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Performance Evaluation of Weighted Greedy Algorithm in Resource Management

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Performance Evaluation of Weighted Greedy Algorithm in Resource Management

By

Harjeet Singh

A Thesis
Submitted to the Faculty of Graduate Studies
through the School of Computer Science
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at the University of Windsor

Windsor, Ontario, Canada

2018

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ABSTRACT

Set covering is a well-studied classical problem with many applications across different fields. More recent work on this problem has taken into account the parallel computing architecture, the datasets at scale, the properties of the datasets, etc. Within the context of web crawling where the data follow the lognormal distribution, a weighted greedy algorithm has been proposed in the literature and demonstrated to outperform the traditional one. In the present work, we evaluate the performance of the weighted greedy algorithm using an open-source dataset in the context of resource management. The data are sampled from a given roadmap with 1.9 millions of nodes. Our research includes three different cost definitions i.e. location cost, driving cost and infrastructure cost. We also consider the different coverage radius to model possible parameters in the application. Our experiment results show that weighted greedy algorithm outperforms the greedy algorithm by 8% in average for all three different cost definitions.

DEDICATION

Dedicated to my parents Jaswant Singh and Paramjeet Kaur
and also rest of my family and friends

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Harjeet Singh

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LIST OF ABBREVIATIONS/SYMBOLS

SNAP- Stanford Network Analysis Project

CV- Coefficient of Variation

P2P- Peer to Peer

RE- Random Edge

RNE- Random Node-Edge

SCP- Set Covering Problem

DF- Document Frequency

QW- Query Weight

MCLP- Maximal Set Covering Problem

NCD- Node Coverage Degree

NNF- New Nodes Fetched

NW- Node Weight

PC- Pearson Product Moment Correlation Coefficient

CHAPTER 1

INTRODUCTION

1.1 Overview

One of the most common problems today is the planning. Planning includes making plans about where to build new facilities in a city, how to allocate the resources and how to use the resources optimally. Solutions to these problems exist with many techniques, and one of them being the solution to the set covering problem. Finding the smallest set of solutions of a problem from many sets of solutions is widely researched in many fields. A set covering problem is presented as an abstract problem, so it captures many different scenarios in the context of knowledge mining, data management, etc. [1].

1.1.1 Set Covering Problem and Its Applications

Set covering is a classical problem in the field of computer science. It is one of the Karp's 21 NP-complete problems. This problem is a base for the entire field of approximation algorithms. Set covering is considered NP-Hard in optimization and search problems and NP-Complete in decision-based problems.

Set Covering is to select a minimum number of subsets in such a way that they contain all the elements from a fixed universe [2]. The most significant factor considered in this process is to minimize the cost of the selected subsets. There are various applications of set covering. Some of them are as follows [1].

Operational Research: - The operational research problem is to locate a facility in such a way that specific sites can reach it. This problem can be solved using set covering algorithms by considering each set of corresponding sites to a facility.

Machine Learning: - In machine learning, items are classified based on examples that cover them. The final goal is to make sure that all items are covered by some example, which is an instance of Set Covering problem.

Planning: - In planning, set covering can be applied to allocate resources when demands vary over time. To cover the requirements for planning, variations of set covering are used [3].

Data Mining: - Set covering can be applied to find the minimal explanations for the patterns in the data. In data mining, the goal is to find a set of features in such a way that every example is a positive example of these features. It can be viewed an instance of set cover problem where each set contains some examples which correspond to a feature.

Information Retrieval: - In Information Retrieval, the goal is to find the smallest set of documents that cover the topics in a query. It leads to an instance of set cover where a set of documents is required in response to a query[4].

1.2 Motivation

In this world, if we want to complete any task we need some resources. Everything and everyone need resources to complete its functioning whether a human being or a machine. Management of these resources is a problem which needs to be studied to get the best use of these resources that we have and to use them for a more extended period. When we think of resource management in the field of planning, there are various problems which need to be addressed.

In strategic planning for big firms whether private or public, facility location is a significantly critical component of their planning. Facility location as a part of

Operational Research is a well-established area in itself [32]. There are various models in this area to help with the decision-making process, and one of the most popular areas in those models is facility location model in covering problem. The concept of covering comes from its applications in daily life. Some of the problems are to determine the number and the location of public facilities like schools, libraries, hospitals, parks, fire stations and various other places.

Another major factor of studying in this area is the need to plan things properly. The rapid growth of population concerning some available resources has forced us to think of solutions to provide resources to people in such a way that demand can be managed in the best possible way. One daily life application of this is the placement of fire stations in a city in such a way that those fire stations can cover the entire area of the city and that the number of those stations is minimized to reduce the operational cost and initial investment in the infrastructure.

Another part that motivated this thesis work is set covering problem. It is a part of Karp's Np -complete problems, a base of approximation algorithms, that had led to the development of various fundamental techniques in this field. The usefulness of set cover problem has been seen at many places of the exciting application.

The weighted greedy algorithm by Wang et al. [16] is a good variation of greedy approach for web crawling but hasn't been tested on any other type of set covering problem. The use of this solution within the field of resource management might give some good results.

1.3 Problem Statement

As the world is dealing with the shortage of resource, there arises a need to either get more resources or to manage those resources appropriately. Study on set covering has provided many useful results for planning and resource management problems.

A weighted greedy algorithm for set covering problem has been proposed by Wang et.al.[16] within the context of web crawling and demonstrated to outperform the traditional greedy algorithm. In our present work, we evaluate the performance of the weighted greedy algorithm using open-source datasets in the context of resource management. It includes the setting of resource allocation on a sample taken from a roadmap with 1.9 million of nodes. The dataset is taken from open source data provided by Stanford Network Analysis Project (SNAP)[35].

1.4 Thesis Organization

The rest of this thesis is organized as follows: Chapter 2 provides a review of some of the concepts and terminologies that are related to this work and provides more details of the areas related to this research. It also includes a review of some of the closely related work of other researchers. In Chapter 3, we define the problem and present the proposed approach. Chapter 4 shows the results of experiments and Chapter 5 concludes the thesis with some suggested future work.

CHAPTER 2

REVIEW

2.1 Dataset

A dataset is a collection of data most commonly corresponding to a database table or matrix where rows and columns define some values. They are large in size and might not be well organized like a database. Most of the times a data set is a collection of data under some experiment. For example:- Temperature data gathered by a probe for every half an hour for one month.

	A	B
1	V1	V2
2	6	1
3	6	5
4	1	0
5	1	6
6	1	385
7	5	4
8	5	6
9	5	98
10	0	1
11	0	2
12	0	469

Fig 2.1: A dataset representing connected nodes of a roadmap

In the above, the dataset for connection among nodes is represented. There are various ways to represent a dataset. It can be a numeric matrix, adjacency matrix or a table with different kind of data types.

2.2 Matrix

A two-dimensional array of numbers arranged in rows and columns is called a matrix. The size of a matrix is determined by its number of rows and columns. Usually, rows are listed first and the columns second. Let's say if a matrix is said to be 3 * 4 then it has three rows and four columns.

$$\begin{bmatrix} 21 & 62 & 33 & 93 \\ 44 & 95 & 66 & 13 \\ 77 & 38 & 79 & 33 \end{bmatrix}$$

Fig 2.2: Example of a Matrix

Various operations can be performed on a matrix like Addition, Scalar Multiplication, and Transposition, etc. There are various types of matrix used in various applications. For example, in Graph Theory, the transpose matrix is used to represent the connection among nodes.

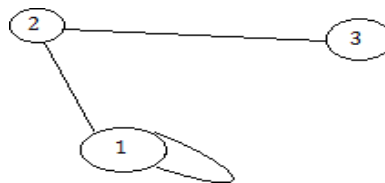


Fig 2.3: A Network Graph

$$\begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Fig 2.4: An adjacency matrix for the above network graph

2.3 Coefficient of Variation

The coefficient of variation (CV) is a measure of relative variability. It is the ratio of the standard deviation to the mean and is also known as a relative standard deviation. Its most common use is in the field of engineering and physics for quality assurance studies. The biggest advantage of the coefficient of variance is that it is unitless. It is used to represent the consistency of the data. Here consistency means the uniformity of data distribution. We can also use it to compare two datasets or samples. The coefficient of variation is also denoted by CV:

$$CV = \frac{S}{\bar{X}} \quad (2.1)$$

Here S stands for standard deviation and X stands for a mean of the sample. The use of CV is limited to some conditions. For example, it should be computed only for data measured on a ratio scale and only for non-negative values. It cannot be used for data on an interval scale.

There are some disadvantages when we use CV under certain conditions. For example Coefficient of Variation will reach infinity, if the mean is close to zero and it is sensitive to small change in the mean.

2.4 Sampling

The first thing comes to mind when one tries to perform some experiment on big data is how to handle big data or how to perform tests on such a big size of data. The technique most commonly used is sampling. A small subset of original data is taken out to perform

the tests, and it is assumed if the experiment is right in a sample then it should also perform well on the original data.

Why reduce data?

- i. It is not always possible to store all the data.
- ii. It is too resource consuming to work with big data.
- iii. It is faster to work with a smaller amount of data.

Why Sample?

There are several reasons why we use sampling approach rather than applying direct experimentation on original data. Some of the reasons are:

- i. Estimation on a sample is easier and more straightforward.
- ii. It is easy to understand.
- iii. Sampling is general and is independent of the analysis to be done.

