}\right)$ is equal to the effective flow rate $\left(\lambda_{i j}\right)$. Therefore, the scale parameter for the Weibull distribution ( $\beta_{i j}$ ) can be represented as

$$
\beta_{i j}=\mu_{i j} \frac{\alpha}{\Gamma[1 / \alpha]}=\lambda_{i j} \frac{\alpha}{\Gamma[1 / \alpha]}
$$

As it can be seen, to determine $\beta_{i j}$ the effective flow rate ( $\lambda_{i j}$ ) between cell $i$ and cell $j$ in the LLMF multiplied by an adjustment factor ( $\delta$ ) which is given by

$$
\begin{equation*}
\delta=\frac{\alpha}{\Gamma[1 / \alpha]} \tag{51}
\end{equation*}
$$

As it can be seen in Table 5.3, the adjustment factor ( $\delta$ ) is given for each level of $c_{a}{ }^{2}$ to ensure that the same average ef-
fective flow is observed at each level of variability. Next, the squared coefficient of variation for the Weibull distribution can be varied by changing $\alpha$. Given equation (49), in Microsoft Excel one can use the solver tool to determine the values of $\alpha$ that yield the corresponding $c_{a}{ }^{2}$ values. It is important to note that the values for the shape parameter $(\alpha)$ and the adjustment factor ( $\delta$ ) are general and can be applied to any family of Weibull distributions. The values for the shape parameter are as given in Table 5.3.

Table 5.3: Parameters for Weibull Distribution

| $C_{a}{ }^{2}$ | $\alpha$ | $\delta$ |
| :--- | :--- | :--- |
| 0.5 | 1.435525 | 1.101 |
| 0.77 | 1.142287 | 1.049 |
| 1 | 1 | 1 |
| 1.23 | 0.903123 | 0.952 |
| 1.5 | 0.821714 | 0.899 |

### 5.1.3 Summary of Testing Procedure for WIP at Input Stations



Figure 5.2: Summary of Testing Procedure

### 5.1.4 Method for Analysis of Test Data

A Generalized Linear Model (GLM) will be used to analyze the data collected from the testing. GLMs are powerful because they unify several statistical techniques under a single modeling paradigm. In the event of comparing means from multiple groups to each other, the use of any of the family of $t$-tests would lead to an increase in the Type 1 error (Roberts \& Russo, 1999). GLMs enable comparing means from multiple groups to each other by incorporating post hoc analysis methods such as Tukey's Range Test (Tukey, 1977) that control for Type I error (McCulloch, Agarwal, \& Neuhaus, 2008). As indicated by Day and Quinn (1989) and SAS Institute Inc (2010), the REGWQ multiple comparison procedure (Ryan, 1960) not only controls for Type I error but has a
higher statistical power (i.e. lower Type II error) than the Tukey's Range Test. Hence, both procedures will be used to verify and validate the comparison of means results.

Gill (2000) and McCulloch, Agarwal, and Neuhaus (2008) both provide detailed descriptions of the GLM and attribute the development of the GLM to Nelder and Wedderburn (1972). The GLM procedure has the capability to perform many different statistical analyses, viz.: simple regression, multiple regression, ANOVA, analysis of covariance, response surface models, weighted regression, polynomial regression, partial correlation, MANOVA, and repeated measures ANOVA (SAS Institute Inc, 2010).

It is important to note that for each layout ( $A, B$, and $C$ ) a separate GLM analysis will be performed. For the GLM, there are two types of input variables to be defined: the dependent variable(s), and the independent variable(s). In this case, the dependent variable is the total WIP at the input station (labeled WIP). The independent variables are the parameters that are varied: the utilization of the conveyor ( $\rho_{L C M H S}$ ), and the coefficient of variation of the input arrival process ( $c_{a}{ }^{2}$ ). Another independent variable considered is an indicator variable (M) for the source of the total WIP at the input station, i.e. WIP from simulation or WIP from estimate, where $1 \rightarrow$ WIP from simulation and $0 \rightarrow$ WIP from estimate. Here, both REGWQ and Tukey's post hoc
analysis methods can test the difference in the total WIP at the input stations for the levels of $M$, i.e., simulation vs. analytical.

Another independent variable (RHOM) considered an indicator variable introduced to capture the interaction of $\rho_{\text {LCMHS }}$ and $M$. Since there are 6 levels of $\rho_{\text {LCMHS }}$ and 2 levels of $M$, RHOM has 12 levels as illustrated in Table 5.4. At it can be seen, simulation values of the total WIP at the input stations are used when RHOM is odd while the analytical estimate of the total WIP at the input stations is used when RHOM is even.

Table 5.4: Description of RHOM

| $\rho_{\text {LCMHS }}$ | M | RHOM |
| :--- | :--- | :--- |
| 0.15 | 1 | 1 |
| 0.15 | 0 | 2 |
| 0.3 | 1 | 3 |
| 0.3 | 0 | 4 |
| 0.45 | 1 | 5 |
| 0.45 | 0 | 6 |
| 0.6 | 1 | 7 |
| 0.6 | 0 | 8 |
| 0.75 | 1 | 9 |
| 0.75 | 0 | 10 |
| 0.9 | 1 | 11 |
| 0.9 | 0 | 12 |

In this manner, one can test the efficacy of the analytical estimate for different levels of $\rho_{L C M H S}$. To further elaborate, if there is no difference in the analytical estimate and the simu-
lation values at a particular $\rho_{\text {LCMHS }}$ then the Tukey's and REGWQ post hoc methods group the two as being statistically indifferent from each other.

Finally, another independent variable (SCVM) considered is an indicator variable introduced to capture the interaction of $C_{a}{ }^{2}$ and M. Since there are 5 levels of $C_{a}{ }^{2}$ and 2 levels of $M$, SCVM has 10 levels as illustrated in


#### Abstract

Table 5.5. At it can be seen, simulation values of the total WIP at the input stations are used when SCVM is odd while the analytical estimate of the total WIP at the input stations is used when SCVM is even. Therefore, every even value of SCVM will have the same WIP as described by the analytical estimate.

In this manner, one can test the efficacy of the analytical estimate for different levels of $c_{a}{ }^{2}$. More specifically, if there is no difference in the analytical estimate and the simulation values at a particular $c_{a}{ }^{2}$ then the Tukey's and REGWQ post hoc methods group the two as being statistically indifferent from each other.


Table 5.5: Description of SCVM

| $C_{a}{ }^{2}$ | $M$ | SCVM |
| :--- | :--- | :--- |
| 0.50 | 1 | 1 |
| 0.50 | 0 | 2 |
| 0.77 | 1 | 3 |
| 0.77 | 0 | 4 |
| 1.00 | 1 | 5 |
| 1.00 | 0 | 6 |
| 1.23 | 1 | 7 |
| 1.23 | 0 | 8 |
| 1.50 | 1 | 9 |
| 1.50 | 0 | 10 |
| Note: | M $=1$ | $->$ Simulation; |
| M $=0$ | $->$ | Analytical Esti- |
| mate |  |  |

To summarize, Table 5.6 presents the independent variables for the GLM procedure along with the different levels for each variable.

Table 5.6: Description of Independent Variables for GLM

Factor
Levels

| Utilization (Conveyor) | $(0.15,0.30,0.45,0.60,0.75,0.90)$ |
| :--- | :--- |
| Arrival Process (SCV) | $(0.50,0.77,1.00,1.23,1.50)$ |
| M | $(0,1)$ |
| RHOM | $(1,2,3,4,5,6,7,8,9,10,11,12)$ |
| SCVM | $(1,2,3,4,5,6,7,8,9,10)$ |
| Note: For each layout $(\mathrm{X}, \mathrm{Y}$, and Z$)$ separate GLM analysis will |  | be performed.

Table 5.7 presents an illustration (not actual test results) of a subset of the input data for the GLM. As it can be seen when $M$ $=0$ (analytical estimate), the 'Run' values are the same since the estimate for the total WIP at the input stations does not change. When $M=1$ (simulation), the "Run" values vary as expected.

Table 5.7: Example of Subset of Total WIP at Input Stations Data table for GLM

| $\rho_{\text {LCMHS }}$ | Layout | $C_{a}{ }^{2}$ | M | RHOM | SCVM | Run |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | 1 | 2 | ... | 10 |
| 0.3 | X | 0.50 | 0 | 4 | 2 | 12.16 | 12.16 | ... | 12.16 |
| 0.3 | X | 0.50 | 1 | 3 | 1 | 12.61 | 12.44 | ... | 12.38 |
| 0.6 | Z | 1.00 | 0 | 8 | 6 | 15.24 | 15.24 | ... | 15.24 |
| 0.6 | Z | 1.00 | 1 | 7 | 5 | 15.46 | 16.07 | ... | 15.59 |
| 0.9 | Y | 1.50 | 0 | 12 | 10 | 39.44 | 39.44 | ... | 39.44 |
| 0.9 | Y | 1.50 | 1 | 11 | 9 | 40.52 | 37.52 | ... | 41.52 |

### 5.1.5 Hypothesis

The total WIP at the input stations from the simulation is tested against the estimate of the total WIP at the input stations as given by equation (40) on page 69. This section describes the hypotheses that will be tested using the GLM procedure.

### 5.1.5.1 Hypothesis Test 1

This is the most general test of the accuracy of the proposed estimate of the total WIP over a variety of utilization levels and arrival distributions. The hypothesis is as follows:

H10 There is no statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

H1 ${ }_{\text {A }}$ There is a statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

In the event $H 1_{0}$ is not accepted, four new hypotheses will be proposed and tested; the outcomes of which will serve to provide the operating conditions under which the estimate of the Total WIP at the input stations as given by equation (40) on page 69 are statistically indifferent from the total WIP at the input stations from the simulation.

### 5.1.5.2 Hypothesis Test 2

This hypothesis tests the levels of utilization over which the analytical estimate and the simulation output are statistically
indifferent for all arrival distributions. The hypothesis is as follows:

H2 $2_{0}$ Given the utilization of the conveyor is within a specified range (to be determined in the analysis); there is no statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.
$\mathrm{H} 2_{\mathrm{A}}$ Given the utilization of the conveyor is within a specified range (to be determined in the analysis); there is a statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

### 5.1.5.3 Hypothesis Test 3

This hypothesis tests if the analytical estimate and the simulation output are statistically indifferent when the squared coefficient of variation of the arrival process is less than 1 ; for all levels of utilization. The hypothesis is as follows:

H30 Given the squared coefficient of variation of the arrival process is less than 1; there is no statistically significant difference between the mean total WIP at the input stations from simulation and 104
the analytical estimate of mean total WIP at the input stations.
$\mathrm{H} 3_{A}$ Given the squared coefficient of variation of the arrival process is less than 1; there is a statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

### 5.1.5.4 Hypothesis Test 4

This hypothesis tests if the analytical estimate and the simulation output are statistically indifferent when the squared coefficient of variation of the arrival process is 1; for all levels of utilization. The hypothesis is as follows:

H40 Given the squared coefficient of variation of the arrival process is 1; there is no statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.
$H 4_{A}$ Given the squared coefficient of variation of the arrival process is 1 ; there is a statistically significant difference between the mean total WIP at
the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

### 5.1.5.5 Hypothesis Test 5

This hypothesis tests if the analytical estimate and the simulation output are statistically indifferent when the squared coefficient of variation of the arrival process is greater than 1 ; for all levels of utilization. The hypothesis is as follows:
$H 5$. Given the squared coefficient of variation of the arrival process is greater than 1; there is no statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.
$H 5_{A}$ Given the squared coefficient of variation of the arrival process is greater than 1; there is a statistically significant difference between the mean total WIP at the input stations from simulation and the analytical estimate of mean total WIP at the input stations.

### 5.2 Testing the LLDP

The goal of testing the LLDP is to compare the proposed methodology of using the wIP as the design criterion while combining the Layout and shortcut solution procedures, against using the total distance travelled as the design criterion to first solve the LLDP and then another algorithm is used separately to solve for the best set of shortcuts that further improves the best layout. This is done by introducing a set of test scenarios that represent all the possible combinations of problems circumscribing the testing goal. Then, for each test Scenario E set of operation parameters are varied. Finally, various hypotheses are tested that compare the test scenarios against each other using the GLM analysis procedure with post-hoc analysis that enables the comparison of means from multiple groups while minimizing the Type I and Type II error.

### 5.2.1 Test Problem Description

Consider a 24 cell LLMF as shown in Figure 5.3. This LLMF tested is a simplified depiction of a 300 mm wafer fabrication facility as described in Agrawal and Heragu (2006), Nazzal and El-Nashar (2007), and SEMATECH (2002).


Figure 5.3: LLMF for the LLDP testing
The flow rates between the facilities are known and represented in the 'from-to' matrix; Layout X (as presented in Appendix A on page 190) is used as the base flow matrix.

### 5.2.2 LLDP Test Scenarios

Four scenarios are presented and described henceforth.

Table 5.8: Type of Test Scenario

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | E | F |
| Distance | G | H |

The left most column represents the design criterion used for the total cost function, while the first row represents the shortcut solution procedure. These represent the constraints of the test scenario; in essence, these constraints will affect the solution methodology as will be discussed in detail within the discussion for each test scenario.

A set of operational specific parameters are varied for each test scenario, each instance of these sets of operational specific parameters will be referred to as a test problem. Each test problem will be run 20 times (as the GA is a stochastic solution process); each run will be referred to as a test run. For each test problem, for each test scenario, each test run will first be solved. Next, given the prescribed solution, the total WIP, as prescribed by equation (52) on page 111, is then computed for each test run. In this manner, various test scenarios can be equivalently compared to each other over the same set of operational specific parameters. Hence, for each test scenario, there are three basic steps employed to determine the solution to the LLDP, as given below:

1. Determine the Objective Function of the LLDP
a. Given that the total cost using the WIP is the design criteria (Test Scenario E and Test Scenario F), there are two design procedures:
i. Combined Layout and shortcut solution procedure (Test Scenario E)
ii. Separate Layout and shortcut solution procedure (Test Scenario F)
b. Given that the total cost using total distance travelled is the design criteria (Test Scenario G and Test Scenario H), there are two design procedures:
i. Combined Layout and shortcut solution procedure (Test Scenario G)
ii. Separate Layout and shortcut solution procedure (Test Scenario H)
2. Solve the LLDP using the $G A$ solution Procedure as prescribed by § 4
a. Combined Layout and shortcut solution procedure (Test Scenario E and Test Scenario G)
i. Apply the genetic algorithm as prescribed by $\$ 4$ to solve the LLDP and get the best layout with the best set of shortcuts for the test scenario
b. Separate Layout and shortcut solution procedure (Test Scenario F and Test Scenario H)
i. First, solve the layout problem using the Genetic Algorithm as prescribed by $\$ 4$ (applying the modification for "layout only" problems as presented in § 4.2.3.1) to get the best layout for the test scenario
ii. Then, for the best layout use the greedy heuristic Johnson et al. (2009) to determine the best set of shortcuts (as described in § 4.2.3.2)
3. Determine the total WIP for the best solution
```
a. For the final solution, the total WIP, as derived from equation (25) and equation (40), is then computed for each test problem
```

$$
\begin{equation*}
E\left(W I P_{L L M F}\right)=E\left(W I P_{\text {CONV }}\right)+E\left(W I P_{\text {INP }}\right) \tag{52}
\end{equation*}
$$

### 5.2.2.1 LLDP Test Scenario E

The total cost based on the $W I P$ on the LLMF is used as the design criterion while combining the Layout and shortcut solution procedures to solve the LLDP with shortcuts. This scenario is representative of the proposed methodology.

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | E |  |
| Distance |  |  |

The steps involved in determining the solution for a test problem for Test Scenario E is as follows:

Step 1: The objective function for the LLDP is given by equation (41).

$$
Z_{E}=C_{W I P}\left[E\left(W I P_{I N P}\right)+E\left(W I P_{\text {CONV }}\right)\right]+C_{s c} \cdot \# \text { Shortcuts }
$$

Step 2: Solve the problem at hand (Layout and shortcut simultaneously) using the $G A$ solution procedure as prescribed by $s 4$ to get the best layout with the best set of shortcuts for the test scenario.

Step 3: For the final solution, determine the total WIP for Test Scenario $\mathrm{E}\left(W I P_{E}\right)$ as given by equation (52).

### 5.2.2.2 LLDP Test Scenario F

The total cost based on the WIP on the LLMF is used as the design criterion to first solve for the Layout and then the greedy heuristic by Johnson et al. (2009) is used separately to solve for the best set of shortcuts that further improves the best layout.

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | F |  |
| Distance |  |  |

The steps involved in determining the solution for a test problem for Test Scenario $F$ is as follows:

Step 1: The objective function to determine the layout is given by

$$
\begin{equation*}
Z_{F}=C_{W I P}\left[E\left(W I P_{I N P}\right)+E\left(W I P_{C O N V}\right)\right] \tag{53}
\end{equation*}
$$

Step 2: First, solve the problem at hand (layout problem only) using the GA solution procedure as prescribed by $\S 4$
(see § 4.2.3.1) to get the best layout for the test scenario. Then, for the best layout use the greedy heuristic Johnson et al. (2009) to determine the best set of shortcuts as described in $\$ 4.2 .3 .2$.

Step 3: For the final solution, determine the total WIP for Test Scenario $F\left(W I P_{F}\right)$ as given by equation (52).

### 5.2.2.3 LLDP Test Scenario G

The total cost based on the total distance travelled by the loads on the LLMF is used as the design criterion while combining the Layout and shortcut solution procedure to solve the LLDP with shortcuts.

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP |  |  |
| Distance | G |  |

The steps involved in determining the solution for a test problem for Test Scenario $G$ is as follows:

Step 1: The objective function for the LLDP is given by

$$
\begin{equation*}
Z_{G}=C_{D i s t} \sum_{\forall i, j}^{i \neq j} \lambda_{i j} \cdot d_{i j}+C_{s c} \cdot \# \text { Shortcuts } \tag{54}
\end{equation*}
$$

Where, $C_{D i s t}$ is the cost per distance unit (further discussed in $\$ 5.2 .4), d_{i j}$ is the distance from location $i$
to location $j$, and $\lambda_{i j}$ is the flow of loads from location i to location j.

Step 2: Solve the problem at hand (Layout and shortcut simultaneously) using the GA solution procedure as prescribed by $\$ 4$ to get the best layout with the best set of shortcuts for the test scenario.

Step 3: For the final solution, determine the total WIP for Test Scenario $G\left(W I P_{G}\right)$ as given by equation (52).

### 5.2.2.4 LLDP Test Scenario H

The total cost based on the total distance travelled by the loads on the LLMF is used as the design criterion to first solve for the Layout and then the greedy heuristic by Johnson et al. (2009) is used separately to solve for the best set of shortcuts that further improves the best layout. This scenario is representative of the traditional methodology used to solve the LLDP.

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP |  |  |
| Distance | H |  |

The steps involved in determining the solution for a test problem for Test Scenario $H$ is as follows:

Step 1: The objective function to determine the layout is given by

$$
\begin{equation*}
Z_{H}=C_{D i s t} \sum_{\forall i, j}^{i \neq j} \lambda_{i j} \cdot d_{i j} \tag{55}
\end{equation*}
$$

Where, $C_{\text {Dist }}$ is the cost per distance unit (further discussed in $\S 5.2 .4), d_{i j}$ is the distance from location i to location $j$, and $\lambda_{i j}$ is the flow of load from location i to location j.

Step 2: First, solve the problem at hand (layout problem only) using the GA solution procedure as prescribed by § 4 (see § 4.2.3.1) to get the best layout for the test scenario. Then, for the best layout use the greedy heuristic Johnson et al. (2009) to determine the best set of shortcuts as described in $\$ 4.2 .3 .2$.

Step 3: For the final solution, determine the total WIP for Test Scenario H (WIP $H_{H}$ as given by equation (52).

### 5.2.3 Parameters to be varied

The set of operational parameters in Table 5.9 are varied to generate the different test problems for each test scenario. Hence, there are 36 different test problems for each test scenario. Since the GA procedure is a stochastic solution procedure, each test problem will be solved 10 times (each referred
to as a 'test run'). Hence, there will be a total of 1440 (4 Test Scenarios * 36 Test Problems * 10 Test Runs) data points.

The number of locations in the LLMF is set to 24 ; Layout $X$ is used as the base flow matrix; the speed on the conveyor is set to $3 \mathrm{ft} / \mathrm{sec}$.

Table 5.9: Parameters to vary for LLDP

|  | Level |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Factor | 1 | 2 | 3 | 4 |
| Shortcut Cost/WIP Cost ( $\Omega)$ | 0.1 | 1 | 10 | 50 |
| Utilization $\left(\rho_{L C M H S}\right)$ | 0.15 | 0.5 | 0.85 |  |
| Turntable Turn Time | 0 | 7 | 15 |  |
| Note: The speed of the conveyor is $3 \mathrm{ft} / \mathrm{sec}$ |  |  |  |  |
| and the arrivals to the LLDP are modeled as a |  |  |  |  |
| Markov Process |  |  |  |  |

$\Omega$ is the ratio of the cost to install a shortcut to the cost of a load (one unit of WIP); $\Omega$ affects the total cost of the LLMF. It is possible to effectively and equivalently vary $C_{D i s t}$ (see $\S$ 5.2.4), and $C_{s c}$ for all the test scenarios for all the test problems, by varying $\Omega$ and arbitrarily setting $C_{W I P}$.

The utilization of the conveyor is selected as a parameter to vary as it directly affects the amount of WIP in the LLMF. This has a significant effect on the choice of layout. Also, as mentioned earlier instead of varying a multitude of factors to test
different scenarios, varying the utilization of the conveyor is sufficient.

The turn time of the turntable is selected as a parameter to vary as it affects the WIP level and the stability of the system. Although a particular Layout and shortcut configuration may have a significant effect on reducing the WIP in the system, it may also render the system unstable. This can be attributed to the instability introduced to the LLMF as a result of the infinite queue formation in front of an unstable turntable (i.e. the utilization of a turntable is greater than or equal to 1) blocking the output station of the preceding cell.

### 5.2.4 Equivalently varying the costs for all scenarios

It is important to note that a relationship has to be developed between $C_{W I P}$ and $C_{\text {Dist }}$ so as to properly vary both problems so the operating conditions are similar and the results to be statistically analyzed are not biased as a result of improper $C_{W I P}$ and $C_{\text {Dist }}$ selections. $C_{W I P}$ is the average cost per unit of WIP, while $C_{\text {Dist }}$ is the cost per unit distance. This section provides a detailed description on the steps involved in determining $C_{\text {Dist }}$.

Why is this important? For each test problem, all the scenarios should have similar likelihoods of selecting shortcuts i.e.,
ideally the total cost saved as a result of installing a shortcut should equivalently offset the cost of installing the shortcut. The $C_{W I P}$ and $C_{D i s t}$ assignments will have the greatest impact on the results when $C_{S C} \gg C_{W I P}$. In such cases, if $C_{D i s t}$ is too low with respect to $C_{W I P}$, the likelihood of selecting shortcuts is much lower for Scenario $G$ and Scenario $H$ than Scenario E and Scenario F. In order to balance the likelihood of selecting shortcuts across all scenarios, the objective functions from Scenario E should equal the objective functions from Scenario G. Similarly, the objective functions from Scenario F should equal the objective functions from Scenario $H$ such that $C_{D i s t} \sum_{\forall i, j}^{i \neq j} \lambda_{i j} \cdot d_{i j}=C_{W I P}\left[E\left(W I P_{I N P}\right)+E\left(W I P_{C O N V}\right)\right]$. Hence, setting the objective functions from Scenario E equal to Scenario $G$ or Scenario $F$ equal to Scenario H yields:

$$
\begin{equation*}
C_{D i s t}=\frac{C_{W I P}\left[E\left(W I P_{I N P}\right)+E\left(W I P_{C O N V}\right)\right]}{\sum_{\forall i, j}^{i \neq j} \lambda_{i j} \cdot d_{i j}} \tag{56}
\end{equation*}
$$

Therefore for each test problem the $C_{\text {Dist }}$ used in Scenario $G$ and Scenario H is determined later from the outcomes of the runs for Scenario E and Scenario F respectively.

For Scenario G, the steps involved in this determination are as follows:

Step 1: Scenario E is run 10 times.

Step 2: For each run of the test problem, at each iteration in the evaluation step of the $G A$ as described in $\$ 4.2 .3$, and for each solution visited the following data is collected: The total WIP in the LLMF and the total distance travelled by the loads for the respective solution each given by $W I P_{\text {Total }}=E\left(W I P_{I N P}\right)+E\left(W I P_{C O N V}\right)$ and $D=\sum_{\forall i, j}^{i \neq j} \lambda_{i j} \cdot d_{i j}$.

Step 3: For each run of the test problem, compute the average of the total WIP in the LLMF $\left(\overline{W I P}_{\text {Total }}\right)$ and average total distance travelled ( $\bar{D}$ ) for all the solutions visited.

Step 4: Using equation (56) and the outcomes from Step 3, for Scenario $G$ of the current test problem, $C_{\text {Dist }}$ is given by

$$
\begin{equation*}
C_{D i s t}=C_{W I P} \cdot \sum_{\forall r u n s}^{A \& B} \frac{\overline{W I P}_{\text {Total }}}{\bar{D}} \tag{57}
\end{equation*}
$$

Next, for the current test problem for Scenario $H$ repeat Steps 1-4 using Scenario $F$ as the seed to determine the cost per unit distance for Scenario H.

In this manner for each test problem, all the scenarios should have similar likelihoods of selecting shortcuts.

### 5.2.5 Summary of the Testing Procedure for the LLDP



Figure 5.4: Summary of Testing Procedure for LLDP

### 5.2.6 Method for Analysis of Test Data for the LLDP

As presented and justified in $\$ 5.1 .4$, the Generalized Linear Model (GLM) will be used to analyze the data collected from the testing of the LLDP, as GLMs enable comparing means from multiple groups to each other by incorporating post hoc analysis methods such as Tukey's Range Test (Tukey, 1977) that control for Type 1 error (McCulloch, Agarwal, \& Neuhaus, 2008).

For the GLM, there are two types of input variables to be defined: the dependent variable(s), and the independent variable(s). In this case, the dependent variable is the total WIP for the LLMF as given by equation (52). The independent variables are the parameters that are varied, viz., the ratio of the cost to install a shortcut to the cost of a load ( $\Omega$ ), the utilization of the conveyor ( $\rho_{\text {LCMHS }}$ ), and the turn time of the turntables ( $t$ ). An independent variable is introduced to model the decision / optimization criterion for the layout ( $\theta$ ) i.e., cost based on $W I P(\theta=1)$ or cost based on total distance travelled ( $\theta=2$ ). Another independent variable is introduced to model the shortcut determination criterion (S) i.e., Layout and shortcuts are determined simultaneously $(S=1)$ or Layout and shortcuts are determined separately $(S=2)$. Finally, a last variable is introduced, to model the various scenarios as described in $\S$ 5.2.2, called Scenario ( $\theta S$ ). $\theta S$ represents the interaction of $\theta$ 122
and $S$, i.e. $\theta S=1$ when $\theta=1$ and $S=1$ (Test Scenario E); $\theta S=$ 2 when $\theta=1$ and $\theta=2$ (Test Scenario F); $\theta S=3$ when $\theta=2$ and $S=1$ (Test Scenario G); and $\theta S=4$ when $\theta=2$ and $S=2$ (Test Scenario H). This information is further summarized in Table 5.10 .

Table 5.10: Description of $\theta S$

|  | S |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Combined $(S=1)$ | Separate $(S=2)$ |  |  |  |
| WIP $(\Theta=1)$ | Scenario $\mathrm{E}(\Theta S=1)$ | Scenario $F(\Theta S=2)$ |  |  |
| Distance $(\Theta=2)$ | Scenario $G(\Theta S=3)$ | Scenario $H(\Theta S=4)$ |  |  |

Table 5.11 summarizes the independent variables (main effects) used for the GLM analysis and presents the various levels of these variables.

Table 5.11: Description of Independent Variables for GLM

|  | Level |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Variable | 1 | 2 | 3 | 4 |
| Shortcut Cost/WIP Cost ( $\Omega$ ) | 0.1 | 1 | 10 | 50 |
| Utilization ( $\rho_{\text {LCMHS }}$ ) | 0.15 | 0.50 | 0.85 |  |
| Turntable Turn Time $(t)$ | 0 | 7 | 15 |  |
| Optimization Criteria $(\theta)$ | 1 | 2 |  |  |
| Shortcut Criteria ( $S$ ) | 1 | 2 |  |  |
| Scenario $(\theta S)$ | 1 | 2 | 3 | 4 |

Here, both REGWQ and Tukey's post hoc analysis methods can test if there is a difference in the total WIP for the levels of $\theta$, $S$, and $\theta S$. In this manner, the different test scenarios can be
evaluated against each other, the effect of the decision criterion for the layout on the WIP can be evaluated, and the effect of the shortcut determination criterion on the WIP can be evaluated. Likewise, the effect of varying the parameters of the LLDP on the WIP can be evaluated too.

Table 5.12 presents an example of a subset of the input data for the GLM. As it can be seen, the first row of data represents the Test Scenario E (when $\theta=1$ and $S=1$ ); the second row of data represents the Test Scenario $F$ (when $\theta=1$ and $S=2$ ); the third row of data represents the Test Scenario $G$ (when $\theta=2$ and $S=1) ;$ and the fourth row of data represents the Test Scenario H (when $\theta=2$ and $S=2$ ).

Table 5.12: Example of Subset of Input Data table for GLM

Run

| $\Omega$ | $\rho_{\text {LCMHS }}$ | t | $\theta$ | S | $\theta \mathrm{S}$ | 1 | 2 | $\ldots$ | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0.1 | 0.15 | 0 | 1 | 1 | 1 | 361.6 | 358.6 | $\ldots$ | 357.8 | 359.7 |
| 1 | 0.5 | 0 | 1 | 2 | 2 | 368.5 | 372.9 | $\ldots$ | 365.8 | 367.5 |
| 10 | 0.85 | 7 | 2 | 1 | 3 | 490.7 | 488.6 | $\ldots$ | 487.2 | 483.1 |
| 50 | 0.85 | 15 | 2 | 2 | 4 | 501.6 | 497 | $\ldots$ | 488.2 | 495.7 |
| Note: | This table is presented for illustrative purposes only. |  |  |  |  |  |  |  |  |  |

### 5.2.8 Hypotheses

This section describes the hypotheses that will be tested using the GLM procedure.

### 5.2.8.1 Hypothesis Test 1

Consider the following test scenarios:

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | E |  |
| Distance | H |  |

This hypothesis tests if the proposed methodology (Test Scenario E) to determine the best Layout and shortcuts simultaneously has a lower total WIP than the traditional methodology (Test Scenario H) to determine the best Layout and shortcuts separately. The hypothesis is as follows:
$H A D D_{0}$ There is no statistically significant difference between the total WIP of the solutions: when using the WIP as the design criterion while combining the Layout and shortcut solution procedure, and when using the total distance travelled as the design criterion to first solve the LLDP and then using another algorithm (for example, the greedy heuristic by Johnson et al. (2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, there is no statistically signifi-
cant difference between the total WIP of the solutions as prescribed by Test Scenario E and Test Scenario H.
$H A D_{A}$ The total WIP of the solution when using the WIP as the design criterion while combining the Layout and shortcut solution procedure is less than the total WIP of the solution when using the total distance travelled as the design criterion to first solve the LLDP and then using another algorithm (for example, the greedy heuristic by Johnson et al. (2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, the total WIP of the solution as prescribed by Test Scenario E is less than the total WIP of the solution as prescribed by Test Scenario H.

### 5.2.8.2 Hypothesis Test 2

Consider the following test scenarios:

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | E | F |

Distance

This hypothesis tests if the combined method for determining the Layout and shortcuts simultaneously (Test Scenario E) has a lower total WIP than the separate method for determining the Layout
and shortcuts (Test Scenario F), while using the cost based on the WIP as the design criterion. The hypothesis is as follows:
$H A B_{0}$ There is no statistically significant difference between the total WIP of the solutions: when using the WIP as the design criterion while combining the Layout and shortcut solution procedure, and when using the WIP as the design criterion to first solve the LLDP and then using another algorithm (for example, the greedy heuristic by (A Johnson et al., 2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, there is no statistically significant difference between the total WIP of the solutions as prescribed by Test Scenario E and Test Scenario F.
$H A B A_{A}$ The total WIP of the solution when using the WIP as the design criterion while combining the Layout and shortcut solution procedure is less than the total WIP of the solution when using the WIP as the design criterion to first solve the LLDP and (for example, the greedy heuristic by Johnson et al. (2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, the total WIP of the solution as prescribed by Test

Scenario E is less than the total WIP of the solution as prescribed by Test Scenario F.

### 5.2.8.3 Hypothesis Test 3

Consider the following test scenarios:

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP | E |  |
| Distance | G |  |

This hypothesis tests if the combined method for determining the Layout and shortcuts simultaneously while using the wIP as the design criterion (Test Scenario E) has a lower total WIP than the combined method for determining the Layout and shortcuts simultaneously while using the total distance travelled as the design criterion (Test Scenario G). The hypothesis is as follows:
$H A C_{0}$ There is no statistically significant difference between the total WIP of the solutions: when using the WIP or when using the total distance travelled as the design criterion as the design criterion while combining the Layout and shortcut solution procedure. Simply stated, there is no statistically significant difference between the total WIP of the solutions as prescribed by Test Scenario E and Test Scenario G.
$H A C_{A}$ The total WIP of the solution when using the WIP as the design criterion while combining the Layout and shortcut solution procedure is less than the total WIP of the solution when using the total distance travelled as the design criterion while combining the Layout and shortcut solution procedure. Simply stated, the total WIP of the solution as prescribed by Test Scenario $E$ is less than the total WIP of the solution as prescribed by Test Scenario G.

