

**IMAGE SEGMENTATION AND SHAPE ANALYSIS OF
BLOOD VESSELS WITH APPLICATIONS TO
CORONARY ATHEROSCLEROSIS**

A Thesis
Presented to
The Academic Faculty

by

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In Partial Fulfillment
of the Requirements for the Degree
Doctor of Philosophy in the
School of Biomedical Engineering

Georgia Institute of Technology
May 2007

IMAGE SEGMENTATION AND SHAPE ANALYSIS OF
BLOOD VESSELS WITH APPLICATIONS TO
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*To my parents Chen, Kairuan and Yang, Jisheng,
and my husband Tinghao.*

ACKNOWLEDGEMENTS

I would like to thank those who have been supporting me and helping me throughout my doctorate years.

First, I would like to thank my PhD advisors, Professor Don Giddens and Professor Allen Tannenbaum for your invaluable guidance throughout my study and research at Georgia Tech. It has been a privilege to be a student of yours, to learn from you and to be inspired by you. I am so grateful to have had such great advisors who not only have incredible foresight and view of the big picture, but also guided me through numerous technical details. I would like to thank my thesis reading committee, Professor Ray Vito, Professor Anthony Yezzi and Professor John Oshinski for your helpful comments and suggestions, which improved my thesis in many aspects. Thanks to Dr. Arthur Stillman for teaching me useful knowledge in medicine, sending me many real-world clinical data sets, and helping me with the validation of the algorithms.

Thank you to everyone who is currently in the Biomedical Imaging Lab and who have been here: Lei, Cecilia, Delphine, Eric, Marc, Yi, Yogesh, Patricio, John, Sam, Xavier, Ponnappan, Shawn, Jimi, Gallagher, Tauseef, Vandana, Eli, and Oleg; and everyone from the Cardiovascular Lab: Amanda, Suo Jin, Binjian, Stephanie, Massimiliano, Sungho and Annica. I have learned much from each and everyone of you, and it's always been a pleasure to spend time in the lab, attend group meetings, and share the knowledge and happiness with you.

I would also like to thank my intern supervisors, Gozde Unal at Siemens Corporate Research and Zhujiang Cao at Vital Images, for being great mentors to me and guiding me through two wonderful internship experiences. I have learned so much from you which I couldn't have learned at school.

To my dear husband Tinghao, your love and support have been keeping me warm at heart for so many years. I cherish all the memories we have had together, and I look forward to creating and sharing many more new memories with you.

Thanks to my parents and every family member in China, for supporting me unconditionally all the time. The distance across half of the earth will never separate you and me.

The last but not least, thanks to every Chinese friend I have met in the US, it's you who have made this place another home away from home.

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SUMMARY

Atherosclerosis is a systemic disease of the vessel wall that occurs in the aorta, carotid, coronary and peripheral arteries. Atherosclerotic plaques in coronary arteries may cause the narrowing (stenosis) or complete occlusion of the arteries and lead to serious results such as heart attacks and strokes. Medical imaging techniques such as X-ray angiography and computed tomography angiography (CTA) have greatly assisted the diagnosis of atherosclerosis in living patients. Analyzing and quantifying vessels in these images, however, is an extremely laborious and time consuming task if done manually. A novel image segmentation approach and a quantitative shape analysis approach are proposed to automatically isolate the coronary arteries and measure important parameters along the vessels.

The segmentation method is based on the active contour model using the level set formulation. Regional statistical information is incorporated in the framework through Bayesian pixel classification. A new conformal factor and an adaptive speed term are proposed to counter the problems of contour leakage and narrowed vessels resulting from the conventional geometric active contours. The proposed segmentation framework is tested and evaluated on a large amount of 2D and 3D, including synthetic and real 2D vessels, 2D non-vessel objects, and eighteen 3D clinical CTA datasets of coronary arteries.

The centerlines of the vessels are proposed to be extracted using harmonic skeletonization technique based on the level contour sets of the harmonic function, which is the solution of the Laplace equation on the triangulated surface of the segmented

vessels. The cross-sectional areas along the vessels can be measured while the centerline is being extracted. Local cross-sectional areas can be used as a direct indicator of stenosis for diagnosis. A comprehensive validation is performed by using digital phantoms and real CTA datasets.

This study provides the possibility of fully automatic analysis of coronary atherosclerosis from CTA images, and has the potential to be used in a real clinical setting along with a friendly user interface. Comparing to the manual segmentation which takes approximately an hour for a single dataset, the automatic approach on average takes less than five minutes to complete, and gives more consistent results across datasets.

CHAPTER I

INTRODUCTION

1.1 Atherosclerosis and Coronary Artery Diseases

Cardiovascular disease (CVD) is the most prevalent cause of death in the United States. Approximately 64,400,000 Americans have one or more types of CVD, and these account for approximately 40 percent of all deaths in the United States per year [1]. CVD includes high blood pressure, coronary heart disease (CHD), congestive heart failure, stroke, and congenital cardiovascular defects. Among these, CHD accounts for approximately 54 percent of deaths of CVD in the United States.

Atherosclerosis is a systemic disease of the vessel wall that occurs in the aorta, carotid, coronary and peripheral arteries [29]. Major consequences of atherosclerosis are myocardial infarction (heart attack), cerebral infarction (stroke), aortic aneurysms, and peripheral vascular disease (gangrene of the legs). Figure 1 and Figure 2 compare the main components of the vascular wall of a normal vessel and vessel with well-developed atheromatous plaque [47]. The most clearly defined layers of a vessel wall are: *intima*, *media*, and *adventitia*. In normal arteries, the intima consists of a single layer of endothelial cells, with minimal underlying sub-endothelial connective tissue. The intima and media are separated by a dense elastic membrane called the *internal elastic lamina*. The media layer consists mainly of smooth muscle cells, and is separated from the adventitia by the *external elastic lamina*. Atherosclerosis is characterized by intimal lesions called atheromas, or atheromatous or fibrofatty plaques, that protrude into and obstruct vascular lumina, weaken the underlying media, and may undergo serious complications. The key processes in atherosclerosis are intimal thickening and lipid accumulation. An atherosclerotic plaque consists of a

raised focal lesion initiating within the intima, having a lipid core and covered by a firm fibrous cap, as shown in Figure 2.

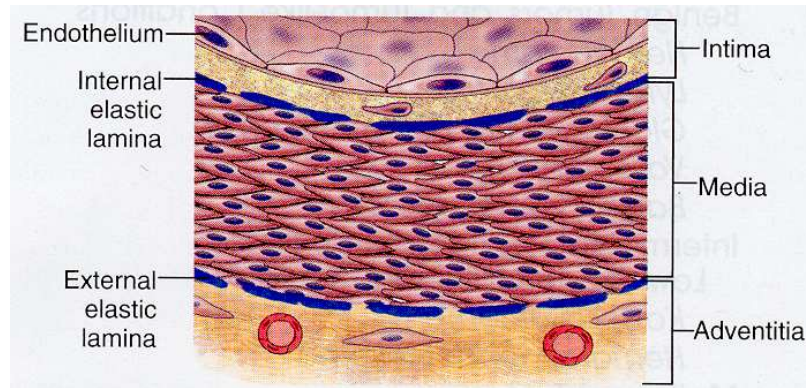


Figure 1: Schematic representation of the major components of a normal vascular wall [47].

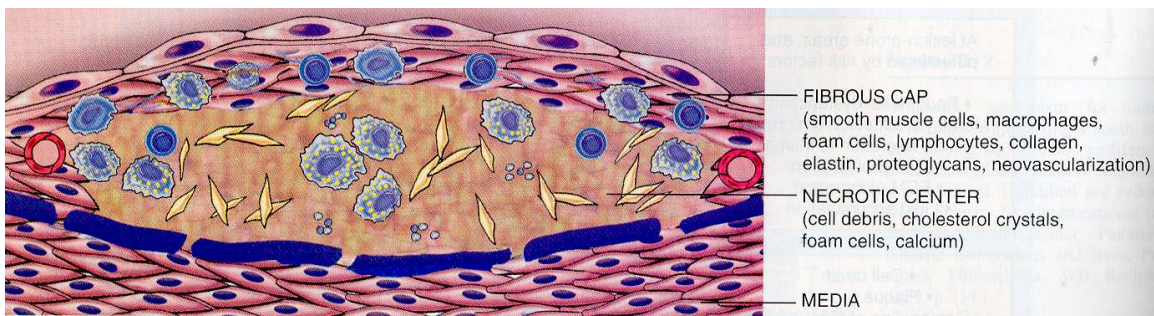


Figure 2: Schematic representation of the major components of a well-developed atherosclerotic plaque [47].

Atherosclerotic lesions usually involve the arterial wall only partially around its circumference and are patchy and variable along the vessel length. Plaques generally continue to change and enlarge; focal and sparsely distributed lesions may become more and more numerous and diffuse as the disease advances. Moreover, atherosclerotic plaques often undergo calcification. Figure 3 illustrates the histology of a vessel cross section showing the typical features of an advanced plaque in the coronary artery. The advanced lesion of atherosclerosis may lead to further pathologic changes

including focal rupture, ulceration or erosion, hemorrhage into a plaque, superimposed thrombosis, and aneurysmal dilation.

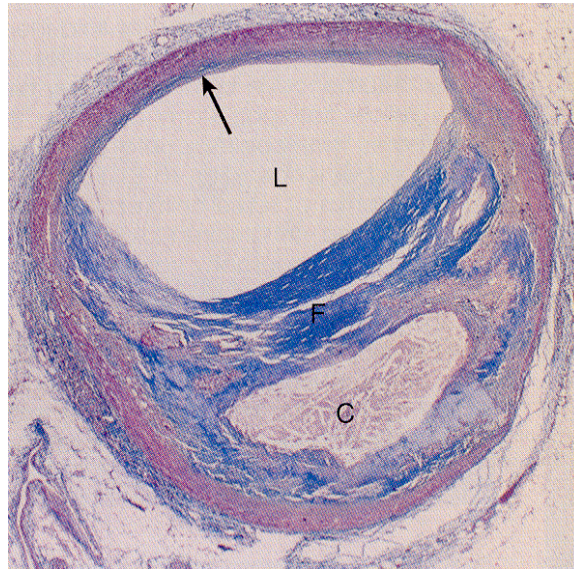


Figure 3: Histological features of an atherosclerotic plaque in a coronary artery [47]. L - lumen, F - fibrous cap, C - central lipid core, arrow - plaque-free segment of the vessel wall.

Coronary arteries are arteries supplying blood to the myocardium (heart muscle) [72]. In general, there are two main coronary arteries, the left coronary artery (LCA) and right coronary artery (RCA), both of which originate from the root of the aorta, immediately above the aortic valve (Figure 4 and Figure 5). For the LCA, the segment between the aorta and the first bifurcation is known as the left main (LM) coronary artery. The LM typically bifurcates into the anterior interventricular (left anterior descending - LAD) artery and the left circumflex (LCX) artery. The RCA normally branches into right marginal and posterior interventricular branch, and in 55% hearts sinuatrial nodal artery. In 45% of hearts the sinuatrial nodal artery arises from the LCA [59]. The exact anatomy of the coronary arteries varies considerably from person to person. Some typical variations and their anatomy can be found in [62].

The coronary artery is one of the vessel types that are extensively involved with

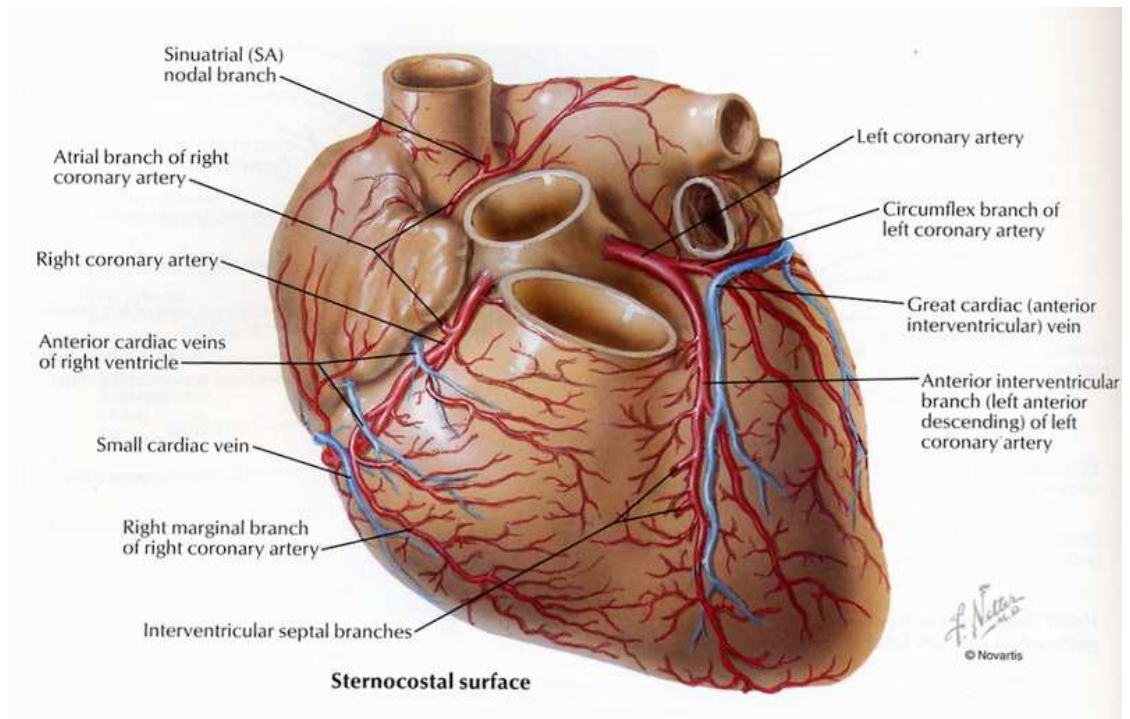


Figure 4: Illustrated anatomy of human coronary arteries and cardiac veins [62].

atherosclerosis. Hence, atherosclerosis is one of the main causes of CHD. Atherosclerotic plaques in coronary arteries may cause stenosis or complete occlusion of the arteries and lead to serious results such as angina pectoris and myocardial infarction. As reported by the American Heart Association [1], in 2006 an estimated 1,200,000 Americans will have a new or recurrent coronary attack, of which 700,000 will have a new coronary attack. It is estimated that an additional 175,000 silent first heart attacks occur each year. It is essential to be able to detect and diagnose atherosclerosis in coronary arteries at its early stage of development, and to apply according treatments using medications or surgical procedures such as diagnostic cardiac catheterization, angioplasty procedures, stent implantation and bypass procedures in order to prevent or delay the serious consequences listed above.

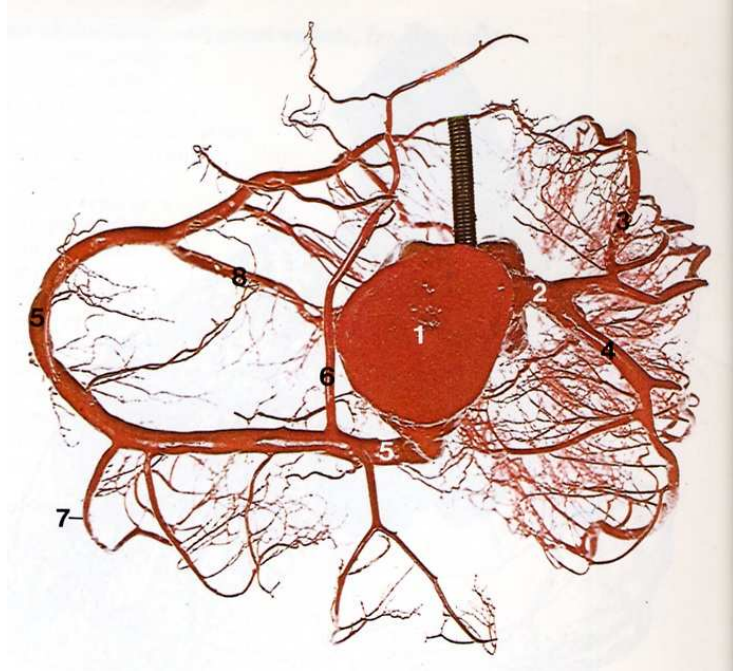


Figure 5: Cast of human coronary arteries viewed from top [59]. 1. Ascending aorta, 2. Left coronary artery, 3. Circumflex branch, 4. Anterior interventricular branch (anterior descending artery), 5. Right coronary artery, 6. Sinuatrial nodal artery, 7. Marginal branch, 8. Posterior interventricular branch.

1.2 Medical Imaging in Assisting the Diagnosis of Coronary Artery Diseases

The use of imaging techniques in cardiac applications has grown immensely in recent years. For coronary artery imaging, the methods can be divided into two categories: invasive imaging and noninvasive imaging [23, 24].

Invasive imaging mainly includes X-ray angiography, intravascular ultrasound (IVUS) and optical coherent tomography (OCT), which are all catheter-based imaging techniques with contrast agents or imaging sensors carried to the desired location inside the vessel by a catheter. Figure 6 shows an example image obtained using X-ray angiography. An X-ray angiography image like this reflects luminal diameter and provides a measure of stenosis with good resolution, and has been the gold standard for diagnosis of coronary lesions for many years. The intrinsic limitation of X-ray

angiography, however, is the ability to acquire only two-dimensional (2D) projections of the vessels, which are indeed three-dimensional (3D) anatomical structures. As a result, the stenosis or lesion may be underestimated by the 2D X-ray angiography images, and the exact 3D geometry of the coronaries can not be recovered from a single 2D image. To overcome the limitations and enable 3D reconstruction of the vessels, several variations of X-ray angiography have been developed. Cineangiograms can be generated from different angles of X-ray projection as well as different time points, so 3D dynamic structures of the coronaries can be reconstructed from these series of 2D images using projective reconstruction techniques. A rotational X-ray angiography system can acquire angiograms at all angles by performing a continuous rotation of a C-arm X-ray emission and detection system. In this way, a complete series of images is obtained in a range of projections, and the images can be re-sampled and reconstructed to create a 3D volume to emulate a computed tomography (CT) scan. However, due to the rotational nature of this imaging technique, the spacial resolution varies from the center of the image volume to the outer field, sometimes bringing trouble for the reconstruction of larger field of views (FOV), and the image quality is usually inferior to a real CT scan.

Catheter-based IVUS and OCT are relatively new techniques to arterial vascular wall imaging. These invasive imaging modalities allow direct and real-time imaging of atherosclerotic plaques and provide a cross-sectional view of the lumen and vessel wall. They both acquire images by carrying an imaging sensor at the tip of the catheter to the desired location and collecting signals from reflected ultrasound beams (for IVUS) or laser beams (for OCT). Figure 7 compares images of the same vessel at the same location, imaged by both OCT (A) and IVUS (B). It can be seen that a calcified plaque at 8-9 o'clock is revealed in both OCT and IVUS images. OCT sometimes is capable of revealing more structures in the vessel wall than IVUS, since some structures are echo-lucent in the ultrasound field. It is also evident that OCT

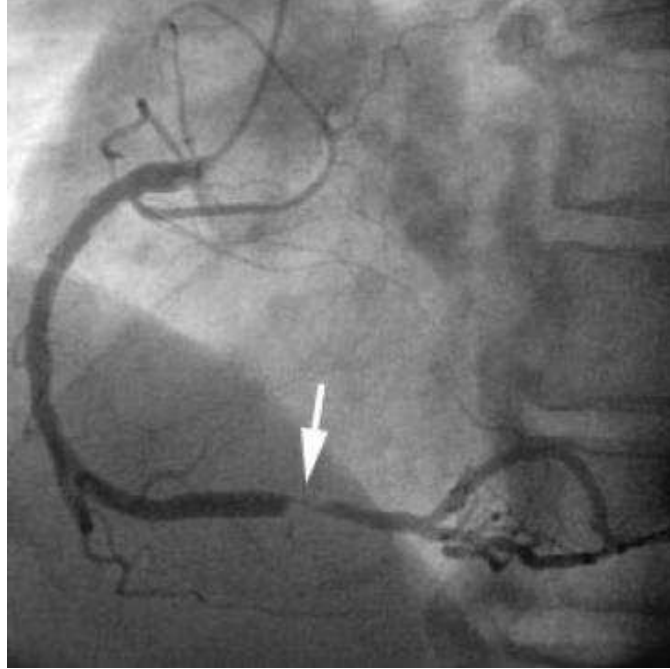


Figure 6: A typical X-ray angiography of the right coronary artery, arrow showing a severe narrowing of the distal segment [88].

has much higher spacial resolution (as high as $10 \mu\text{m}$) than IVUS (usually around $100 \mu\text{m}$). However, OCT suffers from lower penetration, since laser beams attenuate very quickly in the vessel wall. For more comparisons between IVUS and OCT, OCT and histology, see [40] and [98] and the references therein.