How to take a sample of original data?

Now the question arises how to take a sample. For that, there are various sampling algorithms available. Some mostly used are as follow:

Random Walk:- First we pick a random node and then start a random walk on the graph [5]. The next node is selected with a certain probability, the probability by which vertices and edges are sampled [6]. If the random walk is struck at some point, it gets back to a new starting node and starts the random walk again.

Sampling by random node selection:- In random node selection, starting node is selected randomly, and then the next node is selected based on the probability of the node being selected. This probability could be either proportional to the page rank weight [5] of the node, or proportional to a degree of a node, i.e., with how many nodes it is connected. It can be used in peer to peer (P2P) networks like Bit torrent [6].

Sampling by random edge selection:- This is similar to node selection, while edges are randomly selected. It is known as Random Edge (RE) Sampling. The only difference in this one compared to random node selection is that we select edge rather than nodes. A variation of this model is Random Node-Edge (RNE) sampling, in which, first at random, a node is selected and then uniformly at random, an edge corresponding to the node is selected [5].

Forest Fire Model [8]:- In this model, we pick a random seed node and then begin burning outgoing links and corresponding nodes. Once a node is burned, the node at the other end has a chance to burn its link which will continue recursively. For example, a new graduate student arrives at a university and gets acquaintance with some senior students from his department. Those students introduce him to their friends, and those friends may introduce him to their friends which make it a recursive process. This process needs two parameters: a forward burning probability, and a backward burning ratio.

Snowball Sampling Approach [7]:- A snowball sampling approach is something similar to the Forest Fire Model but with little variation, i.e., it does not use two probabilities,

and it can also be carried out without the probability, using a deterministic approach. As the name suggests, it starts with a random node and then grows like a snowball by collecting all the corresponding nodes to that random node and continues.

2.5 Set Covering Algorithms

For set covering algorithms, we first need to know what set covering problem is and what the desired solutions are.

The Set Covering Problem is where we have a given set of elements (A finite universe) $M = \{e_1, e_2, \dots, e_m\}$ and a set of subsets of M , $X = \{S_1, S_2, \dots, S_n\}$. Each subset has a non-negative cost C_i . We have to find a union of subsets $U\{S_i\}$ which has minimum Cost (C) and contains all the elements of M .

The formal definition of set covering is:

$I \subseteq \{S_1, S_2, \dots, S_n\}$ that minimizes $\sum_{(i \in I)} C_i$ and guarantees $U_{(i \in I)} S_i = M$

Set covering problem is also defined on the 0-1 matrix by Carpara and Toth [9]:

Let $A=(a_{ij})$ be a 0-1 $m \times n$ matrix, and $c=(c_j)$ be an n -dimensional integer vector. The value c_j ($j \in N$) represents the cost of column j , assuming that $c_j > 0$ for $j \in N$. $j \in N$ covers a row $i \in M$ if $a_{ij}=1$. SCP calls for a minimum-cost subset S of columns, such that each row $i \in M$ is covered by at least one column $j \in S$. A natural mathematical model for SCP is

$$v(\text{SCP}) = \min \sum_{j \in N} C_j X_j \tag{2.2}$$

Subject to

$$\sum_{j \in N} A_{ij}x_j \geq 1, \text{ for all } i \in M, \quad (2.3)$$

$$x_j \in \{0,1\}, j \in N \quad (2.4)$$

Here Equation (2) makes sure that each row is covered by at least one column and Equation (3) is the integrality constraint [2].

The set covering problem is an NP-Hard problem, and there are many algorithms to solve it. There are two ways to solve this problem: exact algorithms and heuristic algorithms. The exact algorithms are mostly based on branch and bound and branch and cut [12]. The Best exact algorithm for the SCP is CPLEX [14]. Greedy algorithms may be the best fit to solve the significant combinatorial problems quickly. A greedy algorithm is discussed in more detail below.

2.5.1 Greedy Algorithms for Set Covering Problem

Greedy algorithms are a type of heuristic algorithms. There are various reasons why they are used so much. According to [11,15], greedy set cover algorithms are best known polynomial-time approximation algorithms for set cover. They are easy to implement, and that is why they are most commonly used heuristic algorithms.

Classical Greedy Algorithm:- This is the most basic greedy algorithm. It selects the set at each step which contains the largest number of uncovered elements. The process continues until all the elements are covered. Let (X, F) be an instance of set covering problem, where X contains all the elements in the universe and F contain subsets of X . C

is the solution which is initially empty, and S is a single subset. Then the Greedy Algorithm will work like this:

Greedy Set Cover (X, F)

- 1 $U \leftarrow X$
- 2 $C \leftarrow \emptyset$
- 3 While $U \neq \emptyset$ do
 - A. Select an $S \in F$ that maximizes $|S \cap U|$
 - B. $U \leftarrow U - S$
 - C. $C \leftarrow C \cup \{S\}$
- 4 return C

Example: Let $X = \{a, b, c, d, e, f, g, h, i, j\}$ be a universe and $F = \{\{a, b, c, d, e, f\}, \{a, b, c, g, h\}, \{d, e, f, i, j\}, \{g, h, i\}, \{j\}\}$ and let labels for these subsets be S_1, S_2, S_3, S_4, S_5 respectively. Initially, C is empty. In the first step, the greedy algorithm will select $S_1 = \{a, b, c, d, e, f\}$ because coverage of this subset is better than all other subsets. Now solution set is $C = \{\{a, b, c, d, e, f\}\}$.

In the second step, S_4 has the most substantial number of uncovered elements $\{g, h, i\}$, i.e., the greedy algorithm will choose S_4 and now solution set $C = \{\{a, b, c, d, e, f\}, \{g, h, i\}\}$.

In the third step, S_2 has one uncovered element $\{j\}$ and S_5 has one uncovered element $\{j\}$. Either one of them can be selected. Let us selected S_5 , so now the solution set will be $C = \{\{a, b, c, d, e, f\}, \{g, h, i\}, \{j\}\}$. Now all the elements in X are covered, so C is

the final solution set. The greedy algorithm might not give optimal solution every time, but the result is most of the time good enough. Considering the simple implementation, it is worth using it.

There are many variations of Greedy algorithms people use according to their needs, for example, weighted greedy algorithm. In this type of greedy algorithm, weight is assigned to every node which tells the importance of the node, and by how many nodes it is covered. In this situation, we can select a different strategy. For example, if a single node is covered by many nodes then we can say that this node can be added to result later and we try to get the least covered node into the result first. There are many other ways to modify greedy algorithm according to the needs.

2.6 Literature Review

2.6.1 Deep Web Crawling Using a New Set Covering Algorithm

In this paper [16], the authors described a new set covering algorithm for crawling in the deep web. To understand the concepts of this paper, first, we need to know hidden web, web crawling, and query selection. We give a brief explanation of these.

2.6.1.1 Hidden Web or Deep Web

A deep web is referred to as a web-generated from the file system and database and cannot be accessed by URL directly. It is often guarded by search interfaces. Most of the people depend on search engines like Yahoo, Google, etc. to find information on the web but these web search engines only search the surface web. It is estimated that deep web is much larger than the surface web [19]. According to [20], the hidden web comprises of

nearly 550 billion documents which are up to 2,000 times greater than surface web. Hidden Web has more focused content than Surface Web entities.

2.6.1.2 Deep Web Crawling

Fetching the information from the hidden web is termed as deep web crawling. A query is issued which contains some keywords, and with those keywords in the query, we crawl the data from the hidden web. For crawling the deep web, crawlers are used which is a GUI based interface between the web and the user. Hidden Web Crawlers search the hidden website using the given query, and then they give back the results based on the query.

2.6.1.3 Query Selection

It is the process of selecting queries that can cover a maximum number of documents in a corpus. It is an essential step because if the format of a query is not proper, it may give an empty result [18]. According to [17], one should also consider the cost of the query because sometimes some queries might give good results but at the stake of a significant query cost which is not acceptable.

Now that we know some basics about web crawling let's get back to the paper by Wang et al. [16]. In this paper, the authors used set covering with greedy and weighted greedy algorithm for the deep web crawling. The primary task is to select a proper set of queries to minimize the total cost of mapping selected queries into the original database.

They created a four-step framework for deep web crawling:

- i. Randomly select documents from original database to build a sample.

- ii. Create a query pool, i.e., a set of queries based on sampleDB.
- iii. By using sampleDB and query pool, select a proper set of queries.
- iv. Map those selected queries to the original database.

For example, Table 2.1 shows an input matrix for the set covering algorithm. Here $\{d_1, d_2, \dots, d_9\}$ represents documents of a sample database. $\{q_1, q_2, \dots, q_5\}$ represent queries. Let this table be a sample from the original database. Suppose that we run the algorithm on a sample rather than directly on the corpus. Queries selected from a sample database can also perform on the original data source as well [21].

doc number	q_1	q_2	q_3	q_4	q_5
d_1	0	0	1	0	0
d_2	0	0	1	1	0
d_3	1	0	1	0	1
d_4	0	0	1	0	1
d_5	1	0	0	0	1
d_6	1	1	0	1	0
d_7	0	0	0	1	0
d_8	1	1	0	0	1
d_9	0	0	1	1	1

Table 2.1: The Input Matrix for Set Covering Matrix

According to a simple greedy algorithm for unit cost, next query q is the one which covers the maximum number of new documents. Here the authors are using a weighted greedy algorithm. Therefore, they add weights to the documents. It will help to cover small documents first because they can be matched with few queries. Smaller documents are given more weight so that queries covering them can be selected first.