### 5.2.8.4 Hypothesis Test 4

Consider the following test scenarios:

|  | Combined | Separate |
| :--- | :--- | :--- |
| WIP |  |  |
| Distance | G | H |

This hypothesis tests if the combined method for determining the Layout and shortcuts simultaneously (Test Scenario G) has a lower total WIP than the separate method for determining the Layout and shortcuts (Test Scenario H), while using the cost based on the total distance travelled as the design criterion. The hypothesis is as follows:
$H^{H C D}$ There is no statistically significant difference between the total WIP of the solutions: when using the total distance travelled as the design criteri-
on while combining the Layout and shortcut solution procedure, and when using the total distance travelled as the design criterion to first solve the LLDP and then using another algorithm (for example, the greedy heuristic by Johnson et al. (2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, there is no statistically significant difference between the total WIP of the solutions as prescribed by Test Scenario G and Test Scenario H.
$H_{A C D}$ The total WIP of the solution when using the WIP as the design criterion while combining the Layout and shortcut solution procedure is less than the total WIP of the solution when using the WIP as the design criterion to first solve the LLDP and then using another algorithm separately to solve for the set of shortcuts. Simply stated, the total WIP of the solution as prescribed by Test Scenario G is less than the total WIP of the solution as prescribed by Test Scenario H.

### 5.2.8.5 Hypothesis Test 5

Consider the following test scenarios:

|  | Combined |
| :--- | :--- |
| WIP | Separate |
| Distance | H |

This hypothesis is to test if the separate method for prescribing the shortcuts while using the WIP as the design criterion has a lower total WIP than the separate method for prescribing the shortcuts while using the total distance travelled as the design criterion. The hypothesis is as follows:
$H B D_{0}$ There is no statistically significant difference between the total WIP of the solutions: when using the WIP or when using the total distance travelled as the design criterion to first solve the LLDP and then using another algorithm (for example, the greedy heuristic by Johnson et al. (2009)) to separately solve for the best set of shortcuts for the best layout. Simply stated, there is no statistically significant difference between the total WIP of the solutions as prescribed by Test Scenario $F$ and Test Scenario H.
$H_{B D}$ The total WIP of the solution when using the WIP as the design criterion while combining the Layout and


#### Abstract

shortcut solution procedure is less than the total WIP of the solution as prescribed by using the total distance travelled as the design criterion while combining the Layout and shortcut solution procedure. Simply stated, the total WIP of the solution as prescribed by Test Scenario F is less than the total WIP of the solution as prescribed by Test Scenario H.


### 5.2.9 Fine Tuning the Genetic Algorithm Solution Procedure

The test problem as discussed in $\$ 5.2 .1$ on page 107 will be solved using a genetic algorithm. There have been numerous studies on the best settings for a GA under various conditions. These conditional settings have been discussed in great detail in $\S$ 4.2.1.1 on page 80. Table 5.13 presents the parameters of the GA that can be varied to fine tune the solution algorithm.

Table 5.13: Parameters to vary to fine-tune Solution Algorithm

Level

| Parameter | 1 | 2 | 3 |  |
| :--- | :--- | :--- | :--- | :--- |
| Elitism | Yes | No |  |  |
| Selection Type | Ranked | Tournament |  |  |
| Selection Rate | 0.25 | 0.75 | Uniform $\mathrm{U}(0.24$, | $0.76)$ |
| Crossover Rate | 0.4 | 0.6 | 0.8 |  |
| Mutation Rate | 0.01 | 0.03 | Uniform U(0.01, 0.05) |  |
| Population Size | 30 | 50 | 100 | 5000 |
| Maximum Iterations | 1000 | 3000 | 1000 |  |
| Termination Condition | 100 | 500 |  |  |

The elitism parameter is chosen as suggested by various literature to improve the chances of finding the best solution quickly (Cheng et al., 1996; Deb, Pratap, Agarwal, \& Meyarivan, 2002; Deb \& Goel, 2001; Greenhalgh \& Marshall, 2000; Haupt \& Haupt, 2004). Rudolph (2002) suggests that varying (iteratively or over time) both the selection and mutation rates while implementing elitism improves the chances of finding the globally optimal solution. After rigorous testing, Haupt \& Haupt (2004) too suggest that varying the selection and mutation rate has a greater effect on the solution than varying the crossover rate. Hence, the selection rate is varied iteratively and uniformly between 0.50 and 0.75, while the mutation rate is varied iteratively and uniformly between 0.01 and 0.05 . De Jong (1975) suggests using a crossover rate of 0.6 ; hence, the crossover rate is set to 0.6 .

The literature suggests using a variety of population sizes; small population sizes ( $\mathrm{p} \leq 30$ ) improve the short term performance of the GA, while large population sizes ( $\mathrm{p}>30$ ) improve the long run performance of the GA. There is a tradeoff between the population sizes that can be determined for the problem at hand. With small population sizes the $G A$ converges quickly but could get stuck in a local optima (since fewer solutions are visited) while large population sizes are computationally expensive. Hence testing will be performed to determine the best pop-
ulation size to use among the listed population sizes (30, 50, 100).

### 5.2.9.1 Outcomes of Parameter Sweep for the GA solution Algorithm

The parameters in Table 5.12 were varied over an initial set of problems. Table 5.14 presents the set of parameters that had the best performance in terms of: computational time and quality of solution (lowest WIP).

Table 5.14: Final Parameters for GA solution Algorithm

| Parameter | Level |
| :--- | :--- |
| Elitism | Yes |
| Selection Type | Tournament |
| Selection Rate | Uniform U(0.24, 0.76) |
| Crossover Rate | 0.6 |
| Mutation Rate | 0.03 |
| Population Size | 30 |
| Maximum Iterations | 5000 |
| Termination Condition | 500 |

## 6 ANALYSIS OF RESULTS

This chapter present the results and their interpretations for the testing procedures presented $\$ 5.1$ and $\$ 0$. The discussion of the outcomes are provided in $\$ 7$ from page 173. All the analysis was performed in SAS 9.2 using the GLM procedure. All of the tests are performed at the 95\% confidence level.

### 6.1 Results for the Expected Value of WIP at the Input Station testing

This section presents the results and their interpretations for the testing procedure presented in $\$ 5.1$, i.e., testing the analytical estimate for the total WIP at the Input Stations of a conveyor.

It should be noted that the test values for $\rho_{\text {LCMHS }}=0.9$ were omitted from the GLM analysis. For $\rho_{L C M H S}=0.9$, the analytical model does not provide accurate estimates of the total WIP at the input stations. This is not surprising since many of the analytical estimates for queueing models are known to be less accurate at higher levels of utilization requiring alternative formulations at those levels (Buzacott \& Shanthikumar, 1993; Hopp \& Spearman, 2000). It was intended that the proposed analytical estimate would adequately model the total WIP at the input stations for all levels of utilization; but the inability to
capture the dynamics of the system at utilization levels higher that 0.9 warrants further investigation and is included as one of the items on the list of future work. This section presents all the results (even those for the utilization level 0.9) to further validate the exclusion of test values from the GLM analysis.

For each layout, the total WIP at the input stations from the testing (simulation model and analytical estimate) is presented in Appendix $C$ on page 194. For each layout the absolute relative error between the simulation model and the analytical estimate is computed for each replication and listed in Appendix $D$ on page 198. The absolute relative error is given by

$$
\begin{equation*}
\text { Absolute Relative Error }=\frac{\left|W I P_{\text {Sinulation }}-W I P_{\text {Analytical }}\right|}{W I P_{\text {Simulation }}} \tag{58}
\end{equation*}
$$

Using the data from Appendix $C$, summary statistics on the efficacy of the analytical estimate are presented. In Table 6.1, the absolute relative errors \{using equation (58)\} are presented. The first row represents the absolute relative errors in the analytical estimate for each layout for all the levels of utilization. Each subsequent row presents the absolute relative errors in the analytical estimate for each Layout at the specified level of utilization.

The overall performance of the analytical estimate for the total WIP at the input stations of a conveyor is well within the acceptable range of error as presented in past studies (Atmaca, 1994; Y Bozer \& Hsieh, 2004, 2005; Hsieh \& Bozer, 2005; Nazzal et al., 2010, 2008) Furthermore, the analytical model's accuracy is higher at lower utilization levels of the conveyor.

Table 6.1: Average Absolute relative error for each Layout at different levels of $\rho_{L C M H S}$

|  | Absolute relative error |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{\text {LCMHS }}$ | Layout X | Layout Y | Layout | Z |
| All | $9.54 \%$ | $10.06 \%$ | $7.71 \%$ |  |
| 0.15 | $1.51 \%$ | $1.17 \%$ | $7.90 \%$ |  |
| 0.3 | $5.07 \%$ | $4.33 \%$ | $5.14 \%$ |  |
| 0.45 | $4.37 \%$ | $4.63 \%$ | $1.90 \%$ |  |
| 0.6 | $6.45 \%$ | $7.11 \%$ | $4.12 \%$ |  |
| 0.75 | $11.59 \%$ | $12.55 \%$ | $6.03 \%$ |  |
| 0.9 | $28.28 \%$ | $30.56 \%$ | $21.20 \%$ |  |

Table 6.2 provides another perspective of the absolute relative errors of the results for each Layout based on levels of $c_{a}^{2}$. Again, the overall performance of the analytical estimate for the total WIP at the input stations of a conveyor for different levels of $c_{a}^{2}$ is well within the acceptable range of error. Also, when $\rho_{\text {LCMHS }}=0.9$ is excluded from the calculations the performance of the analytical estimate is very good and excels at $c_{a}^{2}=1$ , i.e., Markovian arrival process.

Table 6.2: Average Absolute relative error for each layout at different levels of $\mathrm{Ca}^{2}$

Average Absolute relative error for Layout X Layout $Y$ Layout Z

|  | Layout X |  | Layout Y |  | Layout Z |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $c_{a}^{2}$ | All | $\rho<0.9$ | All | $\rho<0.9$ | All | $\rho<0.9$ |
| 0.5 | $10.44 \%$ | $10.07 \%$ | $8.89 \%$ | $9.83 \%$ | $7.57 \%$ | $6.81 \%$ |
| 0.77 | $6.65 \%$ | $5.18 \%$ | $6.99 \%$ | $4.35 \%$ | $5.98 \%$ | $5.61 \%$ |
| 1 | $7.00 \%$ | $2.65 \%$ | $7.68 \%$ | $2.45 \%$ | $7.29 \%$ | $4.65 \%$ |
| 1.23 | $9.70 \%$ | $3.84 \%$ | $11.51 \%$ | $5.12 \%$ | $7.94 \%$ | $3.78 \%$ |
| 1.5 | $13.94 \%$ | $7.25 \%$ | $15.21 \%$ | $8.03 \%$ | $9.80 \%$ | $4.24 \%$ |

Next, the average errors for each layout at different levels of conveyor utilization and arrival variability are presented in Appendix E on page 202.

Figure 6.1, Figure 6.2, and Figure 6.3 illustrate the average error for each Layout at each level of $c_{a}^{2}$. Notably, when $c_{a}^{2} \leq 1$ the analytical estimate is consistently less than the simulation estimate while the converse is true when $c_{a}^{2}>1$. Clearly, the analytical estimate does not perform well when $\rho_{\text {LCMHS }}=0.9$. Conversely, the analytical estimate performs better at lower conveyor utilizations.

## Layout X



Figure 6.1: Average Error for Layout X

Layout $Y$


Figure 6.2: Average Error for Layout Y

## Layout Z



Figure 6.3: Average Error for Layout Z
Given the high level overview of the results, further probing of the data is warranted. The GLM analysis performed in the next section probes the results and provides statistical validation of some of the observances made in the high level overview while simultaneously determining relationships among various parameters and their overall effect on the total WIP at the input stations of the conveyor. The details of the design of the GLM analysis have been provided in § 5.1.4 on page 97.

### 6.2 GLM Analysis for the Expected Value of WIP at the Input Station

It is important to note that for each layout (X, Y, and Z) a separate GLM analysis is performed. For each layout, only the highlights of the GLM analysis are presented in this section.

For Layout $X$, the exact output of the GLM analysis procedure from SAS is presented in Appendix $F$ on page 203. For Layout $Y$, the exact output of the GLM analysis procedure from SAS is presented in Appendix $G$ on page 213. For Layout $Z$, the exact output of the GLM analysis procedure from SAS is presented in Appendix $H$ on page 222.

### 6.2.1 Analysis of Variance

The following description is adapted from SAS Institute Inc (2010). In the analysis of variance (ANOVA), a dependent variable, i.e. WIP (total WIP at the input stations), is measured under experimental conditions identified by classification variables, known as independent variables, as described in Table 5.6 on page 101.

### 6.2.1.1 ANOVA for Layout x

Table 6.3 presents the analysis of variance of the total WIP at the input stations.

Table 6.3: ANOVA of the WIP at the Input Stations for Layout X

| Source | DF | Sum of <br> Squares | Mean <br> Square | Falue | Pr $>$ F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 17 | 12761.02 | 750.648 | 2931 | $<.0001$ |
| Error | 482 | 123.4226 | 0.25606 |  |  |
| Corrected Total | 499 | 12884.44 |  |  |  |


| R-Square | Coeff Var | Root MSE | WIP Mean |
| :--- | :--- | :--- | :--- |
| 0.9902 | 12.56 | 0.509938 | 4.059303 |


|  |  | Type I | Mean | $F$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Source | DF | SS | Square | Value | Pr $>$ |
| Utilization $\left(\rho_{\text {LCMHS }}\right)$ | 4 | 12708.34 | 3177.086 | 12407 | $<.0001$ |
| SCV $\left(c_{a}^{2}\right)$ | 4 | 24.7323 | 6.18308 | 24.15 | $<.0001$ |
| M | 1 | 0.25341 | 0.25341 | 0.99 | 0.32 |
| SCVM | 4 | 24.7323 | 6.18308 | 24.15 | $<.0001$ |
| RHOM | 4 | 2.95521 | 0.7388 | 2.89 | 0.022 |

To summarize:

- The overall fit of the model is significant and accounts for $99.02 \%$ of the error. Hence, the comparison of means based on this model as presented henceforth is considered reliable.


### 6.2.1.2 ANOVA for Layout $Y$

Table 6.4 presents the analysis of variance of the total WIP at the input stations.

Table 6.4: ANOVA of the WIP at the Input Stations for Layout $Y$

| Source | DF | Sum of <br> Squares | Mean <br> Square | Value | Pr $>$ F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 17 | 13732.3 | 807.7824 | 2550 | $<.0001$ |
| Error | 482 | 152.7002 | 0.31681 |  |  |
| Corrected Total | 499 | 13885 |  |  |  |


| R-Square | Coeff Var | Root MSE | WIP Mean |
| :--- | :--- | :--- | :--- |
| 0.989 | 13.38 | 0.562855 | 4.20814 |


|  | Type I |  | Mean <br> Source | F |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| DF | SS | Square | Value | Pr $>$ F |  |
| Utilization $\left(\rho_{\text {LCMHS }}\right)$ | 4 | 13652.73 | 3413.181 | 10774 | $<.0001$ |
| SCV $\left(c_{a}^{2}\right)$ | 4 | 31.85144 | 7.96286 | 25.13 | $<.0001$ |
| M | 1 | 2.95744 | 2.95744 | 9.34 | 0.002 |
| SCVM | 4 | 31.85144 | 7.96286 | 25.13 | $<.0001$ |
| RHOM | 4 | 12.91498 | 3.22874 | 10.19 | $<.0001$ |

To summarize:

- The overall fit of the model is significant and accounts for $98.9 \%$ of the error. Hence, the comparison of means based on this model as presented henceforth is considered to be reliable.


### 6.2.1.3 ANOVA for Layout Z

Table 6.5 presents the analysis of variance of the total WIP at the input stations.

Table 6.5: ANOVA of the WIP at the Input Stations for Layout $Z$

| Source | DF | Sum of <br> Squares | Mean <br> Square | Falue | Pr $>$ F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 17 | 14966.52 | 880.3834 | 13712 | $<.0001$ |
| Error | 482 | 30.94774 | 0.06421 |  |  |
| Corrected Total | 499 | 14997.47 |  |  |  |


| R-Square | Coeff Var | Root MSE | WIP Mean |
| :--- | :--- | :--- | :--- |
| 0.998 | 6.094 | 0.26801 | 4.398252 |


|  | Type I |  | Mean | F |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Source | DF | SS | Square | Value | Pr $>$ F |
| Utilization $\left(\rho_{\text {LCMHS }}\right)$ | 4 | 14950.22 | 3737.554 | 58211 | $<.0001$ |
| SCV $\left(c_{a}^{2}\right)$ | 4 | 5.20085 | 1.30021 | 20.25 | $<.0001$ |
| M | 1 | 1.9404 | 1.9404 | 30.22 | $<.0001$ |
| SCVM | 4 | 5.20085 | 1.30021 | 20.25 | $<.0001$ |
| RHOM | 4 | 3.96128 | 0.99032 | 15.42 | $<.0001$ |

To summarize:

- The overall fit of the model is significant and accounts for $99.8 \%$ of the error. Hence, the comparison of means based on this model as presented henceforth is considered to be reliable.


### 6.2.2 Comparison of Means

Here, for each of the independent variables (main effects) used for each level of the main effect, the means of the dependent variable (WIP) can be compared using REGWQ and Tukeys multiple comparison test (SAS Institute Inc, 2010). In other words, for each main effect the comparison of means test elucidates any difference in the means of the dependent variable for each level of the main effect, thereby clarifying the influence (or lack thereof) of the main effects on the dependent variable; while controlling for Type I and Type II errors.

### 6.2.2.1 Variable: Utilization of Conveyor ( $\rho_{\text {LСмНS }}$ )

In the tables, the dependent variable WIP is compared across the different levels of the main effect $\rho_{\text {LCMHS }}$ using REGWQ and Tukeys multiple comparison tests for each layout. It should be noted that means with the same letter (under the grouping columns) are not significantly different. This test is performed to ensure the tested system is performing as expected; it serves to validate the tested system.

Table 6.6: REGWQ and Tukeys multiple comparison test for $\rho_{\text {LCMH }}$ for Layout X

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{\text {LCMHS }}$ | N | Mean WIP | REGWQ | Tukey |
| 0.75 | 100 | 13.67 | A | A |
| 0.6 | 100 | 4.45 | B | B |
| 0.45 | 100 | 1.59 | C | C |
| 0.3 | 100 | 0.49 | D | D |
| 0.15 | 100 | 0.10 | E | E |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.7: REGWQ and Tukeys multiple comparison test for $\rho_{\text {LCMHS }}$ for Layout Y

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{\text {LCMHS }}$ | N | Mean WIP | REGWQ | Tukey |
| 0.75 | 100 | 13.67 | A | A |
| 0.6 | 100 | 4.45 | B | B |
| 0.45 | 100 | 1.59 | C | C |
| 0.3 | 100 | 0.49 | D | D |
| 0.15 | 100 | 0.10 | E | E |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.8: REGWQ and Tukeys multiple comparison test for $\rho_{\text {LCMHS }}$ for Layout Z

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{\text {LCMHS }}$ | N | Mean WIP | REGWQ | Tukey |
| 0.75 | 100 | 13.67 | A | A |
| 0.6 | 100 | 4.45 | B | B |
| 0.45 | 100 | 1.59 | C | C |
| 0.3 | 100 | 0.49 | D | D |
| 0.15 | 100 | 0.10 | E | E |
| Note: These tests control the Type I experimentwise error rate |  |  |  |  |
| * Means with the same letter are not significantly different |  |  |  |  |

To summarize:

- For each layout, at each level of $\rho_{\text {LCMHS }}$ there is a significant difference in the total WIP at the input stations
- For each layout, as $\rho_{\text {LCMHS }}$ increases the total WIP at the input stations increase


### 6.2.2.2 Variable: Squared Coefficient of variation of Arrivals $\left(C_{a}{ }^{2}\right)$

In the tables, the dependent variable WIP is compared across the different levels of the main effect $c_{a}^{2}$ using REGWQ and Tukeys multiple comparison tests for each layout. It should be noted that means with the same letter (under the grouping columns) are not significantly different. This test is performed to ensure the system tested is performing as expected; it serves to validate the system tested.

Table 6.9: REGWQ and Tukeys multiple comparison test for $\mathrm{c}_{\mathrm{a}}{ }^{2}$ for Layout X

| $c_{a}^{2}$ | N | Mean | WIP | Grouping* |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | REGWQ |  |  |  |
| 1.5 | 100 | 4.38 |  | A |  | A |  |
| 1.23 | 100 | 4.20 |  |  | B | A | B |
| 1 | 100 | 4.06 |  | C | B | C | B |
| 0.77 | 100 | 3.91 |  | C | D | C | D |
| 0.5 | 100 | 3.74 |  |  | D |  | D |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.10: REGWQ and Tukeys multiple comparison test for $\mathrm{C}_{\mathrm{a}}{ }^{2}$ for Layout Y

|  |  |  | Grouping* |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $c_{a}^{2}$ | N | Mean WIP | REGWQ | Tukey |  |  |
| 1.5 | 100 | 4.57 | A |  | A |  |
| 1.23 | 100 | 4.37 |  | B | A | B |
| 1 | 100 | 4.21 | C | B | C | B |
| 0.77 | 100 | 4.04 | C | D | C | D |
| 0.5 | 100 | 3.85 |  | D |  | D |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.11: REGWQ and Tukeys multiple comparison test for $\mathrm{C}_{\mathrm{a}}{ }^{2}$ for Layout Z

|  |  |  | Grouping* |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $c_{a}^{2}$ | N | Mean WIP | REGWQ | Tukey |  |  |
| 1.5 | 100 | 4.56 | A |  | A |  |
| 1.23 | 100 | 4.46 |  | B | A | B |
| 1 | 100 | 4.39 | C | B | C | B |
| 0.77 | 100 | 4.33 | C | D | C | D |
| 0.5 | 100 | 4.26 |  | D |  | D |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

To summarize:

- For each layout, for adjacent levels of $c_{a}^{2}$ there is no significant difference in the total WIP at the input stations
- For each layout, for non-adjacent levels of $c_{a}^{2}$ there is a significant difference in the total WIP at the input stations
- For each layout, as $c_{a}^{2}$ increases the total WIP at the input stations increase


### 6.2.2.3 Variable: WIP Data Source - Simulation or Analytical Estimate (M)

In the tables, the dependent variable WIP is compared across the different levels of the main effect ' $M$ ' using REGWQ and Tukeys multiple comparison tests for each layout. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect 'M' is introduced to test if there is a significant difference between the simulation output ( $M=1$ ) and the analytical estimate $(M=0)$.

Table 6.12: REGWQ and Tukeys multiple comparison test for $M$ for Layout X

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| M | N | Mean WIP | REGWQ | Tukey |
| 1 | 250 | 4.08 | A | A |
| 0 | 250 | 4.04 | A | A |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.13: REGWQ and Tukeys multiple comparison test for $M$ for Layout Y

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| M | N | Mean WIP | REGWQ | Tukey |
| 1 | 250 | 4.29 | A | A |
| 0 | 250 | 4.13 | B | B |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.14: REGWQ and Tukeys multiple comparison test for $M$ for Layout Z

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $M$ | N | Mean WIP | REGWQ | Tukey |
| 1 | 250 | 4.46 | A | A |
| 0 | 250 | 4.34 | B | B |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

To summarize:

- For Layout $X$, there is no significant difference between the analytical estimate and the simulation estimate of the mean total WIP at the input stations
 between the analytical estimate and the simulation estimate of the mean total WIP at the input stations
- For each layout, the total WIP estimate at the input stations from simulation $(M=1)$ is higher than the total WIP estimate at the input stations from the analytical estimate $(M=0)$


### 6.2.2.4 Variable: Interaction between $M$ and $C_{a}{ }^{2}$ (SCVM)

In the tables, the dependent variable WIP is compared across the different levels of the main effect 'SCVM' using REGWQ and Tukeys multiple comparison tests for each layout. It should be noted that means with the same letter (under the grouping columns)
are not significantly different. It is introduced to test if there is a significant difference between the simulation output ( $M=1$ ) and the analytical estimate $(M=0)$ at different levels of $c_{a}^{2}$.

Table 6.15: REGWQ and Tukeys multiple comparison test for SCVM for Layout X


Table 6.16: REGWQ and Tukeys multiple comparison test for SCVM for Layout $Y$

|  |  | Grouping* |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| SCVM | N | Mean WIP | REGWQ | Tukey |  |
| 9 | 50 | 5.02 | A | A |  |
| 7 | 50 | 4.62 | B |  | B |
| 5 | 50 | 4.28 | C | C | B |
| 2 | 50 | 4.13 | C | C |  |
| 4 | 50 | 4.13 | C | C |  |
| 6 | 50 | 4.13 | C | C |  |
| 8 | 50 | 4.13 | C | C |  |
| 10 | 50 | 4.13 | C | C |  |
| 3 | 50 | 3.94 | C | C |  |
| 1 | 50 | 3.57 | D |  | D |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.17: REGWQ and Tukeys multiple comparison test for SCVM for Layout Z

| SCVM | N | Mean WIP | Grouping* |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | REGWQ |  |  |  |
| 9 | 50 | 4.65 | A |  | A |  |
| 2 | 50 | 4.46 |  | B |  | B |
| 4 | 50 | 4.46 |  | B |  | B |
| 6 | 50 | 4.46 |  | B |  | B |
| 8 | 50 | 4.46 |  | B |  | B |
| 10 | 50 | 4.46 |  | B |  | B |
| 7 | 50 | 4.45 |  | B |  | B |
| 5 | 50 | 4.31 | C | B | C | B |
| 3 | 50 | 4.20 | C | D | C | D |
| 1 | 50 | 4.06 |  | D |  | D |

To summarize:

- For Layout $X$ and Layout $Y$, there is no significant difference in the total WIP at the input stations from the analytical estimate and from the simulation model when $c_{a}^{2}$ is 0.77 and 1
- For Layout Z, there is no significant difference in the total WIP at the input stations from the analytical estimate and from the simulation model when $c_{a}^{2}$ is 1 and 1.23


### 6.2.2.5 Variable: Interaction between $M$ and $\rho_{\text {LCMHS }}$ (RHOM)

In the tables, the dependent variable WIP is compared across the different levels of the main effect 'RHOM' using REGWQ and Tukeys multiple comparison tests for each layout. It should be noted that means with the same letter (under the grouping columns) are not significantly different. It is introduced to test if there is a significant difference between the simulation output ( $\mathrm{M}=1$ ) and the analytical estimate ( $\mathrm{M}=0$ ) at different levels of conveyor utilization $\left(\rho_{\text {LCMHS }}\right)$.

Table 6.18: REGWQ and Tukeys multiple comparison test for RHOM for Layout X

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| RHOM | N | Mean WIP | REGWQ | Tukey |
| 9 | 50 | 13.85 | A | A |
| 10 | 50 | 13.50 | B | B |
| 8 | 50 | 4.48 | C | C |
| 7 | 50 | 4.41 | C | C |
| 6 | 50 | 1.60 | D | D |
| 5 | 50 | 1.57 | D | D |
| 4 | 50 | 0.51 | E | E |
| 3 | 50 | 0.48 | E | E |
| 1 | 50 | 0.10 | F | F |
| 2 | 0.10 | F | F |  |
| Note: These tests control the Type I experimentwise error rate |  |  |  |  | * Means with the same letter are not significantly different

Table 6.19: REGWQ and Tukeys multiple comparison test for RHOM for Layout $Y$

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| RHOM | N | Mean WIP | REGWQ | Tukey |
| 9 | 50 | 14.57 | A | A |
| 10 | 50 | 13.77 | B | B |
| 8 | 50 | 4.61 | C | C |
| 7 | 50 | 4.60 | C | C |
| 6 | 50 | 1.65 | D | D |
| 5 | 50 | 1.64 | D | D |
| 4 | 50 | 0.52 | E | E |
| 3 | 50 | 0.50 | E | E |
| 1 | 50 | 0.10 | F | F |
| 2 | 50 | 0.10 | F | F |

Note: These tests control the Type I experimentwise error rate * Means with the same letter are not significantly different

Table 6.20: REGWQ and Tukeys multiple comparison test for RHOM for Layout Z

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| RHOM | N | Mean WIP | REGWQ | Tukey |
| 9 | 50 | 15.06 | A | A |
| 10 | 50 | 14.60 | B | B |
| 8 | 50 | 4.87 | C | C |
| 7 | 50 | 4.70 | D | D |
| 6 | 50 | 1.76 | E | E |
| 5 | 50 | 1.72 | E | E |
| 4 | 50 | 0.54 | F | F |
| 3 | 50 | 0.52 | F | F |
| 1 | 50 | 0.10 | G | G |
| 2 | 50 | 0.10 | G | G |
| Note: These tests control the Type I experimentwise error rate |  |  |  |  |
| * Means with the same letter are not significantly different |  |  |  |  |

To summarize:

- For Layout $X$ and Layout $Y$, there is no significant difference in the total WIP at the input stations from the analytical estimate and simulation model when $\rho_{\text {LCMHS }}$ is 0.15 , $0.3,0.45$, and 0.6
- For Layout $Z$, there is no significant difference in the total WIP at the input stations from the analytical estimate and simulation model when $\rho_{\text {LCMHS }}$ is $0.15,0.3$, and 0.45


### 6.2.3 Evaluation of Hypotheses

Consider the main effect 'M', which is an indicator variable specifying where the output is from the simulation model ( $\mathrm{M}=1$ ) of from the analytical model $(M=0)$. The results from the GLM
analysis as presented in $\$ 6.2 .2 .3$, indicate that the analytical estimate and the simulation model are significantly different from each other when compared over all levels of utilization and arrival process variability ( $c_{a}^{2}$ ). Hence, from a statistical perspective the analytical estimate for the total WIP cannot be considered a general methodology that holds true over all levels of utilization and $c_{a}^{2}$. With this in mind, one could make the statement with respect to hypothesis test 1 as presented in $\S$ 5.1.5.1:

- H10 (Null hypothesis for Hypothesis Test 1) is rejected However, from a practical perspective, the results as presented in Table 6.1 show that the average absolute relative error of the proposed analytical estimate while excluding conveyor utilization greater than or equal to 0.75 is $4.47 \%$. This error is well within the acceptable range of error as presented in past studies (Atmaca, 1994; Y Bozer \& Hsieh, 2004, 2005; Hsieh \& Bozer, 2005; Nazzal et al., 2010, 2008)

Consider the interaction between the level of utilization and M, i.e., the main effect 'RHOM'. The results from the GLM analysis, as presented in $\$ 6.2 .2 .5$, indicate that the analytical estimate and the simulation model are not significantly different from each other when the conveyor utilization is less than 0.5.

Hence, one could make the statements with respect to hypothesis test 2 as presented in $\S 5.1 .5 .2$ as follows:

- Given that the utilization of the conveyor is less than 0.5; H20 (Null hypothesis for Hypothesis Test 2) is not rejected
- Given that the utilization of the conveyor is greater than 0.5; H20 (Null hypothesis for Hypothesis Test 2) is rejected Consider the interaction between $c_{a}^{2}$ and $M$, i.e., the main effect 'SCVM'. The results from the GLM analysis, as presented in $\S$ 6.2.2.4, indicate that the analytical estimate and the simulation model are not significantly different from each other when $c_{a}^{2}$ is 1.

Hence, one could make the statements:

- Given that the utilization of the conveyor is less than 0.9; H30 (Null hypothesis for Hypothesis Test 3 as presented in § 5.1.5.3) is rejected
- Given that the utilization of the conveyor is less than 0.9; H40 (Null hypothesis for Hypothesis Test 4 as presented in § 5.1.5.4) is not rejected
- Given that the utilization of the conveyor is less than 0.9; H50 (Null hypothesis for Hypothesis Test 5 as presented in § 5.1.5.5) is rejected


### 6.3 Results for the Looped Layout Design Problem testing

This section presents the results and their interpretations for the testing procedure as presented § 0, i.e., testing the efficacy of the proposed methodology to determine the layout of a LLMF with an LCMHS that has shortcuts such that it has the least WIP amongst the alternative (traditional) methods used to determine the layout of a LLMF.

The resultant $W I P$ for the best solutions for each replication of each test problem from the testing is presented in Appendix $I$ on page 231. For the best solutions from the testing, the resulting number of shortcuts is presented in Appendix $J$ on page 237, the resulting number of iterations needed to find the best solutions is presented in Appendix $K$ on page 243 , and the resulting time (in minutes) needed to find the best solutions is presented in Appendix $L$ on page 249. The entire list of each solution (machine and shortcut assignment) will be available upon request ${ }^{2}$. The proceeding tables present a high level of summary analysis of the data from multiple perspectives.