Among all imaging modalities for coronary arteries, IVUS and OCT are currently the most capable in imaging the vessel wall. Different layers of the wall and atherosclerotic plaque constituents can usually be seen in images acquired by these two imaging modalities. The main limitation of these modalities is the fact that real 3D geometry can hardly be recovered from these cross-sectional images if the pull-off trajectory of the catheter is not provided by other imaging methods, such as X-ray angiography. In addition, IVUS and OCT are normally applied to a short segment of the vessel to minimize complications in the catheterization procedure, and it is almost impossible to image every branch of the coronary tree in order to recover the complete shape,

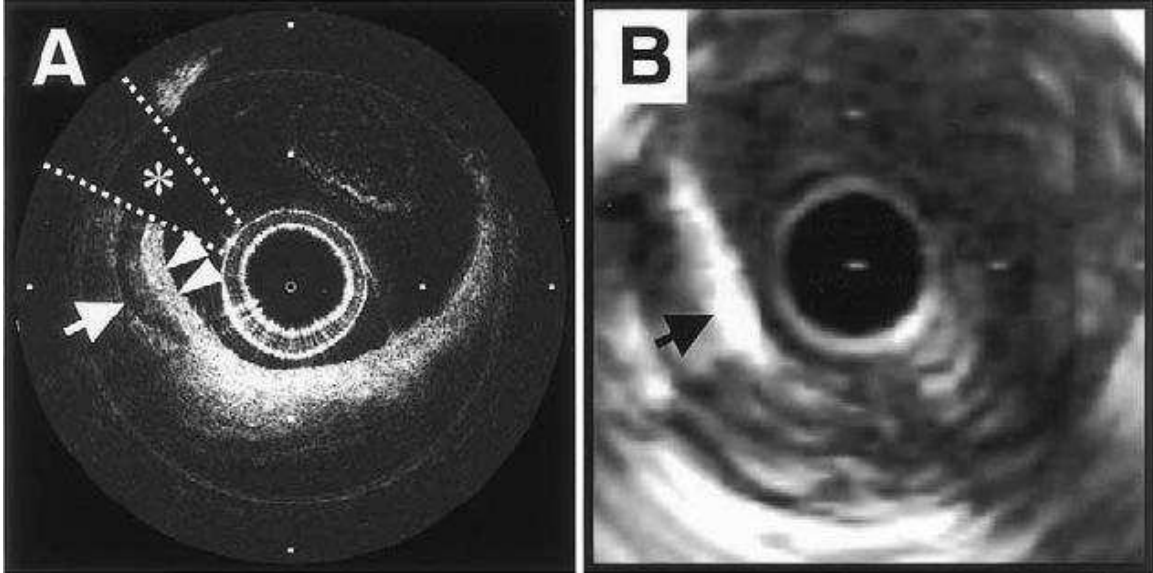


Figure 7: OCT (A) and IVUS (B) images of a coronary artery cross-section. Single arrow in both images indicates a calcified plaque with low intensities in OCT and high intensities in IVUS. Two arrowheads in the OCT image indicate a high intensity region showing a fibrous band overlying the calcification, which is obscured in the IVUS image. The borders of the guide wire artifact (*) are marked by dotted lines in (A) [40].

even when the pull-off trajectories are available.

Although catheter-based imaging approaches can acquire coronary images with quite good image quality and imaging speed, the main drawback of the above techniques is bringing complicated clinical procedures and risks to the patient because of their invasiveness. It is acceptable if the imaging procedure takes place at the same time with a catheter-based treatment procedure, however the invasive imaging techniques are not suitable for observational or routine follow up examinations performed in the same patient on a regular basis.

With the development of engineering technology, noninvasive imaging modalities have become more and more attractive, and more frequently used in clinical settings. Among the noninvasive imaging modalities, computed tomography angiography (CTA) is the most widely used for patients at present, and magnetic resonance imaging (MRI) is currently more preferable for conducting advanced research and

studies. Other than the apparent advantage of being noninvasive, these techniques also provide information of the whole 3D volume rather than 2D projections in the conventional X-ray angiography, or 2D vessel cross-sections in IVUS and OCT.

CTA has been used in various clinical applications including cardiac, head and neck, abdomen, and extremities with a spacial resolution of under 0.5 mm in all three dimensions. The imaging contrast agent is delivered intravenously instead of carried by a catheter to the desired imaging location, which makes the imaging procedure much less invasive. For coronary imaging, CTA is especially good at revealing the blood pool and calcified plaques, which both have high intensities in the images, calcium being higher. Soft plaques can sometimes be observed as well, if the image quality is sufficiently high. Figure 8 shows the same RCA as in Figure 6, imaged using CTA. The 3D volumetric image is re-sampled using the multi-planar reformatting (MPR) technique in order to show the entire vessel on a 2D image. It can be seen that the stenosis at the distal end of this RCA is clearly shown with similar image quality as in the X-ray angiography.

In addition, CTA revealed more information about the plaque as shown in the high intensity region right below the stenosis in Figure 8, which is possibly a ulcerated cavity in the vessel wall [88]. The CTA image also shows calcium deposits in the proximal region which can not be seen in the X-ray angiography. This case indicates that CTA has the ability of non-invasively imaging not only the lumen *in vivo* as well as X-ray angiography, but sometimes with even more information of the vascular wall. Another advantage of CTA is the ability to show cross-sections of the vessel as in IVUS and OCT. Given the center point of the vessel at a certain location and the tangential direction of the centerline (either specified manually or extracted automatically), the 3D CTA data can be re-sampled on the plane defined by the center point and the direction vector. The resolution is usually not as high as intravascular OCT or IVUS, however CTA is still superior to X-ray angiography in this respect.

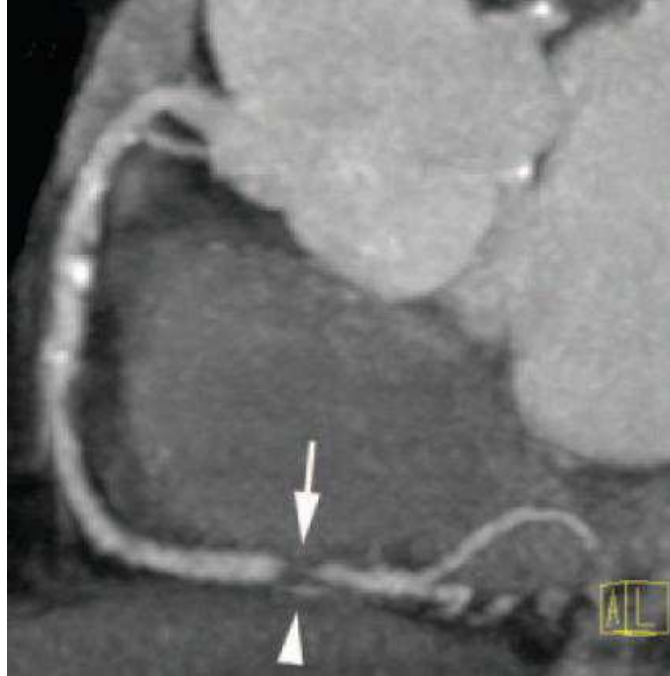


Figure 8: Same RCA as in Figure 6 imaged with a 64 multi-slice CT scanner [88]. The arrow points to the distal end stenosis which was also detected by X-ray angiography. Arrowhead points to an additional high intensity region parallel to the lumen, which could represent an ulcerated cavity. Several calcium deposits in the proximal side are also shown in this image which were not detected by X-ray angiography.

Multi-phase CTA of coronary arteries is also of great interest in recent years. CTA is performed at different time points throughout the cardiac cycle, which enables radiologists to select the best phase for the diagnosis of each individual coronary branch. Multi-phase CTA also has the potential of showing a full 4D (3D geometry plus time) view of the heart along with all coronary arteries if all CTA images of all phases are available.

Magnetic resonance angiography (MRA) is another popular non-invasive imaging technique for blood vessels. The blood pool can appear either black or white when using different imaging protocols. However, the spatial resolution of MRA is usually not as high as CTA, especially for resolution in between slices (sometimes referred to as “slice thickness”). Hence, MRA is more often used for large scale vessels such

as the aorta or large vessels in the brain. *In vivo* imaging of coronary arteries using MRA is still being investigated and is not widely used clinically for the time being.

Digital subtraction angiography (DSA) is a computational technique to better visualize blood vessels by subtracting a non-contrast image (either an MRI or a CT) from a contrast-enhanced image. This technique suppresses the surrounding bones and tissues significantly and the resulting image is usually nice and clean. However DSA normally can not be easily applied to coronary artery imaging for the following reasons. First, DSA requires two sets of images: non-contrast and contrast, which means doubling the radiation dose for CT imaging. Second, DSA requires perfect alignment of the two sets of images in order to subtract one from another. Coronaries are moving structures and it is very hard to acquire perfectly aligned data even if the coronaries are imaged at the same time point during the cardiac cycle. Hence, DSA is most widely used in head and neck MRA imaging, where motion is minimal and there is no X-ray radiation. DSA is not used commonly in CTA, although it is a very attractive technique that can reduce much of the image post processing work.

CTA is the imaging modality of interest in this thesis for its various advantages listed above, and also for the reason that with the 3D volumetric data at hand, image processing and analysis have become more important as compared to the 2D case. The growing number of the images in a single dataset has made viewing images slice by slice an extremely time consuming task for radiologists. It is also desirable that different body organs be visualized and studied separately, instead of displayed with many irrelevant surrounding organs. This is where image segmentation and 3D visualization come into play to provide more possibilities to explore the data extensively so that physicians can perform diagnoses and treatments more accurately and more efficiently.

There are many image segmentation algorithms proposed in the literature, as will be reviewed in more detail in Chapter 2, and some have become standard and have

been described in textbooks [30, 81]. The algorithms vary from the simplest thresholding and edge detection techniques, to more complicated region-based models and active contour models. The problem of image segmentation, however, continues to be an active research field because there is no single framework that fits all applications and meets all requirements. In medical applications, segmentation algorithms need to be accurate to avoid mistakes as much as possible; they need to be reasonably fast; and they also need to be able to effectively separate the interested organs from the other parts of the images. To meet these requirements, an efficient and accurate segmentation algorithm is needed for the task of coronary artery segmentation, which becomes one of the major topics of this thesis.

After the image segmentation is done, several useful tasks can be conducted in addition. The most straightforward would be the surface rendering [33] of the 3D object that has been segmented. By using computer visualization techniques, a 3D surface can be generated and displayed on the 2D computer screen. This also allows users to zoom and rotate in order to observe the object from different perspectives. Shape analysis is an equally important task, especially for complicated structures such as blood vessels. In this thesis, a centerline extraction (also referred to as skeletonization process) approach is proposed to trace the center axis of the segmented and triangulated surface of the vessel, and a method to measure local cross-sectional areas is also proposed for the purpose of quantitative analysis and stenosis detection.

Other applications of 3D segmentation of coronary arteries include generating patient specific geometric boundary conditions for computational fluid dynamic (CFD) simulation of blood flow and study of the relation between the flow patterns and atherosclerotic plaque distribution along the vessel wall [83]. Some cases studied in the thesis have been used to conduct CFD simulations and compared to clinical observations [84]. The detailed formulation of CFD, however, is beyond the scope of this thesis.

1.3 Organization of the Thesis

In the next chapters, we will fully explore the problem of CTA coronary image analysis. In Chapter 2, we start by reviewing the existing image segmentation and vessel analysis methods in the literature followed by the discussion of their advantages and limitations. In Chapter 3 we propose a general image segmentation framework which has the potential to be used for segmenting blood vessels, and in Chapter 4 we apply the proposed algorithm to extract coronary arteries from CTA images. The segmentation process is made fully automatic with the assistance of a automatic heart segmentation method and a Hessian-based vessel filtering technique. We also look at the problem of identifying and segmenting calcified plaques from the images. In Chapter 5 we will present a centerline extraction approach based on the segmented surface of tubular structures, which we call the harmonic skeletonization approach. As we search for the centerlines, we also measure cross-sectional areas of the coronary arteries, which provide a good reference for stenosis detection and evaluation. The final chapter (Chapter 6) concludes the thesis and discusses several possible future directions.

CHAPTER II

BACKGROUND: MEDICAL IMAGE SEGMENTATION AND 3D VESSEL IMAGE ANALYSIS

2.1 Medical Image Segmentation Methods – A Brief Review

Image segmentation algorithms for the delineation of anatomical structures and other regions of interest are becoming increasingly important in assisting and automating specific radiological tasks. These algorithms play a vital role in numerous biomedical imaging applications, such as quantification of tissue volumes, diagnosis and localization of pathology, study of anatomical structures, treatment planning, and computer-guided surgery [70].

2.1.1 Definition of Image Segmentation

Classically, image segmentation is defined as the partitioning of an image into non-overlapping, constituent regions that are homogeneous with respect to some characteristic such as intensity or texture [30, 34, 68]. If the domain of the image is given by Ω , then the segmentation problem is to determine the sets $S_k \subset \Omega$, whose union is the entire domain Ω . Thus, the sets that make up a segmentation must satisfy:

$$\Omega = \bigcup_{k=1}^K S_k \quad (1)$$

where $S_k \cap S_j = \phi$ (a null set) for $k \neq j$, and each S_k is connected. Ideally, a segmentation method finds those sets that correspond to distinct anatomical structures or regions of interest in the image.

Pixel segmentation, rather than classical segmentation, is often a desirable goal

in medical images, particularly when disconnected regions belong to the same tissue class. When the constraint that regions must be connected is removed from the classical segmentation, determining the sets S_k is called pixel classification, and the sets themselves are called classes. Determining the total number of classes K can be a difficult problem [48]. Usually, the value of K is assumed to be known based on prior knowledge of the anatomy being considered. For example, in the segmentation of cardiac images, we assume that $K = 3$, corresponding to blood-filled region, myocardium region, and lung region [100].

The commonly used image segmentation methods include: thresholding, region growing, classifiers, clustering, Markov random field (MRF) models, artificial neural networks, deformable models and atlas-guided approaches. Several of these techniques are often used in conjunction for solving different segmentation problems. Here we only review those which are closely related to this thesis. Other methods can be found in the surveys of image segmentation in literature [6, 17, 70].

2.1.2 Thresholding and Region Growing

Thresholding approaches segment scalar images by creating a binary partitioning of the image intensities. It is a simple yet often effective method for obtaining a segmentation of images in which different structures have contrasting intensities. Thresholding is usually used as an initial step in a sequence of image processing operations. Its main limitation is that typically it does not take into account the spatial characteristics of an image. This causes it to be sensitive to noise and intensity inhomogeneities, which often occur in medical images. Variations on classical thresholding have been proposed to incorporate information based on local intensities and connectivity. A survey of thresholding techniques can be found in [76].

Region growing is a technique that extracts connected regions based on certain criteria such as image intensity and/or edges. A seed is needed to be placed inside

the desired region to extract all the connected pixels according to the criteria. Like thresholding, the simplest form of region growing can be sensitive to noise, and it requires the manual placement of seeds in every region to be segmented. Region growing is seldom used alone but usually combined with other segmentation techniques to delineate small, simple structures such as tumors and lesions [70].

2.1.3 Classifiers and Clustering Methods

Classifiers and clustering methods are pattern recognition techniques that apply to image segmentation problems. Classifiers are known as supervised methods because they require training data, and clustering algorithms are termed unsupervised because they perform classification of the data without the use of training data.

Classifier methods seek to partition a feature space (usually image intensities) by using training data. There are a number of ways in which the training data can be applied. The commonly used nonparametric classifiers include k -nearest neighbor (kNN) and Parzen window; a parametric classifier is usually the maximum-likelihood or Bayes classifier [21]. It is assumed that the pixel intensities are independent samples from a mixture of probability distributions, usually Gaussian for CT and MRI images. The estimation of the means, covariances, and mixing coefficients of the K classes is also needed. Being non-iterative, classifiers are relatively computationally efficient, and they can be applied to multichannel images. The disadvantage is the requirement of manual interaction to obtain training data, which can be laborious. If a same set of training data were used for a large number of images, biased results could be obtained.

Clustering algorithms, on the other hand, do not need training data. But to compensate for this, they iteratively alternate between segmenting the image and characterizing the properties of each class. Three commonly used clustering algorithms are the K -means algorithm, the fuzzy c -means algorithm, and the expectation-maximization (EM) algorithm.

Classifiers and clustering methods do not directly incorporate spatial modeling and can be sensitive to noise. This lack of spatial modeling, however, can provide advantages for fast computation. The use of MRF models [73] can improve the robustness to noise of these algorithms.

2.1.4 Active Contour Models

Active contour models, also called deformable models [92] or “snakes” [41], are physically motivated techniques for segmenting objects using closed parametric curves or surfaces that deform under the influence of internal and external forces. The internal forces serve to impose a smoothing constraint. The external or image forces push the active contour to move toward salient image features like lines and edges. A closed curve or surface is needed to be placed near the desired boundary and then allowed to undergo an iterative relaxation process to delineate the object. Figure 9 shows an example of using a 2D active contour to segment a CT cardiac image. In Figure 9 (a), an initial contour was placed inside the heart chamber, and in Figure 9 (b), the active contour has deformed to fit the boundary of the heart chamber.

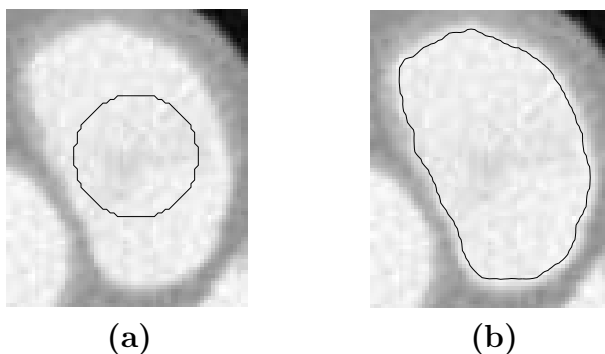


Figure 9: Extraction of the inner boundary of a CT cardiac image. (a) Initial contour. (b) Final contour that segments the heart chamber.

Active contour models have been widely applied in the segmentation of medical images, either alone or incorporated with other image segmentation approaches. They have been used to segment cerebral cortex MR images [107], heart MR images [104],

bone CT images [50], and more. The main advantage of active contours is their ability to incorporate the smoothness of the contours and image features at the same time. The internal forces make the contours robust to noise and spurious edges.

An important extension of active contour models is the use of implicit level-set representation [54, 85] rather than explicit parameterization in order to handle topology changes. A summary of geometric level-set analogues for parametric active contours can be found in [97], and a general review on deformable models in medical image analysis can be found in [56].

Earlier active contour techniques mostly adopted image intensity gradient as the external force in the segmentation model. This type of approach is often referred to as edge-based or gradient-based methods. Another type of technique utilizes region statistical information such as the mean and variance of the intensity of different regions separated by the active contour, and achieves the segmentation by seeking a maximum separation of certain regional measures. This type of approach is also referred to as a region-based technique. Some representative works can be found in Chan and Vese [14], Yezzi [105], and Zhu and Yuille [111].