According to greedy strategy, queries QJ with larger query weight (qw) are preferred. A large qw should be obtained by a small number of documents. In other words, queries with smaller df/qw are preferred. Therefore weighted greedy algorithm will choose next query with smaller df/qw.

For example Table 2 shows the weights based on Table 1. At the bottom of the table, document frequencies and query weights are listed. Here the smallest value for df/qw is 1.85 for q4. q4 is selected, and documents covered by that query are removed from the matrix. See Table 3 for the matrix in the second round.

doc number	q_1	q_2	q_3	q_4	q_5
d_1	0	0	1	0	0
d_2	0	0	0.5	0.5	0
d_3	0.33	0	0.33	0	0.33
d_4	0	0	0.5	0	0.5
d_5	0.5	0	0	0	0.5
d_6	0.33	0.33	0	0.33	0
d_7	0	0	0	1	0
d_8	0.33	0.33	0	0	0.33
d_9	0	0	0.33	0.33	0.33
df	4	2	5	4	5
qw	1.49	0.66	2.66	2.16	1.99
df/qw	2.68	3.03	1.88	1.85	2.51

Table 2.2: The initial table with weights based on Table 1

doc number	q_1	q_2	q_3	q_5
d_1	0	0	1	0
d_3	0.33	0	0.33	0.33
d_4	0	0	0.5	0.5
d_5	0.5	0	0	0.5
d_8	0.33	0.33	0	0.33
df	4	2	5	5
qw	1.16	0.33	1.83	1.66
df/qw	3.44	6.06	2.73	3.01

Table 2.3: Second round weighted matrix

See Table 2.3 now, it has only four queries and five documents left. The process continues until all the documents are removed from the matrix. Table 4 shows the final results of the weighted greedy method. Here q_4 , q_3 , q_1 are selected in the first, second and third round respectively.

column	df	qw	df/qw	cost	unique rows
q_4	4	2.16	1.85	4	4
q_3	5	1.83	2.73	9	7
q_1	4	0.83	4.82	13	9

Table 2.4: Results of the weighted greedy method.

Here the cost is how many total documents can a query fetch. The unique rows column is how many total unique documents are fetched by queries after a certain point. For example, q_3 has a document frequency of 5. Therefore, it adds 5 to the cost and the total

cost after selecting q4 and q3 is 9. q3 can fetch three new documents which means three unique rows. The unique rows fetched by q4 and q3 are 7.

Algorithm 1: Weighted Greedy Algorithm.

Input: *SampleDB*, *QueryPool* QP, $m \times n$ Matrix *A*, where $m=|SampleDB|$
and $n=|QP|$

Output: A set of queries *Q*

1. $Q = \phi$;
 2. Let $B = (b_{ij})$ be a $m \times n$ matrix and $b_{ij} = a_{ij} \times dw_{a_i}^{QP}$;
 3. Based on the matrix *B*, we calculate the query weight for each term and move the q_j that minimizes $\frac{df_j}{qw_{q_j}}$ into *Q* ;
 4. Check if the queries in *Q* can cover all documents in *SampleDB*. If yes, the process ends;
 5. Update matrix *B* by removing the selected query and the documents that are covered by the query. Go to Step 3.
-

The above picture shows the weighted greedy algorithm in [16]. This method performs better than the greedy algorithm as the experiment shows.

Therefore we will be using this same approach in operational research and provide the comparison to see if this weighted greedy method performs better in other scenarios.

2.7 Set Cover Algorithms for Very Large Datasets

Graham et al. [1] showed how to work with large datasets to find a solution to the set covering problem with a standard greedy algorithm. They gave an alternative approach to the greedy algorithm, particularly for disk-resident datasets. The most backdated research on this topic is by Berger et al. [11]. The idea of Berger is recently applied to Map Reduce paradigm [22] to find partial set cover in the distributed case.

They considered a standard unweighted greedy algorithm for the set covering problem. The most significant problem for a greedy algorithm is the use of memory because, for every update of the set, it needs to access information from a disk or access the main memory. Although modern computers have a significant amount of memory, efficient use of memory is necessary. For example, random access to disk will be highly expensive. Graham et al. [1] analyzed the algorithms for external memory model of the running during the execution.

They presented a greedy heuristic using two approaches, inverted index, and multiple passes.

Inverted Index:- This approach is suitable when random access to a location in the memory takes a constant amount of time. In inverted index approach, a priority queue is maintained for each $S_i \setminus C$. The priority queue is a descending order queue of set S_i . Here S_i denotes the collection of m subsets of the universe and C denotes elements covered so far. To update values of $S_i \setminus C$, when a set S_i is added to the solution, it is needed to determine which other sets contain elements of S_i . This step can be done using inverted index in which each item j is associated with

$$T_j = \{i: j \in S_i\} \quad (2.5)$$

T_j is the inverted index of S_i . T_j is created in preprocessing step, and greedy iteration is applied. The inverted index of the example in Fig 2.5 is shown in Fig 2.6.

S_1	ABCDE		S_2	ABDFG
S_3	AFG		S_4	BCG
S_5	GH		S_6	EH
S_7	CI		S_8	A
S_9	E		S_{10}	I

Fig 2.5: Sample input data

A	1, 2, 3, 8		B	1, 2, 4		C	1, 4, 7
D	1, 2		E	1, 6, 9		F	2, 3
G	2, 3, 4, 6		H	4, 6		I	7, 10

Fig 2.6: Inverted Index of Fig 1

This algorithm is expensive due to many random accesses to many locations on disk. It is also tough to predict at which stage T_j will be used.

Multiple Passes:- This approach does not use any priority queue or inverted index. It merely keeps track of set C covered so far. In this approach, every time two sets are compared, we look for those already covered elements in those not selected sets. It makes linear passes through the data which is efficient when the data is resident on the disk. The only disadvantage is that it will be slow if the size of a selected set is large because it might need to go through the entire dataset to add this set.

Graham et al. give a new approach which is better than the standard greedy algorithm. Their approach follows the subsetting of sets according to the size of the sets. Their algorithm works in two loops. They added a parameter $p > 1$ to govern the approximation of the algorithm.

- For $k \rightarrow K$ down to 0:
 - For each set S_i in $\mathcal{S}^{(k)}$:
 - * If $|S_i \setminus C| \geq p^k$: add i to Σ and update C .
 - * Else: let set $S_i \leftarrow S_i \setminus C$ and add the updated set to subcollection $\mathcal{S}^{(k')}$, where the new set size satisfies $p^{k'} \leq |S_i| < p^{k'+1}$ (and therefore $k' < k$).
- For each set S_i in $\mathcal{S}^{(0)}$:
 - If $|S_i \setminus C| = 1$: add i to Σ and update C .

The algorithm by Graham et. al.

Initially, S_i is assigned to sub-collection $\mathcal{S}^{(k)}$ if $p^k \leq |S_i| < p^{k+1}$. Here in the algorithm, K is the largest k with nonempty $\mathcal{S}^{(k)}$. Figure 3 shows the algorithm execution on sample input data in Figure 2.7.

At start of the first step, when $k = 2$:

4-7	ABCDE, ABDFG
2-3	AFG, BCG, GH, EH, CI, AFG
1	A, E, I

At start of the second step, when $k = 1$:

2-3	aFG, bcG, GH, eH, cI, (abd)FG
1	a, e, I

After the third set has been selected:

2-3	bcg, gH, eH, cI, (abd)fg
1	a, e, I

At start of the third step, when $k = 0$:

1	a, e, <u>I</u> , (<u>g</u>)H, (e)H, (c)I
---	--

Fig 2.7: Execution of algorithm by Graham. Et al. on sample data in fig 1

The basic functionality of this algorithm is to arrange the sets according to their sizes. The set with the biggest size is selected and added to the solution set. The rest sets in that

range are reduced to only uncovered elements and appended to the corresponding range of sets. This process continues until all the elements in the universe are covered. The proposed algorithm according to the results is much faster than the conventional algorithms.

This paper gave us an idea to use greedy and variation of greedy with large datasets. We are interested in seeing the behavior of this algorithm in operational research when data is large. The approach followed by this paper was to test on disk-resident data and memory resident data. We are using the leanings from memory resident approach to do our experiments.

2.8 Set Covering in Locating Facilities

In the planning strategy of big public and private firms, facility location is a critical component of the study. In facility locating, covering models are most extensively studied. They are such attractive topics for researchers because of their applicability in the real world. In covering models, the customer can get service from a facility in a predefined area. That predefined distance is called coverage distance or coverage radius [23]. According to Schilling et al. [24], Set covering models can be classified into two major categories: Set Covering Problem (SCP) and Maximal Covering Location Problem (MCLP). The difference between these two is that in SCP, the coverage is required and in MCLP, the coverage is optimized. Classification can also be given based on the solution, i.e., heuristic or optimal.

According to Reza et. al.[25], the first covering model was introduced by Hakimi in 1965 [26]. He used a vertex covering problem in a graph to determine the minimum number of

police needed to cover all the nodes on a highway network. The first mathematical problem was developed by Toregas et al. [27]. It was used for the location of emergency service facilities. We are going to discuss various set covering approaches for locating facilities.