[^0]Table 6.21 presents a summary of the results from the perspective of the type of scenario. Notably, Scenario $E$ has the lowest WIP. It is also interesting to note that Scenarios $A$ and $C$ (combined shortcut methodology) require fewer iterations to reach the best solution but take longer to solve as a result of the additional computation per iteration (to determine the shortcuts). Lastly, the choice of scenario does not seem to have an effect on the number of shortcuts for the best solutions.

Table 6.21: LLDP Results Summary with regards to Scenario

|  | Average |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| Scenario | WIP | $\#$ Shortcuts | $\#$ Iterations | Time (min) |  |
| E | 151.50 | 12.31 | 1164.34 | 72.35 |  |
| F | 293.12 | 12.18 | 1419.97 | 43.57 |  |
| G | 165.68 | 10.94 | 1182.63 | 72.70 |  |
| H | 293.57 | 11.57 | 1384.09 | 39.52 |  |

Table 6.22 presents a summary of the results from the perspective of the utilization of the conveyor $\left(\rho_{L C M H S}\right)$. As expected, when the utilization of the conveyor increases, the WIP increases. It is interesting to note that as $\rho_{L C M H S}$ increases, the number of shortcuts in the LLMF increases. However, $\rho_{L C M H S}$ does not seem to have an effect on the number of iterations and the time required to reach the best solution.

Table 6.23 presents a summary of the results from the perspective of the turntime of the turntables. Contrary to expecta159
tions, the turntime does not seem to have an effect on the WIP in the LLMF, the number of shortcuts, the number of iterations, or the time required to reach the best solution.

Table 6.22: LLDP Results Summary with regards to $\rho_{\text {LCMHS }}$

Average

|  | $\rho_{\text {LCMHS }}$ | WIP | $\#$ Shortcuts | $\#$ Iteration |
| :--- | :--- | :--- | :--- | :--- |
| Time (min) |  |  |  |  |
| 0.15 | 74.66 | 9.59 | 1277.41 | 56.75 |
| 0.5 | 230.41 | 12.11 | 1296.23 | 60.25 |
| 0.85 | 372.84 | 13.54 | 1289.62 | 54.11 |

Table 6.23: LLDP Results Summary with regards to $t$

|  | Average |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| $t$ | WIP | $\#$ Shortcuts | $\#$ Iteration | Time (min) |  |
| 0 | 222.27 | 11.74 | 1286.98 | 56.98 |  |
| 7 | 225.73 | 11.71 | 1297.76 | 57.57 |  |
| 15 | 229.92 | 11.79 | 1278.53 | 56.56 |  |

Table 6.24 presents a summary of the results from the perspective of the ratio between the cost to install a shortcut and the cost of $s$ single load ( $\Omega$ ). As expected, when $\Omega$ increases the WIP increases and the number of shortcuts decreases. $\Omega$ does not seem to have an effect on the number of iterations or the time required to reach the best solution.

Table 6.24: LLDP Results Summary with regards to $\Omega$
Average

|  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
|  | WIP | $\#$ Shortcuts | $\#$ Iteration | Time (min) |  |
| 0.1 | 203.02 | 21.10 | 1238.19 | 54.47 |  |
| 1 | 204.93 | 16.70 | 1273.45 | 55.49 |  |
| 10 | 228.88 | 6.45 | 1283.09 | 54.64 |  |
| 50 | 267.05 | 2.74 | 1356.29 | 63.53 |  |

Table 6.25 presents a summary of the results from the perspective of the optimization criteria $(\theta)$. It seems that minimizing the $\operatorname{WIP}(\theta=1)$, as opposed to minimizing the total distance travelled $(\theta=2)$ yields LLMFs with lower WIP and more shortcuts. $\theta$ does not seem to have an effect on the number of iterations or the time required to reach the best solution.

Table 6.25: LLDP Results Summary with regards to $\theta$

|  | Average |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\theta$ | WIP | $\#$ Shortcuts | \# Iteration | Time (min) |  |
| 1 | 222.31 | 12.24 | 1292.15 | 57.96 |  |
| 2 | 229.63 | 11.25 | 1283.36 | 56.11 |  |

Table 6.26 presents a summary of the results from the perspective of the shortcut criteria (S). It seems that Using the combined method to determine the shortcuts $(S=1)$, as opposed to separate method to determine the shortcuts $(S=2)$, yields LLMFs with lower WIP. Also, as noticed earlier the combined shortcut methodology requires fewer iterations to reach the best solution but takes longer to solve as a result of the additional computa-
tions per iteration (to determine the shortcuts). $S$ does not seem to have an effect on the number of shortcuts for the best solutions.

Table 6.26: LLDP Results Summary with regards to $S$

Average

|  | Average |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| S | WIP | $\#$ Shortcuts | \# Iteration | Time (min) |
| 1 | 158.59 | 11.62 | 1173.48 | 72.53 |
| 2 | 293.35 | 11.87 | 1402.03 | 41.55 |

Given the high level overview of the results further probing of the data is warranted. The GLM analysis performed in the next section probes the results and provides statistical validation of some of the observances made in the high level overview while simultaneously determining relationships among various parameters and their overall effect on the total WIP in the LLMF. The details of the design of the GLM analysis have been provided in § 5.2 .6 on page 122.

### 6.4 GLM Analysis for the Looped Layout Design Problem

 In this case the dependent variable, i.e. WIP is determined for each test problem using equation (52) on page 111 while the independent variables are as described in Table 5.11 on page 123. The exact output of the GLM procedure from $S A S$ is presented inAppendix $M$ on page 255; however, the highlights of the results are presented in this section.

### 6.4.1 Analysis of Variance (ANOVA)

Table 6.27 presents the analysis of variance of the WIP for the LLDP test problem. The following description is adapted from SAS Institute Inc (2010). In the analysis of variance (ANOVA), a dependent variable, i.e. WIP, is measured under experimental conditions identified by classification variables, known as independent variables.

Table 6.27: ANOVA of the WIP for the LLDP

|  |  | Sum of | Mean | $F$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Source | DF | Squares | Square | Value | Pr $>\mathrm{F}$ |
| Model | 10 | 28919642 | 2891964 | 944.1 | $<.0001$ |
| Error | 1429 | 4377221 | 3063.14 |  |  |
| Corrected Total | 1439 | 33296863 |  |  |  |


| R-Square | Coeff Var | Root MSE | WIP Mean |
| :--- | :--- | :--- | :--- | :--- |
| 0.869 | 24.5 | 55.3456 | 225.9037 |


| Source | DF | $\begin{aligned} & \text { Type I } \\ & \text { SS } \end{aligned}$ | Mean Square | F <br> Value | Pr $>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Shortcut Cost/WIP Cost ( $\Omega$ ) | 3 | 963365.6 | 321121.9 | 104.8 | $<.0001$ |
| Utilization $\left(\rho_{L C M H S}\right)$ | 2 | 21381919 | 10690959 | 3490 | $<.0001$ |
| Turntable Turn Time ( $t$ ) | 2 | 13352.99 | 6676.49 | 2.18 | 0.114 |
| Optimization Criteria ( $\theta$ ) | 1 | 19946.72 | 19946.72 | 6.51 | 0.011 |
| Shortcut Criteria (S) | 1 | 6524756 | 6524756 | 2130 | <.0001 |
| Scenario ( $\theta S$ ) | 1 | 16302.16 | 16302.16 | 5.32 | 0.021 |

To summarize:

- The overall fit of the model is significant and accounts for $86.9 \%$ of the error
- $\Omega$ has a significant effect on the WIP for the solutions of the LLDP test problems
- $\rho_{\text {LCMHS }}$ has a significant effect on the WIP for the solutions of the LLDP test problems
- does not have a significant effect on the WIP for the solutions of the LLDP test problems
- $\Theta$ has a significant effect on the WIP for the solutions of the LLDP test problems
- $S$ has a significant effect on the WIP for the solutions of the LLDP test problems
- $\Theta S$ has a significant effect on the WIP for the solutions of the LLDP test problems

The next step is to compare the means of the dependent variable (WIP) for each of the independent variables

### 6.4.2 Comparison of Means

Here, for each main effect the comparison of means tests (REGWQ and Tukeys multiple comparison test) elucidates any difference in the means of the dependent variable (WIP) for each level of the main effect, thereby clarifying the influence (or lack
thereof) of the main effects on the dependent variable (WIP); while controlling for Type I and Type II error.

### 6.4.2.1 Variable: Shortcut Cost / WIP Cost ( $\Omega$ )

In Table 6.28, the dependent variable WIP is compared across the different levels of the main effect $\Omega$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect ' $\Omega$ ' is introduced to test if there is a significant difference in the WIP on the LLMF for different levels of $\Omega$.

Table 6.28: REGWQ and Tukeys multiple comparison test for $\Omega$ for the LLDP

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\Omega$ | N | Mean WIP | REGWQ | Tukey |
| 50 | 360 | 267.05 | A | A |
| 10 | 360 | 228.88 | B | B |
| 1 | 360 | 204.67 | C | C |
| 0.1 | 360 | 203.02 | C | C |

Note: These tests control the Type I experiment-wise error rate * Means with the same letter are not significantly different

To summarize:

- When $\Omega \leq 1$ there is no significant difference in the WIP of the solutions
- When $\Omega>1$ there is significant difference in the WIP of the solutions.
- As the ratio of the cost of the shortcut to the cost of the WIP increases, the WIP of the best solutions increases.


### 6.4.2.2 Variable: Utilization of Conveyor ( $\rho_{\text {LСмНS }}$ )

In Table 6.29, the dependent variable WIP is compared across the different levels of the main effect $\rho_{\text {LCMHS }}$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect ' $\rho_{L C M H S}$ ' is introduced to test if there is a significant difference in the WIP on the LLMF for different levels of $\rho_{\text {LCMHS }}$.

Table 6.29: REGWQ and Tukeys multiple comparison test for $\rho_{\text {LCMHS }}$ for the LLDP

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\rho_{\text {LCMHS }}$ | N | Mean WIP | REGWQ | Tukey |
| 0.85 | 480 | 267.05 | A | A |
| 0.5 | 480 | 228.88 | B | B |
| 0.15 | 480 | 203.02 | C | C |

Note: These tests control the Type I experiment-wise error rate * Means with the same letter are not significantly different

To summarize:

- There is a significant difference in the WIP of the solutions for the different levels of $\rho_{L C M H S}$
- As $\rho_{\text {LCMHS }}$ increases the WIP of the best solutions increases


### 6.4.2.3 Variable: Turntable Turn Time (t)

In Table 6.30, the dependent variable WIP is compared across the different levels of the main effect $t$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect 't' is introduced to test if there is a significant difference in the WIP on the LLMF for different levels of 't'.

Table 6.30: REGWQ and Tukeys multiple comparison test for $t$ for the LLDP

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| $t$ | $N$ | Mean WIP | REGWQ | Tukey |
| 15 | 480 | 229.92 | A | A |
| 7 | 480 | 225.73 | A | A |
| 0 | 480 | 222.27 | A | A |

Note: These tests control the Type I experiment-wise error rate * Means with the same letter are not significantly different

To summarize:

- There is no significant difference in the WIP of the solutions for the different levels of $t$


### 6.4.2.4 Variable: Optimization Criteria ( $\theta$ )

In Table 6.31, the dependent variable WIP is compared across the different levels of the main effect $\theta$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect ' $\theta$ ' is introduced to test if there is a significant difference in the WIP on the LLMF when using the WIP ( $\theta=1$ ) as opposed to the total distance travelled ( $\theta=2$ ); as a factor in the minimizing function for the MFLP.

Table 6.31: REGWQ and Tukeys multiple comparison test for $\theta$ for the LLDP

|  |  |  | Grouping* |  |
| :--- | :--- | :--- | :--- | :--- |
| $\theta$ | N | Mean WIP | REGWQ | Tukey |
| 2 | 720 | 229.63 | A | A |
| 1 | 720 | 222.31 | B | B |

Note: These tests control the Type I experiment-wise error rate * Means with the same letter are not significantly different

To summarize:

- There is a significant difference in the WIP of the solutions for the different levels of $\theta$
- As $\theta$ increases the WIP of the best solutions increases, i.e.,
- Using the WIP $(\theta=1)$, as opposed to the total distance travelled $(\theta=2)$, as a factor in the minimizing
function for the MFLP yields LLMFs with lower WIP (less congestion)


### 6.4.2.5 Variable: Shortcut Selection Criteria (S)

In Table 6.32, the dependent variable WIP is compared across the different levels of the main effect $S$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect ' $S$ ' is introduced to test if there is a significant difference in the WIP on the LLMF when using the combined method to determine the shortcuts $(S=1)$ as opposed to separate method to determine the shortcuts $(S=2)$.

Table 6.32: REGWQ and Tukeys multiple comparison test for $S$ for the LLDP

|  |  | Grouping* |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $S$ | N | Mean WIP | REGWQ | Tukey |
| 2 | 720 | 293.35 | A | A |
| 1 | 720 | 158.59 | B | B |

Note: These tests control the Type I experiment-wise error rate * Means with the same letter are not significantly different

To summarize:

- There is a significant difference in the WIP of the solutions for the different levels of $S$
- As $S$ increases the WIP of the best solutions increases, i.e.,
- Using the combined method to determine the shortcuts $(S=1)$, as opposed to separate method to determine the shortcuts $(S=2)$, yields LLMFs with lower WIP (less congestion)


### 6.4.2.6 Variable: Scenario ( $\theta S$ )

In Table 6.33, the dependent variable WIP is compared across the different levels of the main effect $\theta S$ using REGWQ and Tukeys multiple comparison test. It should be noted that means with the same letter (under the grouping columns) are not significantly different. The main effect $' \theta S$ ' is introduced to test if there is a significant difference in the WIP on the LLMF for different levels of ' $\theta S^{\prime}$ ', i.e., for the different scenarios as described in $\$ 5.2 .2$ and summarized in Table 5.10.

Table 6.33: REGWQ and Tukeys multiple comparison test for $\theta S$ for the LLDP

| $\theta S$ | N | Mean WIP | Grouping* |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | REGWQ | Tukey |
| 4 | 360 | 293.57 | A | A |
| 2 | 360 | 293.12 | A | A |
| 3 | 360 | 165.68 | B | B |
| 1 | 360 | 151.50 | C | C |
| Not $\times$ | $\begin{aligned} & \text { test } \\ & \text { h the } \end{aligned}$ | ol the Ty etter are | experim <br> ignif | se error <br> diffe |

To summarize:

- There is a significant difference in the WIP of the solutions for the some of the different levels of $\theta S$
- $\theta S=1$ has the lowest the WIP of the best solutions
- Scenario E yields LLMFs with the least WIP (least congestion) followed by Scenario G.

Notably, Scenario F and Scenario H yield LLMFs with similar WIP levels.

### 6.4.3 Evaluation of Hypotheses

The results from the test problems for the LLDP show that the proposed methodology outperforms traditional methods used for the MFLP. $\Theta$, $S$, and $\Theta S$ are introduced to measure the effect of the choice of: the optimization criteria $(\Theta)$, the shortcut selection criteria (S), and the interaction of $\Theta$ and $S(\Theta S)$

Consider the main effect $\Theta S$. The results from the GLM analysis, as presented in $\$$ 6.4.2.6, indicate that there is a significant difference in the resultant WIP of the solutions for the different scenarios. Scenario E has the lowest WIP followed by Scenario G and Scenario E is significantly different from Scenario G. Although both Scenario $F$ and Scenario $H$ are significantly different from Scenario E and Scenario G respectively, they are not significantly different from each other.

Given these outcome, one can make the following statements:

- H1。 (Null hypothesis for Hypothesis Test 1 as presented in § 5.2.8.1) is rejected.
- H2o (Null hypothesis for Hypothesis Test 2 as presented in § 5.2.8.2) is rejected.
- H30 (Null hypothesis for Hypothesis Test 3 as presented in $\S$ 5.2.8.3) is rejected.
- H40 (Null hypothesis for Hypothesis Test 4 as presented in $\S$ 5.2.8.4) is rejected.
- H50 (Null hypothesis for Hypothesis Test 5 as presented in § 5.2.8.5) is not rejected.


## 7 DISCUSSION

### 7.1 Expected WIP at the Input Stations of the Conveyor

Although the proposed analytical estimate is not general it performs extremely well for situations that have Markovian arrival processes, i.e., when the time between the arrivals of loads to the system is modeled by the exponential distribution. This outcome is to be expected as the proposed analytical estimate is built using Welch (1964); an M/G/1 approximation that assumes loads arrive according to a Markov process. Ideally, a G/G/1 approximation for the service at the input stations would work best since it would account for any interarrival time variability and could thereby provide better estimates of the total WIP at the input stations. However, currently there is no G/G/1 formulation that takes into account the queueing process in which the first customer of each busy period receives exceptional service, akin to the Type 1 and Type 2 service distributions as described in $\$ 3.2 .2$.

The proposed methodology also performs extremely well when the utilization of the conveyor is less than 0.5 for any arrival process. This is an interesting artifact of the results, as for lower utilizations of the conveyor system it implies that the interarrival time variability does not have much effect on the
total WIP at the input stations of a conveyor. An explanation for this is that at lower utilizations, the loads arriving to the conveyor do not have to wait for long at the input stations as the likelihood of encountering an unoccupied window on the conveyor is high. The effect of the interarrival time variability will be more prevalent in situations where the loads have to wait at the input stations as a result of encountering many unoccupied windows on the conveyor (when the conveyor is busy, i.e. the utilization of the conveyor is high.) This is also reflected in the simulation results for the total WIP at the input stations which show significantly lower total WIP for levels of utilization less than 0.5 in comparison to utilization levels greater than 0.5. Also, for the different levels of interarrival time variability, for utilization levels greater than 0.5 , there is a measureable difference in the total WIP at the input stations. Again, a G/G/1 approximation could provide for better estimates of the total WIP at the input stations.

Overall, from a practical standpoint the proposed analytical estimate of the total WIP at the input stations around a conveyor performs rather well; given that the utilization of the conveyor is less than 0.9, the average absolute relative error of the analytical estimate is 5.59\%. Also, the proposed methodology
for the analytical estimate is the first to develop a distribution for the service at the input stations to the conveyor.

### 7.2 Looped Layout Design Problem

For the testing of the LLDP, the outcomes of the utilization of the conveyor and the ratio of the cost of the shortcut to the cost of the WIP ( $\Omega$ ) were as expected. As with most manufacturing systems, when the utilization of the system increases the overall WIP in the system increases. With regards to $\Omega$, as $\Omega$ increases the relative cost of adding shortcuts increases, hence fewer shortcuts are added. As a result of there being fewer shortcuts, the overall WIP in the system is higher. This is an interesting outcome although this result is intuitive; as a result of adding the shortcut the travelling WIP on the conveyor is reduced thereby reducing the overall WIP on the conveyor, and the converse also hold true.

Next, in the analysis of the turntable turntime, the results show that $t$ had no measureable effect on the overall WIP of the system. This is a very interesting outcome. It is important to note that in prior testing where $t$ was considered to be significant (Hong et al., 2011; Johnson et al., 2009; Nazzal et al., 2010, 2008), the layouts of the facilities upon which simulation studies were performed were not optimized. Therefore, for those
simulation studies the utilization of the turntables was high. Hence, it was incorrectly perceived that the turntime of the turntables had an impact on the level of the overall WIP on the LCMHS .

Now, as a result of finding better layouts (from the GA solution procedure) there is less WIP on the conveyor. Therefore, utilization of the turntables is lower (since the flow of loads on LLMF is more streamlined.) Hence, the actual impact of the turntable turntime is not significant. This interesting outcome can have a significant impact on future considerations in the design process of LLMFs.

Table 7.1: Number of Design with Average Miminum WIP for each test problem
\# of Designs with Average Minimum WIP

|  | Combined | Separate | Total |
| :--- | :--- | :--- | :--- |
| WIP | 32 | 2 | 34 |
| Distance | 2 | 0 | 2 |
| Total | 34 | 2 | 36 |

Consider the optimization criteria ( $\Theta$ ), the results from the analysis show that the resultant WIP when using the WIP as the optimization criteria is significantly different from and lower than the resultant WIP when using the total distance travelled. The best solutions determined by using the WIP as the optimization criteria are better equipped at selecting the layout that
results in the lowest WIP. The best layouts determined by using the distance-based methods do not guarantee the lowest WIP. For individual test problems, it has been observed that systems with the lowest WIP do not always have the lowest total distance travelled among the set of best solutions for the respective test problem. As it can be seen from Table 7.1, for the 36 test problems ${ }^{3}$, 34 out of the 36 problems had the lowest average minimum WIP (for the 10 replications) from the solutions determined by using the WIP as the optimization criteria.

For the shortcut selection criteria (S), the results from the analysis show that the resultant WIP when using the 'combined' design method as the shortcut selection criteria is significantly lower than the resultant $W I P$ when using the separate design method. As proposed, the combined method for determining the shortcuts is akin to a global search method and the magnitude of the difference in the WIP between the combined and separate methods for determining the shortcuts support this claim. Furthermore, as it can be seen from Table 7.1, for the 36 test problems, 34 out of the 36 problems had the lowest average mini-

[^1]mum WIP (for the 10 replications) from the solutions determined by using the combined method as the selection criteria.

Of all the scenarios tested, Scenario E which represents the proposed methodology had the best results while Scenario $H$ which represents the traditional methodology had the worst results. The combined effect of using the WIP as the optimization criteria and using the combined method as the shortcut selection criteria yielded layouts with the lowest congestion. As it can be seen from Table 7.1, for the 36 test problems, 32 out of the 36 problems had the lowest average minimum WIP (for the 10 replications) from the solutions determined by using Scenario E while none of the test problems had the lowest average minimum WIP from the solutions determined by using Scenario H. The outcomes of the testing overwhelmingly support the use of the proposed methodology.

## 8 CONCLUDING REMARKS

### 8.1 Summary of Proposed Methodology

Traditionally, manufacturing facility layout problem methods aim at minimizing the total distance traveled, the material handing cost, or the time in the system (based on distance traveled at a specific speed). Bozer \& Hsieh (2005) suggests that for a LLMF, the most appropriate design criterion for the LLDP with a LCMHS would be to minimize the total WIP on the LCMHS and the input stations for all the cells in the LLMF. This dissertation research proposed an analytical model to estimate the total work in process at the input stations to the closed looped conveyor. Further, a methodology was proposed to solve the looped layout design problem for a looped layout manufacturing facility with a looped conveyor material handling system with shortcuts using a system performance metric, i.e. the work in process (WIP) on the conveyor and at the input stations to the conveyor, as a factor in the minimizing function for the facility layout optimization problem; which is solved heuristically using a permutation genetic algorithm.

Traditionally, the optimal layout of a facility is first determined. After some time of operation, usually if needed, the
best set of shortcuts is determined to alleviate congestion in the LLMF as described by Hong, Johnson, Carlo, Nazzal, and Jimenez (2011). It is the contention of the proposed research that the aforementioned two-step process yields a sub-optimal solution. The proposed methodology also argues the case for determining the shortcut locations across the conveyor simultaneously (while determining the layout of the stations around the loop) versus the traditional method which determines the shortcuts sequentially (after the layout of the stations has been determined).

### 8.2 Summary of Findings

The findings presented summarize those from § Error! Reference source not found..

- The proposed methodology (using the WIP as a factor in the minimizing function for the facility layout while simultaneously solving for the shortcuts) yields a facility layout which is less congested than a facility layout generated by the traditional methods
o Of all methods tested, the proposed methodology performed the best in the testing while the traditional methodology performed the worst
- For the LLDP, using the WIP as the optimization criteria has a significant effect on lowering the overall WIP in the LLMF
- For the LLDP, using the combined method to determine the shortcuts has a significant effect on lowering the overall WIP in the LLMF
- Using, the combined method to determine the shortcuts has the greater impact on lowering the overall WIP in the LLMF when compared to the separate method of designing the Layout and then optimizing the shortcut locations
- The turntable turn time does not have an effect on the overall WIP of the system as a result of the lowered utilization of the turntables
- Statistically, the proposed analytical estimate provides reliable estimates for the total WIP at the input stations to a LCMHS for Markovian arrival processes if the utilization of the conveyor is less than 0.9
- Statistically, the proposed analytical estimate provides reliable estimates for the total WIP at the input stations to a LCMHS for any arrival processes if the utilization of the conveyor is less than 0.5
- Practically, the proposed analytical estimate provides reliable estimates for the total WIP at the input stations to


#### Abstract

a LCMHS for any arrival processes while the utilization of the conveyor is less than 0.75 with an average relative absolute relative error of $4.47 \%$ which is well within the acceptable range of error as presented in past studies


### 8.3 Summary of Contributions

The proposed research mainly contributes to the field of manufacturing facility layout with other contributions to the field of conveyor systems analysis. The contributions are as listed below:

- The proposed methodology presents, tests and validates the use of a combined solution algorithm (solve for the Layout and shortcuts simultaneously) versus the traditional sequential two-step process
- The proposed methodology uses the WIP on the conveyor and the WIP at the input stations to the conveyor as a factor in the minimizing function for the FLP for MFs with a LMCHS
- The proposed methodology uses the combined method to determine the shortcuts at each iteration for the FLP for MFs with a LMCHS
- The proposed methodology uses a custom tailored permutation genetic algorithm to solve the LLDP
- The proposed methodology presents, tests and validates an analytical estimate for the total WIP at the input stations of the conveyor
- the proposed methodology for the analytical estimate develops a distribution for the service times at the input stations to the conveyor where the service time is modeled as the residual conveyor cycle time and the time the load waits for the first unoccupied window
- Prior work from Nazzal, Jimenez, Carlo, Johnson, and Lasrado (2010) is used in the proposed methodology to estimate the WIP on a conveyor with shortcuts
- The proposed methodology presents a multi-phased approach that estimates the WIP on the conveyor and across the shortcuts of the conveyor
- Prior work from Johnson, Carlo, Jimenez, Nazzal, and Lasrado (2009) is used to find the best set of shortcuts on the conveyor
- The greedy heuristic as presented is extremely quick at finding configurations of near optimal configurations of shortcuts around the LCMHS


### 8.4 Implications to Practitioners

The findings of the proposed methodology for both, the LLDP and the analytical estimate for the total WIP at the input stations have significant implications to practitioners.

For the LLDP:

- The proposed methodology enhances the transparency of the LLMF while determining the layout
- With the traditional methodology the practitioner may determine a layout for a facility but has no information about the operational performance of the LLMF
- In addition to determining the layout of the LLMF, the proposed methodology also presents the practitioner with useful information about the operational performance of the LLMF for each considered layout. System performance measures such as time in system, time in queue, etc. can easily be derived using Little's Law if the mean $W I P$ is known
- The finding that the turntable turntime does not affect the overall WIP in the LLMF is of significance
- In an industry such as semiconductor manufacturing, one of the key elements of the manufacturing process is to reduce the vibrations on the conveyor so as to

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maintain the integrity of the semiconductor chips be-
ing manufactured. Since the turntime is of no conse-
quence to the overall WIP in the LLMF, practitioners
can design facilities with slower turntable turn rates
to reduce the possibility of vibrations along the
LCMHS .
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- As the findings of this research have shown, it greatly benefits the practitioner to include shortcuts (if financially feasible) in the design of the layout of the LLMF from the onset if lowering congestion is important

For the analytical estimate of the total WIP at the input station around the conveyor:

- An interesting outcome of the study is that no matter what the combination of arrival rate or speed of the conveyor, for a particular level of utilization (that is an outcome of a given arrival rate and the speed of the conveyor); the expected WIP around the conveyor and at the input stations around the conveyor is the same

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O In the testing of WIP estimates this finding greatly
        simplifies the design of experiment by reducing the
        number of variables that need to be varied
```

- It is important for the practitioner to consider two key parameters of the LCMHS, viz., the utilization of the LCMHS and the arrival process to the LCMHS
o In environments with lower utilization levels (less than 0.5) and arrival process that are close to the Markov process the analytical estimates provides reliable results.


### 8.5 Future Work

For the LLDP:

- Adapt the proposed methodology to include the WIP from production system so as to capture the WIP in the entire manufacturing facility
- Adapt the proposed methodology to consider blocking and recirculation of loads in the estimate for the overall WIP around the conveyor
o In most real world scenarios the assumption that queues have infinite length is unrealistic since most loading and unloading stations have finite buffers
- The proposed methodology considers a rectangular closed loop layout.
o Future work will involve the modification of this methodology to include non-standard closed loop facility shapes
o Future work will involve the modification of this methodology to include non-standard open field facility layout
- Currently, all the shortcuts by design are orthogonal to the LCMHS connecting one side of the conveyor to the other, future work would adapt the proposed methodology to include - Non-orthogonal shortcuts that could provide for
- connecting one side of the conveyor to the other - bypassing stations on the same side of the conveyor

For the analytical estimate of the total WIP at the input stations:

- Adapt the current M/G/1 formulation to a G/G/1 queueing formulation that takes into account the queueing process in which the first customer of each busy period receives exceptional service


### 8.6 Conclusion

A particular choice of a facility Layout can have a significant impact on the ability of a company to maintain lower operational expenses. Furthermore, a poor Layout can result in high material handling costs, excessive work-in-process (WIP), and low or unbalanced equipment utilization. Most traditional MFLP formulations ignore the impact of the facility layout on the operational performance of the $M F$ i.e. the work-in-process (WIP), the throughput, or the cycle time.

The proposed methodology aims at minimizing the WIP on the LLMF by using the WIP on the conveyor and the WIP at input stations of the conveyor as a factor in the minimizing function for the facility layout optimization problem while simultaneously solving for the best set of shortcuts. The proposed methodology is tested on a virtual 300 mm Semiconductor Wafer Fabrication Facility with a looped conveyor material handling system with shortcuts. The results show that the facility layouts generated by the proposed methodology have significantly less congestion than facility layouts generated by traditional methods.

The proposed methodology presented an analytical estimate for the total WIP at the input stations around the conveyor. The validation of the developed analytical estimate of the work in process at the input stations reveals that the proposed method-

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ology works extremely well for systems with Markovian Arrival
Processes.
    At the start of this document it was stated that,
        "every company is looking for an advantage over
        its peers; an important practical question is
        how do companies create this competitive ad-
        vantage in terms of creating value?"
As presented, the proposed methodology for determining the lay-
out for a MF with a LCMHS with shortcuts best positions the MF
to lower its operational expenses by incorporating material han-
dling decisions at the development stage. The result of the pro-
posed facility layout planning strategy is a facility layout
with less congestion that has the potential to drastically re-
duce the operational expenses of a MF, thereby creating value,
in terms of savings in operational expenses, which in turn pro-
vides the company with a competitive advantage over its peers.
```


## APPENDIX A: FROM-TO MATRIX FOR LAYOUT X

| From | To |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 7.87 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0.92 | 0 | 0.73 | 0 | 0 | 1.12 | 0.25 | 0.34 | 0 | 0 | 0 | 0.67 | 0 | 0 | 0 | 0 | 0 | 0 | 1.6 | 3.63 | 0.64 | 0.62 |
| 3 | 1.44 | 1.01 | 0 | 1.06 | 1.29 | 0.26 | 0.51 | 1.46 | 1.36 | 0.48 | 0 | 0 | 0.22 | 0.03 | 0.06 | 0 | 0.46 | 0.36 | 0 | 1.28 | 0.41 | 0.49 | 0.27 | 1.27 |
| 4 | 2.29 | 0 | 1.16 | 0 | 1.15 | 0.35 | 0.79 | 0 | 0 | 0 | 0 | 0 | 0.22 | 0 | 0.17 | 0 | 0.21 | 0 | 0 | 1.94 | 0.05 | 0 | 0 | 2.16 |
| 5 | 1.45 | 0.57 | 0.64 | 0.63 | 0 | 0.23 | 0.47 | 3.54 | 0.32 | 1.08 | 0 | 0 | 0.23 | 0.1 | 0.07 | 0 | 0.42 | 0.37 | 0 | 0.89 | 0.63 | 0.89 | 0.29 | 0.68 |
| 6 | 0 | 0 | 0.52 | 0.49 | 0.14 | 0 | 0.63 | 0 | 0 | 0.81 | 0 | 0 | 1.17 | 0 | 0.41 | 0 | 0 | 0.46 | 1.24 | 0.79 | 0 | 0 | 0 | 0.46 |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.6 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 10.6 | 0 | 0 | 0 | 0 |
| 8 | 0 | 0.01 | 0 | 0 | 0 | 0 | 0 | 0 | 4.08 | 0.98 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1.91 | 3.19 | 0 | 0 |
| 9 | 0 | 0.01 | 0.01 | 0 | 0.01 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.02 | 4.92 | 0 | 0 |
| 10 | 0 | 0 | 0.01 | 0 | 0 | 0 | 0 | 0.02 | 1.28 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.55 | 2.48 | 1.74 | 0 | 0 |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.01 | 4.93 | 0 | 0 |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13 | 0 | 2.73 | 2.47 | 1.07 | 2.99 | 0.95 | 0 | 0 | 0 | 0.27 | 0 | 0 | 0 | 0.05 | 0.13 | 0 | 0 | 1.35 | 2.12 | 0.31 | 0.09 | 0.21 | 0.04 | 0.44 |
| 14 | 0 | 0.49 | 1.6 | 0 | 0.47 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.13 | 0 | 0 | 0 | 0.17 | 0.11 | 0 | 0 | 0.63 | 1.26 | 4.51 | 0.27 |
| 15 | 0 | 0 | 0 | 0 | 0 | 0.68 | 0.65 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.32 | 0 | 0 | 0.68 | 0 | 0 | 0 | 0 | 1.39 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.32 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 6.61 |
| 17 | 0 | 0 | 2.6 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 5.36 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 18 | 0 | 0 | 0.55 | 1.04 | 0.34 | 1.78 | 0 | 0 | 0 | 0.13 | 7.6 | 0 | 0.65 | 0 | 0.05 | 0 | 0 | 0 | 0.6 | 0.14 | 1.65 | 0 | 0 | 1.56 |
| 19 | 0 | 0 | 0 | 0 | 0 | 1.65 | 0 | 0 | 0 | 0 | 0 | 0 | 4.83 | 0 | 0 | 0 | 0 | 1.75 | 0 | 0 | 3.52 | 0 | 0.99 | 1.85 |
| 20 | 2.1 | 0 | 0.49 | 3.65 | 1.34 | 0.34 | 2.11 | 0 | 0 | 0 | 0 | 0 | 0.21 | 0 | 1.52 | 0 | 0.26 | 2.65 | 7.9 | 0 | 0.06 | 0 | 0 | 0.84 |
| 21 | 0.64 | 0.58 | 0.23 | 0.17 | 0.44 | 0.42 | 0.2 | 1.69 | 0.28 | 0.51 | 1.65 | 0 | 0.7 | 3.05 | 0.94 | 2.47 | 0.44 | 3.86 | 1.36 | 0.35 | 0 | 2.07 | 0.86 | 0.44 |
| 22 | 0 | 1.84 | 0.47 | 0 | 1.11 | 0 | 0 | 2.35 | 0.4 | 0.72 | 0 | 0 | 0 | 4.98 | 0 | 4.15 | 1.03 | 4.73 | 0 | 0 | 2.39 | 0 | 1.11 | 0.02 |
| 23 | 0 | 2.9 | 0.19 | 0 | 1.93 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.38 | 0.58 | 0 | 0 | 0.15 | 0.09 | 0 | 1.35 | 0.4 | 0.66 | 0 | 0.45 |
| 24 | 0 | 0.4 | 1.87 | 2.39 | 1.55 | 0.46 | 0 | 0 | 0 | 0.14 | 0 | 0 | 1.13 | 0.18 | 0.06 | 0 | 4.86 | 0.32 | 0.67 | 1.86 | 1.52 | 1.28 | 0.38 | 0 |