2.1.5 Combination of Image Segmentation Methods

Due to the complexity of medical images, a single segmentation method usually can not achieve a good result for desired segmentation objectives. Thus, a combination of different approaches is usually adopted. There is a huge literature of various types of medical applications, and here we only list a few examples of combining different methods for the purpose of segmentation. Baillard *et al.* [7] combined Bayesian pixel classification and active contour models in a level set formulation to segment brain structures from MRI images. Posterior probabilities calculated from the Bayesian classification drive the implicit surface to evolve and capture the boundary of gray matter and white matter of the brain. Pichon *et al.* [69] combined statistics of pixel

intensity and a region growing method, and a employed fast marching method [80] to calculate the arrival time of the growing front. The user determines a time t_0 to pick the best region that represents the desired object. Leventon *et al.* [50] incorporate shape prior information to the level set segmentation framework based on a set of previously segmented data. The shape constraint was defined based on dimensionality reduction techniques on the distance transform of pre-segmented shapes. This method is especially efficient for medical structures that do not vary too much from patient to patient.

The above methods are all general segmentation frameworks which are not specifically designed for blood vessels. In the next section, we will review segmentation methods proposed for blood vessel segmentation and examine some of the specific considerations for this application.

2.2 Previous Work on 3D Vessel Image Analysis

Segmentation makes up a great portion of the 3D vessel image analysis problem, however it is not the sole topic of interest. In fact, the segmentation problem for vessels is largely blended with other problems, such as automatic enhancement and detection, centerline extraction and advanced visualization. Several of these problems are often investigated together to explore the original image fully and perform automatic extraction of significant information as much as possible.

From the perspective of specific applications, many excellent works have been focused on vessel analysis in MRA images, especially cerebral MRA. There is also a special interest recently in analyzing retinal images to extract vessels in the eye [60, 82], where the input images are typically 2D images generated using optical imaging methods. For coronary artery image analysis, most works have been performed on X-ray angiography images due to the availability of this imaging modality for many years. CTA is relatively new for coronary imaging and not much previous work has

been seen in the literature. We will explore this problem extensively in the following chapters of this thesis.

In this section, we first review some methods for enhancing vessel images to better present and visualize the original image. These techniques can also serve as pre-processing steps for further analysis such as automatic segmentation. We then review some general vessel extraction and analysis approaches, with a special focus on 3D applications. After that, we specifically look at vessel analysis studies which have been done on CTA data. Finally, we review important works on coronary artery image processing, which are mainly performed on X-ray angiography. For a comprehensive review of vessel extraction techniques presented in the literature before the year of 2003, see [43] and the references therein. It can also be seen from the tables comparing the performance of different approaches listed in [43] that the use of CTA as an input type is far less than the use of X-ray angiography, MRA and DSA.

2.2.1 Enhancement of Curvilinear Structures

Anisotropic diffusion has been used to smooth and enhance blood vessels in 3D images [44, 45]. The multi-directional diffusion flux is decomposed in an orthogonal basis, which enhances the iso-level contours of the image as well as diffuses along the contours. The method was tested on CT liver images in both MIP (maximum intensity projection) view and iso-surfaces (Figure 10). The noise in the image was significantly suppressed after the diffusion, and details of small vessels are better preserved than using a Gaussian isotropic smoothing filter.

Another type of vessel enhancement technique is based on the Hessian analysis of the Gaussian smoothed image, specifically the eigenvalues of the Hessian matrix. Sato *et al.* [77] identified blood vessels as 3D curvilinear structures that can be enhanced by a 3D multi-scale Hessian-based filter. The filter response can be used to visualize the vessels through isosurface extraction. The multi-scale property enables the filter to

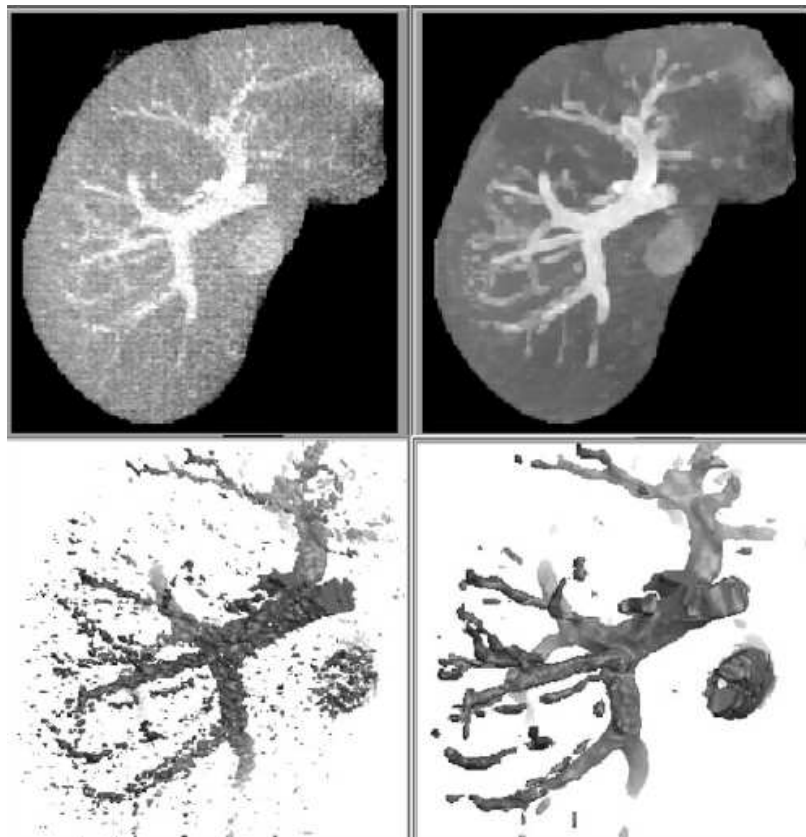


Figure 10: Enhancement of CT liver images using anisotropic diffusion. Upper: MIP views of the liver before (left) and after (right) diffusion; Lower: Iso-surfaces of the vessels before (left) and after (right) diffusion [44].

respond to different sized vessels. The algorithm is presented on a variety of medical datasets, including brain MRI, MRA, lung CT and liver CT images with excellent results by comparing the volume rendering obtained before and after filtering (see Figure 11 for an example).

Frangi *et al.* [28] proposed a vesselness measure using the eigenvalues of the Hessian matrix that effectively distinguishes the line-like structure from blob-like and plate-like structures and also suppresses random noise in the background. A multi-scale method is also employed here to adapt to different vessel sizes. The method was run on both 2D and 3D angiography images, showing a nice suppression of the background.

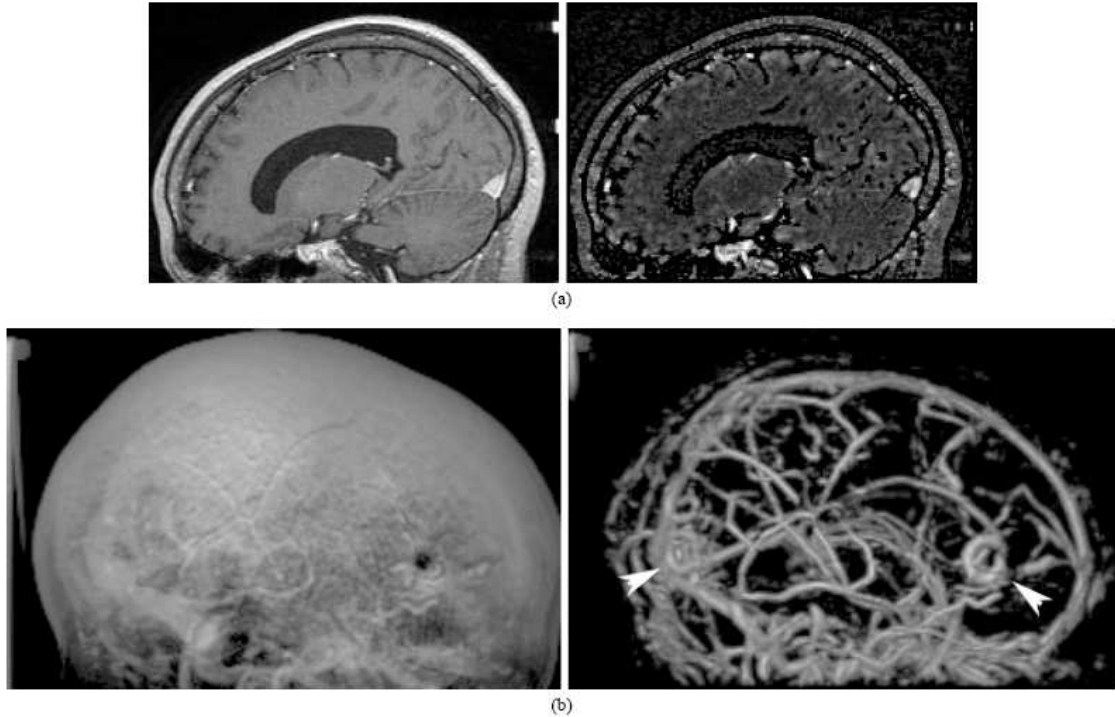


Figure 11: Hessian-based enhancement of brain MRI images. (a) A slice of the input original image (left) and filtered image (right). (b) Volume-rendered images of the input original (left), and filtered images (right). The filter gave high responses to the vessel structures [77].

Vessel enhancement techniques can be useful and helpful not only for better MIP and iso-surface visualization, but for initiating and assisting segmentation as well. In Chapter 4, we will employ the Hessian-based vessel filtering technique to initiate our coronary segmentation process.

2.2.2 General Vessel Extraction and Analysis Approaches

Earlier work by Verdonck *et al.* [93] and Wink *et al.* [94] used an iterative method to find the center axis and vessel boundaries alternately. The 3D data were re-sampled perpendicularly to the the axis and within the re-sampled 2D slices, vessel boundaries were located by detecting high gradients of the image intensity. The segmentation, however, is not accurate enough since it is only based on local gradients, which are sensitive to noise and the threshold chosen.

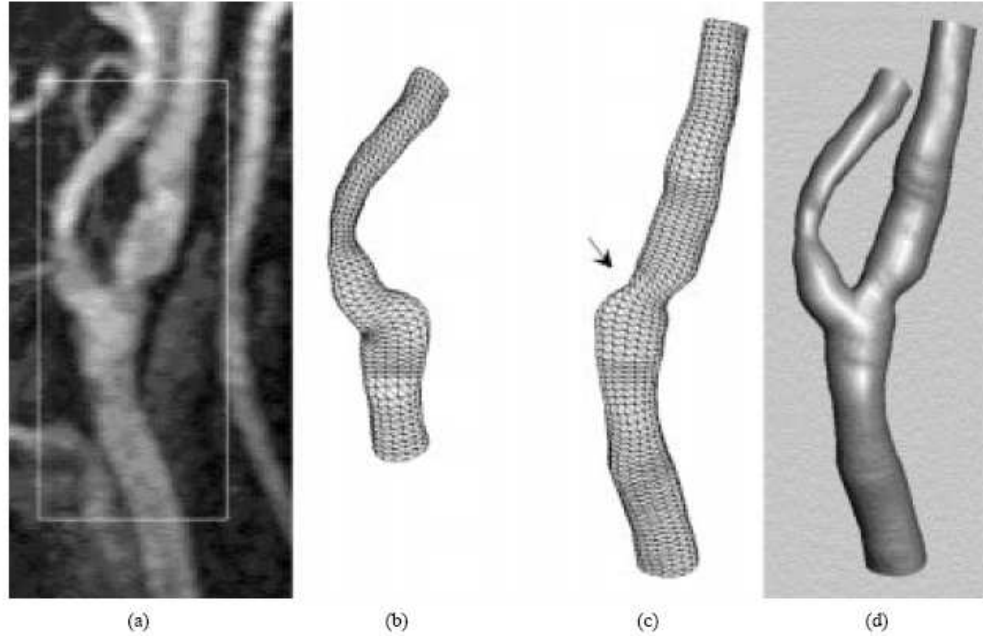


Figure 12: Reconstruction of the vessel surface using a tubular deformable model from contrast enhanced MRA images [106]. (a) Original image of a carotid artery. (b) Reconstructed branch of the external carotid artery (ECA). (c) Reconstructed branch of the internal carotid artery (ICA). (d) The ECA and ICA are merged into a complete carotid model.

Yim *et al.* [106] employed tubular deformable model to reconstruct the vessel surface from MRA images. The surface deforming process is carried on within a tubular coordinate system, thus giving a convenient measure of the cross-sectional area of the vessels. Re-parametrization and vertex merging are needed to avoid problems of self-intersection of the surface. In addition, this method only models single branches of the vessels, so in the case of bifurcation, two branches are needed to be merged to form a Y-shaped structure (Figure 12).

Riedel *et al.* [74] also employed discrete deformable models to segment vessel surfaces from *in vitro* micro-CT coronary artery images. T-snakes (topology adaptive snakes) [57] were used to adapt to the complicated shape of the vessels. The segmentation problem in this work is simpler in that micro-CT gives very high resolution images, and *in vitro* imaging isolates the vessels from other surrounding objects that

usually bring difficulties to the segmentation.

The generalized cylinder model is also adopted by Worz *et al.* [96], where a parametric intensity model is proposed to deal with scale variance in vessel sizes. This work models the cross-sections of the vessels as circles, which sometimes is not true for diseased vessels. Also, there is no constraint between different levels of circles, leading to non-smoothness in the longitudinal direction.

Other model-based methods include [27, 46], where the Hessian enhancement technique is employed in both works. In [46], the vessel is modeled as a cylindrical shape with a series of center points and elliptical cross-sections. In [27], a linear vessel segment defined by two user-defined end points is modeled with a central axis curve coupled with a vessel wall surface. Model-based methods simplify the vessel extraction and representation problem by fitting the shape of the vessel to a certain geometric model, and can be fast and intuitive. However, the model usually has limitations in representing all possible shapes, such as bifurcations and irregular cross-sections, which is often the case for diseased vessels.

The level set formalism has been adopted in several studies of vessel segmentation. Antiga *et al.* [3, 4] used geodesic active surfaces to segment carotid arteries from CTA images. A sparse field approach [95] is used for efficient implementation. The active surface grows like a balloon to capture the vessel boundary with initial seeds placed near the center axis of the vessel (Figure 13). A local smoothing filter is applied on the segmented surface to eliminate protrusion artifacts due to collateral vessels of the carotid artery.

Shape priors were also incorporated in the level set segmentation framework for blood vessels. Lorigo *et al.* [52] proposed the use of co-dimension 2 active contours to incorporate directionality to the mean curvature flow. The vessels are modeled as tubes with varying width. The center axis evolves in the 3D space and an estimation of the local radius is made along the vessel. The method was applied to brain MRA

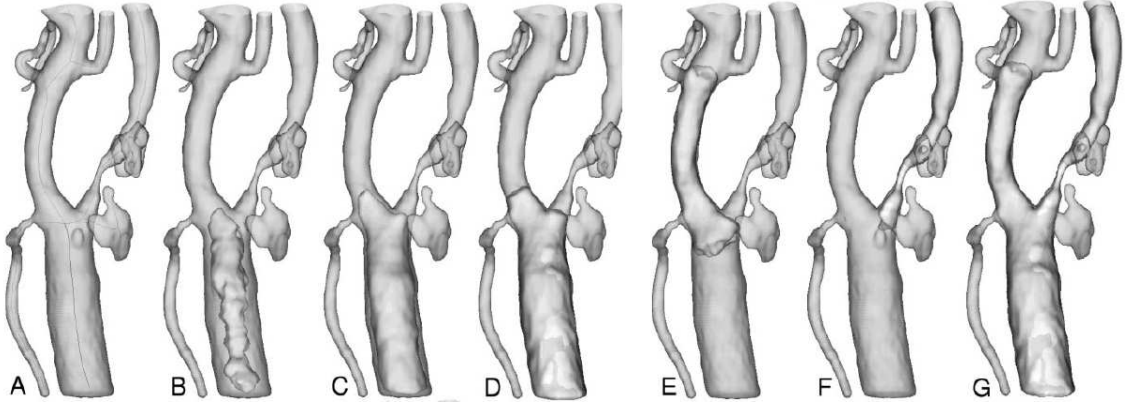


Figure 13: Level set reconstruction of a carotid artery [4]. (A) Iso-surface of the original CTA images with computed centerlines for level sets initialization. (B) Level sets evolving under inflation in the common carotid artery. (C) Level sets approaching the vessel wall. (D) Zero-level set converged to the boundary. (E) Level sets reconstruction of ECA. (F) Reconstruction of ICA. (G) Merging of the three branches in (D)-(F).

images and is effective in extracting small scale vessels. The vessel radii, however, are observed to be smaller than in MIP projections. Nain *et al.* [61] proposed a soft shape prior that incorporates a local ball filter to restrain the shape to be segmented to a long and thin structure. This method prevents leaks effectively, and the level set formulation allows the vessels and adjacent leaked-through regions to be separated automatically after certain times of iterations.

Chen and Amini [15] combined several vessel analysis techniques and proposed a hybrid approach to quantify 3D vascular structures. The MRA image was first enhanced using a Hessian-based method, and then a level set method is applied to the filtered image to segment the vessels. To further refine the result, the vessel surface is triangulated using 3D Delaunay triangulation and used as a parametric deformable model. This hybrid approach was tested on a phantom and three MRA abdomen datasets with encouraging results. No CTA data were tested.

In both parametric deformable models and level sets, the initial placement of the vessel surface is important. If the process is initialized with a single seed point, the

surface tends to over-evolve around the seed, and may leak out of the vessel boundary before the propagating front even reaches the far-end of the vessel. Deschamps and Cohen [20] proposed a freezing-front approach that stops the evolution near the seed based on the distance, and only allows the actual moving front to continue to propagate. This idea is successfully demonstrated on MRA images, however it is a heuristic approach and the stopping criteria must be chosen carefully. It is more desirable that the segmentation process is initialized with a surface near the centerline of the vessel, which must be extracted beforehand either manually or automatically. This leads to the gray-scale centerline extraction problem.

Several studies based on a minimal cost path have been applied to extract vessels in gray-scale 2D and 3D images [5, 18, 51, 63]. This type of approach is essentially searching a path between two user-specified points in order to minimize a total cost along the path. The cost can be defined based on image intensity, gradients or other smoothness constraints. Using wave front propagation and backtracking techniques, the resulting centerline usually lies within the boundary of the vessel. It may not be very well centered, however, and normally needs to be refined. Li and Yezzi [51] addressed this problem by proposing a method to search the vessel path in an augmented space as 4D curves, the fourth dimension being the vessel size. This additional parameter adds more constraint to the model and leads to a better centered vessel axis. The intrinsic nature of the minimal path type technique makes it non-automatic, for the fact that at least two input points are needed for the generation of a single path. For coronary arteries, especially left coronary arteries, more end points are required as input to deal with multiple branches (see Figure 14 for an example).

Many methods have also been proposed to extract skeletons of tubular structures given a segmentation. Most methods in the literature fall into the following two classes [109]: *boundary peeling* (also called thinning or erosion) [38], and *distance coding* (distance transform) [9, 53]. Although both classes of methods have yielded



Figure 14: Centerline extraction and vessel wall segmentation of coronary arteries using a minimal cost path approach [5]. Left: volume-rendered CTA images and three seed points. Center: Segmented region. Right: Axes obtained from the minimal path search.

promising results, these methods usually have problems of preserving connectivity and being smooth, and post processing is commonly needed to clean up the skeleton results. Direct extension of these methods to 3D is usually difficult and may not guarantee a unique solution for a single structure.

Some works attempted to extract the skeleton and segment the vessel surface at the same time [93, 94]. The direction of the vector formed by two previously found skeleton points is extended to generate an orthogonal plane to seek the next skeleton point. The orthogonal plane, however, is not guaranteed to be perpendicular to the newly found direction vector, especially when the vessel is highly curved.