Another paper by Toregas, Swain, et al. [30] gives an emergency vehicle model with a specified time or distance constraint which is on demand. If this kind of constraints is given, then the problem is either to find a solution with minimum time or distance or to find a solution with a minimum number of facilities. They have assumed that the time needed between every two user nodes is known, and the upper limit for the constraint like time or distance can be described. If maximum response time for a node is s , then for any node i that is at most s time away from i , we can provide the emergency service to i . N_i denotes this set for node i . They give a mathematical problem as follows

$x_j = \{ 0 \text{ if no facility is established at point } j,$

$x_j = \{ 1 \text{ if a facility is established at point } j.$

$$\begin{array}{ll}
 \text{Minimize} & z = \sum_{j=1}^{j=n} x_j \\
 \text{(I) subject to:} & \sum_{j \in N_i} x_j \geq 1, \\
 & x_j = (0, 1).
 \end{array}$$

The actual implementation of (I) requires two steps. In the first step, it determines the sets N_i for a given value of s and a given shortest distance matrix. The second step involves the solution of (I) with the sets established in step one.

A paper by Mark S. Daskin [28] describes the stochastic approach for set covering. They used a heuristic algorithm to solve the problem. They considered the problem of covering a location with more than one facility so that in case one facility is not operating; the other can be reached. They have given an algorithm which describes in the case of failure, which facility will cover the locations covered by the failed facility.

CHAPTER 3

PROPOSED APPROACH AND EXPERIMENTAL SETUP

3.1 Introduction

This chapter introduces the use of the weighted greedy algorithm proposed by Wang. Et. al.[16] in the field of resource management. As demonstrated in the paper, it has outperformed the traditional greedy algorithm in the field of web crawling for query selection. Our objective here is to compare the performance of the weighted greedy algorithm with the traditional greedy algorithm in roadmaps.

3.2 Greedy Algorithm

Greedy algorithms are a type of heuristic algorithms. A greedy algorithm always looks for a locally optimal solution. Greedy might not find a globally optimal solution, but it will provide an answer very close to the optimal one with less processing cost. Greedy Algorithms are used in various fields like networking, machine learning, artificial intelligence, etc.

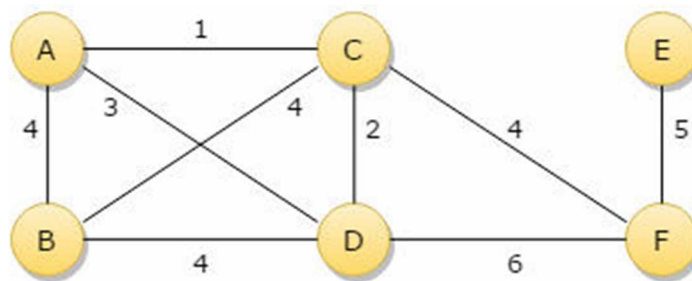


Fig 3.1: A Sample Graph

Figure 3.1 is a sample graph. Suppose that we want to apply a greedy algorithm on this graph to reach from one point to another, say from C to E with the shortest path. The

shortest path is C to F, F to E and the total cost is 9. According to the Greedy algorithm, it will choose the shortest path at a particular instance. Therefore, the path will be C to A, A to D, D to F, F to E and the total cost will be 15. The path chosen by greedy algorithm is not optimal all the time. It only looks for best option at a particular instance. It can be used in multiple scenarios and setups. There are several algorithms used in the set covering based on a greedy approach to solve the problems.

The basic greedy algorithm uses the step by step approach to solve the problem, and at every step, a solution node is chosen for this problem. Greedy is to approximate the globally optimal solution using the locally optimal solution on each step. For every step, one column is selected, and there are various ways to select a column. A column here represents a node.

There are various approaches to apply the greedy approach, it all depends on which factor we want to focus on. Some of the approaches on which solution can be focused are as follows:

- **Minimize the cost:** The next column is selected which has the lowest cost on a particular step. Using the smallest cost at every step, lowest total cost is approximated.
- **Maximize coverage:** Another method is to select the next column which can cover the largest number of nodes that are not yet covered by previously selected nodes. This approach aims to reach the maximum coverage in minimum steps.

- **Combined Approach:** We can also use the combined approach which combines both the above approaches and take into consideration cost and the number of new nodes that can be covered.

Node number	1	2	3	4	5
1	0	0	1	1	0
2	0	0	1	0	1
3	1	1	0	1	0
4	1	0	1	0	0
5	0	1	0	0	0
ncd	2	2	3	2	1
nnf	2	2	3	3	3
ncd/nnf	1	1	1	1	1

Table 3.1: Sample matrix of road network for greedy algorithm

The above matrix represents the input matrix to the greedy algorithm. Here ncd is node coverage degree which means how many nodes can be covered by a node. nnf is new nodes fetched, i.e., how many new nodes can be fetched by this node. Initially, nnf is the same as node frequency, and it changes after some iterations. ncd/nnf is to determine which should be next solution node.

3.3 Weighted Greedy Algorithm

In weighted greedy algorithms, the approach is the same to choose the best at a particular instance. The only difference is that there are weights added to the nodes which have a crucial role in deciding for a particular instance to determine which one is the best. The weighted greedy algorithm, which is used in our approach, is based on choosing the nodes which are less covered, which means areas that are less accessible are covered first. The algorithm is as follows:

Input: an $m \times n$ matrix $A = (a_{ij})$
Output: a solution n -vector $X = (x_1, \dots, x_n)$
Process:

- 1 $c_j = \sum_{i=1}^m a_{ij}; x_j = 0(1 \leq j \leq n); y_i = 0(1 \leq i \leq m);$
- 2 while($\sum_{i=1}^m y_i < m$) {
- 3 find a column q_u that maximizes $rw(u)/c_u;$
- 4 $x_u = 1; y_i = 1$ if $\sum_{j=1}^n a_{ij}x_j \geq 1;$
- 5 }

Node number	1	2	3	4	5
1	0	0	0.5	0.5	0
2	0	0	0.5	0	0.5
3	0.33	0.33	0	0.33	0
4	0.5	0	0.5	0	0
5	0	1	0	0	0

ncd	2	2	3	2	1
nw	0.83	1.33	2	0.83	0.5
ncd/nw	2.409	1.503	1.500	2.409	2

Table 3.2: Sample matrix of road network for weighted greedy algorithm

Here ncd stands for node coverage degree, nw for node weight which is the sum of the significance of all nodes and ncd/nw is used to pick the next solution node. Here node significance stands for the out degree of a node, i.e. the total sum the column of this node in the matrix.

According to the algorithm, more focus should be put on nodes with less coverage, i.e., nodes that can be reached by less number of nodes. As for greedy strategy, nodes with a large number of node weight are preferred, i.e., small nf/nw is preferred.

In the greedy algorithm, it does not matter whether a node is covered later or early, but this is important in the weighted greedy method. In the above table, node 5 is only covered by node 2, so it is essential to cover this node first. We argue that for each node i , if the number of the nodes covering node i is bigger, it is better covering node i later. The reason for this is:

When node i is covered in later steps, more columns covering node i means that there is a possibility to select small cost column covering few new nodes.

When node i is covered in earlier steps, there is a higher possibility of overlapped coverage, because node i will be covered multiple times when more columns will be covering this node.

3.4 Roadmap

Here term roadmap is coined as a network of roads for a particular area demonstrated in the form of edges and vertices. Every node or vertex represents an intersection, and every edge is a link between those nodes. These roadmaps can be created from the data provided in the form of a matrix. Usually, the 0-1 matrix represents which node is connected to the other node.

3.5 Setup Procedure

The primary purpose of our experiment is to test the performance of the weighted greedy algorithm in resource management and compare it with the greedy algorithm regarding solution results. We will run greedy and weighted greedy algorithm on datasets with 100 samples, 50 for coverage radius 1, and 50 for variable coverage radius, using three cost definitions.

Our experimentation works in the following structure:

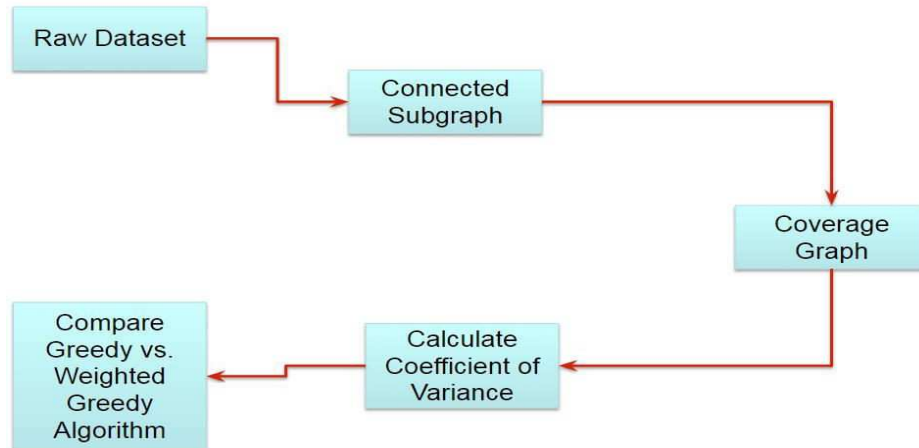


Fig 3.2: Flow of the approach

The raw dataset, Connected Subgraph, and Coverage Graph are the part of data preprocessing where data is being converted into the suitable format as an input for greedy and weighted greedy algorithm. Calculation of Coefficient of Variance is being done as a parameter to compare both algorithms. The last module is a comparison of Greedy vs. Weighted Greedy algorithm where both the algorithms are implemented and executed on same input data to test their performance.