APPENDIX B: FROM-TO MATRIX FOR LAYOUT Y

| From | To |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 1 | 0 | 0 | 0 | 0 | 0 | 8.23 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0.95 | 0 | 0.71 | 0 | 0 | 1.16 | 0.28 | 0.32 | 0 | 0 | 0 | 0.67 | 0 | 0 | 0 | 0 | 0 | 0 | 1.65 | 3.82 | 0.67 | 0.7 |
| 3 | 1.57 | 1.08 | 0 | 0.97 | 1.37 | 0.53 | 0 | 1.6 | 1.5 | 0.49 | 0.23 | 0 | 0.05 | 0.43 | 0.28 | 0 | 0 | 0 | 0.18 | 1.13 | 0.39 | 0.46 | 0.54 | 1.3 |
| 4 | 2.3 | 0 | 1.19 | 0 | 1.18 | 0.75 | 0 | 0 | 0 | 0 | 0.33 | 0 | 0.17 | 0.24 | 0 | 0 | 0 | 0 | 0.25 | 1.13 | 0.04 | 0 | 0.7 | 2.32 |
| 5 | 1.47 | 0.6 | 0.66 | 0.58 | 0 | 0.56 | 0 | 3.66 | 0.31 | 1.05 | 0.18 | 0 | 0.09 | 0.63 | 0.2 | 0 | 0 | 0 | 0.3 | 0.85 | 0.68 | 1 | 0.63 | 0.74 |
| 6 | 0 | 0 | 0.53 | 0.51 | 0.19 | 0 | 13.8 | 0.8 | 0 | 1.25 | 0.31 | 0 | 0.84 | 0 | 0.4 | 0 | 0 | 1.61 | 0.34 | 0.13 | 0 | 0 | 0.86 | 0.53 |
| 7 | 0 | 0 | 0 | 0 | 0 | 1.41 | 0 | 1.47 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 10.9 | 0 |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 4.21 | 4.29 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.05 | 3.26 | 0 | 0 |
| 9 | 0 | 0 | 0.01 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.17 | 5.12 | 0 | 0 |
| 10 | 0 | 0 | 0.01 | 0 | 0 | 0 | 0 | 0.39 | 1.27 | 0 | 9.74 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1.1 | 3.3 | 2.63 | 0 |
| 11 | 0 | 0 | 0 | 0 | 0 | 4.1 | 0 | 0 | 0 | 0.06 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.97 | 5.36 | 0 | 0 |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13 | 0 | 2.87 | 2.53 | 1.06 | 3.13 | 0.42 | 0 | 0.3 | 0 | 0 | 0.6 | 0 | 0 | 0.04 | 4.41 | 0 | 0 | 2.25 | 1.55 | 1.08 | 0.08 | 0.16 | 0.34 | 0.51 |
| 14 | 0 | 0.57 | 1.79 | 0 | 0.55 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.07 | 0 | 4.31 | 0.11 | 8.47 | 0 | 0 | 0.09 | 0.61 | 1.31 | 0.29 | 0.31 |
| 15 | 0 | 0 | 0 | 0 | 0 | 1.28 | 0 | 0 | 0 | 0 | 0 | 0 | 1.47 | 0 | 0 | 0 | 3.43 | 0.77 | 0 | 0 | 1.45 | 0 | 8.25 | 0 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 8.45 | 0 | 0 | 3.5 | 0 | 0 | 0 | 6.84 | 0 | 0 | 0 |
| 17 | 0 | 0 | 2.8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.09 | 3.44 | 10.4 | 0 | 0 | 5.58 | 0 | 0 | 0 | 0 | 0 |
| 18 | 0 | 0 | 0.58 | 1.04 | 0.3 | 0.16 | 0 | 0.13 | 0 | 7.97 | 1.66 | 0 | 0.33 | 0 | 0.07 | 0 | 0 | 0 | 12.9 | 0.13 | 3.49 | 0 | 0.1 | 0.21 |
| 19 | 0 | 0 | 0 | 0 | 0 | 1.78 | 0 | 0 | 0 | 0 | 0 | 0 | 14.5 | 0 | 0.93 | 0 | 0 | 1.85 | 0 | 0 | 0 | 1.39 | 0 | 1.83 |
| 20 | 2.17 | 0 | 0.51 | 3.88 | 1.35 | 2.07 | 0 | 0 | 0 | 0 | 0.35 | 0 | 1.58 | 0.25 | 0 | 0 | 0 | 20 | 0.26 | 0 | 1.76 | 0 | 8.9 | 0.76 |
| 21 | 0.63 | 0.61 | 0.24 | 0.17 | 0.5 | 0.5 | 0 | 1.65 | 0.31 | 2.31 | 0.15 | 0 | 1.65 | 0.51 | 0.8 | 2.98 | 2.53 | 1.73 | 0 | 3.98 | 0 | 2.05 | 0.2 | 10.1 |
| 22 | 0 | 2.03 | 0.54 | 0 | 1.08 | 0 | 0 | 2.55 | 0.39 | 0.71 | 0 | 0 | 0 | 1.05 | 1.11 | 5.36 | 4.31 | 0 | 0 | 4.78 | 5.39 | 0 | 0.03 | 0.04 |
| 23 | 0 | 2.97 | 0.18 | 0 | 2.01 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.38 | 0.78 | 0.35 | 0 | 0 | 0 | 0 | 28.4 | 0.39 | 0.74 | 0 | 0.45 |
| 24 | 0 | 0.38 | 1.64 | 2.38 | 1.78 | 0.24 | 0 | 0.14 | 0 | 0 | 0.3 | 0 | 0.22 | 5.21 | 0.33 | 0 | 0 | 0.79 | 0.85 | 2.22 | 1.62 | 1.36 | 0.35 | 0 |

APPENDIX C: RESULTS FROM WIP AT INPUT STATIONS TESTING

For Layout X
For Layout X Total WIP at Input Stations From

| Test | Rho | SCV | Simulation Rep |  |  |  |  |  |  |  |  |  | Analytical Estimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |
| 1 | 0.15 | 0.5 | 0.095 | 0.097 | 0.097 | 0.096 | 0.094 | 0.095 | 0.093 | 0.095 | 0.095 | 0.097 | 0.097 |
| 2 | 0.3 | 0.5 | 0.474 | 0.473 | 0.474 | 0.474 | 0.475 | 0.471 | 0.471 | 0.475 | 0.472 | 0.474 | 0.507 |
| 3 | 0.45 | 0.5 | 1.478 | 1.466 | 1.484 | 1.470 | 1.472 | 1.467 | 1.480 | 1.497 | 1.484 | 1.480 | 1.602 |
| 4 | 0.6 | 0.5 | 3.949 | 3.981 | 3.948 | 3.985 | 3.958 | 3.945 | 3.977 | 3.951 | 3.967 | 3.984 | 4.480 |
| 5 | 0.75 | 0.5 | 11.219 | 11.198 | 11.207 | 11.275 | 11.290 | 11.214 | 11.143 | 11.264 | 11.260 | 11.290 | 13.498 |
| 6 | 0.9 | 0.5 | 52.709 | 52.361 | 52.828 | 53.767 | 53.837 | 52.093 | 53.174 | 53.167 | 51.539 | 53.546 | 59.393 |
| 7 | 0.15 | 0.77 | 0.095 | 0.096 | 0.097 | 0.096 | 0.096 | 0.095 | 0.095 | 0.096 | 0.097 | 0.097 | 0.097 |
| 8 | 0.3 | 0.77 | 0.482 | 0.482 | 0.480 | 0.480 | 0.479 | 0.477 | 0.480 | 0.477 | 0.474 | 0.479 | 0.507 |
| 9 | 0.45 | 0.77 | 1.523 | 1.524 | 1.526 | 1.523 | 1.514 | 1.526 | 1.523 | 1.518 | 1.518 | 1.522 | 1.602 |
| 10 | 0.6 | 0.77 | 4.223 | 4.204 | 4.190 | 4.200 | 4.187 | 4.200 | 4.190 | 4.186 | 4.193 | 4.179 | 4.480 |
| 11 | 0.75 | 0.77 | 12.667 | 12.567 | 12.597 | 12.638 | 12.576 | 12.634 | 12.658 | 12.685 | 12.695 | 12.519 | 13.498 |
| 12 | 0.9 | 0.77 | 68.852 | 68.176 | 69.430 | 70.506 | 67.858 | 70.132 | 70.540 | 68.940 | 67.450 | 68.779 | 59.393 |
| 13 | 0.15 | 1 | 0.096 | 0.096 | 0.094 | 0.098 | 0.095 | 0.095 | 0.096 | 0.097 | 0.098 | 0.097 | 0.097 |
| 14 | 0.3 | 1 | 0.481 | 0.480 | 0.481 | 0.483 | 0.482 | 0.483 | 0.479 | 0.481 | 0.480 | 0.485 | 0.507 |
| 15 | 0.45 | 1 | 1.560 | 1.552 | 1.562 | 1.564 | 1.569 | 1.564 | 1.563 | 1.555 | 1.556 | 1.562 | 1.602 |
| 16 | 0.6 | 1 | 4.426 | 4.397 | 4.431 | 4.377 | 4.415 | 4.420 | 4.406 | 4.428 | 4.423 | 4.416 | 4.480 |
| 17 | 0.75 | 1 | 13.893 | 13.756 | 13.880 | 13.928 | 13.716 | 13.885 | 13.852 | 13.785 | 13.954 | 13.809 | 13.498 |
| 18 | 0.9 | 1 | 84.675 | 82.300 | 83.888 | 81.491 | 85.873 | 81.907 | 81.043 | 84.559 | 83.696 | 84.548 | 59.393 |
| 19 | 0.15 | 1.23 | 0.096 | 0.097 | 0.097 | 0.097 | 0.101 | 0.098 | 0.100 | 0.098 | 0.099 | 0.097 | 0.097 |
| 20 | 0.3 | 1.23 | 0.482 | 0.489 | 0.487 | 0.486 | 0.489 | 0.487 | 0.484 | 0.489 | 0.486 | 0.487 | 0.507 |
| 21 | 0.45 | 1.23 | 1.611 | 1.595 | 1.608 | 1.611 | 1.607 | 1.592 | 1.597 | 1.603 | 1.618 | 1.627 | 1.602 |
| 22 | 0.6 | 1.23 | 4.597 | 4.584 | 4.606 | 4.570 | 4.624 | 4.626 | 4.641 | 4.637 | 4.622 | 4.641 | 4.480 |
| 23 | 0.75 | 1.23 | 15.057 | 14.875 | 15.104 | 15.035 | 15.058 | 15.140 | 15.132 | 15.093 | 15.003 | 14.881 | 13.498 |
| 24 | 0.9 | 1.23 | 96.440 | 96.191 | 103.152 | 95.726 | 94.651 | 97.005 | 99.316 | 98.081 | 95.823 | 97.644 | 59.393 |
| 25 | 0.15 | 1.5 | 0.099 | 0.099 | 0.099 | 0.101 | 0.098 | 0.100 | 0.100 | 0.098 | 0.101 | 0.098 | 0.097 |
| 26 | 0.3 | 1.5 | 0.493 | 0.492 | 0.494 | 0.495 | 0.490 | 0.493 | 0.496 | 0.496 | 0.491 | 0.491 | 0.507 |
| 27 | 0.45 | 1.5 | 1.695 | 1.669 | 1.694 | 1.698 | 1.680 | 1.669 | 1.699 | 1.679 | 1.669 | 1.692 | 1.602 |
| 28 | 0.6 | 1.5 | 4.900 | 4.863 | 4.857 | 4.887 | 4.850 | 4.840 | 4.869 | 4.868 | 4.895 | 4.883 | 4.480 |
| 29 | 0.75 | 1.5 | 16.644 | 16.303 | 16.513 | 16.407 | 16.451 | 16.580 | 16.346 | 16.631 | 16.523 | 16.529 | 13.498 |
| 30 | 0.9 | 1.5 | 115.708 | 108.513 | 109.759 | 114.271 | 112.672 | 112.827 | 113.684 | 113.119 | 112.035 | 116.096 | 59.393 |

For Layout $\mathbf{Y}$
For Layout Y Total WIP at Input Stations From

| Test | Rho | SCV | Simulation Rep |  |  |  |  |  |  |  |  |  | Analytical Estimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |
| 1 | 0.15 | 0.5 | 0.099 | 0.099 | 0.099 | 0.098 | 0.097 | 0.100 | 0.098 | 0.100 | 0.098 | 0.097 | 0.100 |
| 2 | 0.3 | 0.5 | 0.490 | 0.489 | 0.491 | 0.487 | 0.489 | 0.492 | 0.493 | 0.492 | 0.491 | 0.489 | 0.524 |
| 3 | 0.45 | 0.5 | 1.517 | 1.516 | 1.521 | 1.519 | 1.516 | 1.517 | 1.517 | 1.518 | 1.522 | 1.519 | 1.653 |
| 4 | 0.6 | 0.5 | 4.051 | 4.042 | 4.081 | 4.054 | 4.069 | 4.057 | 4.056 | 4.068 | 4.085 | 4.060 | 4.604 |
| 5 | 0.75 | 0.5 | 11.676 | 11.594 | 11.713 | 11.677 | 11.665 | 11.617 | 11.652 | 11.674 | 11.723 | 11.714 | 13.774 |
| 6 | 0.9 | 0.5 | 57.277 | 57.915 | 57.463 | 56.322 | 56.706 | 57.818 | 57.625 | 57.616 | 57.006 | 57.160 | 59.695 |
| 7 | 0.15 | 0.77 | 0.100 | 0.099 | 0.099 | 0.098 | 0.097 | 0.101 | 0.099 | 0.101 | 0.100 | 0.099 | 0.100 |
| 8 | 0.3 | 0.77 | 0.496 | 0.490 | 0.494 | 0.495 | 0.493 | 0.494 | 0.493 | 0.496 | 0.494 | 0.497 | 0.524 |
| 9 | 0.45 | 0.77 | 1.602 | 1.602 | 1.588 | 1.584 | 1.581 | 1.574 | 1.593 | 1.588 | 1.599 | 1.588 | 1.653 |
| 10 | 0.6 | 0.77 | 4.352 | 4.350 | 4.373 | 4.350 | 4.323 | 4.318 | 4.350 | 4.351 | 4.356 | 4.372 | 4.604 |
| 11 | 0.75 | 0.77 | 13.103 | 13.170 | 13.201 | 13.168 | 13.225 | 13.176 | 13.311 | 13.248 | 13.222 | 13.036 | 13.774 |
| 12 | 0.9 | 0.77 | 76.374 | 73.257 | 75.199 | 76.089 | 73.622 | 73.610 | 75.735 | 74.011 | 75.996 | 73.973 | 59.695 |
| 13 | 0.15 | 1 | 0.101 | 0.101 | 0.100 | 0.100 | 0.100 | 0.098 | 0.102 | 0.101 | 0.100 | 0.099 | 0.100 |
| 14 | 0.3 | 1 | 0.501 | 0.500 | 0.503 | 0.502 | 0.500 | 0.501 | 0.502 | 0.502 | 0.501 | 0.502 | 0.524 |
| 15 | 0.45 | 1 | 1.634 | 1.636 | 1.642 | 1.640 | 1.625 | 1.629 | 1.650 | 1.638 | 1.640 | 1.630 | 1.653 |
| 16 | 0.6 | 1 | 4.599 | 4.623 | 4.616 | 4.596 | 4.593 | 4.580 | 4.625 | 4.642 | 4.637 | 4.607 | 4.604 |
| 17 | 0.75 | 1 | 14.550 | 14.665 | 14.494 | 14.439 | 14.530 | 14.628 | 14.686 | 14.555 | 14.505 | 14.516 | 13.774 |
| 18 | 0.9 | 1 | 91.459 | 89.476 | 89.916 | 88.549 | 92.095 | 92.305 | 91.087 | 90.611 | 90.162 | 87.213 | 59.695 |
| 19 | 0.15 | 1.23 | 0.101 | 0.100 | 0.100 | 0.102 | 0.102 | 0.100 | 0.101 | 0.101 | 0.100 | 0.099 | 0.100 |
| 20 | 0.3 | 1.23 | 0.508 | 0.506 | 0.505 | 0.504 | 0.506 | 0.508 | 0.506 | 0.509 | 0.507 | 0.509 | 0.524 |
| 21 | 0.45 | 1.23 | 1.703 | 1.716 | 1.673 | 1.674 | 1.684 | 1.708 | 1.705 | 1.700 | 1.710 | 1.717 | 1.653 |
| 22 | 0.6 | 1.23 | 4.889 | 4.843 | 4.877 | 4.862 | 4.857 | 4.835 | 4.825 | 4.832 | 4.852 | 4.867 | 4.604 |
| 23 | 0.75 | 1.23 | 16.034 | 15.779 | 16.043 | 15.913 | 15.834 | 15.893 | 15.837 | 15.942 | 15.960 | 16.007 | 13.774 |
| 24 | 0.9 | 1.23 | 106.384 | 104.591 | 105.829 | 105.308 | 106.264 | 104.023 | 102.775 | 110.051 | 106.263 | 104.769 | 59.695 |
| 25 | 0.15 | 1.5 | 0.102 | 0.100 | 0.101 | 0.101 | 0.102 | 0.100 | 0.100 | 0.102 | 0.101 | 0.101 | 0.100 |
| 26 | 0.3 | 1.5 | 0.526 | 0.525 | 0.527 | 0.514 | 0.525 | 0.527 | 0.529 | 0.524 | 0.527 | 0.527 | 0.524 |
| 27 | 0.45 | 1.5 | 1.777 | 1.767 | 1.768 | 1.763 | 1.776 | 1.752 | 1.764 | 1.776 | 1.781 | 1.773 | 1.653 |
| 28 | 0.6 | 1.5 | 5.156 | 5.132 | 5.195 | 5.152 | 5.150 | 5.175 | 5.162 | 5.163 | 5.203 | 5.150 | 4.604 |
| 29 | 0.75 | 1.5 | 17.623 | 17.483 | 17.577 | 17.401 | 17.464 | 17.539 | 17.413 | 17.487 | 17.546 | 17.635 | 13.774 |
| 30 | 0.9 | 1.5 | 125.878 | 120.425 | 122.062 | 120.331 | 123.405 | 120.128 | 119.663 | 122.105 | 124.456 | 122.940 | 59.695 |

## For Layout Z

For Layout $z$ Total WIP at Input Stations From

| Test | Rho | SCV | Simulation Rep |  |  |  |  |  |  |  |  |  | Analytical <br> Estimate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |
| 1 | 0.15 | 0.5 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.104 |
| 2 | 0.3 | 0.5 | 0.513 | 0.513 | 0.516 | 0.512 | 0.513 | 0.511 | 0.512 | 0.512 | 0.512 | 0.516 | 0.544 |
| 3 | 0.45 | 0.5 | 1.747 | 1.749 | 1.743 | 1.744 | 1.749 | 1.751 | 1.748 | 1.751 | 1.753 | 1.749 | 1.725 |
| 4 | 0.6 | 0.5 | 4.586 | 4.611 | 4.610 | 4.591 | 4.591 | 4.584 | 4.604 | 4.614 | 4.598 | 4.603 | 4.872 |
| 5 | 0.75 | 0.5 | 13.354 | 13.271 | 13.410 | 13.428 | 13.307 | 13.271 | 13.324 | 13.387 | 13.479 | 13.375 | 15.058 |
| 6 | 0.9 | 0.5 | 62.129 | 60.944 | 61.030 | 62.463 | 62.100 | 61.152 | 60.774 | 61.373 | 62.706 | 62.751 | 68.773 |
| 7 | 0.15 | 0.77 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.104 |
| 8 | 0.3 | 0.77 | 0.515 | 0.513 | 0.513 | 0.519 | 0.516 | 0.517 | 0.511 | 0.510 | 0.516 | 0.517 | 0.544 |
| 9 | 0.45 | 0.77 | 1.743 | 1.740 | 1.752 | 1.756 | 1.749 | 1.753 | 1.756 | 1.744 | 1.752 | 1.745 | 1.725 |
| 10 | 0.6 | 0.77 | 4.633 | 4.635 | 4.611 | 4.622 | 4.626 | 4.610 | 4.618 | 4.623 | 4.631 | 4.620 | 4.872 |
| 11 | 0.75 | 0.77 | 14.053 | 13.878 | 13.969 | 14.021 | 13.931 | 13.973 | 13.964 | 14.086 | 14.022 | 14.071 | 15.058 |
| 12 | 0.9 | 0.77 | 75.583 | 72.987 | 74.934 | 74.890 | 75.208 | 73.830 | 74.326 | 74.391 | 74.916 | 74.969 | 68.773 |
| 13 | 0.15 | 1 | 0.096 | 0.096 | 0.097 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.104 |
| 14 | 0.3 | 1 | 0.514 | 0.517 | 0.516 | 0.518 | 0.520 | 0.518 | 0.516 | 0.516 | 0.517 | 0.518 | 0.544 |
| 15 | 0.45 | 1 | 1.756 | 1.762 | 1.753 | 1.762 | 1.751 | 1.755 | 1.758 | 1.762 | 1.754 | 1.752 | 1.725 |
| 16 | 0.6 | 1 | 4.676 | 4.650 | 4.627 | 4.650 | 4.644 | 4.642 | 4.634 | 4.646 | 4.633 | 4.656 | 4.872 |
| 17 | 0.75 | 1 | 14.439 | 14.600 | 14.475 | 14.592 | 14.572 | 14.487 | 14.458 | 14.625 | 14.649 | 14.659 | 15.058 |
| 18 | 0.9 | 1 | 87.467 | 88.179 | 85.933 | 85.616 | 86.800 | 85.757 | 82.813 | 88.430 | 87.599 | 86.612 | 68.773 |
| 19 | 0.15 | 1.23 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.096 | 0.097 | 0.097 | 0.104 |
| 20 | 0.3 | 1.23 | 0.520 | 0.519 | 0.517 | 0.517 | 0.521 | 0.519 | 0.519 | 0.511 | 0.523 | 0.520 | 0.544 |
| 21 | 0.45 | 1.23 | 1.771 | 1.759 | 1.761 | 1.767 | 1.760 | 1.766 | 1.758 | 1.757 | 1.766 | 1.761 | 1.725 |
| 22 | 0.6 | 1.23 | 4.740 | 4.762 | 4.704 | 4.724 | 4.690 | 4.662 | 4.679 | 4.794 | 4.762 | 4.693 | 4.872 |
| 23 | 0.75 | 1.23 | 15.157 | 15.224 | 15.294 | 15.116 | 14.964 | 15.089 | 15.316 | 15.282 | 15.187 | 15.126 | 15.058 |
| 24 | 0.9 | 1.23 | 97.470 | 96.299 | 95.890 | 94.038 | 98.563 | 93.438 | 98.442 | 94.355 | 99.468 | 97.255 | 68.773 |
| 25 | 0.15 | 1.5 | 0.097 | 0.096 | 0.096 | 0.096 | 0.096 | 0.097 | 0.096 | 0.096 | 0.097 | 0.097 | 0.104 |
| 26 | 0.3 | 1.5 | 0.523 | 0.521 | 0.524 | 0.521 | 0.521 | 0.522 | 0.521 | 0.520 | 0.525 | 0.521 | 0.544 |
| 27 | 0.45 | 1.5 | 1.783 | 1.776 | 1.767 | 1.776 | 1.766 | 1.773 | 1.774 | 1.775 | 1.772 | 1.775 | 1.725 |
| 28 | 0.6 | 1.5 | 4.947 | 4.921 | 4.948 | 4.878 | 4.921 | 4.950 | 4.950 | 4.947 | 4.909 | 4.928 | 4.872 |
| 29 | 0.75 | 1.5 | 16.159 | 15.686 | 15.980 | 16.089 | 15.950 | 15.792 | 15.835 | 15.966 | 15.875 | 16.023 | 15.058 |
| 30 | 0.9 | 1.5 | 108.275 | 107.093 | 108.557 | 108.392 | 111.542 | 109.732 | 112.363 | 114.658 | 112.511 | 109.357 | 68.773 |

APPENDIX D: ABSOLUTE RELATIVE ERROR FOR WIP AT INPUT STATIONS TESTING

For Layout x
For Layout X Total WIP at Input Stations From

| Rho | SCV | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.15 | 0.5 | $2.04 \%$ | $0.06 \%$ | 0.06\% | $0.98 \%$ | 3.13\% | $2.04 \%$ | $4.24 \%$ | $2.04 \%$ | $2.04 \%$ | $0.06 \%$ |
| 0.3 | 0.5 | 6.98\% | 7.20\% | 6.98\% | $6.98 \%$ | 6.75\% | 7.66\% | 7.66\% | 6.75\% | 7.43\% | 6.98\% |
| 0.45 | 0.5 | 8.41\% | 9.29\% | 7.97\% | 9.00\% | 8.85\% | 9.22\% | 8.26\% | 7.03\% | 7.97\% | 8.26\% |
| 0.6 | 0.5 | 13.44\% | 12.53\% | 13.47\% | 12.42\% | 13.19\% | 13.56\% | 12.65\% | 13.39\% | 12.93\% | 12.45\% |
| 0.75 | 0.5 | 20.31\% | $20.54 \%$ | 20.44\% | 19.71\% | 19.55\% | $20.37 \%$ | 21.13\% | 19.83\% | 19.87\% | 19.55\% |
| 0.9 | 0.5 | 12.68\% | 13.43\% | 12.43\% | 10.46\% | 10.32\% | 14.01\% | 11.70\% | 11.71\% | 15.24\% | 10.92\% |
| 0.15 | 0.77 | $2.04 \%$ | $0.98 \%$ | $0.06 \%$ | $0.98 \%$ | $0.98 \%$ | $2.04 \%$ | $2.04 \%$ | 0.98\% | $0.06 \%$ | $0.06 \%$ |
| 0.3 | 0.77 | 5.20\% | 5.20\% | 5.64\% | 5.64\% | 5.86\% | 6.30\% | 5.64\% | 6.30\% | 6.98\% | 5.86\% |
| 0.45 | 0.77 | 5.20\% | 5.13\% | 5.00\% | $5.20 \%$ | 5.83\% | 5.00\% | 5.20\% | 5.55\% | 5.55\% | 5.27\% |
| 0.6 | 0.77 | 6.08\% | 6.56\% | 6.92\% | $6.67 \%$ | 7.00\% | 6.67\% | $6.92 \%$ | 7.02\% | $6.84 \%$ | 7.20\% |
| 0.75 | 0.77 | 6.56\% | 7.41\% | 7.15\% | $6.80 \%$ | 7.33\% | 6.84\% | 6.63\% | 6.41\% | $6.32 \%$ | $7.82 \%$ |
| 0.9 | 0.77 | 13.74\% | 12.88\% | $14.46 \%$ | 15.76\% | 12.47\% | 15.31\% | 15.80\% | 13.85\% | 11.95\% | 13.65\% |
| 0.15 | 1 | 0.98\% | $0.98 \%$ | 3.13\% | 1.08\% | $2.04 \%$ | $2.04 \%$ | $0.98 \%$ | $0.06 \%$ | 1.08\% | $0.06 \%$ |
| 0.3 | 1 | 5.42\% | 5.64\% | 5.42\% | 4.98\% | 5.20\% | 4.98\% | 5.86\% | 5.42\% | 5.64\% | 4.55\% |
| 0.45 | 1 | 2.71\% | 3.24\% | 2.58\% | 2.45\% | 2.12\% | 2.45\% | 2.51\% | 3.04\% | $2.97 \%$ | 2.58\% |
| 0.6 | 1 | 1.22\% | 1.89\% | 1.10\% | 2.35\% | 1.47\% | 1.36\% | 1.68\% | 1.17\% | 1.29\% | 1.45\% |
| 0.75 | 1 | $2.84 \%$ | 1.88\% | $2.75 \%$ | 3.09\% | 1.59\% | 2.79\% | $2.56 \%$ | 2.08\% | 3.27\% | 2.25\% |
| 0.9 | 1 | $29.86 \%$ | 27.83\% | 29.20\% | 27.12\% | 30.84\% | 27.49\% | $26.71 \%$ | $29.76 \%$ | 29.04\% | 29.75\% |
| 0.15 | 1.23 | 0.98\% | $0.06 \%$ | $0.06 \%$ | $0.06 \%$ | 4.02\% | 1.08\% | 3.06\% | 1.08\% | $2.08 \%$ | $0.06 \%$ |
| 0.3 | 1.23 | 5.20\% | $3.70 \%$ | 4.12\% | 4.34\% | 3.70\% | 4.12\% | 4.77\% | 3.70\% | 4.34\% | 4.12\% |
| 0.45 | 1.23 | $0.54 \%$ | $0.45 \%$ | $0.36 \%$ | $0.54 \%$ | $0.30 \%$ | $0.64 \%$ | $0.33 \%$ | $0.05 \%$ | $0.97 \%$ | 1.52\% |
| 0.6 | 1.23 | 2.55\% | $2.27 \%$ | $2.74 \%$ | 1.97\% | 3.12\% | 3.16\% | 3.47\% | 3.39\% | 3.07\% | 3.47\% |
| 0.75 | 1.23 | 10.36\% | 9.26\% | 10.63\% | 10.22\% | 10.36\% | 10.85\% | 10.80\% | 10.57\% | 10.03\% | 9.30\% |
| 0.9 | 1.23 | 38.41\% | 38.26\% | 42.42\% | 37.96\% | 37.25\% | 38.77\% | $40.20 \%$ | 39.45\% | 38.02\% | 39.17\% |
| 0.15 | 1.5 | 2.08\% | $2.08 \%$ | 2.08\% | 4.02\% | 1.08\% | 3.06\% | 3.06\% | 1.08\% | 4.02\% | 1.08\% |
| 0.3 | 1.5 | 2.85\% | $3.06 \%$ | 2.65\% | $2.44 \%$ | 3.48\% | $2.85 \%$ | 2.23\% | $2.23 \%$ | 3.27\% | 3.27\% |
| 0.45 | 1.5 | 5.47\% | 4.00\% | 5.42\% | $5.64 \%$ | 4.63\% | 4.00\% | 5.69\% | 4.57\% | 4.00\% | 5.30\% |
| 0.6 | 1.5 | 8.57\% | 7.88\% | 7.76\% | 8.33\% | 7.63\% | 7.44\% | 7.99\% | 7.97\% | 8.48\% | 8.25\% |
| 0.75 | 1.5 | 18.90\% | 17.21\% | 18.26\% | 17.73\% | 17.95\% | 18.59\% | 17.42\% | 18.84\% | 18.31\% | 18.34\% |
| 0.9 | 1.5 | 48.67\% | 45.27\% | 45.89\% | 48.02\% | 47.29\% | 47.36\% | $47.76 \%$ | 47.50\% | $46.99 \%$ | 48.84\% |