Lazarus [49] proposed a skeletonization technique called level set diagrams that is specifically designed to extract the medial axis from boundary-based representations of 3D surfaces. The level set diagrams are associated with scalar functions defined over the set of vertices of a polyhedron. Center points of the same level sets are connected to form the 1D medial axis of the 3D surface.

The harmonic skeletonization technique to be employed in this thesis is similar to the formulation of level set diagrams. Instead of using a simple scalar function, e.g., height function (z -coordinates) as in [74], we propose to use the harmonic function

which is the solution of the Laplace equation to achieve better centeredness of the skeleton and the convenience to measure local cross-sectional areas accurately. The details will be described and discussed in Section 5.

For a more comprehensive survey on geometric methods for vessel visualization and quantification, see Buhler [11] and the references therein.

2.2.3 CTA Image Analysis

CTA image analysis has begun to draw much more interest and attention in recent years as the imaging technique rapidly develops and improves. As we have introduced in Chapter 1, CTA for vessel imaging is fast and non-invasive, with a very high and isotropic *in vivo* resolution.

There are many challenges in CTA image analysis, due to the nature of intensity distribution of different anatomical structures in CTA. In MRA and DSA, blood vessels present either very low or very high intensities and the intensity range is normally distinctive in the histogram. Other structures are well-suppressed in the imaging or post subtraction process, thus the MRA and DSA image can be directly visualized by a MIP or a 3D surface/volume rendering, although the direct rendering may not be as clean as further processed images. CTA, on the other hand, is difficult to be directly visualized by MIP on a full dataset. Vessels in CTA have an intensity value in the middle range of the histogram, between the intensity of bones and other soft tissues. In a MIP of CTA, bones or large areas of blood-filled regions (such as a heart ventricle) may occlude thin vessels completely, which makes the full MIP almost impossible to use. Local MIP may assist the visualization of a short segment of the vessel, but it is quite limited by the small FOV. Thus image processing is more important for efficient CTA viewing and analyzing, and also more challenging as compared to MRA/DSA processing.

Here we first look at some interesting CTA investigations on applications other

than coronary arteries. In the next section (2.2.4) we will focus more on coronary artery image analysis studies.

Carotid artery CTA is probably the most studied among all CTA applications. Carotids are larger vessels than coronaries, are more stationary, thus presenting better image quality, and are relatively easier to be processed. In Section 2.2.2 we reviewed the work by Antiga *et al.* [4] (Figure 13) using level set methods to segment each branch of the carotids. Andel *et al.* [2] developed a center lumen line extraction method for carotid arteries using first and second order derivatives of the image, called VAMPIRE (Vascular Analysis using Multiscale Paths Inferred from Ridges and Edges). This method falls in the category of minimal cost path search, where they incorporate the Hessian filter and Canny edge filter into the cost.

In a very recent work by Scherl *et al.* [78], the authors proposed a semi-automatic segmentation method improved from the Chan and Vese [14] model, with special efforts taken to exclude plaques from the lumen segmentation in order to achieve an accurate stenosis evaluation. The algorithm was tested on four phantoms and the MPR cross-sectional images of 10 CTA datasets. By comparing their results with stenosis percentage evaluated by radiologists, a mean error of about 8% was achieved.

Hernandez *et al.* [36] and Holtzman-Gazit and Kimmel [37] analyzed CTA images of patients with brain aneurysms. A challenge in brain CTA vessel segmentation is to distinguish the vessel from the bone, which also has high intensity values. In [36] the authors combined a pixel classifications method with geodesic active regions, where the kNN rule was applied to estimate probability density functions for pixel classification to achieve a different labeling for vessel and bone structures. In [37] a hierarchical approach was adopted to handle the segmentation of multiple objects (bone and vessel). The segmentation algorithm was first applied on the entire image to obtain both the bone and vessel, and then the algorithm was applied again only in the segmented region to separate the two objects.

Another work by Olabbarriaga *et al.* [64] focused on the segmentation of thrombus in abdominal aortic aneurysms from CTA images. In this study, the authors used a double-layered deformable model to fit with both the inner and outer vessel wall of the abdominal aorta. The inner boundary was relatively easy to obtain since the contrast was better between the blood-pool and the vessel wall in a such a large scale vessel, and the points on the outer boundary were driven by the probability of their belonging to the *inside*, *outside* or *on* the boundary, calculated using a nearest neighbor approach.

It can be seen that in CTA image analysis, many of the general vessel analysis methods are employed, such as level sets, deformable models, minimal cost path, Hessian analysis and so on. Due to the specific properties of CTA images, additional efforts were taken into dealing with problems such as bone and vessel separation, plaque and lumen separation, and inner and outer boundary separation. In chapter 4 we will address these problems for CTA coronary segmentation in great detail.

2.2.4 Coronary Artery Image Analysis

A major portion of work on coronary image analysis has been dedicated to X-ray angiography due to its long existence for clinical use. Since X-ray angiography will not be the focus of this thesis, we briefly review a recent work by Blondel *et al.* [8] here and direct interested readers to the references of this paper for other previous works. In [8] a reconstruction technique of coronary arteries from a rotational X-ray projection sequence is presented. This represents a common goal of image post-processing on X-ray angiography, which is to recover the true 3D shape of coronaries from 2D X-ray projections. Three steps were taken in [8] to achieve this goal: 3D centerline reconstruction, 4D motion estimation, and 3D tomographic reconstruction to emulate a CT scan. In fact, most of these laborious processing tasks can be eliminated if a CTA scan is directly performed.

There are a very limited number of works dedicated to coronary CTA analysis in the literature, and the existing methods vary in their performance and the amount of required user interaction. Chen and Molloy [16] proposed a vascular tree reconstruction method in coronary CTA, which involves 3D thinning and skeleton pruning techniques. The method was tested on a cast of the coronary arteries of a pig heart, which does not fully emulate *in vivo* CTA images, since all non-coronary structures in their testing images are well suppressed. Florin *et al.* [26] employed a Particle Filter-based approach for the segmentation of coronary arteries. Successive planes of the vessel are modeled as unknown states of a sequential process, which consist of the orientation, position, shape and appearance of the vessel that are recovered using a particle filter. This interesting probabilistic approach has shown its potential in the segmentation problem, but it would be useful to see more quantitative results than what is presented in the paper in order to evaluate the accuracy of this method. Another interesting work by Szymczak *et al.* [87] used a topological approach to extract coronary vessel cores from CTA images. The method is robust to image artifacts from implanted pacemakers, and shows very good tracking of coronaries in the distal end. Several topological techniques are employed in order to generate a clean result, such as trimming, pruning and gap filling, and the user needs to manually select a tree from the forest to identify the coronary arteries in the later stage of centerline cleaning. This method also needs to be further validated, as mentioned by the authors in the paper, and the segmentation of the vessel is not addressed in this study.

In this chapter, we have reviewed several general image segmentation methods, followed by a comprehensive literature review on previous works which have been performed on blood vessel image analysis. A number of techniques are discussed, including vessel enhancement methods, centerline extraction and skeletonization methods, 3D vessel wall segmentation and reconstruction methods and more. Since this thesis will be focused on coronary CTA analysis, we also looked at some interesting research

on CTA image analysis for different kind of vessels, and finally we reviewed some existing investigations of coronary CTA and discussed their values and limitations. It can be seen that the problem of coronary CTA analysis is far from fully explored. In the next chapter (Chapter 3) we will develop an image segmentation framework with its applicability to CTA coronary segmentation in mind, and compare the proposed method to other well-known segmentation techniques.

CHAPTER III

SEGMENTATION USING BAYESIAN DRIVEN IMPLICIT SURFACES (BDIS)

In this chapter, we present an image segmentation framework based on the geodesic active contour model with a significant improvement on the segmentation performance, which is especially beneficial for CTA blood vessel segmentation. We will start the chapter by reviewing the conventional geodesic active contour model and its limitations, and then move to the proposed algorithm, for which we employ Bayesian probability theory and level set techniques. In 3D, this algorithm yields a segmentation of an object as a surface, implicitly embedded in the level set function and evolved to the boundary of the object driven by Bayesian posterior probabilities. Hence, we call this method Bayesian driven implicit surfaces (BDIS).

3.1 Geodesic Active Contour Models and Limitations

As we have mentioned in the previous chapter, there are two key factors dominating the segmentation using an active contour model. The first is the physical property of the contour itself, such as its smoothness and elasticity; the second is the driving force from the image, which will attract and lead the contour to move toward edges or other salient features in the image, that finally separates the image into different regions according to certain homogeneity criteria.

We begin by discussing the contour itself, and we will add the image term later as we move forward. Let $C = C(p, t)$ be a family of closed curves where t parameterizes the family and p the given curve, where $0 \leq p \leq 1$. We assume that $C(0, t) = C(1, t)$ and similarly for the first derivatives for closed curves. The curve length functional

is defined as:

$$L(t) := \int_0^1 \left\| \frac{\partial C}{\partial p} \right\| dp \quad (2)$$

By taking the first variation of the length functional, we obtain a curve shortening flow, in the sense that the Euclidean curve length shrinks as quickly as possible when the curve evolves:

$$\frac{\partial C}{\partial t} = \kappa \vec{\mathcal{N}}, \quad (3)$$

where κ is the local curvature of the contour, and $\vec{\mathcal{N}}$ is the inward unit normal. The detailed derivation can be found in [89].

For the intrinsic property of being closed, the curve under the evolution of the curve shortening flow (3) will continue to shrink until it vanishes. By adding a constant ν , which we will refer to as the “inflation term”, the curve tends to grow and counteracts the effect of the curvature term when ν is negative [42]:

$$\frac{\partial C}{\partial t} = (\kappa + \nu) \vec{\mathcal{N}}. \quad (4)$$

The image influence can be introduced to the above framework by changing the ordinary Euclidean arc-length function along the curve C given by:

$$ds = \left\| \frac{\partial C}{\partial p} \right\| dp$$

to a geodesic arc length

$$ds_\phi = \phi ds = \phi \left\| \frac{\partial C}{\partial p} \right\| dp$$

by multiplying a conformal factor ϕ , where $\phi = \phi(x, y)$ is a positive differentiable function that is defined based on the given image $I(x, y)$.

We now take the first variation of the following geodesic curve length function:

$$L_\phi(t) = \int_0^1 \phi \left\| \frac{\partial C}{\partial p} \right\| dp, \quad (5)$$

and reach a new evolution equation combining both the internal property of the contour and the external image force:

$$\frac{\partial C}{\partial t} = \phi \kappa N - \nabla \phi \quad (6)$$

As in equation (4), we also add an inflation term to this curve evolution model:

$$\frac{\partial C}{\partial t} = \phi(\kappa + \nu)N - \nabla \phi \quad (7)$$

More details of the geodesic active contours can be found in the work of Caselles *et al.* [12], Kichenassamy *et al.* [42], and Yezzi *et al.* [104].

The level set formulation [66, 80] of Equation 7 is:

$$\frac{\partial \Psi}{\partial t} = \phi \left(\operatorname{div} \left(\frac{\nabla \Psi}{\|\nabla \Psi\|} \right) + \nu \right) \|\nabla \Psi\| + \nabla \phi \cdot \nabla \Psi, \quad (8)$$

where Ψ is the level set function (usually initialized to be a signed distance function) to be updated in each time step, and $\operatorname{div} \left(\frac{\nabla \Psi}{\|\nabla \Psi\|} \right)$ is essentially the curvature κ of the level sets of Ψ , and in 2D:

$$\kappa = \frac{\Psi_{yy}\Psi_x^2 - 2\Psi_x\Psi_y\Psi_{xy} + \Psi_{xx}\Psi_y^2}{(\Psi_x^2 + \Psi_y^2)^{3/2}}. \quad (9)$$

As mentioned above, ϕ is usually associated with the image intensity or intensity gradients to stop the implicit active contour from evolving at image boundaries or salient features. A usual choice of ϕ is:

$$\phi(x, y) = \frac{1}{1 + \|\nabla G_\sigma * I(x, y)\|^2}, \quad (10)$$

where G_σ is a Gaussian smoothing filter with variance σ , and $I(x, y)$ is the image intensity of the pixel located at (x, y) .

The two different representations of the deformable models, namely the parametric active contours (“snakes”) and geometric level-set representations, have both drawn great interest in recent years. They each have their advantages and disadvantages. The snakes model is a fast, intuitive and powerful technique in both 2D and 3D, for

the fact that it directly controls the evolution of points or grids of the actual interface (a contour in 2D or a surface in 3D) of interest. The two main limitations of the snakes are: first, it lacks the ability to naturally handle topology changes without sophisticated re-parameterization schemes; second, re-sampling is needed to keep the points equally spaced and not crossing each other, when the initial and final contours differ greatly. These problems can be solved relatively easily for the 2D case; however the 2D solution usually can not be extended to 3D directly, and it is much more complex to handle the 3D case.

Vessels are objects with complex shape and topology, which has a 3D form in CTA data. The snakes model is thus not an ideal choice for this application. The level set representation, on the other hand, has a number of advantages. The contours and surfaces can naturally split or merge in this formulation, and it is straightforward to extend the 2D implementation to 3D. The only issue with level sets is its computational cost, since the actual interface is embedded in a higher dimensional level set function, which need to be updated iteratively to evolve the interface. We will address the implementation efficiency issue in Chapter 4 as we apply our proposed method to 3D coronary artery segmentation.

The geodesic active contour model reviewed above has been successfully applied to many medical applications. This model, however, has some inherent limitations. It performs better on images that have roundish objects of interest (e.g., Figure 9), with relatively strong intensity gradients at the boundaries. For objects with complicated shapes such as blood vessels, however, the model fails to achieve satisfying results, see Figure 15 for an example. The problems mainly come from the following reasons:

1. The conformal factor ϕ does not provide a stopping force that is good enough to attract the active contour and restrain it from leaking once it reaches the boundaries. Because ϕ is usually designed based on intensity gradients, it ignores the pixel intensity information, which can provide important regional properties of

the image. Also, because the intensity gradients are sensitive to noise, it is necessary that the image convolves with a Gaussian smoothing filter for the calculation of the conformal factor. The Gaussian smoothing, however, blurs and widens the boundary of the desired object, (e.g., Figure 16 (b) (c)), and the segmentation may stop too early before reaching the true boundary and give a smaller segmentation than the real object. For example, thinner vessels were obtained in [52] compared to MIP projections because of using only image gradients to attract the active contour. This may in turn cause the underestimation of cross-sectional areas of the vessels.

2. The constant inflation term ν only drives the active contour in a certain direction without adaptability. This means the initialization of the active contour must be completely inside or outside the desired object, which requires precise manual placement of the initial contour. Also, once the contour leaks through the boundary, there is no additional force to pull it back, thus it will continue to leak without any restraints.

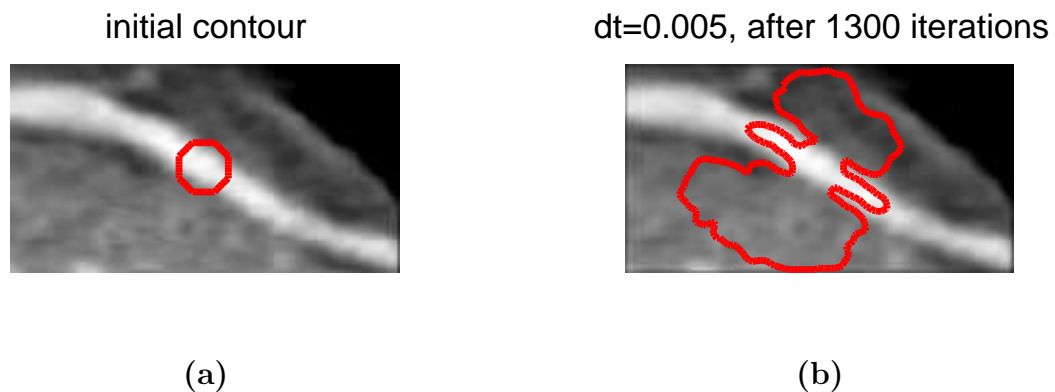


Figure 15: Conventional geodesic active contours fail to segment thin blood vessels. (a) Initial contour; (b) after 1300 iterations leakage appears and the segmented vessel is thinner than the real size.

3.2 An Improved Geodesic Active Contour Model

To address these problems, an adaptive active contour model is proposed. This method incorporates Bayesian pixel classification to the conventional geodesic active contour model and drives the segmentation using posteriors from the Bayesian and pixel labellings from the maximum *a posterior* (MAP) classification.

3.2.1 A New Conformal Factor Based on Bayesian Probabilities

Bayesian classifiers have been used in a number of image segmentation applications [32, 90]. Given the probability density function $p(I(\mathbf{x})|c_k)$ of each image class c_k along with the prior probability $Pr(\mathbf{x} \in c_k)$ of each class, posterior probabilities can be calculated via the Bayes' rule to give the probabilities of a single pixel at position $\mathbf{x} = (x, y)$ with intensity value v belonging to different classes:

$$Pr(\mathbf{x} \in c_k | I(\mathbf{x}) = v) = \frac{Pr(I(\mathbf{x}) = v | \mathbf{x} \in c_k) Pr(\mathbf{x} \in c_k)}{\sum_{\gamma=1}^n Pr(I(\mathbf{x}) = v | \mathbf{x} \in c_\gamma) Pr(\mathbf{x} \in c_\gamma)}. \quad (11)$$

There will be n posteriors for a single pixel if there are n classes presented in the image. The classification of the pixels can be obtained using the MAP rule:

$$C(\mathbf{x}) = \arg \max_{c \in \{c_1, c_2, \dots, c_n\}} Pr^*(\mathbf{x} \in c | I(\mathbf{x}) = v), \quad (12)$$

where $C(\mathbf{x})$ is the class that pixel \mathbf{x} belongs to, and Pr^* is a smoothed version of the posterior probability obtained using anisotropic smoothing [65] described by the following affine invariant flow in 2D:

$$\frac{\partial Pr}{\partial t} = \kappa_{pr}^{1/3} \vec{\mathcal{N}} \quad (13)$$

In 3D, the affine invariant flow becomes:

$$\frac{\partial Pr}{\partial t} = \text{sign}(H) \kappa_{pr+}^{1/4} \vec{\mathcal{N}}, \quad (14)$$

where H and κ_{pr} are the mean curvature and Gaussian curvature of Pr , and $\kappa_{pr+} := \max\{\kappa_{pr}, 0\}$. $\vec{\mathcal{N}}$ is the inward unit normal. This approach may be rigorously justified by the theory of MRF with a non-interacting, analog discontinuity field [91].

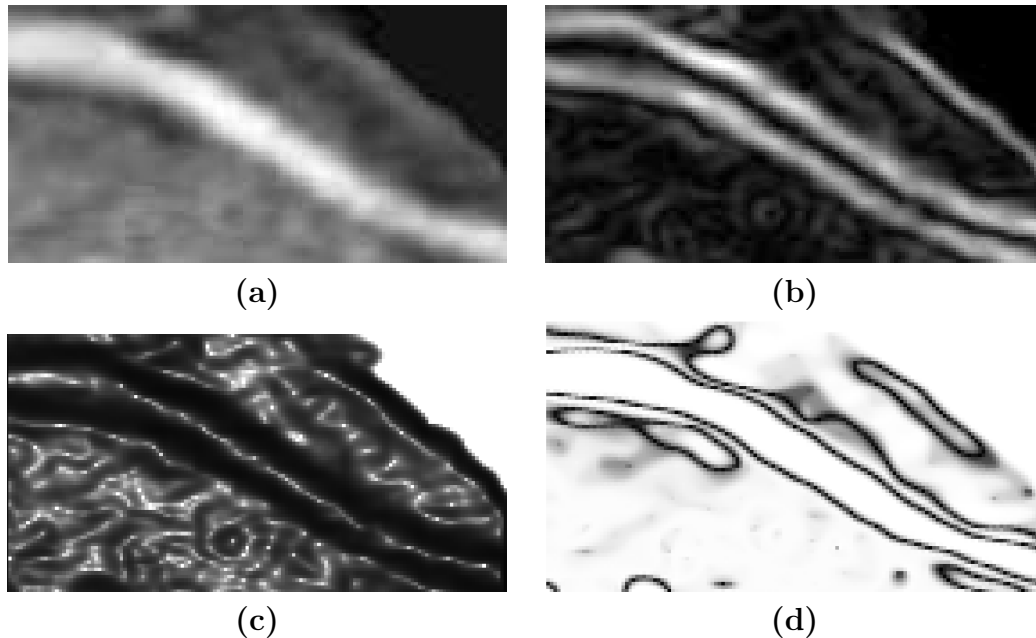


Figure 16: Comparing edge maps between the conventional conformal factor and the proposed function. (a) Original image; (b) Gaussian smoothed gradient image; (c) conventional conformal factor edge map; (d) proposed conformal factor edge map.