3.5.1 Raw Dataset

Raw Dataset is the original data obtained from the SNAP(Stanford Network Analysis Project)[35]. We are using the dataset which is road network of California. Road network for California contains 1,965,206 Nodes and 2,766,607 Edges. This raw dataset is in the form of a matrix with two columns where column 1 denotes the node from which connection is, and the column 2 denotes to which node connection is going.

3.5.2 Connected Subgraph

Working with big data is always a difficult task. There are several issues like memory and hardware resources we have to deal with and to avoid these problems we are using the connected subgraphs of smaller size from these raw datasets. The connected subgraph, as the name suggests is a small portion of the original data coined as a sample. We are using the sample size of 10,000 nodes approximately. This sample is a matrix same as the raw dataset but with smaller size and with all the connection among those selected nodes from the raw dataset.

V1	V2
10	9
10	11
10	84
10	110
9	7
9	10
9	84
11	10
11	12
11	110
84	9
84	10
84	83
84	85
110	10
110	11
110	111
7	9
12	11

Fig 3.3: A 10-node connected subgraph

The above figure 3.3 is an example of connected subgraph with 10 nodes fetched from a raw dataset with all the connection among the nodes. We are using this kind of connected subgraph as an input to build coverage matrix.

3.5.3 Coverage Graph

It is the adjacency matrix generated from connected subgraph. The coverage graph is generated according to the defined coverage. Here coverage is how many nodes can a node cover starting from its neighbors. If we say the coverage graph has coverage value of two, then we can say that a node can cover its neighbors and neighbors of their neighbors. As the coverage value increases, more levels of neighbors each node will cover. The coverage graph is represented in the form of adjacency matrix where 1 denotes that the node can cover that node and 0 denotes it cannot cover that node.

	7	9	10	11	12	83	84	85	110	111
7	0	1	0	0	0	0	0	0	0	0
9	1	0	1	0	0	0	1	0	0	0
10	0	1	0	1	0	0	1	0	1	0
11	0	0	1	0	1	0	0	0	1	0
12	0	0	0	1	0	0	0	0	0	0
83	0	0	0	0	0	0	0	0	0	0
84	0	1	1	0	0	1	0	1	0	0
85	0	0	0	0	0	0	0	0	0	0
110	0	0	1	1	0	0	0	0	0	1
111	0	0	0	0	0	0	0	0	0	0

Fig 3.4: Coverage Matrix with coverage value 1

The above matrix is a representation of connected subgraph in the form of coverage graph where each row represents which nodes a single node can cover. For example, in second-row, node 9 can cover 7, 10 and 84. This matrix has coverage 1, i.e., a node can cover its neighbors only. If this node has coverage 2 then the same node 9 could have covered its neighbors 7, 10 and 84 as well as neighbors of 7, 10, and 84 which are 9, 11,

110, 83 and 85. This coverage graph acts as input for the greedy and weighted greedy algorithm.

3.5.4 Calculation of Coefficient of Variance

This part calculates the coefficient of variance which is used as a parameter to compare the performance of both the algorithms. The coefficient of Variance (CV) is calculated using the standard formula which is standard deviation divided by the mean of the sample. Once the CV is calculated, we can test the performance of algorithms and analyze for a specific CV range how much improvement our algorithms show. For every sample, we calculate the CV once.

In our case, we are calculating the CV of a sample using the formula used by Yan Wang [34] in his approach. We measure the dispersion of node degree (deg) using Coefficient of Variation. We know that the CV is the ratio of standard deviation to the mean, where mean is the sum of the node degree over the total number of nodes in the sample.

$$\mu = \frac{\sum_{i=1}^m deg(i)}{m}. \quad (3.1)$$

Mean here can also be called an average node coverage degree. In the same way, we will calculate the standard deviation of the sample which is

$$SD = \sqrt{\frac{\sum_{i=1}^m (deg(i) - \mu)^2}{m}}, \quad (3.2)$$

Here deg is the degree of a node and μ is the mean calculated above, and m is a total number of nodes in the sample. By definition of this standard deviation and mean, we calculate the value of coefficient of variation (CV) which is

$$CV = \frac{1}{\mu} \sqrt{\frac{\sum_{i=1}^m (deg(i) - \mu)^2}{m}}, \quad (3.3)$$

Once the CV is calculated for the sample, we can compare the algorithms and calculate the improvement of weighted greedy over the greedy algorithm.

3.5.5 Comparison of Greedy and weighted Greedy Algorithm

In this step, a coverage graph with specific CV is supplied as an input to both the algorithms and the algorithms perform their calculations to compute the solution outcome. The solution contains two different answers, one from greedy and one from weighted greedy. The solution contains the number of solution nodes given by each algorithm. Then those solutions are compared using the improvement formulae to check how much improvement the weighted greedy algorithm has over greedy algorithm.

$$IMP = \frac{Cg - Cw}{Cg} \quad (3.4)$$

Formulae to check the improvement

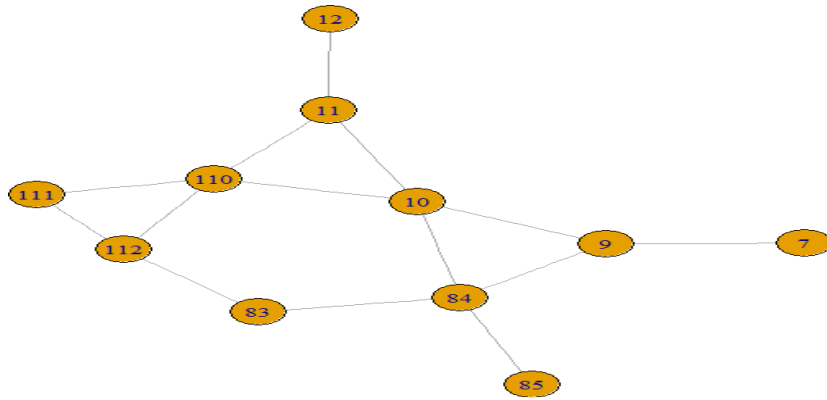


Fig 3.5: Connected Subgraph plot view

Now we convert this subgraph into an adjacency matrix with the coverage radius 1. The matrix produced is as follows:

	7	9	10	84	11	110	12	83	112	85	111
7	0	1	0	0	0	0	0	0	0	0	0
9	1	0	1	1	0	0	0	0	0	0	0
10	0	1	0	1	1	1	0	0	0	0	0
84	0	1	1	0	0	0	0	1	0	1	0
11	0	0	1	0	0	1	1	0	0	0	0
110	0	0	1	0	1	0	0	0	1	0	1
12	0	0	0	0	1	0	0	0	0	0	0
83	0	0	0	1	0	0	0	0	1	0	0
112	0	0	0	0	0	1	0	1	0	0	1
85	0	0	0	1	0	0	0	0	0	0	0
111	0	0	0	0	0	1	0	0	1	0	0

Table 3.4: 01 Matrix of the Subgrap

Now we consider applying the weighted greedy algorithm on this matrix and calculate the node coverage degree(ncd), node weight(nw) and nf/nw. First, we add all the values of each row then replace all the 1's with 1/sum where the sum is the node significance

index. We will perform this step for every individual row, and the resulting matrix is as follows

	7	9	10	84	11	110	12	83	112	85	111
7	0	1	0	0	0	0	0	0	0	0	0
9	0.333	0	0.333	0.333	0	0	0	0	0	0	0
10	0	0.25	0	0.25	0.25	0.25	0	0	0	0	0
84	0	0.25	0.25	0	0	0	0	0.25	0	0.25	0
11	0	0	0.333	0	0	0.333	0.333	0	0	0	0
110	0	0	0.25	0	0.25	0	0	0	0.25	0	0.25
12	0	0	0	0	1	0	0	0	0	0	0
83	0	0	0	0	0	0	0	0	0	0	0
112	0	0	0	0	0	0.333	0	0.333	0	0	0.333
85	0	0	0	1	0	0	0	0	0	0	0
111	0	0	0	0	0	0.5	0	0	0.5	0	0
ncd	1	3	4	4	3	4	1	2	3	1	2
nw	0.33	1.5	1.116	2.083	1.5	1.416	0.333	0.583	1.25	0.25	0.583
ncd/nw	3.03	2	3.43	1.92	2	2.82	3.03	3.43	2.4	4	3.43

Table 3.5: Matrix after division of node weights and calculation of nf, nw, nf/nw

We select the value with smallest nf/nw. Now 84 will be added to the solution and column with node 84 and all rows of nodes it covers will be deleted including 84. The resulting matrix after this step will be

	7	9	10	11	110	12	83	112	85	111
7	0	1	0	0	0	0	0	0	0	0
11	0	0	0.333	0	0.333	0.333	0	0	0	0
110	0	0	0.25	0.25	0	0	0	0.25	0	0.25
12	0	0	0	1	0	0	0	0	0	0
112	0	0	0	0	0.333	0	0.333	0	0	0.333
111	0	0	0	0	0.5	0	0	0.5	0	0
ncd	1	3	4	3	4	1	2	3	1	2
nw	0	1	0.583	1.25	1.166	0.333	0.333	0.75	0	0.583
ncd/nw	Inf	3	6.861063	2.4	3.430532	3.003003	6.006006	4	Inf	3.430532

Table 3.6: Matrix after selection of the first node

Now we again select the minimum values for nf/nw, and node 11 will be selected. The same process will be repeated, and column with node 11 and rows covered by this node will be deleted. The resulting matrix after this round will be

	7	9	10	110	12	83	112	85	111
7	0	1	0	0	0	0	0	0	0
112	0	0	0	0.333	0	0.333	0	0	0.333
111	0	0	0	0.5	0	0	0.5	0	0
ncd	1	3	4	4	1	2	3	1	2
nw	0	1	0	0.833	0	0.333	0.5	0	0.333
ncd/nw	Inf	3 Inf	4.801921	Inf	6.006006	6 Inf	6.006006		

Table 3.7: Matrix after second round

In the same way, after the third round now the selected node will be 9, and the same process will be repeated. In the fourth round, selected result node will be 110, and all the rows will be deleted.