For Layout $\mathbf{Y}$
For Layout Y Total WIP at Input Stations From

| Rho | SCV | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.15 | 0.5 | 1.44\% | 1.44\% | 1.44\% | 2.48\% | 3.54\% | 0.43\% | 2.48\% | 0.43\% | 2.48\% | 3.54\% |
| 0.3 | 0.5 | 7.02\% | 7.24\% | 6.80\% | 7.68\% | 7.24\% | 6.58\% | 6.37\% | 6.58\% | 6.80\% | 7.24\% |
| 0.45 | 0.5 | 8.96\% | 9.03\% | 8.67\% | 8.82\% | 9.03\% | 8.96\% | 8.96\% | 8.89\% | 8.60\% | 8.82\% |
| 0.6 | 0.5 | 13.65\% | 13.90\% | 12.82\% | 13.57\% | 13.15\% | 13.48\% | 13.51\% | 13.18\% | 12.71\% | 13.40\% |
| 0.75 | 0.5 | 17.97\% | 18.81\% | 17.60\% | 17.96\% | 18.08\% | 18.57\% | 18.21\% | 17.99\% | 17.50\% | 17.59\% |
| 0.9 | 0.5 | 4.22\% | 3.07\% | 3.88\% | 5.99\% | 5.27\% | 3.25\% | 3.59\% | 3.61\% | 4.72\% | 4.43\% |
| 0.15 | 0.77 | 0.43\% | 1.44\% | 1.44\% | 2.48\% | 3.54\% | 0.56\% | 1.44\% | 0.56\% | 0.43\% | 1.44\% |
| 0.3 | 0.77 | 5.72\% | 7.02\% | 6.15\% | 5.94\% | 6.37\% | 6.15\% | 6.37\% | 5.72\% | 6.15\% | 5.51\% |
| 0.45 | 0.77 | 3.18\% | 3.18\% | 4.09\% | 4.35\% | 4.55\% | 5.01\% | 3.76\% | 4.09\% | 3.37\% | 4.09\% |
| 0.6 | 0.77 | 5.79\% | 5.84\% | 5.28\% | 5.84\% | 6.50\% | 6.62\% | 5.84\% | 5.82\% | 5.69\% | 5.31\% |
| 0.75 | 0.77 | 5.12\% | 4.59\% | 4.34\% | 4.61\% | 4.15\% | 4.54\% | 3.48\% | 3.97\% | 4.18\% | 5.66\% |
| 0.9 | 0.77 | 21.84\% | 18.51\% | 20.62\% | 21.55\% | 18.92\% | 18.90\% | 21.18\% | 19.34\% | 21.45\% | 19.30\% |
| 0.15 | 1 | 0.56\% | 0.56\% | 0.43\% | 0.43\% | 0.43\% | 2.48\% | 1.54\% | 0.56\% | 0.43\% | 1.44\% |
| 0.3 | 1 | 4.67\% | 4.88\% | 4.25\% | 4.46\% | 4.88\% | 4.67\% | 4.46\% | 4.46\% | 4.67\% | 4.46\% |
| 0.45 | 1 | 1.16\% | 1.03\% | 0.66\% | 0.79\% | 1.72\% | 1.47\% | 0.18\% | 0.91\% | 0.79\% | 1.41\% |
| 0.6 | 1 | 0.11\% | 0.41\% | $0.26 \%$ | 0.17\% | 0.24\% | 0.52\% | 0.45\% | 0.82\% | 0.71\% | $0.06 \%$ |
| 0.75 | 1 | 5.33\% | 6.07\% | 4.96\% | 4.60\% | 5.20\% | 5.84\% | 6.21\% | 5.36\% | 5.04\% | 5.11\% |
| 0.9 | 1 | 34.73\% | 33.28\% | 33.61\% | 32.59\% | 35.18\% | 35.33\% | 34.46\% | 34.12\% | 33.79\% | 31.55\% |
| 0.15 | 1.23 | 0.56\% | 0.43\% | 0.43\% | 1.54\% | 1.54\% | 0.43\% | 0.56\% | 0.56\% | 0.43\% | 1.44\% |
| 0.3 | 1.23 | 3.23\% | 3.63\% | 3.84\% | 4.04\% | 3.63\% | 3.23\% | 3.63\% | 3.02\% | 3.43\% | 3.02\% |
| 0.45 | 1.23 | 2.94\% | 3.68\% | 1.20\% | 1.26\% | 1.85\% | 3.23\% | 3.06\% | 2.77\% | 3.34\% | 3.73\% |
| 0.6 | 1.23 | 5.83\% | 4.93\% | 5.60\% | 5.31\% | 5.21\% | 4.78\% | 4.58\% | 4.72\% | 5.11\% | 5.40\% |
| 0.75 | 1.23 | 14.09\% | 12.70\% | 14.14\% | 13.44\% | 13.01\% | 13.33\% | 13.02\% | 13.60\% | 13.69\% | 13.95\% |
| 0.9 | 1.23 | 43.89\% | 42.93\% | 43.59\% | 43.31\% | 43.82\% | 42.61\% | 41.92\% | 45.76\% | 43.82\% | 43.02\% |
| 0.15 | 1.5 | 1.54\% | $0.43 \%$ | 0.56\% | $0.56 \%$ | 1.54\% | $0.43 \%$ | 0.43\% | 1.54\% | 0.56\% | 0.56\% |
| 0.3 | 1.5 | 0.31\% | 0.12\% | 0.50\% | 2.02\% | 0.12\% | 0.50\% | 0.87\% | 0.07\% | 0.50\% | 0.50\% |
| 0.45 | 1.5 | 6.98\% | 6.46\% | 6.51\% | 6.24\% | 6.93\% | 5.66\% | 6.30\% | 6.93\% | 7.19\% | 6.77\% |
| 0.6 | 1.5 | 10.71\% | 10.29\% | 11.38\% | 10.64\% | 10.60\% | 11.03\% | 10.81\% | 10.83\% | 11.51\% | 10.60\% |
| 0.75 | 1.5 | 21.84\% | 21.21\% | 21.63\% | 20.84\% | 21.13\% | 21.46\% | 20.90\% | 21.23\% | 21.50\% | 21.89\% |
| 0.9 | 1.5 | 52.58\% | 50.43\% | 51.09\% | 50.39\% | 51.63\% | 50.31\% | 50.11\% | 51.11\% | 52.04\% | 51.44\% |

For Layout Z
For Layout Z Total WIP at Input Stations From

| Rho | SCV | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.15 | 0.5 | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% |
| 0.3 | 0.5 | 5.96\% | 5.96\% | 5.35\% | 6.17\% | 5.96\% | 6.38\% | 6.17\% | 6.17\% | 6.17\% | 5.35\% |
| 0.45 | 0.5 | 1.28\% | 1.40\% | 1.06\% | 1.11\% | 1.40\% | 1.51\% | 1.34\% | 1.51\% | 1.62\% | 1.40\% |
| 0.6 | 0.5 | 6.25\% | 5.67\% | 5.69\% | 6.13\% | $6.13 \%$ | 6.29\% | 5.83\% | 5.60\% | 5.97\% | 5.85\% |
| 0.75 | 0.5 | 12.76\% | 13.47\% | 12.29\% | 12.14\% | 13.16\% | 13.47\% | 13.02\% | 12.48\% | 11.72\% | 12.59\% |
| 0.9 | 0.5 | 10.69\% | 12.85\% | 12.69\% | 10.10\% | 10.75\% | 12.46\% | 13.16\% | $12.06 \%$ | 9.68\% | 9.60\% |
| 0.15 | 0.77 | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% |
| 0.3 | 0.77 | 5.55\% | 5.96\% | 5.96\% | 4.74\% | 5.35\% | 5.14\% | 6.38\% | 6.59\% | 5.35\% | 5.14\% |
| 0.45 | 0.77 | 1.06\% | 0.89\% | 1.57\% | 1.79\% | 1.40\% | 1.62\% | 1.79\% | 1.11\% | 1.57\% | 1.17\% |
| 0.6 | 0.77 | 5.17\% | 5.12\% | 5.67\% | 5.42\% | 5.33\% | 5.69\% | 5.51\% | 5.40\% | 5.21\% | 5.47\% |
| 0.75 | 0.77 | 7.15\% | 8.51\% | 7.80\% | 7.40\% | 8.09\% | 7.77\% | $7.84 \%$ | 6.90\% | 7.39\% | 7.02\% |
| 0.9 | 0.77 | 9.01\% | 5.77\% | 8.22\% | 8.17\% | 8.56\% | 6.85\% | 7.47\% | 7.55\% | 8.20\% | 8.26\% |
| 0.15 | 1 | 8.05\% | 8.05\% | 6.94\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% |
| 0.3 | 1 | 5.76\% | 5.14\% | 5.35\% | 4.94\% | 4.54\% | 4.94\% | 5.35\% | 5.35\% | 5.14\% | 4.94\% |
| 0.45 | 1 | 1.79\% | 2.12\% | 1.62\% | 2.12\% | 1.51\% | 1.73\% | 1.90\% | 2.12\% | 1.68\% | 1.57\% |
| 0.6 | 1 | 4.20\% | 4.78\% | 5.31\% | 4.78\% | 4.92\% | 4.97\% | 5.15\% | 4.87\% | 5.17\% | 4.65\% |
| 0.75 | 1 | 4.29\% | 3.14\% | 4.03\% | 3.20\% | 3.34\% | 3.94\% | 4.15\% | 2.96\% | $2.79 \%$ | 2.72\% |
| 0.9 | 1 | $21.37 \%$ | $22.01 \%$ | 19.97\% | 19.67\% | 20.77\% | 19.80\% | 16.95\% | $22.23 \%$ | 21.49\% | 20.60\% |
| 0.15 | 1.23 | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | 8.05\% | $6.94 \%$ | $6.94 \%$ |
| 0.3 | 1.23 | 4.54\% | $4.74 \%$ | 5.14\% | 5.14\% | 4.34\% | 4.74\% | $4.74 \%$ | 6.38\% | 3.94\% | 4.54\% |
| 0.45 | 1.23 | 2.62\% | 1.96\% | 2.07\% | 2.40\% | 2.01\% | 2.35\% | 1.90\% | 1.85\% | 2.35\% | 2.07\% |
| 0.6 | 1.23 | 2.80\% | 2.32\% | 3.58\% | 3.14\% | 3.89\% | 4.51\% | 4.14\% | 1.64\% | 2.32\% | 3.82\% |
| 0.75 | 1.23 | 0.65\% | 1.09\% | 1.54\% | $0.38 \%$ | $0.63 \%$ | $0.20 \%$ | 1.68\% | 1.46\% | $0.85 \%$ | $0.45 \%$ |
| 0.9 | 1.23 | 29.44\% | 28.58\% | 28.28\% | $26.87 \%$ | 30.22\% | $26.40 \%$ | 30.14\% | 27.11\% | $30.86 \%$ | 29.29\% |
| 0.15 | 1.5 | $6.94 \%$ | 8.05\% | 8.05\% | 8.05\% | 8.05\% | $6.94 \%$ | 8.05\% | 8.05\% | $6.94 \%$ | $6.94 \%$ |
| 0.3 | 1.5 | 3.94\% | $4.34 \%$ | 3.74\% | $4.34 \%$ | 4.34\% | 4.14\% | 4.34\% | 4.54\% | 3.54\% | 4.34\% |
| 0.45 | 1.5 | 3.28\% | 2.90\% | 2.40\% | 2.90\% | 2.35\% | 2.73\% | 2.79\% | 2.84\% | 2.68\% | 2.84\% |
| 0.6 | 1.5 | 1.51\% | 0.99\% | 1.53\% | 0.11\% | 0.99\% | 1.57\% | 1.57\% | 1.51\% | $0.74 \%$ | 1.13\% |
| 0.75 | 1.5 | 6.81\% | 4.00\% | 5.77\% | 6.41\% | 5.59\% | 4.65\% | 4.90\% | 5.68\% | 5.14\% | 6.02\% |
| 0.9 | 1.5 | 36.48\% | 35.78\% | 36.65\% | 36.55\% | 38.34\% | 37.33\% | 38.79\% | 40.02\% | 38.87\% | 37.11\% |

APPENDIX E: AVERAGE ERROR FOR WIP AT INPUT STATIONS TESTING

Average Error

| Rho | SCV | Layout X | Layout Y | Layout Z |
| :--- | :--- | :--- | :--- | :--- |
| 0.15 | 0.5 | $-1.62 \%$ | $-1.96 \%$ | $-8.05 \%$ |
| 0.3 | 0.5 | $-7.14 \%$ | $-6.95 \%$ | $-5.96 \%$ |
| 0.45 | 0.5 | $-8.42 \%$ | $-8.87 \%$ | $1.36 \%$ |
| 0.6 | 0.5 | $-13.00 \%$ | $-13.34 \%$ | $-5.94 \%$ |
| 0.75 | 0.5 | $-20.13 \%$ | $-18.03 \%$ | $-12.71 \%$ |
| 0.9 | 0.5 | $-12.27 \%$ | $-4.20 \%$ | $-11.39 \%$ |
| 0.15 | 0.77 | $-0.98 \%$ | $-1.14 \%$ | $-8.05 \%$ |
| 0.3 | 0.77 | $-5.86 \%$ | $-6.11 \%$ | $-5.61 \%$ |
| 0.45 | 0.77 | $-5.29 \%$ | $-3.96 \%$ | $1.40 \%$ |
| 0.6 | 0.77 | $-6.79 \%$ | $-5.85 \%$ | $-5.40 \%$ |
| 0.75 | 0.77 | $-6.92 \%$ | $-4.46 \%$ | $-7.58 \%$ |
| 0.9 | 0.77 | $14.01 \%$ | $20.18 \%$ | $7.81 \%$ |
| 0.15 | 1 | $-0.77 \%$ | $-0.23 \%$ | $-7.94 \%$ |
| 0.3 | 1 | $-5.31 \%$ | $-4.58 \%$ | $-5.14 \%$ |
| 0.45 | 1 | $-2.66 \%$ | $-1.01 \%$ | $1.82 \%$ |
| 0.6 | 1 | $-1.50 \%$ | $0.17 \%$ | $-4.88 \%$ |
| 0.75 | 1 | $2.51 \%$ | $5.37 \%$ | $-3.45 \%$ |
| 0.9 | 1 | $28.78 \%$ | $33.88 \%$ | $20.51 \%$ |
| 0.15 | 1.23 | $1.08 \%$ | $0.17 \%$ | $-7.83 \%$ |
| 0.3 | 1.23 | $-4.21 \%$ | $-3.47 \%$ | $-4.82 \%$ |
| 0.45 | 1.23 | $0.29 \%$ | $2.71 \%$ | $2.16 \%$ |
| 0.6 | 1.23 | $2.92 \%$ | $5.15 \%$ | $-3.21 \%$ |
| 0.75 | 1.23 | $10.24 \%$ | $13.50 \%$ | $0.77 \%$ |
| 0.9 | 1.23 | $39.02 \%$ | $43.48 \%$ | $28.75 \%$ |
| 0.15 | 1.5 | $2.38 \%$ | $0.56 \%$ | $-7.60 \%$ |
| 0.3 | 1.5 | $-2.83 \%$ | $0.14 \%$ | $-4.16 \%$ |
| 0.45 | 1.5 | $4.88 \%$ | $6.60 \%$ | $2.77 \%$ |
| 0.6 | 1.5 | $8.03 \%$ | $10.84 \%$ | $1.16 \%$ |
| 0.75 | 1.5 | $18.16 \%$ | $21.36 \%$ | $5.50 \%$ |
| 0.9 | 1.5 | $47.38 \%$ | $51.13 \%$ | $37.62 \%$ |
|  |  |  |  |  |

## APPENDIX F: GLM PROCEDURE SAS OUTPUT FOR WIP AT INPUT STATIONS - LAYOUT X




```
                Minimum Significant Difference 0.196
                    Means with the same letter are not significantly different.
    Tukey Grouping Mean N N arrivals
            A 4.38247 100 1.5
            A 4.20281 100 1.23
            B
            B C 4.05821 100 1
            C
            D C 
            D
            D 3.74310 100 0.5
            The SAS System
5
            The GLM Procedure
    Tukey's Studentized Range (HSD) Test for WIP_welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
                    II error rate than REGWQ.
                Alpha 0.05
            Error Degrees of Freedom 482
            Error Mean Square 0.256063
            Critical Value of Studentized Range 2.77879
            Minimum Significant Difference 0.0889
            Means with the same letter are not significantly different.
            Tukey Grouping Mean N M
            A 4.08182 250 1
            A
            A 4.03679 250 0
            The SAS System
6
                    The GLM Procedure
    Tukey's Studentized Range (HSD) Test for WIP_welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
```







## APPENDIX G: GLM PROCEDURE SAS OUTPUT FOR WIP AT INPUT STATIONS - LAYOUT Y




```
Minimum Significant Difference 0.218
Means with the same letter are not significantly different.
    Tukey Grouping Mean N N arrivals
            A 4.57326 100 1.5
            A 4.37407 100 1.23
            B
            B C 4.20628 100 1
            C
            D C 4.03751 100 0.77
            D
            D }\quad3.84960\quad100\quad0.
            The SAS System
5
            The GLM Procedure
    Tukey's Studentized Range (HSD) Test for WIP_welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
                    II error rate than REGWQ.
            Alpha 0.05
            Error Degrees of Freedom 482
            Error Mean Square 0.316805
            Critical Value of Studentized Range 2.77879
            Minimum Significant Difference 0.0989
            Means with the same letter are not significantly different.
            Tukey Grouping Mean N M
                    A 4.28505 250 1
            B 4.13123 250 0
                The SAS System
6
            The GLM Procedure
    Tukey's Studentized Range (HSD) Test for WIP_welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type






\section*{APPENDIX H: GLM PROCEDURE SAS OUTPUT FOR WIP AT INPUT STATIONS - LAYOUT Z}


```

                                    Minimum Significant Difference 0.0981
    Means with the same letter are not significantly different.
Tukey Grouping Mean N arrivals
A 4.55601 100 1.5
B 4.45766 100 1.23
B
C B 4.38737 100 1
C
C D D 4.32821 100 0.77
D
D 4.26199 100 0.5
The SAS System
5
The GLM Procedure
Tukey's Studentized Range (HSD) Test for WIP_welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
II error rate than REGWQ
Alpha 0.05
Error Degrees of Freedom 482
Error Mean Square 0.064207
Critical Value of Studentized Range 2.77879
Minimum Significant Difference 0.0445
Means with the same letter are not significantly different.
Tukey Grouping Mean N M
A 4.46055 250 0
B 4.33596 250 1
The SAS System
6
The GLM Procedure
Tukey's Studentized Range (HSD) Test for WIP welch
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type



| Alpha | 0.05 |
| :--- | :---: |
| Error Degrees of | Freedom 482 |
| Error Mean Square | 0.064207 |
|  |  |
|  |  |
| Number of Means | 2 |
| Critical Range | 0.0445324 |

Means with the same letter are not significantly different.



APPENDIX I: WIP FROM THE LLDP TESTING

WIP from Replication

| Test | $\Omega$ | $\rho_{\text {LCMHS }}$ | t | $\theta$ | S | $\theta$ S | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.10 | 0.15 | 0 | 1 | 1 | 1 | 32.78 | 31.26 | 31.44 | 33.94 | 31.32 | 32.64 | 31.06 | 32.56 | 31.83 | 31.51 |
| 2 | 0.10 | 0.15 | 0 | 1 | 2 | 2 | 88.57 | 84.05 | 88.59 | 84.98 | 85.06 | 84.08 | 88.70 | 84.04 | 85.29 | 90.18 |
| 3 | 0.10 | 0.15 | 0 | 2 | 1 | 3 | 31.29 | 33.72 | 34.47 | 30.58 | 31.86 | 34.82 | 33.80 | 31.26 | 35.06 | 35.28 |
| 4 | 0.10 | 0.15 | 0 | 2 | 2 | 4 | 85.29 | 84.07 | 85.82 | 85.34 | 84.87 | 84.07 | 86.12 | 85.01 | 85.25 | 88.73 |
| 5 | 0.10 | 0.15 | 7 | 1 | 1 | 1 | 35.48 | 34.61 | 35.36 | 37.94 | 35.02 | 35.28 | 37.24 | 35.32 | 36.83 | 34.77 |
| 6 | 0.10 | 0.15 | 7 | 1 | 2 | 2 | 90.37 | 87.10 | 87.08 | 87.08 | 87.63 | 88.27 | 87.10 | 88.37 | 88.47 | 90.39 |
| 7 | 0.10 | 0.15 | 7 | 2 | 1 | 3 | 37.33 | 38.30 | 39.29 | 40.52 | 35.32 | 38.10 | 36.38 | 34.81 | 36.39 | 40.21 |
| 8 | 0.10 | 0.15 | 7 | 2 | 2 | 4 | 91.40 | 88.51 | 88.00 | 92.89 | 87.14 | 87.14 | 90.23 | 94.72 | 92.86 | 87.12 |
| 9 | 0.10 | 0.15 | 15 | 1 | 1 | 1 | 40.81 | 44.30 | 39.90 | 43.37 | 41.68 | 40.29 | 41.40 | 39.70 | 42.75 | 39.13 |
| 10 | 0.10 | 0.15 | 15 | 1 | 2 | 2 | 92.82 | 94.31 | 96.26 | 92.82 | 94.66 | 91.48 | 92.44 | 95.61 | 92.54 | 91.92 |
| 11 | 0.10 | 0.15 | 15 | 2 | 1 | 3 | 45.10 | 44.61 | 45.12 | 42.72 | 41.93 | 39.81 | 41.23 | 41.55 | 43.44 | 42.80 |
| 12 | 0.10 | 0.15 | 15 | 2 | 2 | 4 | 92.96 | 91.67 | 91.75 | 94.96 | 93.16 | 93.56 | 93.02 | 91.62 | 92.99 | 98.45 |
| 13 | 0.10 | 0.50 | 0 | 1 | 1 | 1 | 103.60 | 104.27 | 102.72 | 103.64 | 108.96 | 111.47 | 106.19 | 104.41 | 103.04 | 109.68 |
| 14 | 0.10 | 0.50 | 0 | 1 | 2 | 2 | 285.93 | 306.31 | 290.16 | 281.85 | 309.84 | 280.58 | 296.43 | 284.49 | 280.66 | 293.27 |
| 15 | 0.10 | 0.50 | 0 | 2 | 1 | 3 | 111.49 | 111.48 | 122.27 | 106.22 | 107.93 | 109.05 | 105.70 | 110.95 | 105.16 | 117.95 |
| 16 | 0.10 | 0.50 | 0 | 2 | 2 | 4 | 283.95 | 306.37 | 280.86 | 296.82 | 291.94 | 309.61 | 285.33 | 291.55 | 288.93 | 280.88 |
| 17 | 0.10 | 0.50 | 7 | 1 | 1 | 1 | 107.77 | 108.58 | 107.85 | 114.90 | 111.46 | 109.37 | 106.80 | 111.05 | 108.20 | 107.82 |
| 18 | 0.10 | 0.50 | 7 | 1 | 2 | 2 | 293.71 | 284.66 | 306.25 | 308.82 | 283.81 | 289.68 | 284.98 | 300.77 | 305.25 | 288.26 |
| 19 | 0.10 | 0.50 | 7 | 2 | 1 | 3 | 110.37 | 116.66 | 119.45 | 116.02 | 109.89 | 121.24 | 122.51 | 108.01 | 112.32 | 110.91 |
| 20 | 0.10 | 0.50 | 7 | 2 | 2 | 4 | 284.22 | 283.94 | 283.80 | 283.89 | 292.16 | 283.84 | 283.64 | 289.38 | 306.04 | 299.62 |
| 21 | 0.10 | 0.50 | 15 | 1 | 1 | 1 | 113.50 | 115.87 | 115.11 | 121.11 | 112.88 | 122.32 | 112.20 | 120.47 | 113.56 | 114.20 |
| 22 | 0.10 | 0.50 | 15 | 1 | 2 | 2 | 292.29 | 306.59 | 288.30 | 288.26 | 288.34 | 292.64 | 308.76 | 303.61 | 288.10 | 292.81 |
| 23 | 0.10 | 0.50 | 15 | 2 | 1 | 3 | 115.37 | 115.67 | 115.79 | 116.34 | 112.69 | 116.14 | 113.23 | 120.59 | 118.41 | 121.66 |
| 24 | 0.10 | 0.50 | 15 | 2 | 2 | 4 | 288.56 | 288.55 | 299.43 | 292.75 | 297.18 | 292.93 | 291.27 | 289.76 | 300.74 | 288.68 |
| 25 | 0.10 | 0.85 | 0 | 1 | 1 | 1 | 187.18 | 177.82 | 177.46 | 183.33 | 175.06 | 187.32 | 188.44 | 175.20 | 180.61 | 189.73 |


| 26 | 0.10 | 0.85 | 0 | 1 | 2 | 2 | 479.13 | 514.66 | 487.53 | 479.54 | 485.10 | 486.11 | 506.20 | 496.68 | 486.04 | 493.57 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 27 | 0.10 | 0.85 | 0 | 2 | 1 | 3 | 193.16 | 182.96 | 182.31 | 185.07 | 181.86 | 216.65 | 192.65 | 178.42 | 199.18 | 186.69 |
| 28 | 0.10 | 0.85 | 0 | 2 | 2 | 4 | 510.55 | 509.91 | 506.76 | 499.96 | 480.11 | 498.46 | 485.07 | 484.19 | 479.59 | 487.22 |
| 29 | 0.10 | 0.85 | 7 | 1 | 1 | 1 | 181.12 | 191.18 | 185.03 | 192.27 | 181.12 | 185.42 | 186.75 | 180.15 | 178.80 | 182.12 |
| 30 | 0.10 | 0.85 | 7 | 1 | 2 | 2 | 521.32 | 482.23 | 505.32 | 518.29 | 482.32 | 489.88 | 529.04 | 509.68 | 482.30 | 534.50 |
| 31 | 0.10 | 0.85 | 7 | 2 | 1 | 3 | 192.50 | 182.55 | 198.26 | 180.73 | 203.17 | 182.25 | 182.61 | 182.38 | 177.26 | 189.08 |
| 32 | 0.10 | 0.85 | 7 | 2 | 2 | 4 | 514.76 | 516.33 | 500.15 | 533.77 | 492.69 | 488.23 | 508.40 | 485.00 | 528.25 | 482.82 |
| 33 | 0.10 | 0.85 | 15 | 1 | 1 | 1 | 184.54 | 200.26 | 183.63 | 207.96 | 186.51 | 186.72 | 203.90 | 187.65 | 188.08 | 192.33 |
| 34 | 0.10 | 0.85 | 15 | 1 | 2 | 2 | 491.93 | 491.86 | 508.85 | 487.20 | 487.28 | 504.56 | 489.10 | 504.80 | 496.70 | 519.90 |
| 35 | 0.10 | 0.85 | 15 | 2 | 1 | 3 | 189.98 | 190.47 | 191.59 | 191.86 | 192.19 | 189.50 | 193.88 | 187.32 | 198.03 | 186.39 |
| 36 | 0.10 | 0.85 | 15 | 2 | 2 | 4 | 513.93 | 487.94 | 487.08 | 505.66 | 503.56 | 523.02 | 504.88 | 491.74 | 492.49 | 490.23 |
| 37 | 1 | 0.15 | 0 | 1 | 1 | 1 | 36.52 | 33.72 | 35.13 | 34.01 | 38.46 | 36.52 | 34.81 | 35.78 | 37.33 | 37.86 |
| 38 | 1 | 0.15 | 0 | 1 | 2 | 2 | 84.03 | 85.70 | 89.04 | 87.94 | 91.46 | 88.89 | 89.35 | 88.61 | 84.01 | 85.25 |
| 39 | 1 | 0.15 | 0 | 2 | 1 | 3 | 41.71 | 42.45 | 43.59 | 43.71 | 39.33 | 41.47 | 38.93 | 40.21 | 40.54 | 45.82 |
| 40 | 1 | 0.15 | 0 | 2 | 2 | 4 | 88.89 | 84.07 | 90.88 | 86.00 | 88.18 | 84.09 | 85.69 | 85.90 | 84.11 | 84.10 |
| 41 | 1 | 0.15 | 7 | 1 | 1 | 1 | 42.02 | 36.57 | 42.15 | 40.37 | 41.26 | 41.38 | 39.46 | 40.69 | 40.17 | 43.47 |
| 42 | 1 | 0.15 | 7 | 1 | 2 | 2 | 88.13 | 90.52 | 87.05 | 87.08 | 90.43 | 92.55 | 88.76 | 88.09 | 91.14 | 88.77 |
| 43 | 1 | 0.15 | 7 | 2 | 1 | 3 | 46.88 | 47.73 | 43.26 | 45.51 | 41.54 | 46.71 | 48.01 | 42.63 | 42.68 | 46.71 |
| 44 | 1 | 0.15 | 7 | 2 | 2 | 4 | 88.36 | 88.46 | 89.28 | 87.21 | 87.55 | 90.08 | 92.38 | 88.43 | 92.31 | 87.13 |
| 45 | 1 | 0.15 | 15 | 1 | 1 | 1 | 45.53 | 47.93 | 43.74 | 44.41 | 43.76 | 44.58 | 44.44 | 44.30 | 45.12 | 44.61 |
| 46 | 1 | 0.15 | 15 | 1 | 2 | 2 | 92.94 | 96.62 | 95.74 | 95.12 | 99.73 | 96.70 | 94.61 | 92.25 | 95.50 | 94.12 |