The proposed method redefines the conformal factor using the smoothed posterior probabilities. Suppose we have a bimodal image with class c_{in} representing the object to be segmented, and class c_{out} representing the background, we define the conformal factor as the squared difference between the posteriors that pixel \mathbf{x} belongs to c_{in} and c_{out} :

$$\phi(\mathbf{x}) = (Pr^*(\mathbf{x} \in c_{in}) - Pr^*(\mathbf{x} \in c_{out}))^2 \quad (15)$$

This can be extended to n classes ($n > 2$) by using the squared difference between the largest two posterior probabilities for a single pixel.

Figure 16 shows the comparison between the commonly used conformal factor based on gradient and the proposed conformal factor based on posterior probabilities. The proposed factor is smoother and has a much better defined dark valley at the boundaries than the conformal factor that only uses the gradient information.

3.2.2 An Adaptive Inflation Term

For the inflation term, we define an adaptive ν based on the MAP classification results:

$$\nu(\mathbf{x}) = \begin{cases} -k_1 & \text{if } C(\mathbf{x}) = c_{in} \\ +k_2 & \text{if } C(\mathbf{x}) = c_{out} \end{cases} \quad k_1, k_2 > 0 \quad (16)$$

This means when the contour is inside the object, the inflation term will force it to expand, and when the contour is outside the object, this term will force it to shrink. The proposed inflation term prevents leakage effectively. And because there is an extra force to pull the contour back once it leaks, k_1 can be set to a larger constant than in the conventional active contour model to inflate the bubble faster and push through the thin and curvy shape of blood vessels.

3.2.3 Estimation of Probability Density Functions

The estimation of probability density functions (pdfs) is an important step for Bayesian classification, since it essentially determines the final classification results. There are two types of methods for this task, namely parametric and non-parametric. For CT images, a parametric approach is usually adopted, as we will use here for the reason that the noise model of CT images is approximately Gaussian. The pdf $p(y)$ of an image is equivalent to the normalized histogram:

$$\int_{-\infty}^{\infty} p(y)dy = 1, \text{ and } p(y) \geq 0, \forall y,$$

of which each peak can be approximated using a Gaussian function:

$$p(I(\mathbf{x})|\mathbf{x} \in c_k) = \mathcal{N}(y; \mu_k, \sigma_k) = \frac{1}{\sqrt{2\pi}\sigma_k} \exp\left(-\frac{(y - \mu_k)^2}{2\sigma_k^2}\right), \quad (17)$$

where μ_k and σ_k are the mean and standard deviation of the current class c_k . A typical coronary CTA image has three or four peaks (classes) in the histogram, which correspond to the air in the lung, tissue, blood pool and calcification, if any. The complete histogram can then be represented by a Gaussian mixture model, where each

Gaussian function corresponds to a peak in the histogram with a weighting coefficient a_k :

$$p(y) = \sum_{k=1}^n a_k \mathcal{N}(y; \mu_k, \sigma_k),$$

where $y = I(\mathbf{x})$ are intensity levels existing in the image I , and n is the total number of components in the Gaussian mixture, which is equivalent to the total number of classes in the image.

We then estimate the parameters for all Gaussian components:

$$\theta = \{\mu_1, \dots, \mu_n, \sigma_1, \dots, \sigma_n, a_1, \dots, a_n\}$$

using the expectation maximization (EM) method (Hartley [35], Dempster *et al.* [19], McLachlan and Krishnan [58]), which consists of the following two iterative steps:

The E-step: for each sampled pixel with intensity y_i and each class c_k , estimate:

$$Pr(\mathbf{x} \in c_k | y_i; \theta) = \frac{Pr(y_i | \mathbf{x} \in c_k; \theta) a_k}{\sum_{\gamma=1}^n Pr(y_i | \mathbf{x} \in c_\gamma; \theta) a_\gamma} \quad (18)$$

using the values of parameters θ from the last M-step.

The M-step: update parameters for each component according to the following:

$$\begin{aligned} a_k &= \frac{\sum_{i=1}^M Pr(\mathbf{x} \in c_k | y_i; \theta)}{M}, \\ \mu_k &= \frac{\sum_{i=1}^M Pr(\mathbf{x} \in c_k | y_i; \theta) y_i}{\sum_{i=1}^M Pr(\mathbf{x} \in c_k | y_i; \theta)}, \\ \sigma_k^2 &= \frac{\sum_{i=1}^M Pr(\mathbf{x} \in c_k | y_i; \theta) (y_i - \mu_k)^2}{\sum_{i=1}^M Pr(\mathbf{x} \in c_k | y_i; \theta)}, \end{aligned}$$

where M is the total number of sampled pixels.

The process is repeated until the parameters converge or for a fixed number of iterations. For our applications, we initialize the parameters using a rough k-means clustering technique.

Figure 17 shows an example of running the EM algorithm on the image listed in Figure 9 in Chapter 2. The Gaussian mixture (in black) defined by the estimated parameters approximates the original histogram (in blue) reasonably well. The red profiles show each individual component of the estimated Gaussian mixture.

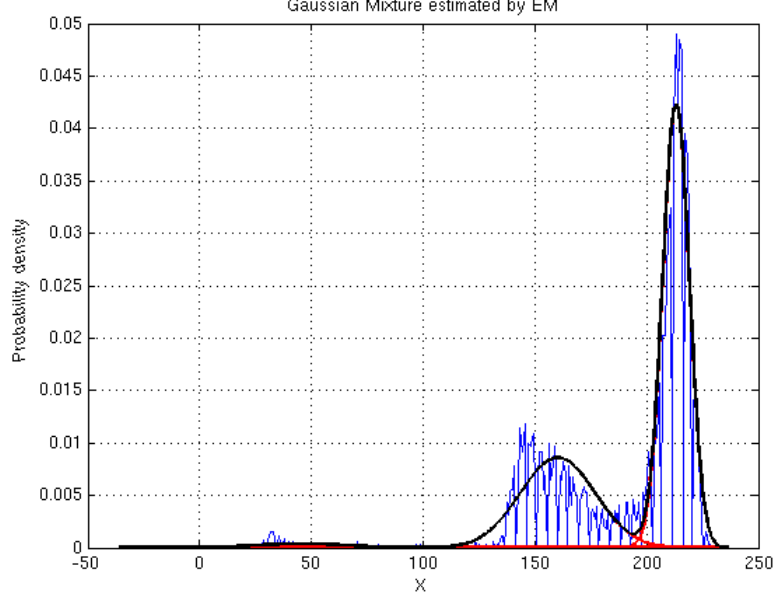


Figure 17: An example of using EM to approximate an image histogram. In blue: the original histogram; in black: the estimated Gaussian mixture profile; in red: each individual component in the Gaussian mixture.

3.2.4 Numerical Implementation Using Level Sets

To first test the effectiveness of the algorithm on 2D images, the proposed model was implemented through a standard finite difference scheme. Equation (8) can be re-written as:

$$\Psi_t = \phi \kappa \|\nabla \Psi\| + (\nu \phi + \frac{\nabla \Psi}{\|\nabla \Psi\|} \cdot \nabla \phi) \|\nabla \Psi\|, \quad (19)$$

where central differences are used for the first term, and an upwind scheme is used for the second term for stability. More specifically, the numerical scheme can be written as [80]:

$$\begin{aligned} \Psi_{ij}^{n+1} = & \Psi_{ij}^n + \Delta t ((\phi_{ij} \kappa_{ij}^n ((D_{ij}^{0x})^2 + (D_{ij}^{0y})^2)^{1/2}) \\ & + (\max(\nu \phi_{ij}, 0) \nabla^+ + \min(\nu \phi_{ij}, 0) \nabla^-) \\ & + (\max((\phi_x)_{ij}, 0) D_{ij}^{-x} + \min((\phi_x)_{ij}, 0) D_{ij}^{+x} \\ & + \max((\phi_y)_{ij}, 0) D_{ij}^{-y} + \min((\phi_y)_{ij}, 0) D_{ij}^{+y})) \end{aligned} \quad (20)$$

where κ_{ij}^n can be calculated by Equation (9) using central differences of Ψ , which are:

$$\begin{aligned}\Psi_x &= D_{ij}^{0x} = \frac{\Psi_{i+1,j} - \Psi_{i-1,j}}{2\Delta x}, \\ \Psi_y &= D_{ij}^{0y} = \frac{\Psi_{i,j+1} - \Psi_{i,j-1}}{2\Delta y},\end{aligned}\tag{21}$$

$$\begin{aligned}\Psi_{xx} &= D_{ij}^{0xx} = \frac{\Psi_{i+1,j} - 2\Psi_{i,j} + \Psi_{i-1,j}}{\Delta x^2}, \\ \Psi_{yy} &= D_{ij}^{0yy} = \frac{\Psi_{i,j+1} - 2\Psi_{i,j} + \Psi_{i,j-1}}{\Delta y^2},\end{aligned}\tag{22}$$

$$\Psi_{xy} = D_{ij}^{0xy} = \frac{\Psi_{i+1,j+1} + \Psi_{i-1,j-1} - \Psi_{i+1,j-1} - \Psi_{i-1,j+1}}{\Delta x \Delta y}.\tag{23}$$

D_{ij}^{0x} , D_{ij}^{0y} are central differences of Ψ along x and y directions (Equation (21)), $D_{ij}^{-x} = \frac{\Psi_{i,j} - \Psi_{i-1,j}}{\Delta x}$, $D_{ij}^{-y} = \frac{\Psi_{i,j} - \Psi_{i,j-1}}{\Delta y}$ are one sided backward differences, $D_{ij}^{+x} = \frac{\Psi_{i+1,j} - \Psi_{i,j}}{\Delta x}$, $D_{ij}^{+y} = \frac{\Psi_{i,j+1} - \Psi_{i,j}}{\Delta y}$ are one sided forward differences, and ∇^+ , ∇^- are:

$$\nabla^+ = (\max(D_{ij}^{-x}, 0)^2 + \min(D_{ij}^{+x}, 0)^2 + \max(D_{ij}^{-y}, 0)^2 + \min(D_{ij}^{+y}, 0)^2)^{1/2}$$

$$\nabla^- = (\max(D_{ij}^{+x}, 0)^2 + \min(D_{ij}^{-x}, 0)^2 + \max(D_{ij}^{+y}, 0)^2 + \min(D_{ij}^{-y}, 0)^2)^{1/2}$$

The conformal factor ϕ has been calculated ahead of time, and ϕ_x , ϕ_y are calculated using central differences. Reinitialization of the level set function is performed after a fixed number of iterations for stability purposes.

3.3 2D Experimental Results

The proposed method was tested on 2D synthetic images and real CT images of both vessels and non-vessels.

Figure 18 shows an example of running the algorithm on a synthetic image of branched vessels. The vessels are hand-drawn with additive Gaussian noise. The initial contour crosses the boundary of the vessels and differs largely from the actual vessel boundary. Due to the adaptive inflation term, the contour shrinks or expands locally according to the local image characteristics. This emulates the property of region-based deformable models [14, 104].

Figure 19 shows an example of a coronary artery CT image. The image was generated through curved multi-planar reformatting (MPR) from a 3D dataset. It is the same image as in Figure 15, where the conventional geodesic active contour fails to segment the vessel. In this new result, also by starting with an initial contour crossing the boundary of the vessel, the proposed method successfully segments the image as shown in Figure 19 (d).

In Figure 20 we compare the segmentation of a heart chamber using three different methods. The original image is shown in (a1), and the initial contour is placed inside the object of interest as in (a2). On each row of two images that follows, we show the evolution contours and the final segmentation as a binary mask. The figures in (b1) and (b2) are the results of using the conventional gradient-based method with a uni-directional inflation term. It can be seen that the contour moves toward the boundary initially; however it fails to stay at the boundary and start to leak after more iterations, due to the fact that the gradient-based conformal factor defined by (10) never becomes zero at the boundary, although it may be very small. Also, once it leaks, the uni-directional inflation term keeps pushing the contour to grow, without the ability to remedy the leakage. The final result is certainly not satisfying.

Figures 20 (c1) and (c2) show the results obtained using a region-based segmentation method proposed by Chan and Vese [14]. This method is essentially seeking a maximum global separation of the average intensity inside and outside the object by minimizing the following functional:

$$\begin{aligned}
 F(m_1, m_2, C) = & \mu \cdot \text{Length}(C) + \lambda_1 \int_{\text{inside}(C)} |I(x, y) - m_1|^2 dx dy \\
 & + \lambda_2 \int_{\text{outside}(C)} |I(x, y) - m_2|^2 dx dy,
 \end{aligned} \tag{24}$$

where $\mu \geq 0$, $\lambda_1, \lambda_2 > 0$ are fixed parameters, C is the curve, $I(x, y)$ is the original image, and m_1 and m_2 are the mean values of the image intensity inside and outside of contour C , which are updated dynamically as C evolves. This model has the nice

property of utilizing the region intensity information of the image and being able to segment images without strong edges. However, it is a fully global method which segments all regions in the image with similar intensity no matter where the initial contour is placed. This may be a good property for certain applications, but for segmenting coronary arteries from CTA, this method will lead to the segmentation of not only the vessels, but other unwanted blood-filled regions, such as the aorta and ventricles of the heart. As shown in (c1) and (c2), although our goal is to segment only the heart chamber in the image and the initial contour was placed fully inside the chamber, the segmentation result contains all regions in the image with similar intensity level.

Finally we show in Figures 20 (d1) and (d2) the results of the proposed method using BDIS. The final segmentation shows the desired heart chamber, and the evolution process shows a very good convergence at the boundary without any leakage. The curves also evolve faster and smoother as comparing to the gradient-based approach in (b1), due to the smooth high value of ϕ in homogeneous regions in the image.

With these 2D testing results, we conclude this chapter where we proposed a new segmentation method with great potential and proven abilities in segmenting coronary CTA imagery. The method addressed the commonly seen problems of leakage and under-segmentation in the conventional geodesic active contour models, by using Bayesian probability estimation with pdf parameters calculated through EM and level set methods.

In the next chapter, we will propose a complete framework for the fully automatic segmentation of coronary arteries from 3D CTA images.

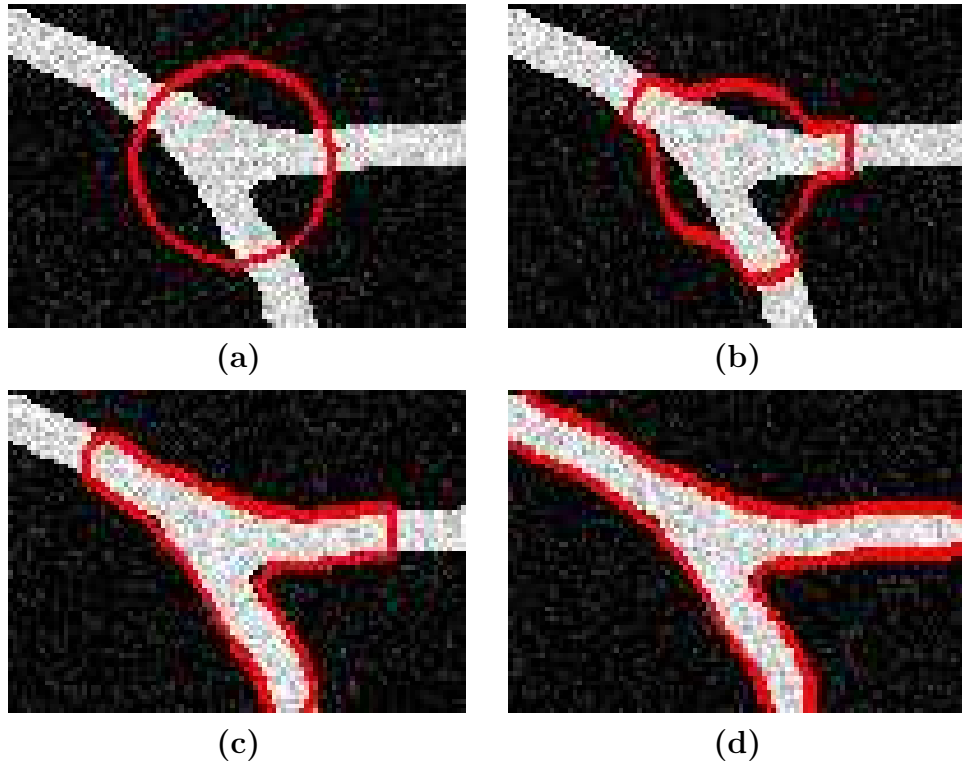


Figure 18: Segmentation of a synthetic vessel image using the proposed method. (a) Initial contour; (b) after 120 iterations; (c) after 500 iterations; (d) after 1000 iterations, final segmentation.

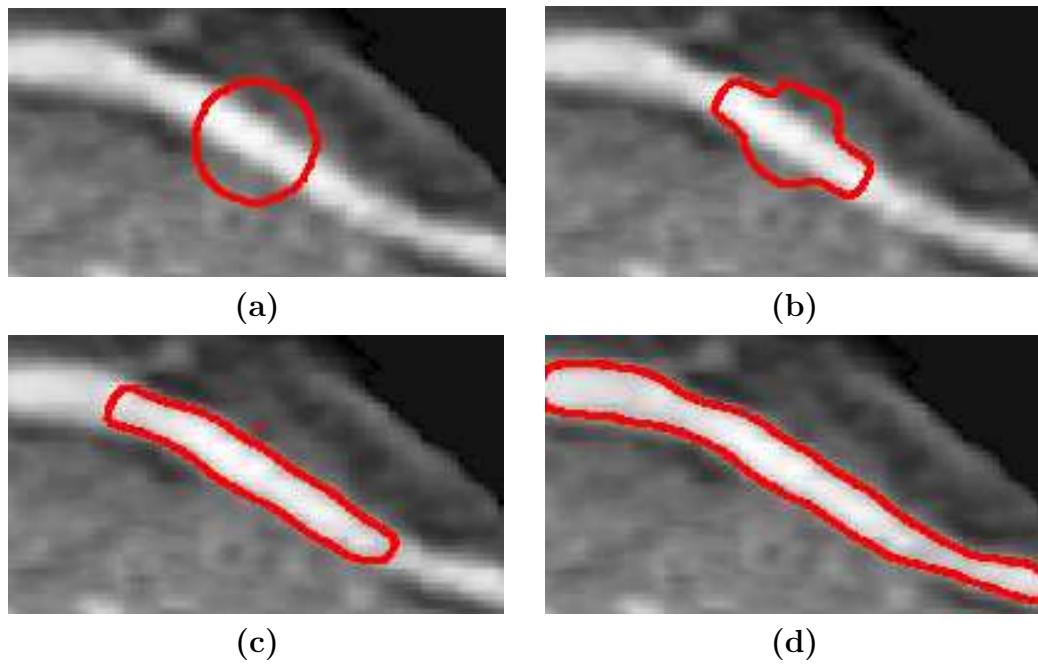


Figure 19: Segmentation of a real coronary artery image (MPR image), the same as in Figure 15, where the conventional geodesic active contours fail to segment. (a) Initial contour; (b) after 150 iterations (c) after 600 iterations; (d) after 1600 iterations, final segmentation.