	7	10	110	12	83	112	85	111
112	0	0	0.333	0	0.333	0	0	0.333
111	0	0	0.5	0	0	0.5	0	0
nf	1	4	4	1	2	3	1	2
nw	0	0	0.833	0	0.333	0.5	0	0.333
nf/nw	Inf	Inf	4.801921	Inf	6.006006	6 Inf	6.006006	

Table 3.8: Matrix after the third round

The nodes selected as result nodes are 84,11,9,110

node	nf	nw	Nf/nw	cost	Unique rows
84	4	2.08	1.92	4	5
11	3	1.25	2.40	7	8
9	3	1	3	10	9
110	4	0.83	4.80	14	11

Table 3.9: Solution table for Weighted Greedy algorithm

In this example, a greedy algorithm can start from any random node because initially, the value of new node fetched will be 1 for every node. Let's say it starts at 10.

	10	9	11	84	110	7	12	83	85	111	112
10	0	1	1	1	1	0	0	0	0	0	0
9	1	0	0	1	0	1	0	0	0	0	0
11	1	0	0	0	1	0	1	0	0	0	0
84	1	1	0	0	0	0	0	1	1	0	0
110	1	0	1	0	0	0	0	0	0	1	1
7	0	1	0	0	0	0	0	0	0	0	0
12	0	0	1	0	0	0	0	0	0	0	0
83	0	0	0	1	0	0	0	0	0	0	0
85	0	0	0	1	0	0	0	0	0	0	0
111	0	0	0	0	1	0	0	0	0	0	0
112	0	0	0	0	1	0	0	0	0	0	0
ncd	4	3	3	4	4	1	1	1	1	1	1
nnf	4	3	3	4	4	1	1	1	1	1	1
nnv	1	1	1	1	1	1	1	1	1	1	1

Table 3.10: Matrix at the starting point for greedy algorithm

The above is the matrix at the initial stage after calculating node coverage degree(ncd), new nodes fetched(nnf) and new node value(nnv). Starting from node 10 we will delete rows covered by node 10 and delete node 10 from columns.

	9	11	84	110	7	12	83	85	111	112
7	1	0	0	0	0	0	0	0	0	0
12	0	1	0	0	0	0	0	0	0	0
83	0	0	1	0	0	0	0	0	0	0
85	0	0	1	0	0	0	0	0	0	0
111	0	0	0	1	0	0	0	0	0	0
112	0	0	0	1	0	0	0	0	0	0
ncd	3	3	4	4	1	1	1	1	1	1
nnf	1	1	2	2	0	0	0	0	0	0
nnv	3	3	2	2	Inf	Inf	Inf	Inf	Inf	Inf

Table 3.11: Matrix after first round of greedy

In the same way, the process will continue, and the solution for greedy algorithm will be as follows

node	ncd	nnf	ncd/nnf	cost	Unique rows
10	4	4	1	4	5
110	4	2	2	8	7
84	4	2	2	12	9
11	3	1	3	15	10
9	3	1	3	18	11

Table 3.12: Solution table for greedy algorithm

From the above two solution tables, we see that weighted greedy found 4 solutions with a total cost of 14 whereas greedy algorithm found 5 solutions with a total cost of 18.

3.7 Technologies Used

3.7.1 R

R is a GNU project developed in bell laboratories by John Chambers and his colleagues [36]. It is an environment for statistical computing and graphics. R is open source software, and it can run on UNIX, Linux, Windows and Mac operating systems. It is mostly used for data manipulation, calculation, and graphical display. Following are some of its features:

- It has excellent graphical facilities for data analysis and display.
- A simple and well developed useful programming language allowing user-defined recursive functions.
- An efficient storage facility and data handling language.
- A suite of operators for calculations on matrices.

We can extend R easily with packages and anybody can publish his or her packages for specific tasks.

3.7.2 iGraph Library

It is a package used to plot and analyze the network graphs. We used this package to create our coverage matrix for variable coverage. This library can be used to create and plot network graphs from edge or vertex table and vice versa.

3.7.3 R Studio

RStudio is an open source IDE for R. It is also available with a commercial license for organizations not able to use AGPL software [37]. It also offers other excellent products which include RStudio Server open source and licensed as well to host applications on the local server. Shiny io creates applications using R with minimal support and host applications on the Shiny server.

CHAPTER 4

EXPERIMENTATION AND RESULTS

In this chapter, we present the experiment results, obtained using the greedy and weighted greedy method. The purpose is to test whether the weighted greedy is better than the greedy algorithm in resource allocation setup.

4.1 Data

We are going to perform the experimentation on a dataset by extracting several regional maps from it. The Dataset contains 1,965,206 Nodes, but we will use regional maps of 10,000 nodes. We will experiment with two different kinds of inputs: one will be with Coverage Radius 1, and the other will be with Coverage Radius greater than one. We will run both algorithms on 50 regional maps of coverage radius 1, and 50 regional maps of variable coverage radius. We will check the improvement of the weighted greedy algorithm in different scenarios like under different coverage radius or different cost definitions.

The algorithms will be performed on the symmetric matrix of 10000 * 10000 Nodes. We will try to cover the gap of CV range between 0.3 and 1. In previous research, there are no results available for this range. Here CV represents the dispersion of node coverage degree.