| 56 | 1 | 0.50 | 7 | 2 | 2 | 4 | 300.58 | 287.20 | 283.87 | 285.82 | 283.96 | 289.34 | 283.93 | 287.28 | 299.45 | 284.16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 57 | 1 | 0.50 | 15 | 1 | 1 | 1 | 114.00 | 124.91 | 115.06 | 116.03 | 113.60 | 115.16 | 110.80 | 114.74 | 114.20 | 112.59 |
| 58 | 1 | 0.50 | 15 | 1 | 2 | 2 | 296.53 | 288.22 | 289.97 | 314.29 | 296.61 | 292.13 | 288.18 | 303.14 | 297.11 | 291.30 |
| 59 | 1 | 0.50 | 15 | 2 | 1 | 3 | 126.85 | 133.36 | 137.98 | 121.18 | 122.46 | 121.29 | 128.87 | 120.99 | 126.11 | 123.94 |
| 60 | 1 | 0.50 | 15 | 2 | 2 | 4 | 298.25 | 301.87 | 291.06 | 307.50 | 300.46 | 315.67 | 288.85 | 288.31 | 292.89 | 288.16 |
| 61 | 1 | 0.85 | 0 | 1 | 1 | 1 | 183.09 | 179.06 | 177.11 | 178.70 | 174.88 | 180.82 | 179.02 | 181.93 | 176.50 | 179.37 |
| 62 | 1 | 0.85 | 0 | 1 | 2 | 2 | 509.14 | 489.45 | 479.21 | 503.48 | 479.22 | 486.69 | 479.20 | 484.20 | 484.30 | 482.33 |
| 63 | 1 | 0.85 | 0 | 2 | 1 | 3 | 205.87 | 203.69 | 184.28 | 173.66 | 191.97 | 202.23 | 212.93 | 198.93 | 192.00 | 195.81 |
| 64 | 1 | 0.85 | 0 | 2 | 2 | 4 | 505.46 | 489.20 | 496.86 | 493.65 | 498.38 | 495.51 | 513.46 | 515.44 | 527.63 | 484.23 |
| 65 | 1 | 0.85 | 7 | 1 | 1 | 1 | 180.79 | 183.42 | 183.71 | 192.53 | 182.46 | 196.47 | 182.50 | 181.20 | 181.32 | 181.35 |
| 66 | 1 | 0.85 | 7 | 1 | 2 | 2 | 482.66 | 482.60 | 482.53 | 494.20 | 509.94 | 487.22 | 508.61 | 505.08 | 482.60 | 489.18 |
| 67 | 1 | 0.85 | 7 | 2 | 1 | 3 | 205.07 | 186.31 | 187.54 | 186.48 | 215.35 | 190.70 | 198.15 | 205.74 | 185.03 | 194.58 |
| 68 | 1 | 0.85 | 7 | 2 | 2 | 4 | 521.61 | 482.79 | 500.19 | 482.40 | 514.59 | 483.16 | 484.70 | 496.73 | 485.11 | 503.69 |
| 69 | 1 | 0.85 | 15 | 1 | 1 | 1 | 187.40 | 186.10 | 200.98 | 182.42 | 199.51 | 186.59 | 191.19 | 182.42 | 187.11 | 193.44 |
| 70 | 1 | 0.85 | 15 | 1 | 2 | 2 | 507.19 | 519.26 | 486.82 | 486.68 | 532.51 | 492.82 | 497.26 | 493.84 | 487.25 | 508.22 |
| 71 | 1 | 0.85 | 15 | 2 | 1 | 3 | 193.98 | 202.75 | 208.32 | 207.96 | 187.91 | 206.96 | 208.40 | 213.46 | 202.77 | 201.87 |
| 72 | 1 | 0.85 | 15 | 2 | 2 | 4 | 494.93 | 529.93 | 514.41 | 487.06 | 508.69 | 487.65 | 487.76 | 556.08 | 494.13 | 501.49 |
| 73 | 10 | 0.15 | 0 | 1 | 1 | 1 | 56.84 | 58.99 | 59.60 | 59.11 | 59.26 | 61.54 | 58.40 | 58.04 | 57.96 | 62.85 |
| 74 | 10 | 0.15 | 0 | 1 | 2 | 2 | 85.60 | 84.00 | 88.15 | 88.61 | 89.54 | 84.00 | 83.99 | 88.13 | 86.49 | 84.06 |
| 75 | 10 | 0.15 | 0 | 2 | 1 | 3 | 69.10 | 73.07 | 76.47 | 70.31 | 58.56 | 68.58 | 72.93 | 84.02 | 69.59 | 74.21 |
| 76 | 10 | 0.15 | 0 | 2 | 2 | 4 | 84.01 | 89.88 | 84.90 | 87.06 | 90.53 | 85.34 | 86.53 | 84.08 | 85.01 | 91.68 |
| 77 | 10 | 0.15 | 7 | 1 | 1 | 1 | 62.62 | 60.07 | 60.82 | 59.48 | 62.79 | 60.37 | 60.69 | 62.28 | 61.87 | 63.43 |
| 78 | 10 | 0.15 | 7 | 1 | 2 | 2 | 87.16 | 91.55 | 87.04 | 87.92 | 87.06 | 93.81 | 98.59 | 87.48 | 93.14 | 87.13 |
| 79 | 10 | 0.15 | 7 | 2 | 1 | 3 | 78.09 | 72.75 | 61.27 | 77.27 | 72.09 | 75.28 | 73.29 | 59.43 | 64.78 | 76.97 |
| 80 | 10 | 0.15 | 7 | 2 | 2 | 4 | 92.66 | 89.64 | 87.99 | 87.21 | 87.18 | 90.25 | 87.95 | 91.46 | 88.01 | 92.90 |
| 81 | 10 | 0.15 | 15 | 1 | 1 | 1 | 65.57 | 64.83 | 67.09 | 63.36 | 66.48 | 66.19 | 67.88 | 66.71 | 65.87 | 64.92 |
| 82 | 10 | 0.15 | 15 | 1 | 2 | 2 | 91.59 | 97.76 | 96.04 | 91.60 | 91.61 | 98.29 | 92.12 | 93.34 | 92.71 | 91.56 |
| 83 | 10 | 0.15 | 15 | 2 | 1 | 3 | 67.53 | 69.49 | 77.98 | 66.67 | 70.58 | 80.59 | 81.82 | 68.31 | 76.88 | 77.07 |
| 84 | 10 | 0.15 | 15 | 2 | 2 | 4 | 92.29 | 91.67 | 98.38 | 91.66 | 97.66 | 99.60 | 93.04 | 92.13 | 91.82 | 93.40 |
| 85 | 10 | 0.50 | 0 | 1 | 1 | 1 | 161.41 | 163.52 | 151.03 | 168.85 | 166.65 | 157.22 | 138.68 | 171.83 | 154.59 | 155.43 |
| 234 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 86 | 10 | 0.50 | 0 | 1 | 2 | 2 | 303.32 | 305.43 | 295.53 | 302.51 | 280.80 | 298.94 | 282.92 | 280.64 | 284.05 | 290.79 |
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| 87 | 10 | 0.50 | 0 | 2 | 1 | 3 | 179.69 | 189.15 | 176.18 | 171.20 | 173.60 | 181.96 | 174.19 | 176.15 | 196.13 | 169.71 |
| 88 | 10 | 0.50 | 0 | 2 | 2 | 4 | 301.56 | 284.81 | 296.53 | 285.89 | 290.72 | 280.70 | 283.54 | 290.83 | 286.24 | 280.78 |
| 89 | 10 | 0.50 | 7 | 1 | 1 | 1 | 152.16 | 171.99 | 155.40 | 183.37 | 154.89 | 164.50 | 169.32 | 170.00 | 153.54 | 169.33 |
| 90 | 10 | 0.50 | 7 | 1 | 2 | 2 | 289.04 | 301.93 | 294.42 | 309.84 | 287.79 | 300.42 | 305.90 | 283.86 | 285.50 | 299.07 |
| 91 | 10 | 0.50 | 7 | 2 | 1 | 3 | 170.76 | 167.31 | 166.42 | 180.88 | 167.63 | 174.68 | 163.18 | 178.66 | 183.70 | 183.27 |
| 92 | 10 | 0.50 | 7 | 2 | 2 | 4 | 289.03 | 286.60 | 301.56 | 295.37 | 288.35 | 284.36 | 304.84 | 298.45 | 305.62 | 290.78 |
| 93 | 10 | 0.50 | 15 | 1 | 1 | 1 | 164.82 | 153.41 | 155.91 | 185.03 | 161.62 | 149.55 | 158.10 | 160.73 | 150.27 | 154.37 |
| 94 | 10 | 0.50 | 15 | 1 | 2 | 2 | 306.90 | 288.39 | 288.20 | 288.14 | 288.35 | 293.78 | 294.77 | 291.09 | 296.58 | 288.05 |
| 95 | 10 | 0.50 | 15 | 2 | 1 | 3 | 171.71 | 188.75 | 169.25 | 179.11 | 186.65 | 208.65 | 172.39 | 169.53 | 205.02 | 185.95 |
| 96 | 10 | 0.50 | 15 | 2 | 2 | 4 | 292.91 | 288.82 | 296.80 | 306.80 | 288.41 | 301.72 | 288.25 | 288.70 | 300.15 | 300.03 |
| 97 | 10 | 0.85 | 0 | 1 | 1 | 1 | 253.23 | 221.56 | 263.58 | 221.90 | 221.60 | 225.59 | 222.91 | 232.51 | 234.67 | 227.58 |
| 98 | 10 | 0.85 | 0 | 1 | 2 | 2 | 525.16 | 479.19 | 493.65 | 489.89 | 492.71 | 479.12 | 487.46 | 486.26 | 482.47 | 479.08 |
| 99 | 10 | 0.85 | 0 | 2 | 1 | 3 | 288.67 | 276.59 | 262.38 | 306.43 | 254.88 | 250.36 | 239.64 | 262.69 | 282.42 | 280.62 |
| 100 | 10 | 0.85 | 0 | 2 | 2 | 4 | 496.27 | 480.10 | 489.62 | 492.46 | 493.79 | 479.12 | 479.31 | 485.69 | 481.71 | 516.59 |
| 101 | 10 | 0.85 | 7 | 1 | 1 | 1 | 249.59 | 228.43 | 227.64 | 231.10 | 228.55 | 245.62 | 246.85 | 264.04 | 229.89 | 254.21 |
| 102 | 10 | 0.85 | 7 | 1 | 2 | 2 | 487.02 | 520.51 | 494.47 | 489.14 | 507.76 | 491.71 | 512.01 | 482.23 | 514.30 | 482.17 |
| 103 | 10 | 0.85 | 7 | 2 | 1 | 3 | 280.91 | 288.23 | 270.03 | 246.93 | 275.77 | 245.20 | 293.43 | 276.67 | 274.37 | 283.43 |
| 104 | 10 | 0.85 | 7 | 2 | 2 | 4 | 484.75 | 516.86 | 485.23 | 482.75 | 506.33 | 491.79 | 487.32 | 505.14 | 527.44 | 501.95 |
| 105 | 10 | 0.85 | 15 | 1 | 1 | 1 | 229.60 | 243.84 | 223.16 | 258.30 | 248.97 | 237.00 | 253.39 | 244.96 | 222.07 | 253.77 |
| 106 | 10 | 0.85 | 15 | 1 | 2 | 2 | 492.54 | 507.81 | 519.71 | 489.04 | 535.44 | 492.74 | 487.09 | 543.84 | 490.24 | 487.30 |
| 107 | 10 | 0.85 | 15 | 2 | 1 | 3 | 301.71 | 278.23 | 280.06 | 277.04 | 271.32 | 263.22 | 263.92 | 303.25 | 301.10 | 284.51 |
| 108 | 10 | 0.85 | 15 | 2 | 2 | 4 | 501.49 | 497.22 | 489.46 | 491.76 | 493.89 | 514.88 | 494.06 | 500.99 | 487.25 | 496.53 |
| 109 | 50 | 0.15 | 0 | 1 | 1 | 1 | 84.13 | 84.04 | 88.73 | 86.44 | 83.98 | 87.04 | 89.34 | 84.01 | 84.55 | 84.62 |
| 110 | 50 | 0.15 | 0 | 1 | 2 | 2 | 85.71 | 85.20 | 86.24 | 84.03 | 88.75 | 86.48 | 84.03 | 84.06 | 84.02 | 84.08 |
| 111 | 50 | 0.15 | 0 | 2 | 1 | 3 | 84.47 | 84.03 | 91.24 | 84.01 | 85.86 | 85.42 | 89.18 | 84.48 | 84.58 | 84.02 |
| 112 | 50 | 0.15 | 0 | 2 | 2 | 4 | 84.19 | 85.23 | 91.64 | 90.32 | 85.74 | 90.50 | 86.00 | 87.05 | 88.61 | 88.02 |
| 113 | 50 | 0.15 | 7 | 1 | 1 | 1 | 88.70 | 90.90 | 87.08 | 93.28 | 88.37 | 88.22 | 91.39 | 91.72 | 92.80 | 87.20 |
| 114 | 50 | 0.15 | 7 | 1 | 2 | 2 | 87.14 | 87.04 | 93.23 | 93.27 | 88.27 | 93.51 | 90.34 | 87.67 | 87.28 | 87.66 |
| 115 | 50 | 0.15 | 7 | 2 | 1 | 3 | 92.47 | 87.12 | 87.14 | 91.33 | 96.02 | 87.25 | 89.77 | 93.38 | 87.13 | 91.59 |
| 235 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 116 | 50 | 0.15 | 7 | 2 | 2 | 4 | 93.61 | 87.53 | 91.85 | 88.86 | 87.07 | 90.12 | 93.92 | 87.15 | 88.40 | 90.43 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 117 | 50 | 0.15 | 15 | 1 | 1 | 1 | 92.82 | 96.30 | 94.42 | 96.11 | 95.12 | 95.97 | 96.26 | 98.68 | 92.51 | 91.80 |
| 118 | 50 | 0.15 | 15 | 1 | 2 | 2 | 95.34 | 98.39 | 92.02 | 94.44 | 92.94 | 95.47 | 96.81 | 92.06 | 91.49 | 93.30 |
| 119 | 50 | 0.15 | 15 | 2 | 1 | 3 | 92.60 | 92.82 | 91.46 | 99.90 | 93.08 | 91.63 | 92.92 | 94.28 | 99.25 | 94.08 |
| 120 | 50 | 0.15 | 15 | 2 | 2 | 4 | 95.76 | 94.95 | 98.10 | 97.69 | 97.16 | 91.68 | 91.82 | 92.56 | 94.95 | 95.03 |
| 121 | 50 | 0.50 | 0 | 1 | 1 | 1 | 256.17 | 234.13 | 240.10 | 281.79 | 283.97 | 280.84 | 237.64 | 237.17 | 255.57 | 230.89 |
| 122 | 50 | 0.50 | 0 | 1 | 2 | 2 | 280.64 | 281.61 | 287.25 | 284.77 | 300.80 | 297.74 | 289.00 | 303.36 | 284.94 | 305.16 |
| 123 | 50 | 0.50 | 0 | 2 | 1 | 3 | 297.18 | 292.66 | 281.07 | 280.69 | 280.71 | 288.97 | 302.99 | 280.87 | 280.95 | 286.46 |
| 124 | 50 | 0.50 | 0 | 2 | 2 | 4 | 283.51 | 307.59 | 285.33 | 305.54 | 282.23 | 283.50 | 294.50 | 286.16 | 291.56 | 280.56 |
| 125 | 50 | 0.50 | 7 | 1 | 1 | 1 | 284.97 | 257.97 | 236.54 | 244.57 | 242.21 | 238.19 | 246.96 | 234.10 | 235.01 | 299.31 |
| 126 | 50 | 0.50 | 7 | 1 | 2 | 2 | 283.84 | 287.84 | 301.95 | 300.78 | 308.68 | 283.89 | 319.26 | 284.93 | 302.93 | 283.80 |
| 127 | 50 | 0.50 | 7 | 2 | 1 | 3 | 286.64 | 292.91 | 299.80 | 288.10 | 283.98 | 285.23 | 283.83 | 304.34 | 297.83 | 306.03 |
| 128 | 50 | 0.50 | 7 | 2 | 2 | 4 | 286.61 | 283.88 | 295.56 | 288.05 | 299.51 | 283.98 | 283.63 | 287.88 | 304.92 | 301.07 |
| 129 | 50 | 0.50 | 15 | 1 | 1 | 1 | 249.13 | 250.20 | 236.55 | 305.64 | 259.60 | 251.15 | 289.82 | 250.54 | 290.96 | 212.14 |
| 130 | 50 | 0.50 | 15 | 1 | 2 | 2 | 321.10 | 288.12 | 288.27 | 294.33 | 294.22 | 305.70 | 299.13 | 288.11 | 316.24 | 297.37 |
| 131 | 50 | 0.50 | 15 | 2 | 1 | 3 | 310.33 | 311.29 | 303.60 | 302.09 | 303.87 | 288.28 | 302.39 | 288.78 | 291.08 | 252.41 |
| 132 | 50 | 0.50 | 15 | 2 | 2 | 4 | 288.23 | 301.44 | 291.09 | 288.32 | 298.70 | 288.36 | 304.13 | 301.71 | 307.06 | 320.42 |
| 133 | 50 | 0.85 | 0 | 1 | 1 | 1 | 329.88 | 332.55 | 326.39 | 337.25 | 332.67 | 336.34 | 321.39 | 338.93 | 348.17 | 353.47 |
| 134 | 50 | 0.85 | 0 | 1 | 2 | 2 | 479.24 | 495.93 | 508.43 | 479.67 | 517.89 | 479.69 | 481.92 | 479.46 | 505.65 | 493.41 |
| 135 | 50 | 0.85 | 0 | 2 | 1 | 3 | 348.59 | 337.96 | 339.19 | 404.58 | 345.53 | 333.27 | 396.19 | 397.68 | 327.08 | 351.56 |
| 136 | 50 | 0.85 | 0 | 2 | 2 | 4 | 496.88 | 519.09 | 485.24 | 539.56 | 514.75 | 493.65 | 482.24 | 486.43 | 485.21 | 482.20 |
| 137 | 50 | 0.85 | 7 | 1 | 1 | 1 | 333.98 | 326.23 | 321.90 | 339.56 | 336.08 | 334.14 | 364.60 | 344.32 | 336.88 | 352.23 |
| 138 | 50 | 0.85 | 7 | 1 | 2 | 2 | 482.17 | 489.17 | 482.35 | 482.21 | 485.62 | 520.54 | 482.68 | 496.75 | 505.28 | 489.74 |
| 139 | 50 | 0.85 | 7 | 2 | 1 | 3 | 358.29 | 425.59 | 421.82 | 343.95 | 348.41 | 418.16 | 395.13 | 336.14 | 413.08 | 337.27 |
| 140 | 50 | 0.85 | 7 | 2 | 2 | 4 | 488.01 | 485.52 | 508.86 | 483.38 | 509.87 | 512.14 | 498.76 | 507.20 | 489.81 | 490.49 |
| 141 | 50 | 0.85 | 15 | 1 | 1 | 1 | 351.26 | 370.62 | 336.11 | 343.25 | 344.96 | 362.19 | 352.93 | 336.31 | 351.22 | 352.75 |
| 142 | 50 | 0.85 | 15 | 1 | 2 | 2 | 490.38 | 515.94 | 492.75 | 521.71 | 496.44 | 487.19 | 487.22 | 494.39 | 514.53 | 525.76 |
| 143 | 50 | 0.85 | 15 | 2 | 1 | 3 | 339.94 | 339.88 | 362.63 | 415.21 | 334.74 | 404.34 | 440.52 | 377.29 | 434.19 | 344.15 |
| 144 | 50 | 0.85 | 15 | 2 | 2 | 4 | 491.90 | 494.15 | 517.54 | 497.35 | 487.28 | 520.57 | 509.66 | 486.85 | 494.37 | 487.36 |

## APPENDIX J: SOLUTIONS \# SHORTCUTS FROM THE LLDP TESTING

| Test | $\Omega$ | $\rho_{\text {LСсмнs }}$ | t | $\theta$ | S | $\theta S$ | 1 | 2 | Number of Shortcuts for Replication |  |  |  |  |  | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  | 3 | 4 | 5 | 6 | 7 | 8 |  |  |
| 1 | 0.10 | 0.15 | 0 | 1 | 1 | 1 | 21 | 21 | 22 | 20 | 23 | 21 | 21 | 21 | 21 | 21 |
| 2 | 0.10 | 0.15 | 0 | 1 | 2 | 2 | 22 | 22 | 19 | 21 | 19 | 21 | 19 | 21 | 18 | 21 |
| 3 | 0.10 | 0.15 | 0 | 2 | 1 | 3 | 21 | 18 | 20 | 21 | 19 | 19 | 20 | 20 | 19 | 21 |
| 4 | 0.10 | 0.15 | 0 | 2 | 2 | 4 | 19 | 21 | 18 | 19 | 20 | 20 | 19 | 21 | 18 | 18 |
| 5 | 0.10 | 0.15 | 7 | 1 | 1 | 1 | 21 | 21 | 20 | 21 | 22 | 20 | 21 | 21 | 21 | 21 |
| 6 | 0.10 | 0.15 | 7 | 1 | 2 | 2 | 21 | 22 | 19 | 19 | 20 | 18 | 21 | 22 | 17 | 21 |
| 7 | 0.10 | 0.15 | 7 | 2 | 1 | 3 | 21 | 20 | 20 | 20 | 22 | 19 | 20 | 20 | 20 | 20 |
| 8 | 0.10 | 0.15 | 7 | 2 | 2 | 4 | 20 | 20 | 19 | 21 | 20 | 20 | 21 | 20 | 22 | 21 |
| 9 | 0.10 | 0.15 | 15 | 1 | 1 | 1 | 23 | 20 | 22 | 20 | 21 | 19 | 20 | 21 | 21 | 21 |
| 10 | 0.10 | 0.15 | 15 | 1 | 2 | 2 | 22 | 21 | 20 | 19 | 20 | 19 | 18 | 21 | 21 | 20 |
| 11 | 0.10 | 0.15 | 15 | 2 | 1 | 3 | 21 | 21 | 23 | 21 | 21 | 20 | 20 | 19 | 20 | 21 |
| 12 | 0.10 | 0.15 | 15 | 2 | 2 | 4 | 21 | 19 | 19 | 20 | 19 | 19 | 21 | 21 | 20 | 20 |
| 13 | 0.10 | 0.50 | 0 | 1 | 1 | 1 | 23 | 21 | 21 | 22 | 22 | 21 | 21 | 23 | 22 | 22 |
| 14 | 0.10 | 0.50 | 0 | 1 | 2 | 2 | 23 | 20 | 22 | 20 | 22 | 23 | 22 | 22 | 22 | 23 |
| 15 | 0.10 | 0.50 | 0 | 2 | 1 | 3 | 21 | 22 | 22 | 22 | 20 | 21 | 22 | 21 | 21 | 22 |
| 16 | 0.10 | 0.50 | 0 | 2 | 2 | 4 | 21 | 22 | 20 | 21 | 22 | 21 | 21 | 22 | 22 | 21 |
| 17 | 0.10 | 0.50 | 7 | 1 | 1 | 1 | 21 | 21 | 21 | 20 | 22 | 22 | 22 | 23 | 20 | 22 |
| 18 | 0.10 | 0.50 | 7 | 1 | 2 | 2 | 21 | 22 | 22 | 22 | 22 | 22 | 20 | 23 | 22 | 21 |
| 19 | 0.10 | 0.50 | 7 | 2 | 1 | 3 | 22 | 22 | 20 | 20 | 22 | 22 | 20 | 22 | 22 | 21 |
| 20 | 0.10 | 0.50 | 7 | 2 | 2 | 4 | 23 | 20 | 23 | 21 | 21 | 23 | 21 | 23 | 20 | 22 |
| 21 | 0.10 | 0.50 | 15 | 1 | 1 | 1 | 22 | 22 | 21 | 20 | 21 | 22 | 21 | 21 | 22 | 22 |
| 22 | 0.10 | 0.50 | 15 | 1 | 2 | 2 | 21 | 22 | 21 | 21 | 19 | 21 | 20 | 21 | 21 | 22 |
| 23 | 0.10 | 0.50 | 15 | 2 | 1 | 3 | 22 | 19 | 22 | 22 | 20 | 22 | 21 | 21 | 23 | 20 |
| 24 | 0.10 | 0.50 | 15 | 2 | 2 | 4 | 21 | 22 | 23 | 21 | 22 | 23 | 20 | 21 | 22 | 21 |
| 25 | 0.10 | 0.85 | 0 | 1 | 1 | 1 | 21 | 20 | 21 | 23 | 21 | 22 | 22 | 22 | 21 | 22 |
| 26 | 0.10 | 0.85 | 0 | 1 | 2 | 2 | 22 | 21 | 22 | 21 | 21 | 22 | 20 | 22 | 23 | 22 |


| 27 | 0.10 | 0.85 | 0 | 2 | 1 | 3 | 22 | 19 | 22 | 22 | 21 | 21 | 22 | 22 | 23 | 21 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 28 | 0.10 | 0.85 | 0 | 2 | 2 | 4 | 20 | 22 | 22 | 23 | 21 | 20 | 21 | 24 | 22 | 20 |
| 29 | 0.10 | 0.85 | 7 | 1 | 1 | 1 | 21 | 22 | 22 | 22 | 21 | 22 | 22 | 22 | 21 | 23 |
| 30 | 0.10 | 0.85 | 7 | 1 | 2 | 2 | 22 | 20 | 22 | 20 | 20 | 23 | 20 | 21 | 20 | 21 |
| 31 | 0.10 | 0.85 | 7 | 2 | 1 | 3 | 21 | 22 | 22 | 21 | 20 | 20 | 22 | 21 | 21 | 21 |
| 32 | 0.10 | 0.85 | 7 | 2 | 2 | 4 | 22 | 21 | 23 | 21 | 23 | 22 | 21 | 21 | 21 | 22 |
| 33 | 0.10 | 0.85 | 15 | 1 | 1 | 1 | 22 | 22 | 22 | 22 | 21 | 21 | 22 | 21 | 20 | 21 |
| 34 | 0.10 | 0.85 | 15 | 1 | 2 | 2 | 21 | 22 | 21 | 22 | 21 | 22 | 22 | 23 | 22 | 21 |
| 35 | 0.10 | 0.85 | 15 | 2 | 1 | 3 | 23 | 22 | 21 | 22 | 22 | 21 | 23 | 22 | 22 | 20 |
| 36 | 0.10 | 0.85 | 15 | 2 | 2 | 4 | 23 | 22 | 22 | 22 | 21 | 21 | 23 | 23 | 22 | 21 |
| 37 | 1 | 0.15 | 0 | 1 | 1 | 1 | 13 | 16 | 14 | 15 | 14 | 13 | 14 | 14 | 12 | 14 |
| 38 | 1 | 0.15 | 0 | 1 | 2 | 2 | 15 | 12 | 15 | 16 | 15 | 15 | 12 | 14 | 16 | 14 |
| 39 | 1 | 0.15 | 0 | 2 | 1 | 3 | 10 | 10 | 9 | 10 | 10 | 10 | 11 | 11 | 10 | 8 |
| 40 | 1 | 0.15 | 0 | 2 | 2 | 4 | 13 | 10 | 13 | 12 | 12 | 12 | 12 | 12 | 13 | 11 |
| 41 | 1 | 0.15 | 7 | 1 | 1 | 1 | 12 | 16 | 13 | 14 | 12 | 13 | 14 | 13 | 12 | 13 |
| 42 | 1 | 0.15 | 7 | 1 | 2 | 2 | 15 | 14 | 14 | 12 | 12 | 14 | 15 | 13 | 13 | 14 |
| 43 | 1 | 0.15 | 7 | 2 | 1 | 3 | 11 | 9 | 10 | 10 | 11 | 9 | 9 | 11 | 12 | 9 |
| 44 | 1 | 0.15 | 7 | 2 | 2 | 4 | 13 | 11 | 12 | 12 | 10 | 11 | 14 | 14 | 12 | 12 |
| 45 | 1 | 0.15 | 15 | 1 | 1 | 1 | 13 | 12 | 14 | 13 | 15 | 14 | 13 | 14 | 14 | 13 |
| 46 | 1 | 0.15 | 15 | 1 | 2 | 2 | 11 | 13 | 12 | 14 | 16 | 14 | 15 | 15 | 15 | 14 |
| 47 | 1 | 0.15 | 15 | 2 | 1 | 3 | 10 | 12 | 10 | 11 | 10 | 12 | 9 | 11 | 11 | 11 |
| 48 | 1 | 0.15 | 15 | 2 | 2 | 4 | 9 | 12 | 12 | 12 | 13 | 14 | 12 | 12 | 11 | 12 |
| 49 | 1 | 0.50 | 0 | 1 | 1 | 1 | 20 | 20 | 20 | 19 | 19 | 20 | 19 | 18 | 20 | 20 |
| 50 | 1 | 0.50 | 0 | 1 | 2 | 2 | 18 | 18 | 18 | 20 | 17 | 19 | 18 | 17 | 20 | 17 |
| 51 | 1 | 0.50 | 0 | 2 | 1 | 3 | 17 | 17 | 15 | 16 | 16 | 16 | 16 | 15 | 18 | 16 |
| 52 | 1 | 0.50 | 0 | 2 | 2 | 4 | 18 | 19 | 17 | 18 | 19 | 16 | 19 | 20 | 15 | 19 |
| 53 | 1 | 0.50 | 7 | 1 | 1 | 1 | 20 | 20 | 20 | 20 | 19 | 20 | 20 | 18 | 20 | 19 |
| 54 | 1 | 0.50 | 7 | 1 | 2 | 2 | 19 | 17 | 19 | 19 | 18 | 19 | 19 | 19 | 18 | 19 |
| 55 | 1 | 0.50 | 7 | 2 | 1 | 3 | 15 | 16 | 16 | 16 | 15 | 14 | 17 | 16 | 17 | 17 |
| 56 | 1 | 0.50 | 7 | 2 | 2 | 4 | 16 | 17 | 19 | 17 | 19 | 19 | 18 | 21 | 17 | 17 |


| 57 | 1 | 0.50 | 15 | 1 | 1 | 1 | 19 | 18 | 19 | 20 | 20 | 19 | 21 | 21 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 58 | 1 | 0.50 | 15 | 1 | 2 | 2 | 18 | 20 | 19 | 22 | 20 | 18 | 18 | 18 | 17 | 20 |
| 59 | 1 | 0.50 | 15 | 2 | 1 | 3 | 15 | 16 | 15 | 16 | 16 | 17 | 17 | 17 | 15 | 16 |
| 60 | 1 | 0.50 | 15 | 2 | 2 | 4 | 18 | 18 | 16 | 20 | 19 | 20 | 19 | 16 | 17 | 17 |
| 61 | 1 | 0.85 | 0 | 1 | 1 | 1 | 20 | 21 | 21 | 22 | 21 | 21 | 20 | 20 | 20 | 21 |
| 62 | 1 | 0.85 | 0 | 1 | 2 | 2 | 18 | 21 | 20 | 21 | 20 | 20 | 19 | 20 | 20 | 20 |
| 63 | 1 | 0.85 | 0 | 2 | 1 | 3 | 18 | 18 | 19 | 21 | 19 | 17 | 17 | 19 | 18 | 18 |
| 64 | 1 | 0.85 | 0 | 2 | 2 | 4 | 19 | 21 | 19 | 17 | 19 | 18 | 20 | 18 | 19 | 20 |
| 65 | 1 | 0.85 | 7 | 1 | 1 | 1 | 20 | 21 | 21 | 20 | 22 | 20 | 21 | 21 | 21 | 21 |
| 66 | 1 | 0.85 | 7 | 1 | 2 | 2 | 17 | 17 | 19 | 19 | 20 | 20 | 19 | 19 | 20 | 18 |
| 67 | 1 | 0.85 | 7 | 2 | 1 | 3 | 18 | 20 | 19 | 20 | 17 | 20 | 20 | 19 | 19 | 20 |
| 68 | 1 | 0.85 | 7 | 2 | 2 | 4 | 19 | 19 | 20 | 19 | 20 | 19 | 18 | 18 | 20 | 18 |
| 69 | 1 | 0.85 | 15 | 1 | 1 | 1 | 20 | 21 | 21 | 21 | 22 | 20 | 23 | 21 | 21 | 20 |
| 70 | 1 | 0.85 | 15 | 1 | 2 | 2 | 17 | 22 | 19 | 20 | 21 | 22 | 20 | 20 | 20 | 20 |
| 71 | 1 | 0.85 | 15 | 2 | 1 | 3 | 18 | 18 | 18 | 19 | 19 | 19 | 20 | 17 | 19 | 19 |
| 72 | 1 | 0.85 | 15 | 2 | 2 | 4 | 19 | 20 | 19 | 20 | 20 | 19 | 20 | 21 | 19 | 21 |
| 73 | 10 | 0.15 | 0 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 74 | 10 | 0.15 | 0 | 1 | 2 | 2 | 4 | 4 | 4 | 3 | 4 | 4 | 4 | 4 | 4 | 3 |
| 75 | 10 | 0.15 | 0 | 2 | 1 | 3 | 3 | 3 | 3 | 3 | 4 | 3 | 3 | 2 | 3 | 3 |
| 76 | 10 | 0.15 | 0 | 2 | 2 | 4 | 2 | 4 | 2 | 3 | 4 | 3 | 3 | 3 | 3 | 3 |
| 77 | 10 | 0.15 | 7 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 78 | 10 | 0.15 | 7 | 1 | 2 | 2 | 4 | 4 | 4 | 4 | 3 | 4 | 3 | 4 | 4 | 4 |
| 79 | 10 | 0.15 | 7 | 2 | 1 | 3 | 3 | 3 | 4 | 3 | 3 | 3 | 3 | 4 | 4 | 3 |
| 80 | 10 | 0.15 | 7 | 2 | 2 | 4 | 4 | 4 | 3 | 4 | 4 | 4 | 4 | 3 | 4 | 4 |
| 81 | 10 | 0.15 | 15 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 82 | 10 | 0.15 | 15 | 1 | 2 | 2 | 4 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 83 | 10 | 0.15 | 15 | 2 | 1 | 3 | 4 | 4 | 3 | 4 | 4 | 3 | 3 | 4 | 3 | 3 |
| 84 | 10 | 0.15 | 15 | 2 | 2 | 4 | 3 | 3 | 4 | 4 | 4 | 3 | 3 | 3 | 4 | 3 |
| 85 | 10 | 0.50 | 0 | 1 | 1 | 1 | 7 | 7 | 7 | 6 | 6 | 7 | 8 | 6 | 8 | 7 |
| 86 | 10 | 0.50 | 0 | 1 | 2 | 2 | 10 | 9 | 5 | 7 | 6 | 8 | 7 | 9 | 7 | 8 |


| 87 | 10 | 0.50 | 0 | 2 | 1 | 3 | 5 | 4 | 5 | 6 | 5 | 5 | 5 | 6 | 4 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88 | 10 | 0.50 | 0 | 2 | 2 | 4 | 5 | 6 | 5 | 8 | 6 | 7 | 4 | 6 | 6 | 7 |
| 89 | 10 | 0.50 | 7 | 1 | 1 | 1 | 8 | 6 | 8 | 6 | 8 | 6 | 6 | 6 | 7 | 6 |
| 90 | 10 | 0.50 | 7 | 1 | 2 | 2 | 8 | 6 | 6 | 9 | 9 | 7 | 6 | 7 | 7 | 8 |
| 91 | 10 | 0.50 | 7 | 2 | 1 | 3 | 6 | 6 | 6 | 5 | 6 | 6 | 6 | 5 | 5 | 5 |
| 92 | 10 | 0.50 | 7 | 2 | 2 | 4 | 5 | 6 | 7 | 6 | 6 | 5 | 6 | 6 | 7 | 7 |
| 93 | 10 | 0.50 | 15 | 1 | 1 | 1 | 7 | 8 | 8 | 6 | 7 | 8 | 8 | 8 | 8 | 8 |
| 94 | 10 | 0.50 | 15 | 1 | 2 | 2 | 11 | 6 | 5 | 8 | 8 | 8 | 5 | 7 | 7 | 8 |
| 95 | 10 | 0.50 | 15 | 2 | 1 | 3 | 6 | 6 | 6 | 6 | 5 | 4 | 6 | 6 | 4 | 5 |
| 96 | 10 | 0.50 | 15 | 2 | 2 | 4 | 7 | 6 | 6 | 8 | 5 | 7 | 6 | 6 | 8 | 7 |
| 97 | 10 | 0.85 | 0 | 1 | 1 | 1 | 9 | 10 | 8 | 10 | 11 | 10 | 11 | 10 | 10 | 11 |
| 98 | 10 | 0.85 | 0 | 1 | 2 | 2 | 12 | 9 | 11 | 11 | 13 | 13 | 12 | 12 | 11 | 11 |
| 99 | 10 | 0.85 | 0 | 2 | 1 | 3 | 6 | 7 | 7 | 6 | 8 | 8 | 9 | 8 | 6 | 7 |
| 100 | 10 | 0.85 | 0 | 2 | 2 | 4 | 9 | 9 | 8 | 7 | 7 | 10 | 10 | 10 | 10 | 10 |
| 101 | 10 | 0.85 | 7 | 1 | 1 | 1 | 10 | 11 | 10 | 10 | 10 | 10 | 9 | 8 | 10 | 8 |
| 102 | 10 | 0.85 | 7 | 1 | 2 | 2 | 10 | 14 | 9 | 10 | 13 | 11 | 11 | 13 | 11 | 11 |
| 103 | 10 | 0.85 | 7 | 2 | 1 | 3 | 6 | 6 | 7 | 8 | 7 | 8 | 6 | 7 | 7 | 7 |
| 104 | 10 | 0.85 | 7 | 2 | 2 | 4 | 9 | 7 | 9 | 7 | 9 | 10 | 8 | 9 | 12 | 9 |
| 105 | 10 | 0.85 | 15 | 1 | 1 | 1 | 11 | 10 | 11 | 9 | 9 | 10 | 9 | 10 | 11 | 10 |
| 106 | 10 | 0.85 | 15 | 1 | 2 | 2 | 11 | 8 | 12 | 9 | 11 | 11 | 12 | 10 | 11 | 11 |
| 107 | 10 | 0.85 | 15 | 2 | 1 | 3 | 7 | 7 | 7 | 7 | 8 | 7 | 7 | 6 | 6 | 7 |
| 108 | 10 | 0.85 | 15 | 2 | 2 | 4 | 9 | 9 | 9 | 8 | 10 | 9 | 8 | 8 | 9 | 8 |
| 109 | 50 | 0.15 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 110 | 50 | 0.15 | 0 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 111 | 50 | 0.15 | 0 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 112 | 50 | 0.15 | 0 | 2 | 2 | 4 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 113 | 50 | 0.15 | 7 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 114 | 50 | 0.15 | 7 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 115 | 50 | 0.15 | 7 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 116 | 50 | 0.15 | 7 | 2 | 2 | 4 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |


| 117 | 50 | 0.15 | 15 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118 | 50 | 0.15 | 15 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 119 | 50 | 0.15 | 15 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 120 | 50 | 0.15 | 15 | 2 | 2 | 4 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 121 | 50 | 0.50 | 0 | 1 | 1 | 1 | 3 | 3 | 3 | 2 | 2 | 2 | 3 | 3 | 3 | 3 |
| 122 | 50 | 0.50 | 0 | 1 | 2 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 3 | 3 |
| 123 | 50 | 0.50 | 0 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 124 | 50 | 0.50 | 0 | 2 | 2 | 4 | 2 | 2 | 3 | 3 | 2 | 2 | 2 | 2 | 2 | 2 |
| 125 | 50 | 0.50 | 7 | 1 | 1 | 1 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 |
| 126 | 50 | 0.50 | 7 | 1 | 2 | 2 | 2 | 3 | 2 | 2 | 2 | 3 | 3 | 4 | 2 | 3 |
| 127 | 50 | 0.50 | 7 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| 128 | 50 | 0.50 | 7 | 2 | 2 | 4 | 2 | 2 | 2 | 2 | 2 | 3 | 2 | 2 | 3 | 2 |
| 129 | 50 | 0.50 | 15 | 1 | 1 | 1 | 3 | 3 | 3 | 2 | 3 | 3 | 2 | 3 | 2 | 4 |
| 130 | 50 | 0.50 | 15 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 3 | 3 | 3 | 2 |
| 131 | 50 | 0.50 | 15 | 2 | 1 | 3 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 |
| 132 | 50 | 0.50 | 15 | 2 | 2 | 4 | 2 | 2 | 2 | 2 | 3 | 3 | 2 | 2 | 3 | 2 |
| 133 | 50 | 0.85 | 0 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 134 | 50 | 0.85 | 0 | 1 | 2 | 2 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 135 | 50 | 0.85 | 0 | 2 | 1 | 3 | 4 | 4 | 4 | 3 | 4 | 4 | 3 | 3 | 4 | 4 |
| 136 | 50 | 0.85 | 0 | 2 | 2 | 4 | 4 | 3 | 4 | 3 | 4 | 4 | 4 | 3 | 4 | 4 |
| 137 | 50 | 0.85 | 7 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 138 | 50 | 0.85 | 7 | 1 | 2 | 2 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 139 | 50 | 0.85 | 7 | 2 | 1 | 3 | 4 | 3 | 3 | 4 | 4 | 3 | 3 | 4 | 3 | 4 |
| 140 | 50 | 0.85 | 7 | 2 | 2 | 4 | 4 | 4 | 4 | 4 | 3 | 4 | 4 | 4 | 3 | 4 |
| 141 | 50 | 0.85 | 15 | 1 | 1 | 1 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 142 | 50 | 0.85 | 15 | 1 | 2 | 2 | 4 | 4 | 4 | 4 | 3 | 4 | 4 | 4 | 4 | 3 |
| 143 | 50 | 0.85 | 15 | 2 | 1 | 3 | 4 | 4 | 4 | 3 | 4 | 3 | 3 | 4 | 3 | 4 |
| 144 | 50 | 0.85 | 15 | 2 | 2 | 4 | 4 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | 3 | 4 |