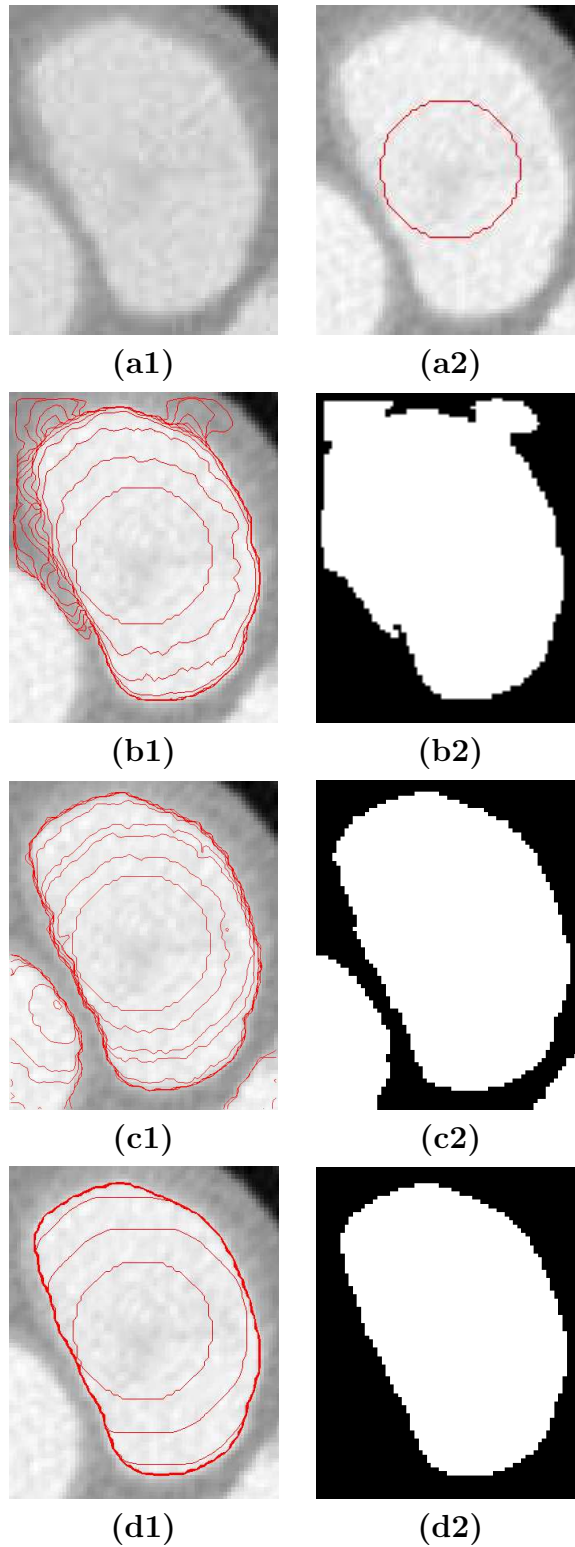


Figure 20: Segmentation of a heart chamber. a1. the original image; a2. the initial contour; b1 and b2. evolution contours and final segmentation using the conventional gradient-based method; c1 and c2. results of a region-based method; d1 and d2. results of the proposed method. See text for details.

CHAPTER IV

FULLY AUTOMATIC DETECTION AND SEGMENTATION OF CORONARY ARTERIES IN 3D

In this chapter, we present a fully automatic segmentation framework for coronary arteries in 3D CTA images. We start by a simple lung and heart segmentation using mathematical morphological approaches to eliminate vessels in the lung and define the region of interest (ROI) for further processing. We then use a Hessian-based vessel filtering technique to enhance vessels within the ROI. An isosurface from the Hessian filtering response serves as the initial surface for a further segmentation step using the Bayesian driven implicit surfaces (BDIS) method proposed in the previous chapter. We also examine implementation and optimization details as we apply BDIS to 3D datasets.

In the final section, we present the segmentation results on 18 real clinical datasets and compare them quantitatively with manual segmentation by evaluating the sensitivity, specificity, and accuracy of the proposed method.

Figure 21 and Figure 22 show a series of coronary CTA images as they are in their original form. It can be seen that the LM appears first in the image and as we go forward, the LM bifurcates into two branches, LAD and LCX, which further bifurcate into smaller branches. The RCA starts to appear in the last three slices in Figure 21. At first the slices cut through the RCA in its longitudinal direction, and then gradually change into orthogonal direction. RCA presents less variations than the left coronary tree.

We number the datasets used in this thesis in a sequential manner as they appear in the following sections. Shown in Figure 21 and Figure 22 are images from Dataset

#1.

4.1 Lung and Heart Segmentation

The segmentation of the lung and heart is an important preprocessing step to the segmentation of coronary arteries. The goal of this step is to segment the heart from the original images and eliminate the lung and other structures. The main purpose is to mask out vessels in the lung and bone structures in the chest which will bring many false positive detections in the Hessian-based vessel filtering process that follows.

We show the detailed steps for lung and heart segmentation by an example shown in Figure 23 and Figure 24. The same steps are applied to all 2D slices to obtain a 3D heart mask. For efficiency purposes, these steps are applied to down-sampled images by a factor of 4. This size of image is sufficient for lung and heart segmentation since in this step it is not necessary to obtain a very refined segmentation.

Figure 23 **(a)** shows the original image slice. By applying a thresholding on **(a)**:

$$I_{out}(x, y) = \begin{cases} 0, & \text{if } I_{in}(x, y) \geq thresh \\ 1, & o.w \end{cases}$$

where *thresh* is the typical intensity of the air in CT images, we obtain **(b)**, where white represents the air in the lungs, and black represents all other structures. The result in **(b)** is then dilated using a circular disk as the structural element and becomes **(c)**. In order to eliminate holes presented in **(c)**, we run another morphological operation “hole filling” [30] to obtain the lung mask **(d)**. This mask is able to eliminate all vessels in the lungs. From **(d)** we detect four tipping points **(e)** and then connect them with Bresenham lines [10] **(f)**. The tipping points are detected automatically by searching for extreme values of the x-coordinate.

We then dilate the current mask (Figure 23 **(f)**) again and generate Figure 24 **(g)**. Another “hole filling” is performed on **(g)** to obtain **(h)**. By subtracting **(g)** from **(h)**, we obtain an approximate heart mask **(i)**. Due to the dilation done for **(g)**,

we need to dilate **(i)** using the same sized structural element to recover the shape, as in **(j)**, which is the final heart mask. The last row compares the original image **(k)** with the masked image **(l)**. It can be seen that the heart has been kept and other structures have been eliminated completely.

Figure 25 compares the 3D volume rendering of the original **(a)** and masked **(b)** images. It is apparent that the vessels in the lung and bones in the chest have been eliminated effectively in **(b)** by applying the mask, and the masked image is much cleaner than the original one. The masked image now solely represents the heart and some segments of the left coronary arteries can already be seen on the surface of the heart.

4.2 *Multi-Scale Vessel Filtering*

In this section, we apply a 3D Hessian-based filter [28, 102] to enhance the coronary arteries in CTA images and generate an initial surface for further refined BDIS segmentation. The filter is performed in a multi-scaled fashion in order to respond to vessels of different sizes. Only voxels within the heart mask are calculated for a filter response; voxels outside the mask are ignored. Notice that we still do the filtering on the original image rather than the masked image, since the sharp edges between the heart and the masking background will bring strong false filter responses.

This Hessian-based filter is a voxel-based filter, meaning that each voxel is calculated for a filter response. We start by calculating the second order derivatives of the intensity values to form a Hessian matrix for each voxel:

$$\nabla^2 I(\mathbf{x}) = \begin{bmatrix} I_{xx}(\mathbf{x}) & I_{xy}(\mathbf{x}) & I_{xz}(\mathbf{x}) \\ I_{yx}(\mathbf{x}) & I_{yy}(\mathbf{x}) & I_{yz}(\mathbf{x}) \\ I_{zx}(\mathbf{x}) & I_{zy}(\mathbf{x}) & I_{zz}(\mathbf{x}) \end{bmatrix}, \quad (25)$$

where $\mathbf{x} = (x, y, z)$ represents a voxel location in 3D, and each element in the Hessian matrix can be calculated by convolving the image with the second order derivatives

Table 1: Possible patterns in 3D based on Hessian eigenvalues. Adapted from [28].

λ_1	λ_2	λ_3	orientation pattern
N	N	N	noisy, no preferred direction
L	L	H-	plate-like structure (bright)
L	L	H+	plate-like structure (dark)
L	H-	H-	tubular structure (bright)
L	H+	H+	tubular structure (dark)
H-	H-	H-	blob-like structure (bright)
H+	H+	H+	blob-like structure (dark)

of a 3D Gaussian function with a standard deviation of σ :

$$I_{uv}(\mathbf{x}; \sigma) = \left(\frac{\partial^2}{\partial u \partial v} G(\mathbf{x}; \sigma) \right) * I(\mathbf{x}). \quad (26)$$

By adjusting σ we adjust the width of the Gaussian function to adapt to different vessel sizes. In CTA, the variation in the size of coronary arteries is not large. In general, two scales (two values of σ) are sufficient to extract all coronary artery branches.

We then compute the eigenvalues (λ_1, λ_2 and λ_3) of the Hessian matrix (25). Frangi *et al.* [28] summarized the relationship between different combinations of the eigenvalues and their corresponding possible 3D patterns (Table 1). The shape of coronary arteries in CTA images are bright tubular structures, listed as the fourth row of Table 1, where λ_1 is approximately zero, and λ_2 and λ_3 are negative numbers with high absolute values:

$$\begin{cases} 0 \approx |\lambda_1| \ll |\lambda_2| \leq |\lambda_3|, \\ \lambda_2 < 0, \lambda_3 < 0. \end{cases} \quad (27)$$

To discriminate the tubular structure from other types of structures, a vesselness measure is defined:

$$M(x, \sigma) = \begin{cases} 0, & \text{if } \lambda_2 > 0 \text{ or } \lambda_3 > 0 \\ \left(1 - \exp\left(-\frac{R_A^2}{2\alpha^2}\right)\right) \exp\left(-\frac{R_B^2}{2\beta^2}\right) \left(1 - \exp\left(-\frac{S^2}{2c^2}\right)\right), & \text{otherwise,} \end{cases} \quad (28)$$

where

$$R_A = \frac{|\lambda_2|}{|\lambda_3|}, R_B = \frac{\lambda_1}{\sqrt{|\lambda_2\lambda_3|}}, S = \sqrt{\sum_{1 \leq i \leq 3} \lambda_i^2}.$$

In measure (28), R_A is able to discriminate tubular structures from plate-like structures, R_B mainly differentiates blob-like structures from other structures and also favors tubular structures, and S penalizes random background noise. α , β and c are constants that control the balance between the three terms. We have used $\alpha = 0.5$, $\beta = 0.5$, $c = 10$ for all cases.

Finally, to incorporate contributions from every scale, the maximum value of all scales at each voxel is selected to be the final filter response:

$$M_{multi}(x) = \max_{\sigma} M(x; \sigma). \quad (29)$$

Figure 26 demonstrates the effectiveness of the above multi-scale vessel filter. In **(a)** we show the volume rendering of the images after the lung and heart segmentation, where all tissues in the heart present in the rendering, and in **(b)** we show the rendering of the vessel filter response as a volume of images. Since for each voxel there exists a vesselness measure, the filter response is essentially another volume of images with the same size as the original images which can also be rendered in the same fashion. It can be seen that most tissues in the heart other than the vessels have been effectively suppressed, and the shape of both LCA and RCA can be clearly seen in the filter response.

The next step is to extract a surface of the vessels from the filter response in order to generate an initial surface for BDIS segmentation. The iso-surface at 30% of the maximum filter response is extracted. This iso-surface threshold is heuristically selected and worked well for all our testing cases. The iso-surface contains some small fragments which do not belong to the coronary arteries. In order to remove these fragments, a size filter is applied to all connected regions in the thresholded image volume. The isolated regions which are too small in size are thus eliminated.

Figure 27 shows the final surface which represents the coronary arteries of both sides. It can be seen that the structures of the vessels are very well extracted, however the boundaries are quite ragged and in some locations the vessels are disconnected. In the next section (4.3), we will use this surface as the initial surface for a much more refined BDIS segmentation.

Before we conclude this section, we show another example to demonstrate the importance of the heart segmentation step. In Figure 28, we compare the vessel filter responses performed on the whole image (middle) and image within the heart mask (right). It is apparent that the vessels in the lung brought a tremendous amount of false filter responses in the original image, while in the masked image, the filter response focuses only on the coronary arteries.

Another benefit of performing the heart segmentation is to improve the speed for vessel filtering. Since this is a voxel-based approach, the computation will be significantly faster if the number of voxels is reduced. The heart segmentation eliminated all voxels outside the heart, which reduces approximately 1/3 amount of voxels to be processed and hence improves the speed by about 30%. Also, for the sake of computation efficiency, the vessel filtering step is performed on a down-sampled image volume by a factor of 2, which contains 1/8 of the original voxels. The resolution is sufficient for vessel filtering, while the computation speed is maximized. The computational time for each dataset will be reported in section 4.4, Table 4.

4.3 3D Segmentation of Coronary Arteries Using BDIS

In this section, we apply the proposed BDIS algorithm to coronary artery segmentation using the initial surface obtained from the Hessian-based vessel filtering in the previous section. We first show the detailed numerical implementation in 3D, along with some optimization considerations, and then show an example to demonstrate the

segmentation on a healthy volunteer (Dataset #2). In the BDIS segmentation process, we have considered three classes (blood, tissue and background) for all datasets, and calcified plaques are initially classified and segmented as the blood. An additional step is taken to remove calcium from the segmented blood region in diseased vessels to finally offer a true lumen segmentation. The difference between the initial blood mask and the final lumen mask represents the calcified plaques.

4.3.1 Numerical Details and Optimization

We rewrite Equation (19) in Chapter 3 here, which is the updating equation for the level set function:

$$\Psi_t = \phi\kappa\|\nabla\Psi\| + \left(\nu\phi + \frac{\nabla\Psi}{\|\nabla\Psi\|} \cdot \nabla\phi\right)\|\nabla\Psi\|.$$

The 3D implementation can be extended straightforwardly from the 2D case, which is essentially the same as in 3D except for the addition of a third dimension. We still show the details here since the 3D implementation is rarely seen in the literature:

$$\begin{aligned} \Psi_{ijk}^{n+1} = & \Psi_{ijk}^n + \Delta t \left((\phi_{ijk}\kappa_{ijk}^n ((D_{ijk}^{0x})^2 + (D_{ijk}^{0y})^2 + (D_{ijk}^{0z})^2)^{1/2}) \right. \\ & + (\max(\nu_{ijk}\phi_{ijk}, 0)\nabla^+ + \min(\nu_{ijk}\phi_{ijk}, 0)\nabla^-) \\ & + (\max((\phi_x)_{ijk}, 0)D_{ijk}^{-x} + \min((\phi_x)_{ijk}, 0)D_{ijk}^{+x} \\ & + \max((\phi_y)_{ijk}, 0)D_{ijk}^{-y} + \min((\phi_y)_{ijk}, 0)D_{ijk}^{+y} \\ & \left. + \max((\phi_z)_{ijk}, 0)D_{ijk}^{-z} + \min((\phi_z)_{ijk}, 0)D_{ijk}^{+z} \right), \end{aligned} \quad (30)$$

where in 3D

$$\begin{aligned} \kappa_{ijk}^n = & [(D_{ijk}^{0xx} + D_{ijk}^{0yy})(D_{ijk}^{0z})^2 - 2D_{ijk}^{0x}D_{ijk}^{0y}D_{ijk}^{0xy} \\ & (D_{ijk}^{0yy} + D_{ijk}^{0zz})(D_{ijk}^{0x})^2 - 2D_{ijk}^{0y}D_{ijk}^{0z}D_{ijk}^{0yz} \\ & (D_{ijk}^{0xx} + D_{ijk}^{0zz})(D_{ijk}^{0y})^2 - 2D_{ijk}^{0x}D_{ijk}^{0z}D_{ijk}^{0xz}] \end{aligned}$$

$$/((D_{ijk}^{0x})^2 + (D_{ijk}^{0y})^2 + (D_{ijk}^{0z})^2)^{3/2}, \quad (31)$$

D_{ijk}^{0x} , D_{ijk}^{0y} and D_{ijk}^{0z} are central differences for the first derivatives which can be calculated using Equation (21) in Chapter 3, D_{ijk}^{0xx} , D_{ijk}^{0yy} , D_{ijk}^{0zz} , D_{ijk}^{0xy} , D_{ijk}^{0xz} and D_{ijk}^{0yz} are second order derivatives (Equations (22) and (23)), and ∇^+ , ∇^- are:

$$\begin{aligned} \nabla^+ &= (\max(D_{ijk}^{-x}, 0)^2 + \min(D_{ijk}^{+x}, 0)^2 + \max(D_{ijk}^{-y}, 0)^2 + \min(D_{ijk}^{+y}, 0)^2 \\ &\quad + \max(D_{ijk}^{-z}, 0)^2 + \min(D_{ijk}^{+z}, 0)^2)^{1/2}, \\ \nabla^- &= (\max(D_{ijk}^{+x}, 0)^2 + \min(D_{ijk}^{-x}, 0)^2 + \max(D_{ijk}^{+y}, 0)^2 + \min(D_{ijk}^{-y}, 0)^2 \\ &\quad + \max(D_{ijk}^{+z}, 0)^2 + \min(D_{ijk}^{-z}, 0)^2)^{1/2}. \end{aligned}$$

$\Psi(x, y, z, t)$ is essentially a scalar field defined on the 3D space being updated by Equation (30). A full computation for all grid points in 3D is very computational expensive. Here we adopt a well-known “narrow band” approach to reduce the computation cost. Only a narrow band of grid points around the zero level set is being updated for each iteration and other grid points are ignored. Since vessels are long and thin structures that stretch in long distances in the 3D space but with very limited surface areas which correspond to small number of grid points on the zero level set, the narrow band approach is especially efficient for this application.

Another concern is the initialization of the level set function. Ψ is usually initialized to be a signed distance function with negative values inside the surface and positive values outside [80]. However, in a large 3D volume the computation of such a distance function takes a extremely long time. Also for numerical stability, the signed distance function is needed to be re-initialized after a certain number of iterations. This is often referred to as “re-distancing” in the literature. The need for re-distancing adds more computation cost since this is usually necessary to be performed several times before reaching the final solution. To address this issue, we divide the 3D volume into sub-volumes, and perform the computation on smaller volumes, since the

calculation of 3D distance function on small volumes takes significantly less time than large volumes. We also notice that the initial surfaces of the vessels only occupy some of the sub-volumes, so we perform the computation only within these volumes and ignore the others. This will further reduce the computation cost. The size of the sub-volume is heuristically selected to be $30 \times 30 \times 30$ for the coronary segmentation.

Here we show the segmentation results on a healthy case (Dataset #2) to demonstrate the algorithm. More results on diseased vessels and more datasets will be tested and validated in the next few sections.

Figure 29 compares the 2D contours on two example slices of the initial shape obtained using the Hessian-based vessel filtering and the final shape obtained by BDIS. These are slice #6 and #23 from Dataset #2. It can be seen that the final contours exhibit much smoother appearance than the initial contours, although the initial contours already lie within the vessels. The final contours define the vessel boundaries precisely (as we will also quantitatively show in Section 4.4) with sub-voxel accuracy due to the property of level set segmentation. We should mention that we show the results here in 2D only for demonstration, however the algorithm is performed in a true 3D manner.