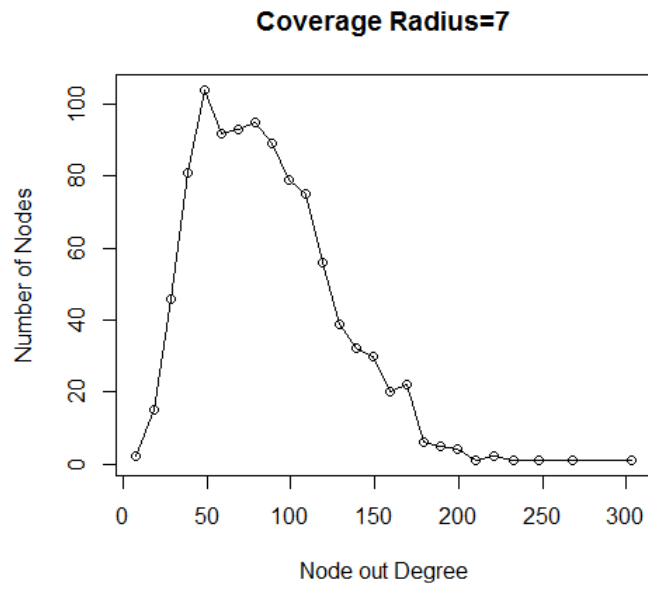


Fig4.1: Distribution of node coverage degree in Coverage Radius 7

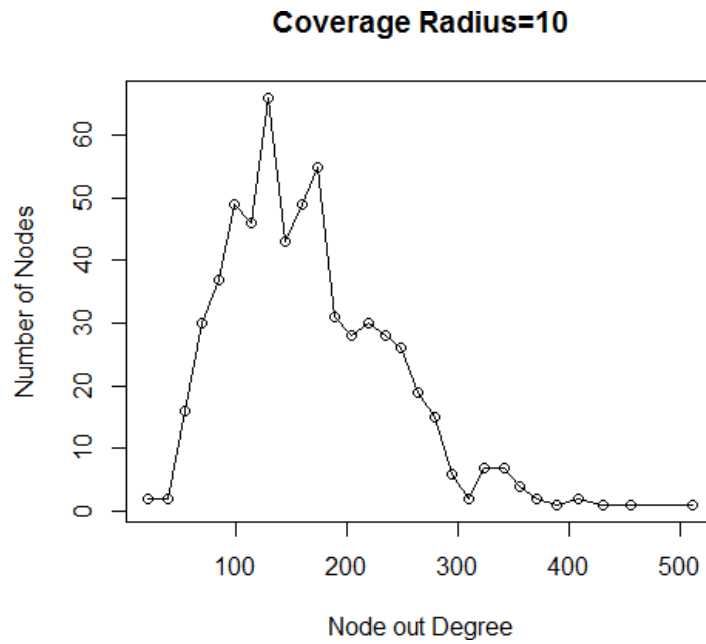


Fig4.2: Distribution of node coverage degree in Variable Coverage Radius 10

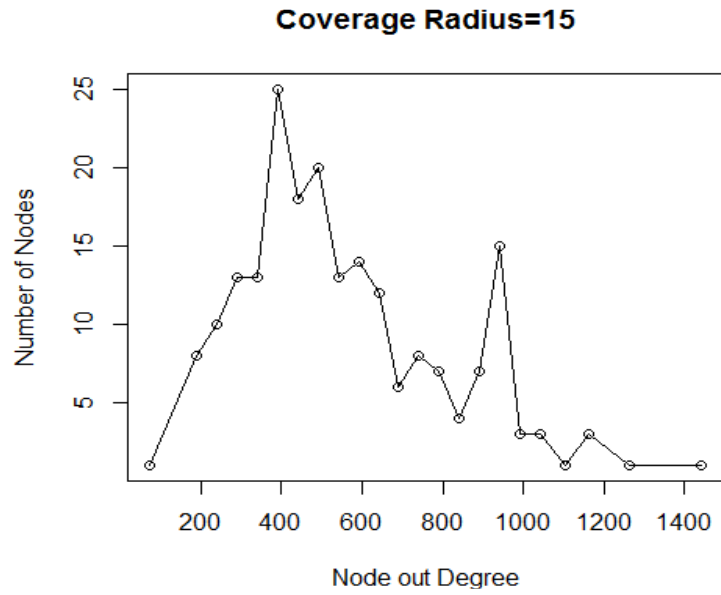


Fig4.3: Distribution of node coverage degree in Variable Coverage Radius 15

Data Source	Number of Samples	Rows(m)	Columns(n)	Node Coverage Degree			
				max	min	mean	CV
Coverage Radius 1	50	10000	10000	8	1	2.75	0.37
Variable Coverage Radius	50	10000	10000	9744	20	898.11	0.42

Table 4.1: The properties of data source with two types of data: one with coverage radius 1, and the other with variable coverage radius

The above graphs represent the distribution of node out degree under two scenarios: one with coverage radius 1, and the other with coverage radius greater than one. The table

represents the properties of two different versions of the data we are using. We are showing these results for 50 samples of each data. Both types of samples have about 10000 rows and 10000 columns. The table shows the maximum and a minimum number of node coverage degree, average mean of node coverage degree and average CV of samples.

4.2 Cost Definition

We also want to see how different cost definitions will affect the performance of the algorithm. We have used three types of cost definitions as follows:

Infrastructure Cost: With this type, the cost of selecting any node is one. It corresponds to the situation in traditional set covering problem where the ultimate goal is to minimize the number of nodes selected. It is also called set covering with unit cost. This type of cost corresponds to the cost of building a station, for example, a medical facility, food service or fuel station.

Location Cost: With this type of cost definition, the cost of a node is the out-degree of this node. For example, if a node is connected to five other nodes, then the out-degree of this node is five.

Driving Cost: This cost is the sum of the distance between this node and each node it covers. The distance between two nodes is the length of the shortest path between them in regional map.

4.3 Results

We divide the data into two parts and three subparts. Data is divided into two parts: one is coverage radius 1, and the other with coverage radius greater than 1. These two categories are then tested using both greedy and weighted greedy algorithms using three different scenarios of cost definitions.

We used 50 regional maps with coverage radius 1, and 50 maps for with variable coverage radius greater than 1. We have run the greedy and weighted greedy algorithm three times on every regional map using each cost definition.

With our experiments, the weighted greedy algorithm turns out to be very efficient on our data sources according to tables and figures:

- The cost calculated in all different scenarios by the weighted greedy algorithm is less than that from greedy algorithm.
- On average, on regional maps with variable coverage radius, the weighted greedy algorithm outperformed greedy algorithm by approximately 8%

Cost Definition	Coverage Radius 1 (IMP %)			Coverage Radius >1 (IMP %)		
	MAX	MIN	AVE	MAX	MIN	AVE
Infrastructure Cost	3	1	1.4	25	1	10
Location Cost	3	0.5	1.2	25	0.8	5
Driving Cost	2	0.6	0.9	33	9	9

Table 4.2: Performance Improvement of Weighted greedy over greedy algorithm regarding solution nodes in three different cost definition scenarios

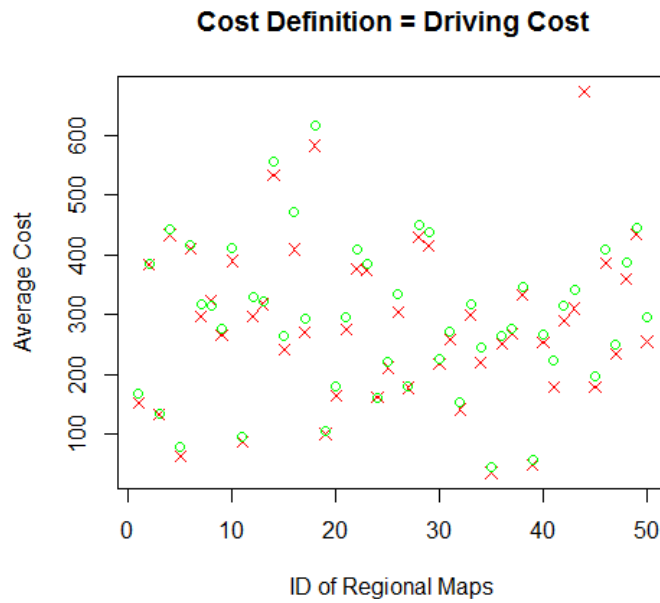


Fig 4.4: Cost difference of solution nodes under Driving Cost

x- Weighted Greedy Algorithm 0-Greedy Algorithm

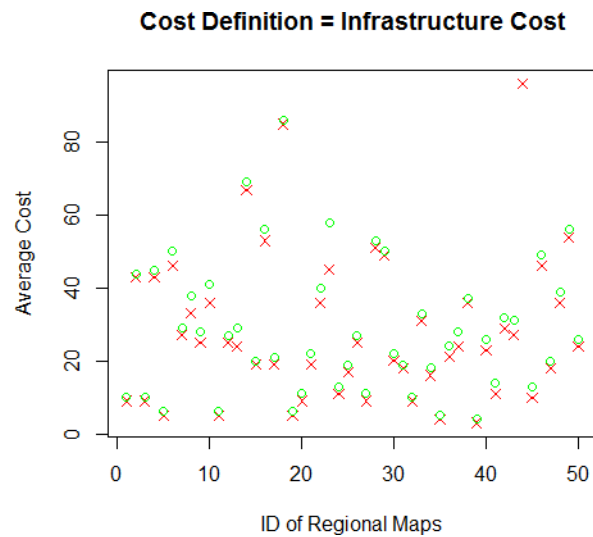


Fig 4.5: Cost difference of solution nodes under Infrastructure Cost

x- Weighted Greedy Algorithm 0-Greedy Algorithm

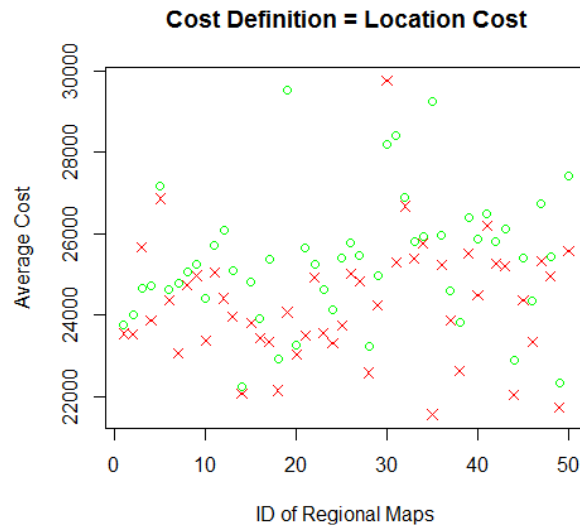


Fig 4.6: Cost difference of solution nodes under Location Cost

x- Weighted Greedy Algorithm 0-Greedy Algorithm

In the above figures, we can observe that in average results from greedy cost more than those of weighted greedy for all the cost definitions. This cost can correspond to location related cost, building cost of each facility etc. in different scenarios.

4. 4 Impact of data distribution

The only difference between the weighted greedy algorithm and a greedy algorithm is that $nw/cost$ is replaced by $new/cost$. The main idea is that newly covered rows should not be considered in the same way: there should be difference in covering different rows. If all rows are covered by the same number of columns, which means all node weights are the same, then the weighted greedy algorithm will be same as the greedy algorithm. In other words, if out degree of all the nodes is the same, then both algorithms work in the same manner. The cost saving can only be expected when we have different node

coverage degrees, i.e., some nodes have larger coverage degree than the others. The bigger the dispersion of node coverage degree is, the more improvement we achieved with the weighted greedy algorithm [34].

As we have shown our results on two different kinds of data with different coverage radius and different data distribution, we measure the improvement using the dispersion of node coverage degree. We will measure the improvement of the weighted greedy algorithm to the CV. To do so, we use the Pearson Product Moment Correlation Coefficient (PC). PC is used to measure the correlation between two variables X and Y. It gives a value between -1 to +1 where -1 means decreasing linear correlation and +1 means increasing linear correlation. Definition of PC is as follows:

It is defined as the product of covariance of the two variables divided by the product of their standard deviations.

$$\rho = \frac{\sum_{i=1}^n (X_i - \bar{X}) \times (Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^n (Y_i - \bar{Y})^2}} \quad (4.1)$$

The following graph shows the relationship between the CV and improvement of the weighted greedy algorithm over greedy algorithm for each regional map.