## APPENDIX K: SOLUTIONS \# ITERATIONS FROM THE LLDP TESTING

Number of Iterations for Replication

| Test | $\Omega$ | $\rho_{\text {LCMHS }}$ | t | $\theta$ | S | $\theta S$ | 1 | 2 | 3 | 4 | 5 | 6 | Replicati |  | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  | 7 | 8 |  |  |
| 1 | 0.10 | 0.15 | 0 | 1 | 1 | 1 | 1005 | 1146 | 1260 | 896 | 980 | 1309 | 953 | 1253 | 870 | 930 |
| 2 | 0.10 | 0.15 | 0 | 1 | 2 | 2 | 1663 | 1302 | 1439 | 1417 | 1573 | 1363 | 1696 | 1784 | 1156 | 1266 |
| 3 | 0.10 | 0.15 | 0 | 2 | 1 | 3 | 1029 | 820 | 751 | 982 | 1840 | 742 | 1777 | 955 | 671 | 848 |
| 4 | 0.10 | 0.15 | 0 | 2 | 2 | 4 | 1920 | 827 | 1765 | 1088 | 1197 | 1221 | 1615 | 1304 | 1064 | 1553 |
| 5 | 0.10 | 0.15 | 7 | 1 | 1 | 1 | 793 | 1525 | 1000 | 1042 | 988 | 884 | 906 | 889 | 789 | 1413 |
| 6 | 0.10 | 0.15 | 7 | 1 | 2 | 2 | 1275 | 1657 | 1441 | 759 | 1360 | 1070 | 1438 | 2425 | 1011 | 1032 |
| 7 | 0.10 | 0.15 | 7 | 2 | 1 | 3 | 1047 | 802 | 962 | 699 | 771 | 856 | 811 | 1614 | 881 | 850 |
| 8 | 0.10 | 0.15 | 7 | 2 | 2 | 4 | 2484 | 1724 | 1793 | 1838 | 1148 | 1416 | 1127 | 919 | 1989 | 1159 |
| 9 | 0.10 | 0.15 | 15 | 1 | 1 | 1 | 794 | 955 | 862 | 1137 | 771 | 976 | 952 | 839 | 952 | 880 |
| 10 | 0.10 | 0.15 | 15 | 1 | 2 | 2 | 1662 | 2049 | 861 | 1146 | 932 | 1010 | 1003 | 1175 | 1576 | 2190 |
| 11 | 0.10 | 0.15 | 15 | 2 | 1 | 3 | 972 | 882 | 810 | 896 | 723 | 1660 | 666 | 1216 | 816 | 798 |
| 12 | 0.10 | 0.15 | 15 | 2 | 2 | 4 | 1068 | 1093 | 1464 | 1376 | 827 | 995 | 2529 | 2643 | 1125 | 952 |
| 13 | 0.10 | 0.50 | 0 | 1 | 1 | 1 | 1722 | 2064 | 798 | 924 | 954 | 1131 | 783 | 1234 | 1328 | 993 |
| 14 | 0.10 | 0.50 | 0 | 1 | 2 | 2 | 1466 | 1604 | 1103 | 1028 | 1105 | 881 | 1083 | 2558 | 1676 | 1265 |
| 15 | 0.10 | 0.50 | 0 | 2 | 1 | 3 | 1321 | 964 | 962 | 932 | 1425 | 1297 | 1028 | 1117 | 928 | 950 |
| 16 | 0.10 | 0.50 | 0 | 2 | 2 | 4 | 2852 | 1084 | 1674 | 1513 | 998 | 1432 | 853 | 1705 | 1509 | 1036 |
| 17 | 0.10 | 0.50 | 7 | 1 | 1 | 1 | 880 | 929 | 890 | 1718 | 1714 | 1936 | 929 | 748 | 950 | 747 |
| 18 | 0.10 | 0.50 | 7 | 1 | 2 | 2 | 1005 | 2441 | 1146 | 1217 | 1216 | 2067 | 1572 | 1119 | 766 | 2040 |
| 19 | 0.10 | 0.50 | 7 | 2 | 1 | 3 | 824 | 1119 | 1327 | 2127 | 897 | 710 | 823 | 778 | 1523 | 1238 |
| 20 | 0.10 | 0.50 | 7 | 2 | 2 | 4 | 855 | 1126 | 943 | 1412 | 1124 | 2092 | 1147 | 748 | 1510 | 834 |
| 21 | 0.10 | 0.50 | 15 | 1 | 1 | 1 | 1210 | 770 | 1150 | 840 | 857 | 1302 | 1061 | 678 | 840 | 741 |
| 22 | 0.10 | 0.50 | 15 | 1 | 2 | 2 | 1272 | 1483 | 1489 | 1277 | 809 | 1538 | 859 | 1424 | 1338 | 1965 |
| 23 | 0.10 | 0.50 | 15 | 2 | 1 | 3 | 1583 | 1049 | 737 | 838 | 1063 | 805 | 816 | 1786 | 1516 | 1863 |
| 24 | 0.10 | 0.50 | 15 | 2 | 2 | 4 | 1684 | 1075 | 985 | 1871 | 1149 | 1584 | 864 | 952 | 848 | 1079 |
| 25 | 0.10 | 0.85 | 0 | 1 | 1 | 1 | 706 | 1205 | 1379 | 1024 | 936 | 1507 | 1254 | 928 | 1137 | 750 |
| 26 | 0.10 | 0.85 | 0 | 1 | 2 | 2 | 1307 | 942 | 838 | 1536 | 1688 | 1772 | 967 | 902 | 2006 | 1910 |


| 27 | 0.10 | 0.85 | 0 | 2 | 1 | 3 | 1004 | 935 | 1332 | 907 | 805 | 837 | 688 | 1017 | 1317 | 1237 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 28 | 0.10 | 0.85 | 0 | 2 | 2 | 4 | 1489 | 1569 | 871 | 1048 | 2240 | 1278 | 1712 | 2682 | 1595 | 1403 |
| 29 | 0.10 | 0.85 | 7 | 1 | 1 | 1 | 861 | 1433 | 1256 | 1006 | 876 | 973 | 1251 | 1524 | 903 | 813 |
| 30 | 0.10 | 0.85 | 7 | 1 | 2 | 2 | 1831 | 2888 | 976 | 1535 | 1623 | 953 | 953 | 2630 | 988 | 2073 |
| 31 | 0.10 | 0.85 | 7 | 2 | 1 | 3 | 1144 | 845 | 1358 | 1239 | 2302 | 872 | 1708 | 1218 | 1509 | 1355 |
| 32 | 0.10 | 0.85 | 7 | 2 | 2 | 4 | 1007 | 820 | 3171 | 953 | 1650 | 1785 | 872 | 943 | 967 | 888 |
| 33 | 0.10 | 0.85 | 15 | 1 | 1 | 1 | 1091 | 1479 | 856 | 1121 | 760 | 824 | 859 | 935 | 976 | 1039 |
| 34 | 0.10 | 0.85 | 15 | 1 | 2 | 2 | 2484 | 2655 | 1158 | 869 | 1430 | 1535 | 2008 | 1032 | 1787 | 1051 |
| 35 | 0.10 | 0.85 | 15 | 2 | 1 | 3 | 798 | 1011 | 692 | 893 | 776 | 834 | 1383 | 1130 | 1044 | 861 |
| 36 | 0.10 | 0.85 | 15 | 2 | 2 | 4 | 1424 | 2726 | 925 | 960 | 970 | 1509 | 1182 | 1652 | 1166 | 1685 |
| 37 | 1 | 0.15 | 0 | 1 | 1 | 1 | 1015 | 1417 | 1126 | 1390 | 677 | 930 | 1674 | 1418 | 1398 | 726 |
| 38 | 1 | 0.15 | 0 | 1 | 2 | 2 | 1247 | 1657 | 975 | 1021 | 1153 | 942 | 1118 | 2256 | 932 | 924 |
| 39 | 1 | 0.15 | 0 | 2 | 1 | 3 | 1027 | 1625 | 1101 | 892 | 766 | 1304 | 1104 | 831 | 1284 | 1305 |
| 40 | 1 | 0.15 | 0 | 2 | 2 | 4 | 1015 | 2534 | 987 | 2396 | 1400 | 1633 | 1464 | 1101 | 1084 | 1133 |
| 41 | 1 | 0.15 | 7 | 1 | 1 | 1 | 1673 | 1483 | 1243 | 925 | 1294 | 672 | 1189 | 741 | 1095 | 594 |
| 42 | 1 | 0.15 | 7 | 1 | 2 | 2 | 854 | 892 | 2074 | 769 | 1420 | 1183 | 1206 | 1022 | 1815 | 2045 |
| 43 | 1 | 0.15 | 7 | 2 | 1 | 3 | 851 | 807 | 2214 | 1244 | 1135 | 1228 | 673 | 932 | 1816 | 880 |
| 44 | 1 | 0.15 | 7 | 2 | 2 | 4 | 1032 | 986 | 1082 | 1185 | 959 | 1467 | 1624 | 2207 | 1398 | 900 |
| 45 | 1 | 0.15 | 15 | 1 | 1 | 1 | 809 | 947 | 1380 | 877 | 998 | 1636 | 1132 | 912 | 910 | 1146 |
| 46 | 1 | 0.15 | 15 | 1 | 2 | 2 | 1058 | 1551 | 954 | 1311 | 771 | 1456 | 1864 | 2465 | 919 | 1253 |
| 47 | 1 | 0.15 | 15 | 2 | 1 | 3 | 1000 | 725 | 1482 | 661 | 1154 | 929 | 1041 | 1437 | 964 | 805 |
| 48 | 1 | 0.15 | 15 | 2 | 2 | 4 | 1664 | 1686 | 1960 | 1509 | 1289 | 847 | 2428 | 1449 | 1835 | 714 |
| 49 | 1 | 0.50 | 0 | 1 | 1 | 1 | 814 | 723 | 902 | 977 | 1279 | 874 | 787 | 724 | 718 | 955 |
| 50 | 1 | 0.50 | 0 | 1 | 2 | 2 | 1816 | 2698 | 1597 | 789 | 1530 | 839 | 2087 | 1211 | 1382 | 2415 |
| 51 | 1 | 0.50 | 0 | 2 | 1 | 3 | 1388 | 1413 | 1222 | 1501 | 1695 | 693 | 1007 | 789 | 1195 | 1941 |
| 52 | 1 | 0.50 | 0 | 2 | 2 | 4 | 1383 | 2087 | 1085 | 1693 | 1566 | 1365 | 1153 | 1142 | 985 | 1432 |
| 53 | 1 | 0.50 | 7 | 1 | 1 | 1 | 960 | 1374 | 1497 | 1490 | 2716 | 813 | 962 | 846 | 1115 | 822 |
| 54 | 1 | 0.50 | 7 | 1 | 2 | 2 | 2048 | 1563 | 2797 | 910 | 2633 | 1262 | 1003 | 828 | 2987 | 1412 |
| 55 | 1 | 0.50 | 7 | 2 | 1 | 3 | 798 | 1901 | 758 | 1257 | 788 | 988 | 1170 | 927 | 866 | 696 |
| 56 | 1 | 0.50 | 7 | 2 | 2 | 4 | 1690 | 4024 | 1744 | 1165 | 1836 | 1349 | 1285 | 1201 | 1038 | 1799 |


| 57 | 1 | 0.50 | 15 | 1 | 1 | 1 | 1132 | 1441 | 1184 | 903 | 1114 | 1039 | 876 | 941 | 634 | 1707 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 58 | 1 | 0.50 | 15 | 1 | 2 | 2 | 1181 | 959 | 774 | 1096 | 1008 | 1061 | 1919 | 930 | 2446 | 873 |
| 59 | 1 | 0.50 | 15 | 2 | 1 | 3 | 972 | 729 | 897 | 1294 | 1239 | 939 | 1443 | 1315 | 1284 | 1097 |
| 60 | 1 | 0.50 | 15 | 2 | 2 | 4 | 862 | 1355 | 1341 | 1323 | 980 | 913 | 2339 | 1482 | 1342 | 832 |
| 61 | 1 | 0.85 | 0 | 1 | 1 | 1 | 1131 | 2244 | 789 | 1672 | 1507 | 785 | 1192 | 914 | 867 | 2167 |
| 62 | 1 | 0.85 | 0 | 1 | 2 | 2 | 1014 | 1585 | 2235 | 986 | 1276 | 1418 | 1456 | 808 | 1632 | 1363 |
| 63 | 1 | 0.85 | 0 | 2 | 1 | 3 | 711 | 935 | 1193 | 1619 | 1722 | 733 | 1494 | 740 | 1284 | 795 |
| 64 | 1 | 0.85 | 0 | 2 | 2 | 4 | 904 | 1496 | 951 | 1828 | 1062 | 1452 | 1654 | 1303 | 837 | 1892 |
| 65 | 1 | 0.85 | 7 | 1 | 1 | 1 | 1271 | 901 | 1514 | 1074 | 1093 | 1397 | 898 | 898 | 911 | 1755 |
| 66 | 1 | 0.85 | 7 | 1 | 2 | 2 | 1004 | 1543 | 1734 | 1403 | 1677 | 1824 | 980 | 1293 | 996 | 1191 |
| 67 | 1 | 0.85 | 7 | 2 | 1 | 3 | 811 | 1150 | 1008 | 680 | 883 | 926 | 1207 | 841 | 1378 | 781 |
| 68 | 1 | 0.85 | 7 | 2 | 2 | 4 | 1757 | 1489 | 1010 | 1553 | 1208 | 1133 | 2494 | 1145 | 1872 | 1342 |
| 69 | 1 | 0.85 | 15 | 1 | 1 | 1 | 807 | 2192 | 1009 | 871 | 862 | 742 | 806 | 892 | 1028 | 715 |
| 70 | 1 | 0.85 | 15 | 1 | 2 | 2 | 807 | 3994 | 1411 | 1115 | 1141 | 1402 | 1368 | 1591 | 2686 | 1008 |
| 71 | 1 | 0.85 | 15 | 2 | 1 | 3 | 1263 | 830 | 1594 | 1221 | 893 | 910 | 1417 | 901 | 804 | 754 |
| 72 | 1 | 0.85 | 15 | 2 | 2 | 4 | 2190 | 1389 | 853 | 1855 | 1167 | 1502 | 1733 | 989 | 1239 | 1735 |
| 73 | 10 | 0.15 | 0 | 1 | 1 | 1 | 861 | 810 | 1213 | 2050 | 768 | 976 | 1007 | 1544 | 1089 | 690 |
| 74 | 10 | 0.15 | 0 | 1 | 2 | 2 | 779 | 1386 | 930 | 1083 | 883 | 1867 | 1447 | 1932 | 930 | 1708 |
| 75 | 10 | 0.15 | 0 | 2 | 1 | 3 | 1246 | 790 | 728 | 1146 | 1112 | 1970 | 1201 | 1263 | 1543 | 1084 |
| 76 | 10 | 0.15 | 0 | 2 | 2 | 4 | 1396 | 895 | 1030 | 1483 | 1849 | 1089 | 1206 | 2098 | 1714 | 1088 |
| 77 | 10 | 0.15 | 7 | 1 | 1 | 1 | 874 | 2498 | 942 | 976 | 1608 | 1359 | 2028 | 1634 | 825 | 840 |
| 78 | 10 | 0.15 | 7 | 1 | 2 | 2 | 1056 | 1894 | 1254 | 1199 | 2000 | 1491 | 748 | 896 | 899 | 1308 |
| 79 | 10 | 0.15 | 7 | 2 | 1 | 3 | 1072 | 1405 | 938 | 1453 | 952 | 1724 | 779 | 777 | 805 | 1308 |
| 80 | 10 | 0.15 | 7 | 2 | 2 | 4 | 1020 | 1699 | 1026 | 1840 | 1529 | 1616 | 1248 | 948 | 2031 | 1079 |
| 81 | 10 | 0.15 | 15 | 1 | 1 | 1 | 1844 | 892 | 903 | 1500 | 2236 | 1712 | 1004 | 1652 | 1343 | 1772 |
| 82 | 10 | 0.15 | 15 | 1 | 2 | 2 | 1217 | 1170 | 1246 | 1140 | 1507 | 1152 | 1212 | 846 | 997 | 2233 |
| 83 | 10 | 0.15 | 15 | 2 | 1 | 3 | 1851 | 745 | 1756 | 1219 | 1616 | 1005 | 946 | 1022 | 1483 | 1373 |
| 84 | 10 | 0.15 | 15 | 2 | 2 | 4 | 1120 | 971 | 1017 | 1474 | 2257 | 921 | 947 | 948 | 1039 | 930 |
| 85 | 10 | 0.50 | 0 | 1 | 1 | 1 | 1574 | 793 | 1230 | 1374 | 831 | 909 | 722 | 1067 | 1061 | 1799 |
| 86 | 10 | 0.50 | 0 | 1 | 2 | 2 | 1089 | 1626 | 840 | 2125 | 2697 | 938 | 1257 | 936 | 2158 | 839 |


| 87 | 10 | 0.50 | 0 | 2 | 1 | 3 | 1149 | 826 | 1147 | 717 | 1357 | 1189 | 2139 | 748 | 951 | 985 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88 | 10 | 0.50 | 0 | 2 | 2 | 4 | 867 | 1322 | 1005 | 1245 | 1163 | 1424 | 1268 | 1142 | 1131 | 2296 |
| 89 | 10 | 0.50 | 7 | 1 | 1 | 1 | 1196 | 760 | 1004 | 1322 | 1248 | 2059 | 1400 | 1522 | 1348 | 1101 |
| 90 | 10 | 0.50 | 7 | 1 | 2 | 2 | 1155 | 1327 | 1905 | 1315 | 1346 | 1862 | 1016 | 2378 | 2084 | 1409 |
| 91 | 10 | 0.50 | 7 | 2 | 1 | 3 | 2959 | 953 | 1564 | 938 | 1208 | 995 | 1492 | 1246 | 980 | 1323 |
| 92 | 10 | 0.50 | 7 | 2 | 2 | 4 | 1092 | 1428 | 836 | 1799 | 1663 | 1166 | 884 | 1131 | 796 | 923 |
| 93 | 10 | 0.50 | 15 | 1 | 1 | 1 | 904 | 809 | 1019 | 1069 | 1889 | 981 | 909 | 765 | 1575 | 1340 |
| 94 | 10 | 0.50 | 15 | 1 | 2 | 2 | 1084 | 1717 | 1517 | 1428 | 1404 | 1350 | 952 | 1316 | 1491 | 2165 |
| 95 | 10 | 0.50 | 15 | 2 | 1 | 3 | 934 | 1895 | 890 | 900 | 1425 | 1410 | 1667 | 753 | 741 | 1376 |
| 96 | 10 | 0.50 | 15 | 2 | 2 | 4 | 1172 | 1913 | 1164 | 1235 | 1750 | 1322 | 1229 | 1230 | 1432 | 1046 |
| 97 | 10 | 0.85 | 0 | 1 | 1 | 1 | 2470 | 1124 | 727 | 756 | 769 | 922 | 1338 | 1030 | 893 | 761 |
| 98 | 10 | 0.85 | 0 | 1 | 2 | 2 | 1372 | 1356 | 845 | 1490 | 1679 | 2282 | 1545 | 939 | 1827 | 1377 |
| 99 | 10 | 0.85 | 0 | 2 | 1 | 3 | 1223 | 1351 | 1056 | 646 | 2144 | 2074 | 776 | 729 | 833 | 884 |
| 100 | 10 | 0.85 | 0 | 2 | 2 | 4 | 1299 | 1238 | 1038 | 718 | 1235 | 1556 | 1033 | 1217 | 1504 | 1030 |
| 101 | 10 | 0.85 | 7 | 1 | 1 | 1 | 1246 | 1191 | 723 | 858 | 1077 | 717 | 1965 | 715 | 1708 | 1270 |
| 102 | 10 | 0.85 | 7 | 1 | 2 | 2 | 1072 | 1200 | 1100 | 1314 | 1280 | 923 | 1788 | 1160 | 1550 | 1814 |
| 103 | 10 | 0.85 | 7 | 2 | 1 | 3 | 798 | 1333 | 793 | 1208 | 1321 | 708 | 1343 | 907 | 1009 | 1288 |
| 104 | 10 | 0.85 | 7 | 2 | 2 | 4 | 1827 | 1164 | 1179 | 1422 | 1040 | 1397 | 1292 | 1858 | 968 | 1306 |
| 105 | 10 | 0.85 | 15 | 1 | 1 | 1 | 788 | 850 | 1149 | 940 | 814 | 1856 | 1086 | 1482 | 1014 | 1029 |
| 106 | 10 | 0.85 | 15 | 1 | 2 | 2 | 1978 | 1986 | 1110 | 2319 | 1784 | 1343 | 911 | 1239 | 1270 | 2499 |
| 107 | 10 | 0.85 | 15 | 2 | 1 | 3 | 967 | 960 | 990 | 1087 | 1571 | 1088 | 2329 | 1498 | 998 | 864 |
| 108 | 10 | 0.85 | 15 | 2 | 2 | 4 | 971 | 1426 | 1701 | 1211 | 990 | 2635 | 1880 | 1097 | 1546 | 1823 |
| 109 | 50 | 0.15 | 0 | 1 | 1 | 1 | 1356 | 1084 | 1445 | 1037 | 1867 | 1315 | 1821 | 1093 | 3456 | 1160 |
| 110 | 50 | 0.15 | 0 | 1 | 2 | 2 | 1098 | 1047 | 900 | 1109 | 743 | 867 | 1535 | 1862 | 1484 | 1279 |
| 111 | 50 | 0.15 | 0 | 2 | 1 | 3 | 1576 | 1365 | 907 | 1050 | 1576 | 1711 | 1291 | 1337 | 1988 | 1528 |
| 112 | 50 | 0.15 | 0 | 2 | 2 | 4 | 1456 | 1286 | 750 | 917 | 1654 | 1706 | 1822 | 907 | 905 | 1099 |
| 113 | 50 | 0.15 | 7 | 1 | 1 | 1 | 1005 | 1145 | 1264 | 767 | 1152 | 1323 | 1205 | 938 | 1253 | 1604 |
| 114 | 50 | 0.15 | 7 | 1 | 2 | 2 | 1057 | 1359 | 1122 | 1173 | 1385 | 834 | 1280 | 1340 | 1862 | 859 |
| 115 | 50 | 0.15 | 7 | 2 | 1 | 3 | 1040 | 2400 | 966 | 1327 | 772 | 1167 | 1998 | 1117 | 1032 | 969 |
| 116 | 50 | 0.15 | 7 | 2 | 2 | 4 | 1372 | 2065 | 1470 | 1838 | 1005 | 801 | 1928 | 1432 | 1861 | 1850 |


| 117 | 50 | 0.15 | 15 | 1 | 1 | 1 | 2649 | 1890 | 1660 | 866 | 822 | 828 | 864 | 1460 | 3377 | 1210 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118 | 50 | 0.15 | 15 | 1 | 2 | 2 | 1395 | 1470 | 1426 | 1278 | 1623 | 1622 | 1066 | 1956 | 1377 | 1302 |
| 119 | 50 | 0.15 | 15 | 2 | 1 | 3 | 1268 | 2269 | 2036 | 1047 | 2054 | 1522 | 1909 | 1579 | 1036 | 887 |
| 120 | 50 | 0.15 | 15 | 2 | 2 | 4 | 822 | 1275 | 939 | 1258 | 1086 | 1642 | 2292 | 1668 | 1267 | 1987 |
| 121 | 50 | 0.50 | 0 | 1 | 1 | 1 | 887 | 2190 | 786 | 964 | 999 | 1898 | 1002 | 2378 | 927 | 1041 |
| 122 | 50 | 0.50 | 0 | 1 | 2 | 2 | 1461 | 2271 | 1239 | 2064 | 1358 | 1523 | 1330 | 1095 | 2619 | 1123 |
| 123 | 50 | 0.50 | 0 | 2 | 1 | 3 | 1150 | 1078 | 1765 | 1324 | 2307 | 881 | 1366 | 1046 | 1740 | 1290 |
| 124 | 50 | 0.50 | 0 | 2 | 2 | 4 | 706 | 1720 | 1091 | 1135 | 806 | 1467 | 1134 | 1311 | 1182 | 1843 |
| 125 | 50 | 0.50 | 7 | 1 | 1 | 1 | 834 | 898 | 1795 | 1986 | 916 | 935 | 841 | 939 | 1521 | 1415 |
| 126 | 50 | 0.50 | 7 | 1 | 2 | 2 | 969 | 1251 | 1362 | 721 | 845 | 1596 | 1742 | 1419 | 3264 | 1049 |
| 127 | 50 | 0.50 | 7 | 2 | 1 | 3 | 1081 | 763 | 1519 | 1554 | 2162 | 1090 | 962 | 1387 | 1009 | 956 |
| 128 | 50 | 0.50 | 7 | 2 | 2 | 4 | 1368 | 1004 | 1535 | 2592 | 1137 | 2038 | 1410 | 1410 | 869 | 1311 |
| 129 | 50 | 0.50 | 15 | 1 | 1 | 1 | 1171 | 1023 | 2143 | 1464 | 1357 | 805 | 752 | 1095 | 1539 | 1449 |
| 130 | 50 | 0.50 | 15 | 1 | 2 | 2 | 1863 | 1489 | 2239 | 1184 | 1091 | 1120 | 1196 | 1337 | 760 | 759 |
| 131 | 50 | 0.50 | 15 | 2 | 1 | 3 | 1010 | 1062 | 1831 | 922 | 1926 | 2059 | 1386 | 2272 | 788 | 1063 |
| 132 | 50 | 0.50 | 15 | 2 | 2 | 4 | 2994 | 1145 | 1427 | 1374 | 1539 | 1140 | 1515 | 1175 | 794 | 862 |
| 133 | 50 | 0.85 | 0 | 1 | 1 | 1 | 1084 | 1063 | 980 | 920 | 1536 | 1748 | 1222 | 1000 | 902 | 1442 |
| 134 | 50 | 0.85 | 0 | 1 | 2 | 2 | 3190 | 1208 | 1198 | 747 | 1760 | 897 | 1227 | 1266 | 961 | 1769 |
| 135 | 50 | 0.85 | 0 | 2 | 1 | 3 | 1351 | 983 | 930 | 1206 | 938 | 929 | 2416 | 1245 | 2511 | 722 |
| 136 | 50 | 0.85 | 0 | 2 | 2 | 4 | 1114 | 852 | 2115 | 889 | 1872 | 1216 | 1192 | 2712 | 1585 | 1408 |
| 137 | 50 | 0.85 | 7 | 1 | 1 | 1 | 1012 | 1101 | 1337 | 1822 | 932 | 927 | 1166 | 1044 | 795 | 1149 |
| 138 | 50 | 0.85 | 7 | 1 | 2 | 2 | 2027 | 1071 | 1071 | 3003 | 1665 | 874 | 1737 | 2826 | 1244 | 1052 |
| 139 | 50 | 0.85 | 7 | 2 | 1 | 3 | 1133 | 1359 | 860 | 844 | 1827 | 2010 | 1327 | 957 | 1075 | 1351 |
| 140 | 50 | 0.85 | 7 | 2 | 2 | 4 | 2395 | 1828 | 2132 | 865 | 1150 | 902 | 1020 | 1005 | 1473 | 1344 |
| 141 | 50 | 0.85 | 15 | 1 | 1 | 1 | 847 | 682 | 1749 | 1431 | 1355 | 1133 | 1271 | 1654 | 874 | 737 |
| 142 | 50 | 0.85 | 15 | 1 | 2 | 2 | 985 | 1334 | 1125 | 1233 | 1074 | 1926 | 967 | 959 | 944 | 1340 |
| 143 | 50 | 0.85 | 15 | 2 | 1 | 3 | 1434 | 1287 | 1179 | 1738 | 1485 | 1495 | 1569 | 931 | 976 | 819 |
| 144 | 50 | 0.85 | 15 | 2 | 2 | 4 | 1563 | 2254 | 1075 | 1207 | 866 | 792 | 1330 | 1790 | 1178 | 875 |