In Figure 30 and Figure 31 we show a series of segmentation results as 2D contours from Dataset #2. Both LCA and RCA are successfully tracked and delineated with a reasonable distal-end sensitivity. Figure 34 (Upper) shows the final segmentation as a 3D surface. Comparing to the vessel filtering result (initial surface) in Figure 27, the final surface is much smoother and some broken branches in the initial surface are connected automatically, thanks to the ability of level sets in handling topological changes.

4.3.2 Removing Calcified Plaques

We have assumed that there are three classes in the image volume, being the blood-filled region, tissue, and lungs. In diseased vessels with calcified plaques, the calcium deposits are initially classified as the blood-filled region due to their high values in image intensity. An additional step is performed to remove the calcium from the segmentation mask, thus the remainder is a volume mask which solely represents the lumen.

Figure 35 demonstrates the calcium removing task using three examples. Starting from the segmentation that includes both the lumen and calcium, we calculate an Otsu threshold [67] using all pixels within the “lumen + calcium” mask, and use this threshold to separate the calcium from the lumen. The Otsu threshold is calculated based on the minimization of the intraclass variance of the background (lumen) and the foreground (calcium) regions.

The left column of Figure 35 shows three slices of images showing the initial segmentation result from Dataset #8, Dataset #15, and Dataset #16, respectively. The right column shows the result after removing the calcified plaques. It can be seen that the red contours now delineate the true boundary of the lumen itself.

4.4 Results and Validation

In this section, we show the segmentation results on 18 real clinical datasets, including the two datasets we have used in the previous sections as examples. Most datasets were acquired at Emory clinic using a Siemens Sensation 64 slice CT scanner, except that Dataset #2 was acquired using a GE LightSpeed Pro 16 scanner. The image acquisition process is not performed as part of this thesis, but by CT specialists at Emory, under an IRB-approved protocol. The acquisition date, volume size and spacial resolution are listed in Table 2. The average volume size is $313 \times 362 \times 210$, and the average pixel resolution is $0.3703\text{mm} \times 0.3703\text{mm} \times 0.7361\text{mm}$ over all 18

Table 2: Segmentation results and validation for 18 datasets. Part I - Data properties.

Data	Study Date	Volume Size	Resolution (<i>mm</i>)
#1	Dec. 2004	340 × 408 × 210	0.3906 × 0.3906 × 0.7500
#2	Nov. 2004	288 × 340 × 174	0.4883 × 0.4883 × 0.6250
#3	Nov. 2006	340 × 340 × 192	0.4082 × 0.4082 × 0.7500
#4	Dec. 2006	328 × 372 × 226	0.3652 × 0.3652 × 0.7500
#5	Sept. 2006	328 × 372 × 188	0.3848 × 0.3848 × 0.7500
#6	Feb. 2006	328 × 372 × 218	0.3730 × 0.3730 × 0.7500
#7	July 2003	248 × 280 × 136	0.4883 × 0.4883 × 0.6250
#8	Nov. 2006	328 × 372 × 228	0.3418 × 0.3418 × 0.7500
#9	Dec. 2006	328 × 372 × 238	0.3516 × 0.3516 × 0.7500
#10	Oct. 2006	328 × 372 × 202	0.3008 × 0.3008 × 0.7500
#11	Nov. 2006	328 × 372 × 222	0.3379 × 0.3379 × 0.7500
#12	May 2006	300 × 356 × 180	0.2891 × 0.2891 × 0.7500
#13	Dec. 2006	300 × 356 × 248	0.2871 × 0.2871 × 0.7500
#14	Nov. 2006	320 × 356 × 210	0.3301 × 0.3301 × 0.7500
#15	Mar. 2006	320 × 376 × 226	0.3555 × 0.3555 × 0.7500
#16	May 2006	308 × 376 × 222	0.4199 × 0.4199 × 0.7500
#17	Dec. 2006	276 × 344 × 226	0.4238 × 0.4238 × 0.7500
#18	Sept. 2006	304 × 392 × 242	0.3301 × 0.3301 × 0.7500
mean ±std	N/A	313 × 362 × 210 ± 23, ± 26, ± 27	0.3703 × 0.3703 × 0.7361 ±0.0574, ±0.0574, ±0.0393

datasets.

We list the final segmentation as 3D surfaces of all datasets in Figure 36 and Figure 37 to show their geometries. It can be seen that coronary arteries exhibit great variations in their shapes, including vessel thickness, number of branches, bifurcation angles, etc.

All datasets were also segmented manually by a trained person by delineating the lumen boundaries on each individual axial slice using a Wacom® tablet pen. The pen was used instead of the mouse in order to simulate the drawing on paper with a real pencil for better accuracy. The contour drawing was performed within a software tool “MRIcro” [75], where the axial slices can be viewed and closed contours can be

drawn on the slices by the tablet pen. A surface rendering of manually segmented Dataset #2 is shown in Figure 34 (Lower). Since there are no constraints enforced on the third dimension when doing manual segmentations, the surface is not as smooth as the automatic segmentation result as shown in Figure 34 (Upper).

We compare the results of our proposed automatic segmentation with the manual segmentation using four measures to quantify their differences. The comparison is performed in terms of contours on the 2D axial slices since manual segmentation were all done in this manner. We first evaluate the sensitivity of the proposed method by looking at the percentage of overlapped contours between the automatic segmentation and manual segmentation (true positives) among the total number of contours in the manual segmentation:

$$Sensitivity = \frac{\text{number of overlapped contours}}{\text{total number of contours in manual seg.}} \times 100\%. \quad (32)$$

The sensitivity gives an evaluation on the ability of the proposed approach to detect as many vessels as presented in the image. A higher sensitivity normally implies a better distal end detection of the coronary arteries. The sensitivity of every dataset is reported in the first column of Table 3 and the average sensitivity over all 18 datasets is 89.63% with a standard deviation of 4.42%.

We then evaluate the specificity by calculating 100% minus the percentage of contours which exist in the automatic segmentation, but not in the manual segmentation (false positives), among the total number of contours in the automatic segmentation:

$$Specificity = \left(1 - \frac{\text{number of contours in auto, but not in manual}}{\text{total number of contours in auto seg.}} \right) \times 100\%. \quad (33)$$

The specificity evaluates the occurrence of false positive detections, usually due to a contour leakage or the pick-up of bright noise. In rare occasions the false positive detection is due to the better sensitivity of the automatic segmentation than the manual segmentation, where a true vessel contour is missed by the manual segmentation, but was detected by the automatic approach. The specificity of every dataset is

reported in the second column of Table 3. The average specificity over all 18 datasets is 94.51% with a standard deviation of 3.33%.

The third and fourth measures focus on the detailed comparison between each contour pairs in the automatic and manual segmentation. For these two measures we compare all true positive vessel contours (overlapped contours) in every dataset by calculating their mean distance error and maximum distance error.

To calculate the distance between two contours, a set of discrete points are first generated using Matlab function *contourc* to represent the zero-level set contour on each slice, and then a distance map is calculated using function *bwdist* from the manual segmentation mask. Each zero-level set contour point corresponds to a point in the manual segmentation distance map, which gives a distance from this point to the manual segmentation contour. All distances from the zero-level set contour points to the manual segmentation contour are calculated, and the mean and maximum distances are recorded. For each dataset a mean distance error (MDE) and a mean maximum distance error (MMDE) are then calculated over all true positive contours in this dataset. The results are shown in the last four columns of Table 3 in terms of *pixel* and *mm*. The mean MDE over all 18 datasets is about 0.7 pixels, which is $0.2676mm$ and the MMDE is about 3 pixels, which is equivalent to $1.1225mm$ in distance.

We also recorded the computation time for each datasets in Table 4. The time for computing the heart mask and performing the vessel filtering are recorded as a whole, and the BDIS segmentation is recorded separately. It is observed that the heart segmentation and vessel filtering, which on average takes 4.0754 minutes, takes significantly longer time than the BDIS segmentation, which on average only takes 0.7372 minutes. The average total computation time is 4.8126 minutes. The last two columns of Table 4 recorded the number of branches extracted by the proposed method. On average, about four branches are extracted for LCA and 2 for RCA,

Table 3: Segmentation results and validation for 18 datasets. Part II - Quantitative comparison between automatic and manual segmentation. (¹MDE - Mean Distance Error, ²MMDE - Mean Maximum Distance Error)

Data	Sensitivity (%)	Specificity (%)	MDE ¹ (<i>pix</i>)	MDE (<i>mm</i>)	MMDE ² (<i>pix</i>)	MMDE (<i>mm</i>)
#1	88.38	94.62	1.3714	0.5357	4.0953	1.5997
#2	91.37	97.94	1.2229	0.5971	3.3384	1.6301
#3	85.51	92.52	1.0612	0.4332	5.2635	2.1486
#4	86.65	90.89	0.8824	0.3223	3.6074	1.3175
#5	92.28	87.77	0.8904	0.3426	3.6258	1.3951
#6	80.69	94.74	1.0266	0.3830	3.7691	1.4060
#7	91.16	99.22	0.2639	0.1289	1.5152	0.7398
#8	91.09	95.64	0.8040	0.2748	4.1167	1.4071
#9	94.77	98.53	0.7405	0.2603	2.9240	1.0280
#10	86.55	98.95	0.2586	0.0778	2.2053	0.6633
#11	90.32	91.71	0.3004	0.1015	2.1607	0.7301
#12	95.51	93.06	0.6657	0.1924	2.5847	0.7472
#13	92.80	97.18	0.3641	0.1045	2.2855	0.6562
#14	90.29	96.77	0.1955	0.0645	1.6957	0.5597
#15	97.88	93.75	0.2864	0.1018	2.1420	0.7614
#16	89.84	94.35	0.7392	0.3104	3.5282	1.4816
#17	81.04	95.55	0.8302	0.3519	2.6422	1.1198
#18	87.24	88.02	0.7079	0.2337	2.4631	0.8130
mean	89.63	94.51	0.7006	0.2676	2.9979	1.1225
±std	±4.42	±3.33	±0.3453	±0.1535	±0.9545	±0.4322

Table 4: Segmentation results and validation for 18 datasets. Part III - Computation time and number of branches segmented. Tested using Pentium(R) 4 CPU 3.60 GHz, 2.00 GB of RAM, in Matlab. (¹ Heart & VF: Heart segmentation and Vessel Filtering)

Data	Time (<i>min</i>) Heart & VF ¹	Time (<i>min</i>) 3D BDIS	Total time (<i>min</i>)	# LCA branches	# RCA branches
#1	4.4748	0.7775	5.2523	4	1
#2	2.5555	0.4960	3.0515	5	2
#3	4.0234	0.7958	4.8192	5	2
#4	4.9977	0.9435	5.9412	5	2
#5	4.0139	0.7597	4.7736	5	2
#6	4.2829	0.7540	5.0369	4	3
#7	1.7246	0.2770	2.0016	3	1
#8	4.2718	0.7826	5.0544	4	2
#9	4.5916	0.8981	5.4897	6	2
#10	4.3990	0.7193	5.1183	4	3
#11	4.5176	0.7417	5.2593	4	3
#12	3.1602	0.6573	3.8175	4	3
#13	3.9819	0.8621	4.8440	5	2
#14	4.3337	0.7182	5.0519	4	1
#15	4.9690	0.8442	5.8132	5	2
#16	4.8225	0.7320	5.5545	5	2
#17	3.7319	0.6462	4.3781	4	2
#18	4.5058	0.8646	5.3704	3	3
mean	4.0754	0.7372	4.8126	4.3889	2.0556
±std	±0.8190	±0.1500	±0.9832	±0.7556	±0.7049

which represent the typical number of large branches on both sides.

With the above validation and evaluation results, we conclude this chapter where we presented a fully automatic approach for the segmentation of coronary arteries from contrast CTA images. The algorithm is mainly composed of three consecutive steps: lung and heart segmentation, vessel filtering, and BDIS segmentation. An additional effort was taken to deal with cases where calcified plaques present in the images. The proposed method is validated using 18 clinical datasets with a large variety of geometries. The result is quite encouraging, with the mean distance error

of well under one pixel, comparing to the manual segmentation result. The whole process for an image volume with an average size of $313 \times 362 \times 210$, which contains approximately 24 million voxels, takes well under 5 minutes to complete on a Pentium(R) 4 3.60GHz CPU with 2GB of RAM in Matlab.

The fully automatic segmentation can greatly assist clinicians in making diagnosis of coronary artery disease, by isolating the vessels from other irrelevant anatomical structures and visualizing the complete coronary tree from the proximal to distal end. The algorithm is developed in order to achieve an optimal performance, with current average sensitivity of 89.63 %, specificity of 94.51 % and pixel-wise accuracy of MDE = 0.7 pix. These quantitative results indicate that with minimal user adjusting and editing, the clinicians can obtain a 100 % satisfying result for diagnosis. Depending on the locations the discrepancies occur, some cases may not need to be further adjusted, since the discrepancy may not directly relate to any clinical significant segment of the vessels. For example, the sensitivity of the algorithm tends to decrease when approaching the distal end of the vessel; however, many critical lesions normally occur in the more proximal end instead of the very distal end of the vessels. Hence, this algorithm provides reasonably good results, which at least can serve as a good starting point for clinicians to efficiently explore the datasets, and make additional adjustments accordingly if necessary. The segmentation result also has the potential of being used for further measurement of significant parameters, as will be presented in the next chapter.

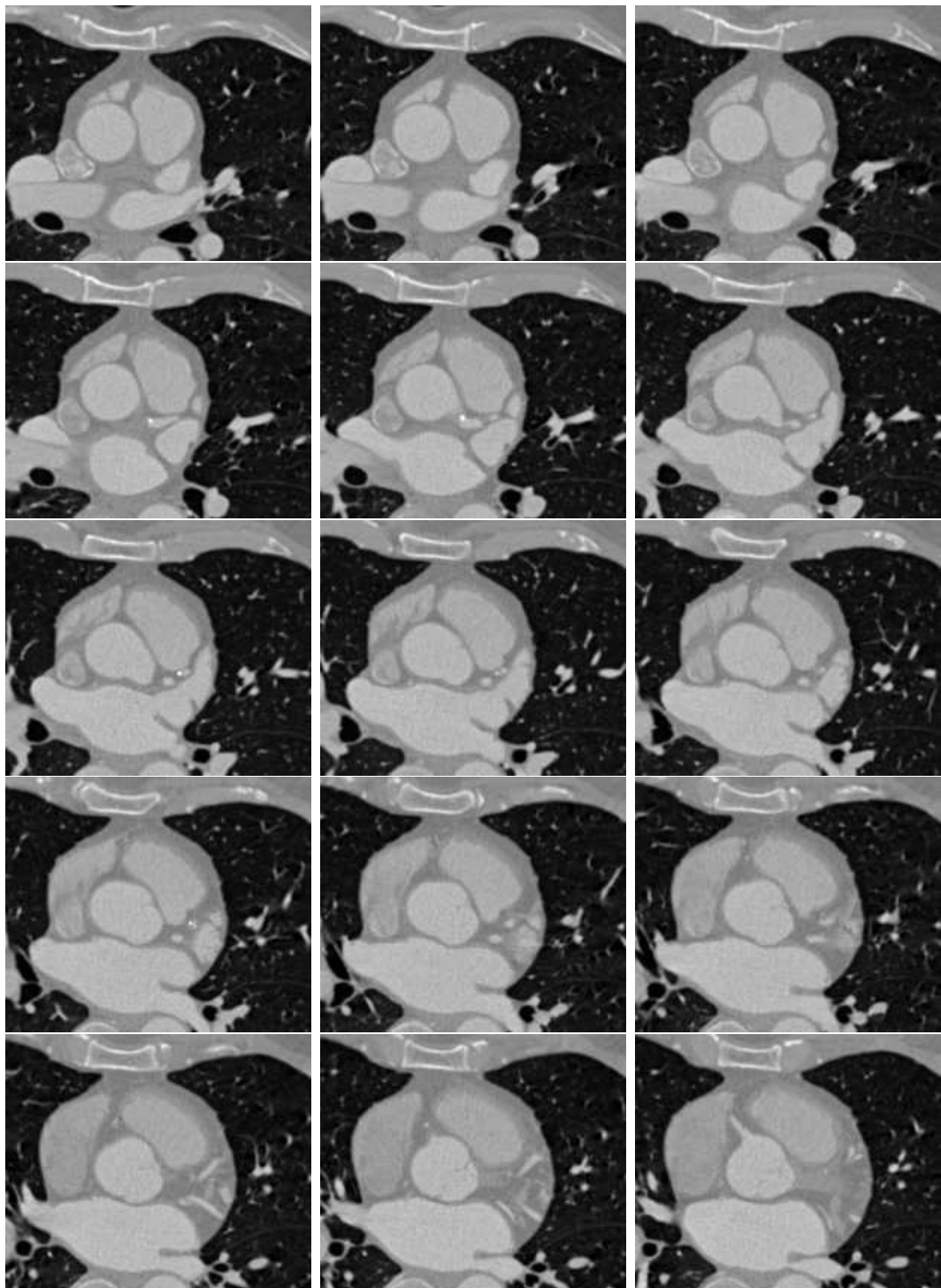


Figure 21: Original coronary artery CTA images, Dataset #1, Part I.

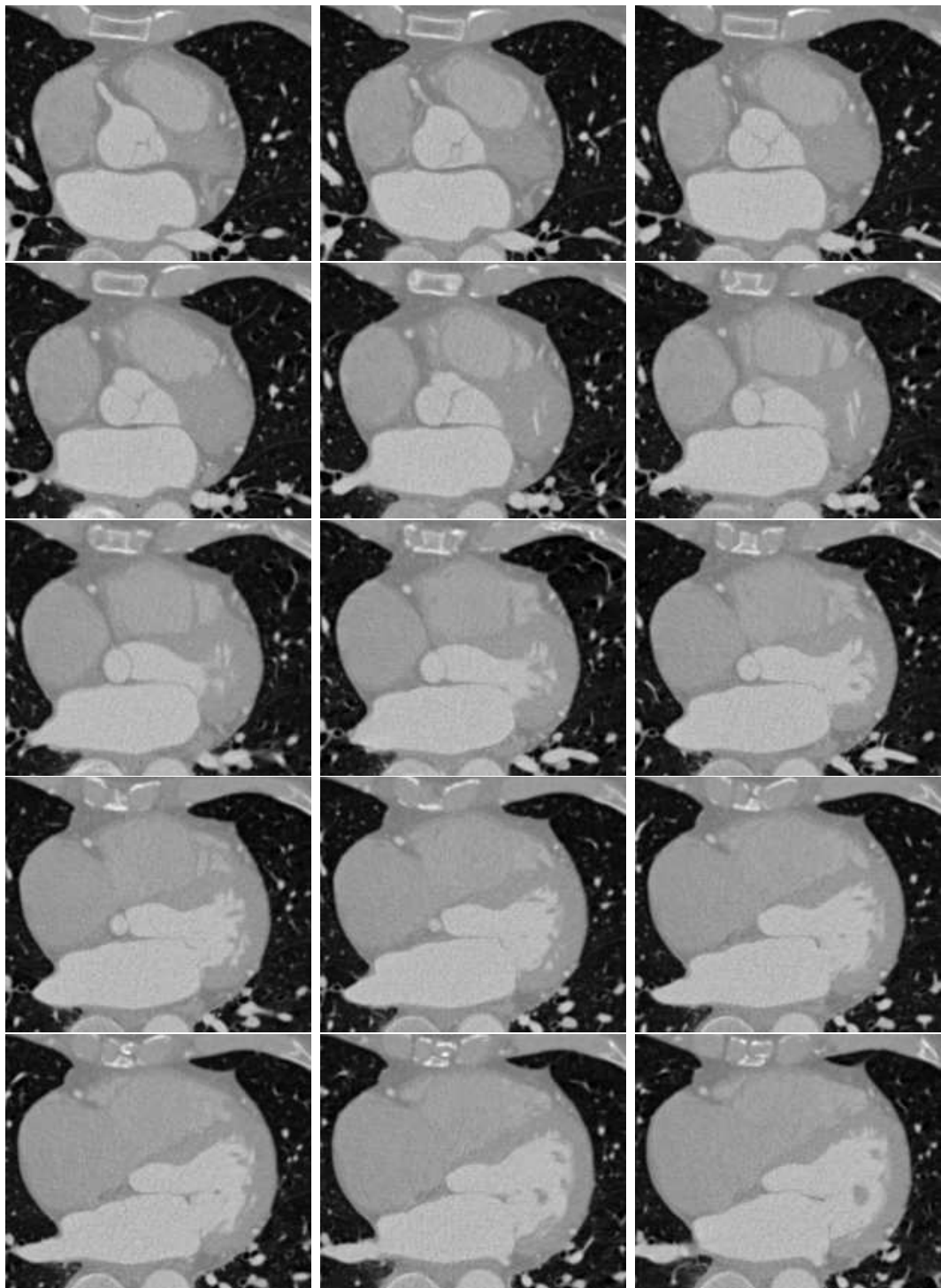


Figure 22: Original coronary artery CTA images, Dataset #1, Part II.