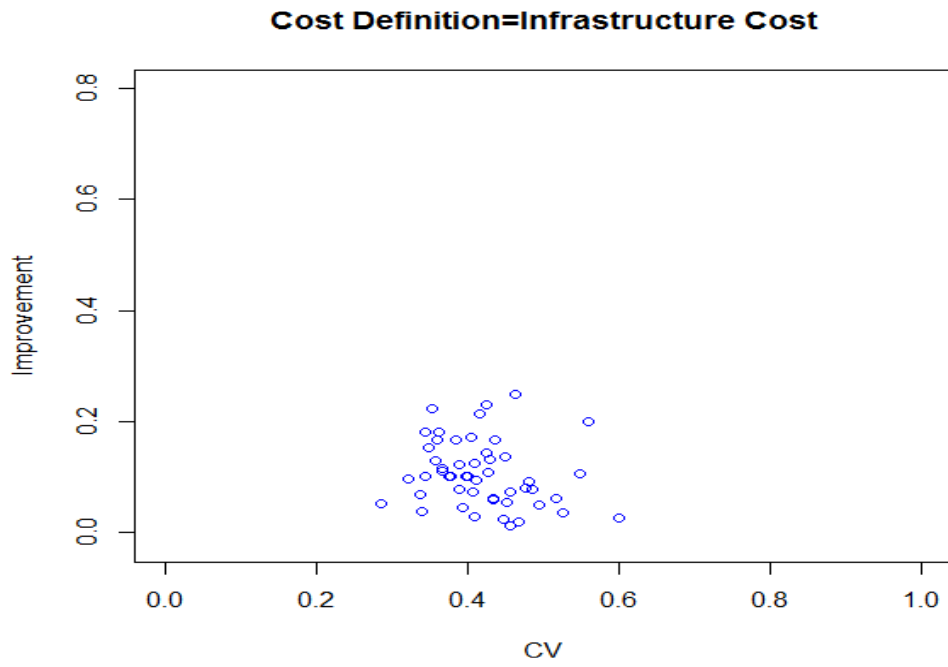


Fig 4.7: Relationship between CV and improvement on Infrastructure Cost regional maps

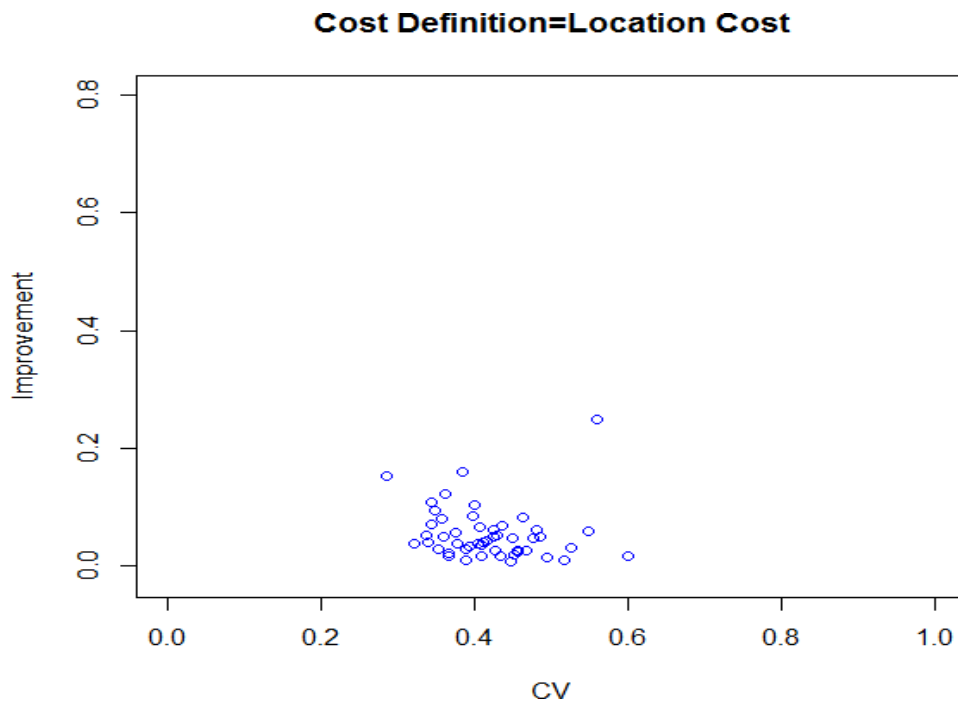


Fig 4.8: Relationship between CV and improvement on Location Cost regional maps

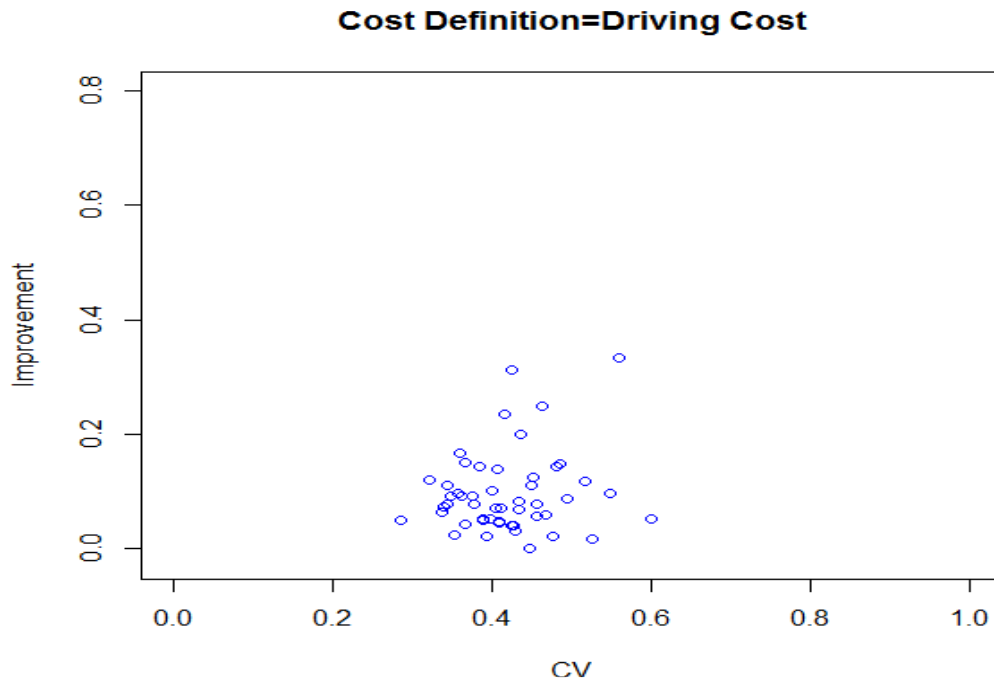


Fig 4.9: Relationship between CV and improvement on Driving Cost regional maps

Base on all the results for different cost definitions, the ρ of different cost definition results is as follows:

Cost Definition	P-value
Infrastructure Cost	0.19
Location Cost	0.49
Driving Cost	0.23

Table 4.3: P-value for different cost definitions

These positive values of ρ and the figures above tell us that there is a positive linear correlation with CV to the Node Coverage Degree. From all the above, we can conclude

that the improvement of the weighted greedy algorithm depends upon the dispersion of the degree of coverage. The more the dispersion is, the better the algorithm will perform.

CHAPTER 5

CONCLUSION & FUTURE WORK

5.1 Conclusion

In this thesis, we tested the weighted greedy algorithm in the field of resource allocation. We tested the algorithm with the traditional greedy algorithm with different cost definitions. The results show that it possesses the same properties as in web crawling by outperforming the greedy algorithm. The results from three cost definitions show that this algorithm can be used while considering the different cost definitions.

The weighted greedy algorithm was initially designed for web crawling, but the results from our work show that it can be efficiently used in other fields as well. In the thesis by Y. Wang [34], it was tested using the Beasley data where CV's fall within a specific range, but in our work, results for different CV range were produced using the real data. The results also showed the positive linear correlation between CV and the improvement of weighted greedy algorithm, same as in the web crawling setup.

The weighted greedy outperforms the greedy algorithm method not only regarding solution nodes but also regarding the cost as well. This application of cost-effectiveness of the weighted greedy algorithm can be handy in the field of resource allocation. Better planning techniques can be generated in the field of resource allocation using this algorithm. It can also come in handy when decisions are to be made focusing on least accessible areas because this algorithm tries to cover those areas first which can only be accessed by limited nodes.

5.2 Future Work

Allocation of resources is a big problem when we have limited number of resources. The weighted greedy algorithm showed promising results in our setup, but many things can be considered for future improvement.

Parallel processing of the operations of the algorithms can be considered to improve the speed and efficiency of the algorithm. We have run this algorithm in parallel with multiple inputs, and it performed reasonably well. In future, if parallel processing can be applied to internal operations of the algorithm, then it can be tested on bigger data sets.

Another aspect is to test it in other fields of Computer Science to check whether there are any other applications of this algorithm in other fields. There are various applications of set covering algorithms, and it can be tested in those applications to check whether it is generally applicable in all the fields or not. We can also build some better algorithms using the concept of this algorithm according to the required field.

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