## APPENDIX L: SOLUTION TIMES (MINUTES) FROM THE LLDP

 TESTINGSolution Time (minutes) for Replication

| Test | $\Omega$ | $\rho_{\text {LCMHS }}$ | $\mathrm{t}$ | $\theta$ | S | $\theta \mathrm{S}$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 1 | 0.10 | 0.15 | 0 | 1 | 1 | 1 | 45.03 | 59.45 | 60.22 | 40.33 | 44.33 | 61.93 | 45.60 | 55.87 | 41.02 | 44.43 |
| 2 | 0.10 | 0.15 | 0 | 1 | 2 | 2 | 37.37 | 32.42 | 34.95 | 35.75 | 40.47 | 33.80 | 48.87 | 50.77 | 30.40 | 29.23 |
| 3 | 0.10 | 0.15 | 0 | 2 | 1 | 3 | 51.12 | 36.90 | 32.83 | 45.43 | 93.70 | 35.92 | 83.27 | 51.33 | 30.35 | 42.12 |
| 4 | 0.10 | 0.15 | 0 | 2 | 2 | 4 | 59.28 | 23.75 | 48.12 | 31.28 | 30.45 | 31.62 | 44.93 | 34.57 | 26.52 | 38.85 |
| 5 | 0.10 | 0.15 | 7 | 1 | 1 | 1 | 33.00 | 72.40 | 47.67 | 46.98 | 46.87 | 42.23 | 43.03 | 44.68 | 35.10 | 69.63 |
| 6 | 0.10 | 0.15 | 7 | 1 | 2 | 2 | 31.30 | 43.92 | 41.60 | 18.67 | 30.92 | 26.77 | 37.47 | 85.23 | 36.48 | 28.00 |
| 7 | 0.10 | 0.15 | 7 | 2 | 1 | 3 | 55.90 | 41.25 | 46.62 | 34.73 | 38.08 | 43.83 | 44.95 | 92.55 | 50.63 | 45.12 |
| 8 | 0.10 | 0.15 | 7 | 2 | 2 | 4 | 86.25 | 61.37 | 59.62 | 56.40 | 33.43 | 38.30 | 29.53 | 22.48 | 54.52 | 35.03 |
| 9 | 0.10 | 0.15 | 15 | 1 | 1 | 1 | 33.30 | 44.02 | 39.15 | 50.65 | 35.38 | 44.70 | 44.97 | 36.25 | 44.43 | 39.48 |
| 10 | 0.10 | 0.15 | 15 | 1 | 2 | 2 | 37.50 | 51.33 | 20.55 | 22.88 | 19.13 | 21.10 | 20.03 | 25.80 | 37.80 | 65.98 |
| 11 | 0.10 | 0.15 | 15 | 2 | 1 | 3 | 52.48 | 42.85 | 37.10 | 40.33 | 32.45 | 80.98 | 30.08 | 57.13 | 37.42 | 35.10 |
| 12 | 0.10 | 0.15 | 15 | 2 | 2 | 4 | 21.08 | 24.15 | 35.55 | 36.57 | 18.77 | 21.70 | 80.10 | 100.78 | 36.85 | 23.25 |
| 13 | 0.10 | 0.50 | 0 | 1 | 1 | 1 | 134.33 | 172.23 | 57.82 | 63.92 | 66.17 | 79.27 | 55.23 | 84.65 | 93.98 | 69.45 |
| 14 | 0.10 | 0.50 | 0 | 1 | 2 | 2 | 53.72 | 64.83 | 44.20 | 35.48 | 38.97 | 29.82 | 35.78 | 112.45 | 84.48 | 54.43 |
| 15 | 0.10 | 0.50 | 0 | 2 | 1 | 3 | 100.32 | 82.20 | 72.48 | 66.03 | 102.20 | 100.28 | 73.32 | 82.30 | 63.87 | 64.05 |
| 16 | 0.10 | 0.50 | 0 | 2 | 2 | 4 | 135.92 | 49.70 | 69.13 | 65.20 | 36.53 | 39.98 | 24.87 | 53.58 | 41.13 | 32.03 |
| 17 | 0.10 | 0.50 | 7 | 1 | 1 | 1 | 60.08 | 76.45 | 75.00 | 125.48 | 139.25 | 164.05 | 66.80 | 48.35 | 64.50 | 49.68 |
| 18 | 0.10 | 0.50 | 7 | 1 | 2 | 2 | 33.37 | 101.48 | 51.38 | 44.82 | 44.92 | 81.60 | 66.07 | 44.20 | 25.33 | 81.13 |
| 19 | 0.10 | 0.50 | 7 | 2 | 1 | 3 | 65.12 | 85.20 | 103.22 | 174.80 | 68.50 | 47.33 | 56.38 | 52.63 | 110.55 | 95.38 |
| 20 | 0.10 | 0.50 | 7 | 2 | 2 | 4 | 30.83 | 40.13 | 31.98 | 48.42 | 42.37 | 85.75 | 39.82 | 19.55 | 44.90 | 24.32 |
| 21 | 0.10 | 0.50 | 15 | 1 | 1 | 1 | 91.83 | 70.20 | 91.73 | 61.35 | 60.37 | 89.02 | 75.67 | 44.95 | 58.17 | 49.82 |
| 22 | 0.10 | 0.50 | 15 | 1 | 2 | 2 | 44.13 | 55.97 | 55.97 | 50.55 | 27.98 | 56.83 | 31.67 | 54.48 | 51.35 | 77.85 |
| 23 | 0.10 | 0.50 | 15 | 2 | 1 | 3 | 127.07 | 77.05 | 48.50 | 60.20 | 88.57 | 59.90 | 55.97 | 133.92 | 117.88 | 140.25 |
| 24 | 0.10 | 0.50 | 15 | 2 | 2 | 4 | 76.77 | 43.17 | 35.28 | 75.78 | 47.82 | 63.28 | 32.97 | 30.63 | 27.52 | 39.40 |
| 25 | 0.10 | 0.85 | 0 | 1 | 1 | 1 | 35.93 | 74.57 | 91.73 | 61.57 | 49.73 | 86.05 | 71.77 | 52.37 | 61.28 | 39.53 |
| 26 | 0.10 | 0.85 | 0 | 1 | 2 | 2 | 33.50 | 25.95 | 20.15 | 40.82 | 53.32 | 55.05 | 29.13 | 23.47 | 62.60 | 66.42 |


| 27 | 0.10 | 0.85 | 0 | 2 | 1 | 3 | 58.97 | 49.43 | 70.38 | 50.92 | 42.82 | 41.83 | 35.55 | 52.08 | 73.95 | 71.57 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 28 | 0.10 | 0.85 | 0 | 2 | 2 | 4 | 42.73 | 46.42 | 23.97 | 26.97 | 74.60 | 42.48 | 51.58 | 96.23 | 55.98 | 33.60 |
| 29 | 0.10 | 0.85 | 7 | 1 | 1 | 1 | 44.47 | 87.28 | 74.82 | 58.63 | 46.67 | 53.20 | 67.50 | 86.40 | 51.47 | 44.22 |
| 30 | 0.10 | 0.85 | 7 | 1 | 2 | 2 | 54.20 | 108.37 | 34.27 | 42.67 | 51.38 | 27.93 | 24.48 | 89.85 | 34.03 | 64.23 |
| 31 | 0.10 | 0.85 | 7 | 2 | 1 | 3 | 68.40 | 45.37 | 74.77 | 68.35 | 137.25 | 51.52 | 97.65 | 72.18 | 85.50 | 80.88 |
| 32 | 0.10 | 0.85 | 7 | 2 | 2 | 4 | 27.95 | 19.80 | 105.82 | 24.83 | 32.08 | 40.98 | 24.38 | 23.18 | 24.27 | 22.28 |
| 33 | 0.10 | 0.85 | 15 | 1 | 1 | 1 | 57.97 | 90.17 | 53.63 | 64.35 | 39.13 | 42.97 | 46.30 | 49.70 | 50.70 | 55.62 |
| 34 | 0.10 | 0.85 | 15 | 1 | 2 | 2 | 83.30 | 108.32 | 40.53 | 23.05 | 39.02 | 47.12 | 68.10 | 33.00 | 53.33 | 33.02 |
| 35 | 0.10 | 0.85 | 15 | 2 | 1 | 3 | 41.35 | 53.33 | 35.27 | 47.47 | 41.40 | 44.07 | 78.08 | 61.10 | 61.13 | 47.37 |
| 36 | 0.10 | 0.85 | 15 | 2 | 2 | 4 | 40.47 | 98.42 | 31.73 | 25.33 | 25.43 | 45.20 | 34.57 | 49.45 | 34.65 | 48.98 |
| 37 | 1 | 0.15 | 0 | 1 | 1 | 1 | 52.07 | 75.78 | 64.73 | 80.53 | 37.60 | 291.42 | 102.60 | 89.78 | 80.13 | 41.85 |
| 38 | 1 | 0.15 | 0 | 1 | 2 | 2 | 31.93 | 51.45 | 29.63 | 24.97 | 32.22 | 24.42 | 28.85 | 73.90 | 30.78 | 23.13 |
| 39 | 1 | 0.15 | 0 | 2 | 1 | 3 | 58.18 | 97.57 | 65.13 | 48.25 | 43.78 | 71.88 | 64.95 | 49.68 | 77.77 | 75.75 |
| 40 | 1 | 0.15 | 0 | 2 | 2 | 4 | 27.42 | 87.77 | 33.33 | 83.32 | 48.00 | 49.03 | 46.33 | 32.02 | 22.82 | 20.90 |
| 41 | 1 | 0.15 | 7 | 1 | 1 | 1 | 96.42 | 97.87 | 78.45 | 54.50 | 308.52 | 37.73 | 67.83 | 39.83 | 60.33 | 29.02 |
| 42 | 1 | 0.15 | 7 | 1 | 2 | 2 | 19.32 | 23.00 | 64.30 | 22.05 | 36.68 | 34.10 | 34.03 | 26.65 | 54.12 | 66.10 |
| 43 | 1 | 0.15 | 7 | 2 | 1 | 3 | 50.43 | 43.35 | 134.83 | 76.23 | 65.03 | 73.98 | 37.87 | 54.50 | 108.13 | 51.07 |
| 44 | 1 | 0.15 | 7 | 2 | 2 | 4 | 27.05 | 25.18 | 28.22 | 32.50 | 26.42 | 43.58 | 50.28 | 71.05 | 49.60 | 25.98 |
| 45 | 1 | 0.15 | 15 | 1 | 1 | 1 | 41.22 | 56.03 | 86.58 | 54.55 | 52.17 | 334.80 | 67.72 | 50.17 | 49.73 | 61.62 |
| 46 | 1 | 0.15 | 15 | 1 | 2 | 2 | 28.87 | 44.25 | 27.42 | 39.00 | 20.83 | 39.60 | 61.40 | 91.40 | 29.83 | 30.12 |
| 47 | 1 | 0.15 | 15 | 2 | 1 | 3 | 61.18 | 36.90 | 86.27 | 36.25 | 64.18 | 52.15 | 58.77 | 86.12 | 55.88 | 44.08 |
| 48 | 1 | 0.15 | 15 | 2 | 2 | 4 | 51.05 | 52.12 | 60.70 | 48.42 | 37.45 | 23.10 | 84.37 | 53.80 | 53.78 | 15.83 |
| 49 | 1 | 0.50 | 0 | 1 | 1 | 1 | 41.80 | 44.75 | 57.00 | 62.43 | 80.65 | 50.15 | 40.48 | 40.52 | 37.18 | 52.80 |
| 50 | 1 | 0.50 | 0 | 1 | 2 | 2 | 53.37 | 96.20 | 56.87 | 23.75 | 46.33 | 23.37 | 65.88 | 39.97 | 41.22 | 82.95 |
| 51 | 1 | 0.50 | 0 | 2 | 1 | 3 | 89.63 | 87.97 | 73.35 | 91.05 | 100.98 | 40.27 | 51.98 | 43.02 | 69.27 | 115.03 |
| 52 | 1 | 0.50 | 0 | 2 | 2 | 4 | 45.48 | 69.85 | 35.80 | 50.68 | 51.82 | 39.73 | 30.90 | 32.42 | 27.25 | 40.92 |
| 53 | 1 | 0.50 | 7 | 1 | 1 | 1 | 53.00 | 89.68 | 95.63 | 91.58 | 181.32 | 54.00 | 51.37 | 46.98 | 63.88 | 46.60 |
| 54 | 1 | 0.50 | 7 | 1 | 2 | 2 | 62.12 | 52.38 | 100.22 | 33.35 | 91.80 | 46.13 | 29.02 | 22.77 | 108.53 | 52.95 |
| 55 | 1 | 0.50 | 7 | 2 | 1 | 3 | 48.08 | 111.43 | 46.73 | 73.60 | 44.57 | 54.12 | 71.10 | 54.53 | 48.58 | 38.22 |
| 56 | 1 | 0.50 | 7 | 2 | 2 | 4 | 49.73 | 177.50 | 66.93 | 29.53 | 47.17 | 36.72 | 31.03 | 27.57 | 23.10 | 42.70 |


| 57 | 1 | 0.50 | 15 | 1 | 1 | 1 | 57.62 | 75.98 | 65.02 | 46.07 | 58.80 | 56.32 | 48.50 | 49.95 | 31.82 | 94.33 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 58 | 1 | 0.50 | 15 | 1 | 2 | 2 | 33.72 | 25.80 | 18.30 | 28.10 | 25.65 | 28.60 | 60.05 | 30.18 | 78.08 | 28.13 |
| 59 | 1 | 0.50 | 15 | 2 | 1 | 3 | 54.05 | 38.35 | 48.72 | 74.77 | 71.62 | 52.70 | 76.00 | 75.28 | 73.58 | 61.58 |
| 60 | 1 | 0.50 | 15 | 2 | 2 | 4 | 21.45 | 33.75 | 38.48 | 38.37 | 25.80 | 22.62 | 74.32 | 53.63 | 41.25 | 21.28 |
| 61 | 1 | 0.85 | 0 | 1 | 1 | 1 | 58.75 | 134.78 | 46.30 | 93.70 | 85.32 | 41.40 | 64.03 | 50.75 | 47.85 | 123.05 |
| 62 | 1 | 0.85 | 0 | 1 | 2 | 2 | 30.40 | 45.43 | 75.33 | 30.38 | 35.40 | 39.92 | 42.92 | 20.63 | 45.42 | 43.35 |
| 63 | 1 | 0.85 | 0 | 2 | 1 | 3 | 38.35 | 47.63 | 64.25 | 96.80 | 101.90 | 40.53 | 81.80 | 39.45 | 70.02 | 43.38 |
| 64 | 1 | 0.85 | 0 | 2 | 2 | 4 | 22.77 | 42.83 | 27.67 | 54.68 | 27.83 | 31.98 | 42.85 | 26.37 | 14.83 | 37.20 |
| 65 | 1 | 0.85 | 7 | 1 | 1 | 1 | 69.53 | 47.45 | 83.03 | 62.12 | 60.33 | 80.18 | 49.35 | 45.05 | 48.43 | 107.17 |
| 66 | 1 | 0.85 | 7 | 1 | 2 | 2 | 29.17 | 44.68 | 54.43 | 43.12 | 51.32 | 58.12 | 29.57 | 35.98 | 28.10 | 32.03 |
| 67 | 1 | 0.85 | 7 | 2 | 1 | 3 | 44.73 | 63.32 | 54.78 | 34.03 | 45.80 | 49.05 | 66.75 | 48.50 | 79.45 | 43.88 |
| 68 | 1 | 0.85 | 7 | 2 | 2 | 4 | 49.47 | 46.92 | 28.63 | 42.40 | 35.32 | 32.60 | 87.05 | 35.68 | 45.08 | 37.15 |
| 69 | 1 | 0.85 | 15 | 1 | 1 | 1 | 42.02 | 130.77 | 60.90 | 48.57 | 45.98 | 38.38 | 41.73 | 48.83 | 56.03 | 39.27 |
| 70 | 1 | 0.85 | 15 | 1 | 2 | 2 | 18.08 | 159.35 | 58.07 | 32.53 | 30.90 | 39.77 | 39.85 | 48.73 | 98.57 | 32.82 |
| 71 | 1 | 0.85 | 15 | 2 | 1 | 3 | 70.37 | 46.43 | 87.70 | 74.07 | 50.48 | 50.27 | 75.25 | 51.00 | 45.33 | 40.77 |
| 72 | 1 | 0.85 | 15 | 2 | 2 | 4 | 66.40 | 46.92 | 22.83 | 57.20 | 38.05 | 44.25 | 55.33 | 28.92 | 34.97 | 54.87 |
| 73 | 10 | 0.15 | 0 | 1 | 1 | 1 | 51.80 | 48.82 | 80.80 | 147.10 | 48.73 | 54.87 | 61.42 | 93.35 | 71.95 | 40.20 |
| 74 | 10 | 0.15 | 0 | 1 | 2 | 2 | 17.65 | 38.87 | 26.80 | 28.40 | 23.28 | 56.82 | 48.82 | 65.77 | 29.48 | 52.72 |
| 75 | 10 | 0.15 | 0 | 2 | 1 | 3 | 83.10 | 46.88 | 40.53 | 75.47 | 72.77 | 129.77 | 82.55 | 80.15 | 99.95 | 72.48 |
| 76 | 10 | 0.15 | 0 | 2 | 2 | 4 | 40.88 | 24.65 | 26.50 | 41.77 | 59.12 | 34.02 | 33.97 | 59.10 | 47.70 | 27.62 |
| 77 | 10 | 0.15 | 7 | 1 | 1 | 1 | 51.43 | 191.83 | 65.32 | 60.25 | 100.97 | 90.18 | 142.75 | 110.28 | 52.90 | 49.18 |
| 78 | 10 | 0.15 | 7 | 1 | 2 | 2 | 27.35 | 57.68 | 38.63 | 34.03 | 63.72 | 48.72 | 19.77 | 21.38 | 22.83 | 35.32 |
| 79 | 10 | 0.15 | 7 | 2 | 1 | 3 | 69.98 | 92.67 | 58.27 | 93.23 | 60.85 | 106.57 | 47.98 | 44.88 | 47.72 | 85.82 |
| 80 | 10 | 0.15 | 7 | 2 | 2 | 4 | 28.72 | 48.72 | 30.70 | 53.60 | 40.55 | 43.08 | 30.75 | 17.08 | 41.82 | 23.40 |
| 81 | 10 | 0.15 | 15 | 1 | 1 | 1 | 111.42 | 55.68 | 53.60 | 89.10 | 142.45 | 116.98 | 65.55 | 108.25 | 84.23 | 117.98 |
| 82 | 10 | 0.15 | 15 | 1 | 2 | 2 | 37.25 | 33.20 | 34.72 | 30.60 | 42.75 | 32.90 | 33.10 | 21.67 | 23.97 | 73.48 |
| 83 | 10 | 0.15 | 15 | 2 | 1 | 3 | 134.57 | 44.63 | 114.65 | 77.07 | 104.52 | 61.68 | 56.37 | 61.55 | 91.00 | 88.18 |
| 84 | 10 | 0.15 | 15 | 2 | 2 | 4 | 30.28 | 21.55 | 20.48 | 31.60 | 58.78 | 22.73 | 18.23 | 19.03 | 21.38 | 17.90 |
| 85 | 10 | 0.50 | 0 | 1 | 1 | 1 | 96.72 | 45.63 | 68.87 | 78.47 | 47.67 | 52.50 | 38.68 | 57.35 | 65.13 | 109.78 |
| 86 | 10 | 0.50 | 0 | 1 | 2 | 2 | 30.32 | 50.02 | 23.97 | 66.08 | 96.52 | 30.65 | 33.38 | 25.43 | 65.87 | 24.75 |


| 87 | 10 | 0.50 | 0 | 2 | 1 | 3 | 67.88 | 47.90 | 68.35 | 41.43 | 81.35 | 75.07 | 143.70 | 45.42 | 54.68 | 59.38 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88 | 10 | 0.50 | 0 | 2 | 2 | 4 | 20.78 | 32.57 | 25.88 | 33.83 | 33.60 | 40.33 | 37.60 | 31.55 | 31.45 | 74.93 |
| 89 | 10 | 0.50 | 7 | 1 | 1 | 1 | 63.67 | 43.93 | 53.98 | 78.05 | 73.07 | 128.40 | 91.15 | 92.02 | 83.67 | 66.75 |
| 90 | 10 | 0.50 | 7 | 1 | 2 | 2 | 30.52 | 36.95 | 55.40 | 39.65 | 36.12 | 56.80 | 31.63 | 77.92 | 76.53 | 44.38 |
| 91 | 10 | 0.50 | 7 | 2 | 1 | 3 | 201.05 | 63.58 | 101.32 | 55.43 | 72.90 | 60.38 | 90.47 | 81.97 | 59.70 | 80.68 |
| 92 | 10 | 0.50 | 7 | 2 | 2 | 4 | 31.23 | 33.25 | 17.80 | 41.10 | 42.35 | 28.53 | 17.48 | 22.35 | 15.50 | 18.53 |
| 93 | 10 | 0.50 | 15 | 1 | 1 | 1 | 46.48 | 45.62 | 60.17 | 61.45 | 103.25 | 51.68 | 45.17 | 36.30 | 87.40 | 72.90 |
| 94 | 10 | 0.50 | 15 | 1 | 2 | 2 | 26.00 | 44.32 | 41.62 | 36.22 | 33.88 | 33.02 | 20.77 | 30.60 | 36.02 | 62.92 |
| 95 | 10 | 0.50 | 15 | 2 | 1 | 3 | 56.22 | 111.20 | 51.90 | 50.13 | 82.68 | 79.87 | 94.30 | 40.17 | 37.80 | 75.52 |
| 96 | 10 | 0.50 | 15 | 2 | 2 | 4 | 26.62 | 44.95 | 28.62 | 27.97 | 46.32 | 35.92 | 29.70 | 28.85 | 32.62 | 22.98 |
| 97 | 10 | 0.85 | 0 | 1 | 1 | 1 | 149.18 | 59.68 | 34.50 | 34.45 | 35.95 | 44.98 | 63.48 | 53.37 | 44.68 | 35.95 |
| 98 | 10 | 0.85 | 0 | 1 | 2 | 2 | 27.50 | 31.85 | 18.03 | 33.80 | 40.80 | 69.70 | 48.53 | 22.83 | 47.20 | 36.48 |
| 99 | 10 | 0.85 | 0 | 2 | 1 | 3 | 69.52 | 77.72 | 62.82 | 32.35 | 128.37 | 127.53 | 45.20 | 36.93 | 42.95 | 47.22 |
| 100 | 10 | 0.85 | 0 | 2 | 2 | 4 | 27.80 | 28.40 | 22.98 | 13.17 | 25.63 | 40.28 | 25.57 | 27.62 | 39.47 | 22.78 |
| 101 | 10 | 0.85 | 7 | 1 | 1 | 1 | 64.10 | 63.52 | 37.48 | 45.90 | 55.27 | 33.32 | 102.48 | 38.10 | 87.98 | 67.52 |
| 102 | 10 | 0.85 | 7 | 1 | 2 | 2 | 24.33 | 26.12 | 24.93 | 27.88 | 30.60 | 19.30 | 45.80 | 31.12 | 38.67 | 47.55 |
| 103 | 10 | 0.85 | 7 | 2 | 1 | 3 | 42.35 | 72.02 | 40.43 | 63.75 | 69.87 | 34.57 | 66.47 | 47.47 | 48.85 | 68.37 |
| 104 | 10 | 0.85 | 7 | 2 | 2 | 4 | 44.60 | 30.07 | 27.10 | 33.92 | 24.93 | 34.00 | 30.92 | 54.03 | 27.58 | 33.70 |
| 105 | 10 | 0.85 | 15 | 1 | 1 | 1 | 40.67 | 49.83 | 68.88 | 62.50 | 47.23 | 105.80 | 66.93 | 81.27 | 59.40 | 62.63 |
| 106 | 10 | 0.85 | 15 | 1 | 2 | 2 | 58.30 | 68.62 | 37.83 | 76.38 | 60.73 | 42.78 | 25.42 | 34.10 | 37.55 | 87.45 |
| 107 | 10 | 0.85 | 15 | 2 | 1 | 3 | 64.80 | 56.23 | 58.70 | 65.80 | 100.92 | 67.83 | 151.33 | 105.00 | 61.75 | 48.05 |
| 108 | 10 | 0.85 | 15 | 2 | 2 | 4 | 24.77 | 40.20 | 52.70 | 35.42 | 26.30 | 87.13 | 72.20 | 34.98 | 43.50 | 60.62 |
| 109 | 50 | 0.15 | 0 | 1 | 1 | 1 | 89.80 | 79.65 | 102.03 | 68.38 | 126.15 | 86.77 | 123.97 | 75.05 | 274.00 | 91.72 |
| 110 | 50 | 0.15 | 0 | 1 | 2 | 2 | 30.35 | 27.68 | 23.15 | 29.85 | 18.83 | 20.95 | 47.40 | 64.02 | 51.87 | 39.73 |
| 111 | 50 | 0.15 | 0 | 2 | 1 | 3 | 101.40 | 96.15 | 60.35 | 65.87 | 108.77 | 115.22 | 89.00 | 92.35 | 138.92 | 105.80 |
| 112 | 50 | 0.15 | 0 | 2 | 2 | 4 | 30.35 | 24.77 | 12.08 | 14.83 | 32.92 | 36.60 | 38.97 | 17.63 | 14.97 | 19.30 |
| 113 | 50 | 0.15 | 7 | 1 | 1 | 1 | 61.67 | 74.72 | 88.57 | 47.98 | 71.57 | 83.43 | 76.18 | 58.93 | 80.83 | 104.80 |
| 114 | 50 | 0.15 | 7 | 1 | 2 | 2 | 31.37 | 38.78 | 29.52 | 33.03 | 39.60 | 23.72 | 34.27 | 39.58 | 60.03 | 24.72 |
| 115 | 50 | 0.15 | 7 | 2 | 1 | 3 | 67.68 | 172.18 | 68.13 | 86.82 | 46.37 | 70.38 | 130.48 | 77.00 | 64.55 | 59.48 |
| 116 | 50 | 0.15 | 7 | 2 | 2 | 4 | 38.15 | 66.73 | 48.00 | 56.38 | 30.62 | 20.45 | 58.60 | 47.08 | 59.25 | 63.55 |


| 117 | 50 | 0.15 | 15 | 1 | 1 | 1 | 177.63 | 114.75 | 117.57 | 56.63 | 50.25 | 49.25 | 52.73 | 95.17 | 270.97 | 88.38 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 118 | 50 | 0.15 | 15 | 1 | 2 | 2 | 39.32 | 41.53 | 41.55 | 37.77 | 48.00 | 53.28 | 31.92 | 60.52 | 46.85 | 38.13 |
| 119 | 50 | 0.15 | 15 | 2 | 1 | 3 | 79.87 | 156.48 | 146.83 | 70.23 | 131.93 | 115.57 | 136.43 | 106.40 | 68.40 | 44.28 |
| 120 | 50 | 0.15 | 15 | 2 | 2 | 4 | 16.23 | 26.32 | 20.28 | 27.48 | 24.67 | 38.82 | 64.78 | 47.38 | 30.78 | 43.03 |
| 121 | 50 | 0.50 | 0 | 1 | 1 | 1 | 53.05 | 158.32 | 52.03 | 59.03 | 57.53 | 129.38 | 67.28 | 160.67 | 61.77 | 64.10 |
| 122 | 50 | 0.50 | 0 | 1 | 2 | 2 | 43.08 | 77.10 | 42.08 | 64.00 | 43.18 | 45.05 | 40.47 | 32.03 | 92.45 | 40.10 |
| 123 | 50 | 0.50 | 0 | 2 | 1 | 3 | 73.68 | 70.60 | 119.90 | 87.75 | 164.23 | 63.92 | 89.90 | 65.55 | 117.65 | 65.27 |
| 124 | 50 | 0.50 | 0 | 2 | 2 | 4 | 13.45 | 39.70 | 25.55 | 23.85 | 15.73 | 31.97 | 26.32 | 28.90 | 25.97 | 43.73 |
| 125 | 50 | 0.50 | 7 | 1 | 1 | 1 | 48.55 | 55.58 | 102.57 | 121.67 | 62.10 | 54.73 | 49.77 | 59.73 | 97.07 | 92.15 |
| 126 | 50 | 0.50 | 7 | 1 | 2 | 2 | 28.53 | 37.02 | 40.97 | 19.92 | 20.78 | 48.03 | 56.63 | 46.72 | 122.28 | 40.40 |
| 127 | 50 | 0.50 | 7 | 2 | 1 | 3 | 70.03 | 45.77 | 94.82 | 104.10 | 154.17 | 77.67 | 61.42 | 95.90 | 65.12 | 60.77 |
| 128 | 50 | 0.50 | 7 | 2 | 2 | 4 | 39.87 | 28.65 | 46.00 | 98.90 | 40.13 | 69.13 | 49.22 | 45.22 | 23.88 | 36.37 |
| 129 | 50 | 0.50 | 15 | 1 | 1 | 1 | 72.57 | 64.47 | 150.23 | 103.08 | 90.00 | 48.77 | 44.72 | 71.67 | 102.28 | 90.95 |
| 130 | 50 | 0.50 | 15 | 1 | 2 | 2 | 58.75 | 47.75 | 76.60 | 40.55 | 31.42 | 30.02 | 32.17 | 41.10 | 23.00 | 17.63 |
| 131 | 50 | 0.50 | 15 | 2 | 1 | 3 | 61.93 | 69.77 | 125.00 | 60.20 | 133.65 | 148.75 | 98.65 | 163.20 | 51.77 | 62.32 |
| 132 | 50 | 0.50 | 15 | 2 | 2 | 4 | 95.00 | 36.77 | 33.68 | 35.15 | 38.70 | 27.98 | 31.77 | 22.52 | 12.72 | 14.15 |
| 133 | 50 | 0.85 | 0 | 1 | 1 | 1 | 64.57 | 71.17 | 64.93 | 56.88 | 94.40 | 114.20 | 77.30 | 63.30 | 55.67 | 86.18 |
| 134 | 50 | 0.85 | 0 | 1 | 2 | 2 | 121.58 | 44.42 | 34.83 | 21.72 | 45.80 | 24.58 | 30.65 | 35.27 | 26.13 | 51.15 |
| 135 | 50 | 0.85 | 0 | 2 | 1 | 3 | 89.72 | 63.37 | 54.97 | 73.60 | 55.35 | 53.57 | 161.77 | 90.42 | 185.58 | 50.47 |
| 136 | 50 | 0.85 | 0 | 2 | 2 | 4 | 27.52 | 21.68 | 64.30 | 27.10 | 54.43 | 31.97 | 26.77 | 73.73 | 49.47 | 32.78 |
| 137 | 50 | 0.85 | 7 | 1 | 1 | 1 | 57.58 | 72.60 | 88.17 | 116.03 | 58.23 | 56.87 | 66.52 | 65.28 | 47.75 | 68.57 |
| 138 | 50 | 0.85 | 7 | 1 | 2 | 2 | 63.73 | 35.07 | 30.17 | 111.32 | 67.12 | 25.43 | 51.05 | 103.15 | 43.20 | 28.27 |
| 139 | 50 | 0.85 | 7 | 2 | 1 | 3 | 71.13 | 88.13 | 54.33 | 48.28 | 112.27 | 133.78 | 87.92 | 60.93 | 66.72 | 84.13 |
| 140 | 50 | 0.85 | 7 | 2 | 2 | 4 | 84.27 | 71.77 | 69.77 | 20.98 | 24.25 | 19.08 | 20.92 | 22.55 | 33.48 | 32.35 |
| 141 | 50 | 0.85 | 15 | 1 | 1 | 1 | 48.77 | 39.55 | 116.30 | 95.58 | 84.50 | 71.07 | 73.53 | 108.23 | 52.88 | 41.10 |
| 142 | 50 | 0.85 | 15 | 1 | 2 | 2 | 24.55 | 34.23 | 31.13 | 33.20 | 29.72 | 66.25 | 31.33 | 24.08 | 23.62 | 36.32 |
| 143 | 50 | 0.85 | 15 | 2 | 1 | 3 | 90.52 | 82.73 | 73.03 | 111.57 | 97.40 | 93.37 | 98.98 | 57.95 | 57.82 | 48.32 |
| 144 | 50 | 0.85 | 15 | 2 | 2 | 4 | 42.85 | 72.58 | 35.12 | 33.28 | 22.75 | 19.60 | 34.98 | 55.90 | 36.47 | 23.37 |

> APPENDIX M: GLM PROCEDURE SAS OUTPUT FOR THE LLDP


```
        The GLM Procedure
            Tukey's Studentized Range (HSD) Test for WIP
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
    II error rate than REGWQ.
        Alpha 0.05
        Error Degrees of Freedom 1429
        Error Mean Square 3052.952
        Critical Value of Studentized Range 3.63754
        Minimum Significant Difference 10.593
    Means with the same letter are not significantly different.
        Tukey Grouping Mean N Omega
            A 267.046 360 50
            B 228.877 360 10
            C 204.933 360 1
            C 
                The SAS System
4
                    The GLM Procedure
            Tukey's Studentized Range (HSD) Test for WIP
NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher
Type
            II error rate than REGWQ.
        Alpha 0.05
        Error Degrees of Freedom 1429
        Error Mean Square 3052.952
        Critical Value of Studentized Range 3.31796
        Minimum Significant Difference 8.3678
    Means with the same letter are not significantly different.
    Tukey Grouping Mean N Rho
            A 372.840 480 0.85
            B 230.411 480 0.5
            C 74.656 480 0.15
            The SAS System
5






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[^0]:    ${ }^{2}$ This list has been excluded from the document as it does not add any value but takes up over a 100 pages. Upon request, the author will provide the solution list.

[^1]:    3 For each of the 36 test problems there are four scenarios, and for each scenario there are 10 replications.