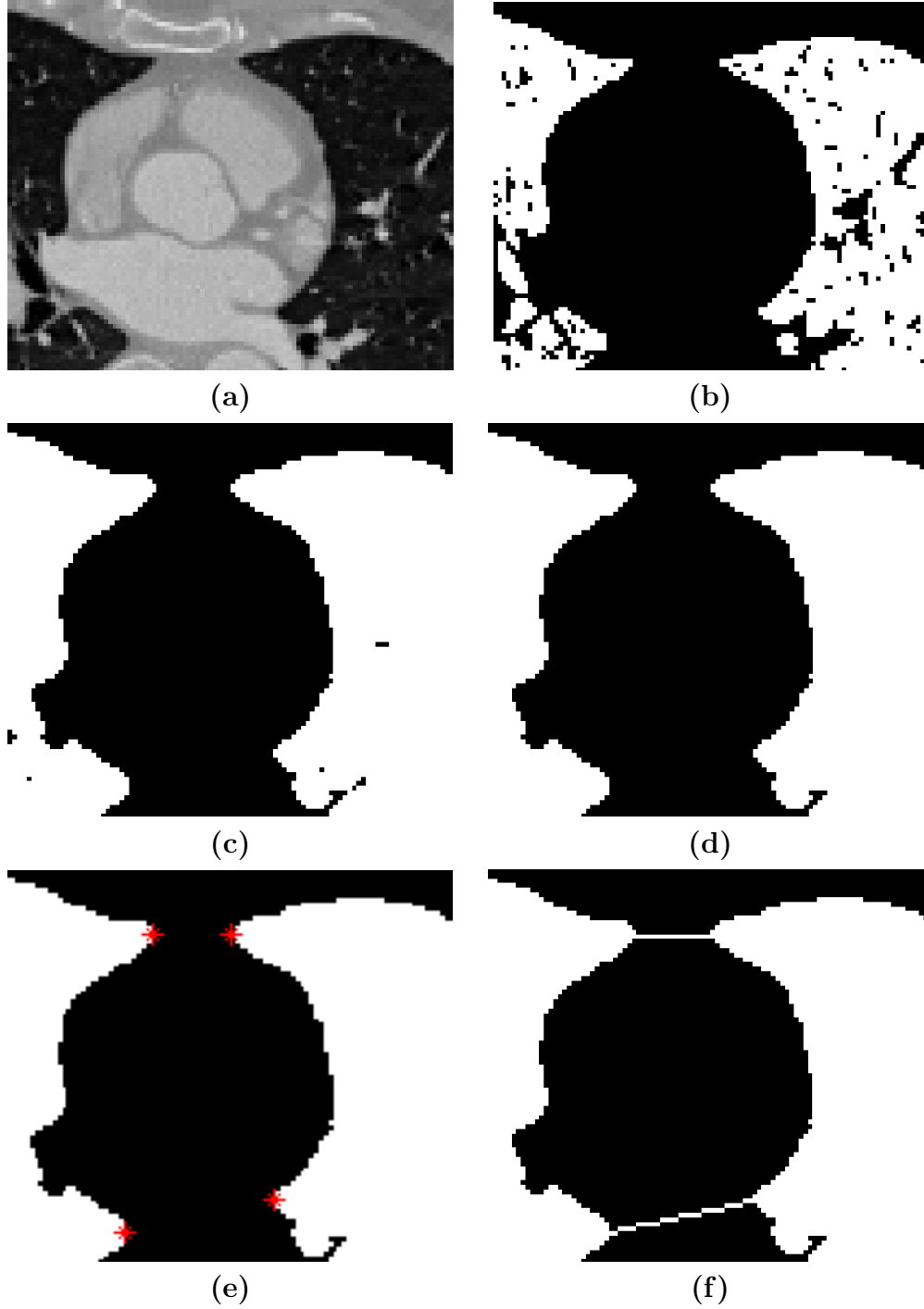


Figure 23: Lung and heart segmentation, Dataset #1, Part I. (a)→(b) thresholding, (b)→(c) dilation, (c)→(d) hole filling, (d)→(e) tipping point detection, (e)→(f) Bresenham lines. See text for details.

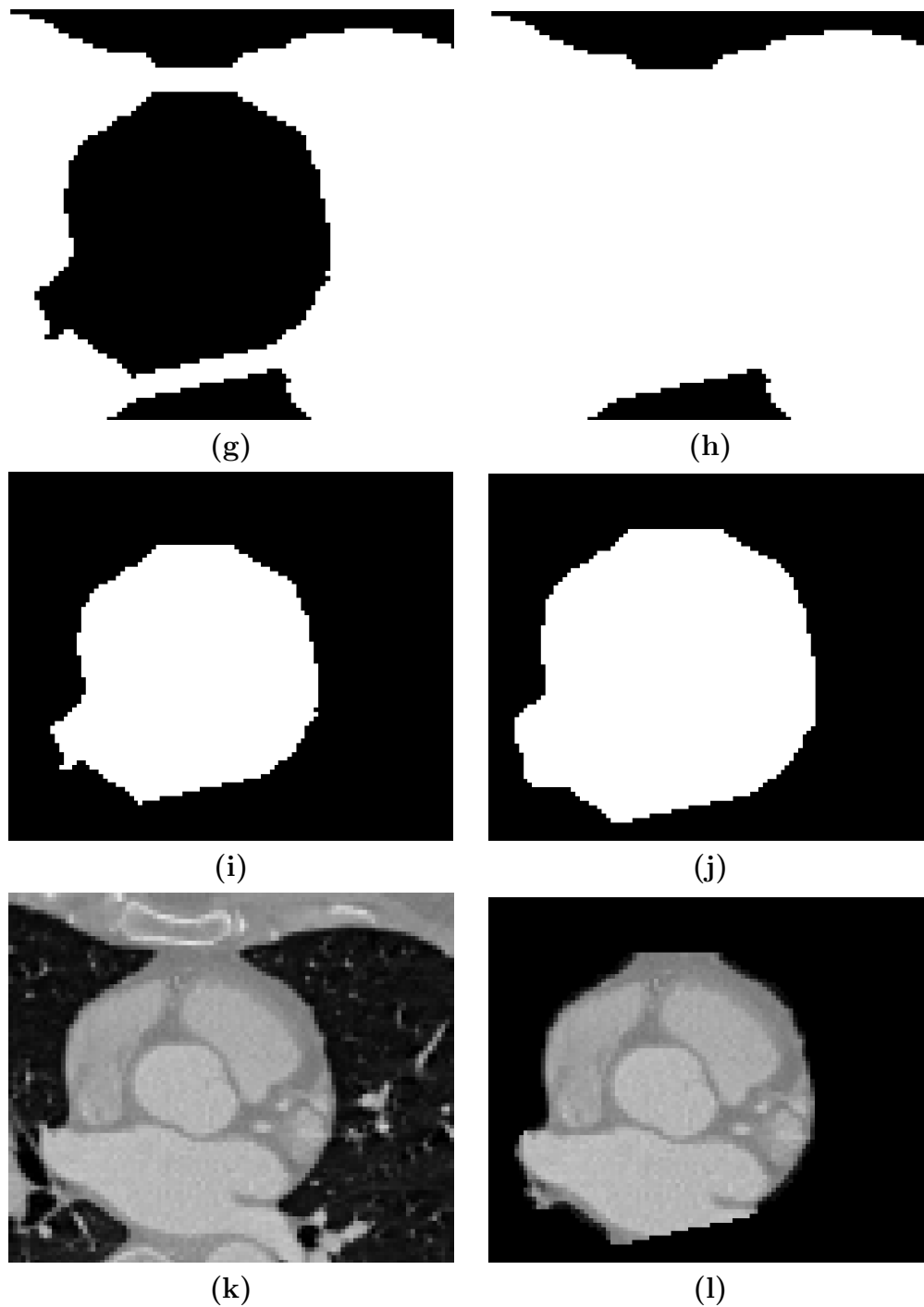
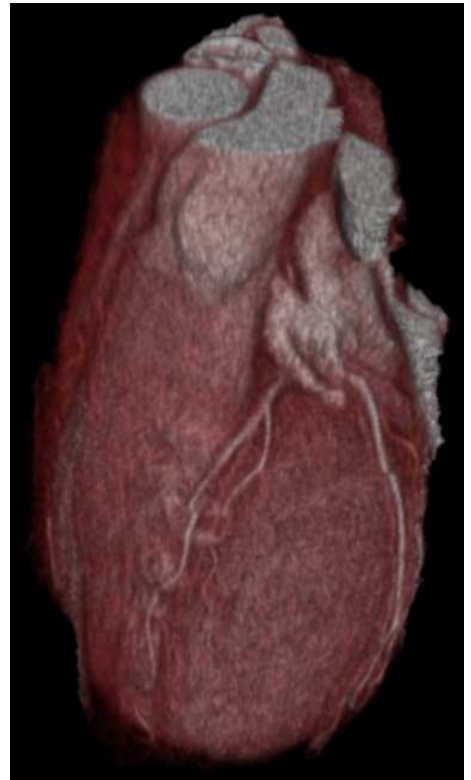


Figure 24: Lung and heart segmentation, Dataset #1, Part II. (f)→(g) dilation, (g)→(h) hole filling, (g)&(h)→(i) subtraction, (i)→(j) dilation, (k) Original image, (l) masked image. See text for details.



(a)



(b)

Figure 25: Volume rendering of the images before (a) and after (b) heart segmentation. Dataset #1.



(a)



(b)

Figure 26: Volume rendering of the images before (a) and after (b) vessel filtering. Dataset #2.



Figure 27: The output of vessel filtering as iso-surfaces. Dataset #2.

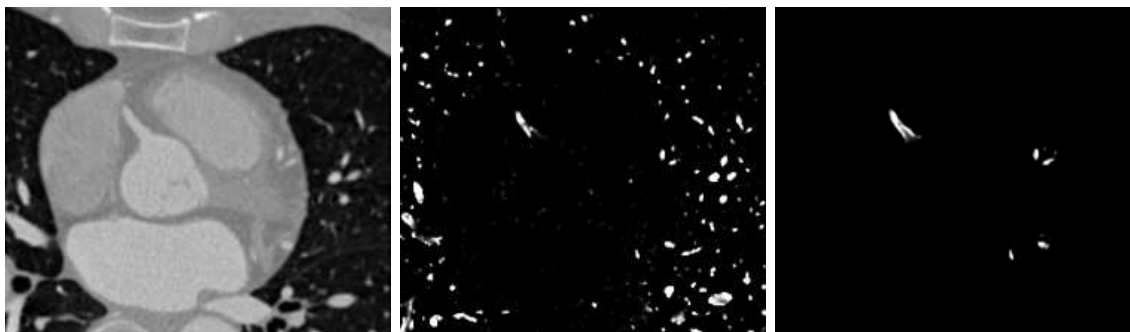


Figure 28: Comparing vessel filter response with and without heart segmentation. Dataset #1. Left: original image, Middle: result of applying the filter on the original image, Right: result on pixels within the heart mask.

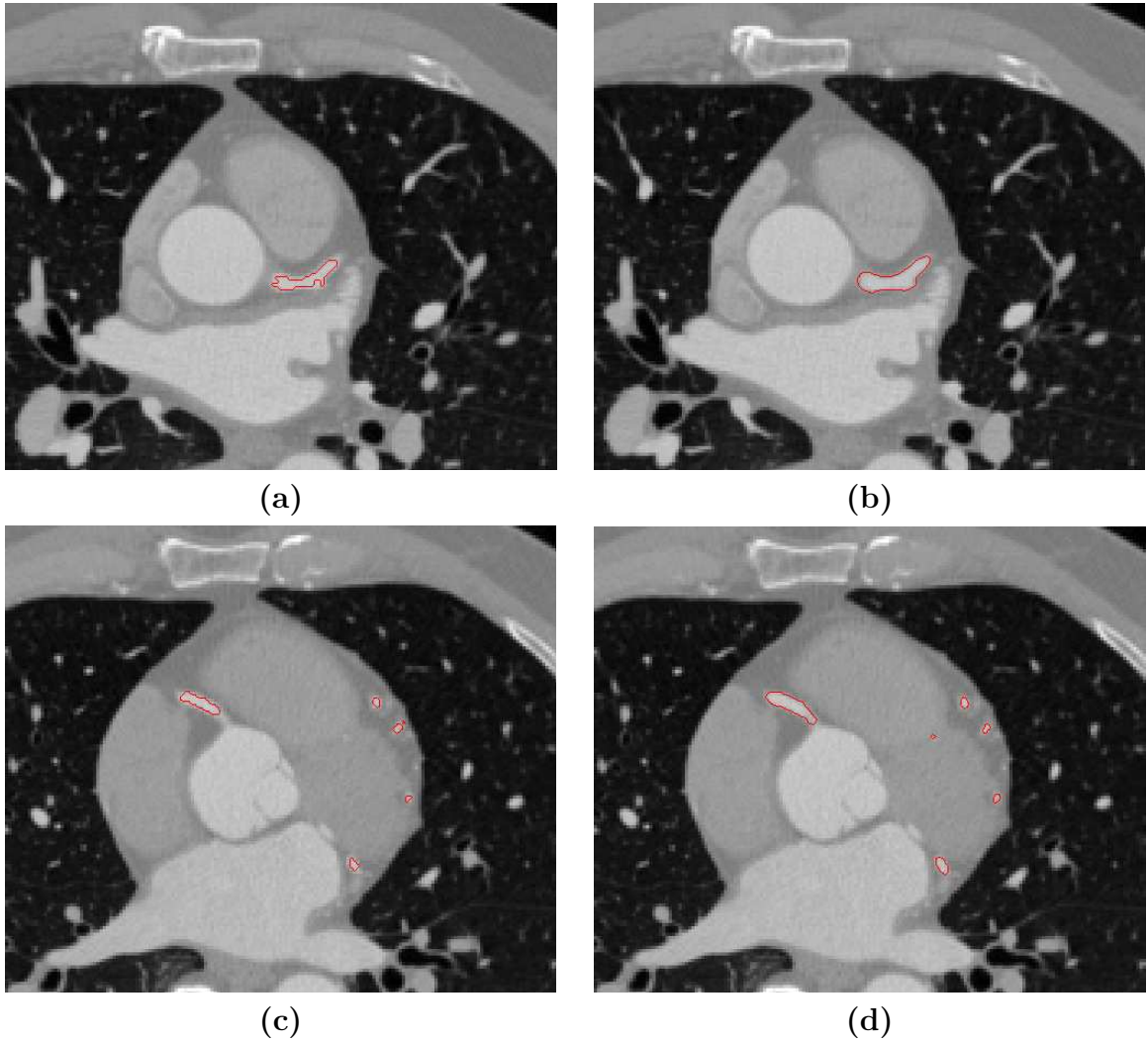


Figure 29: Comparing segmentation contours before and after BDIS. Dataset #2. (a) Initial contour on slice #6, (b) BDIS result on slice #6; (c) Initial contour on slice #23, (d) BDIS result on slice #23.

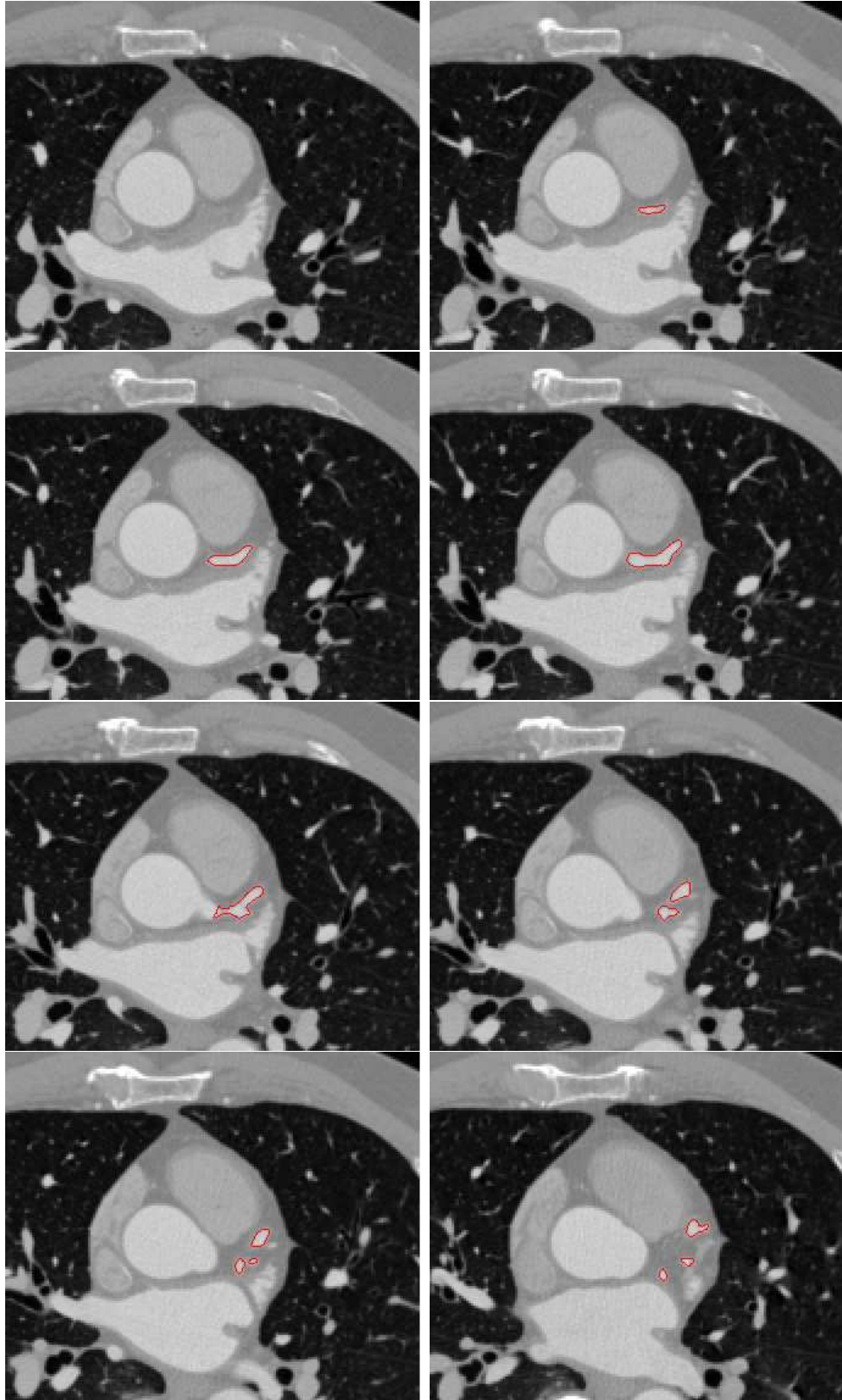


Figure 30: Segmentation results shown in 2D as contours. Dataset #2, Part I.

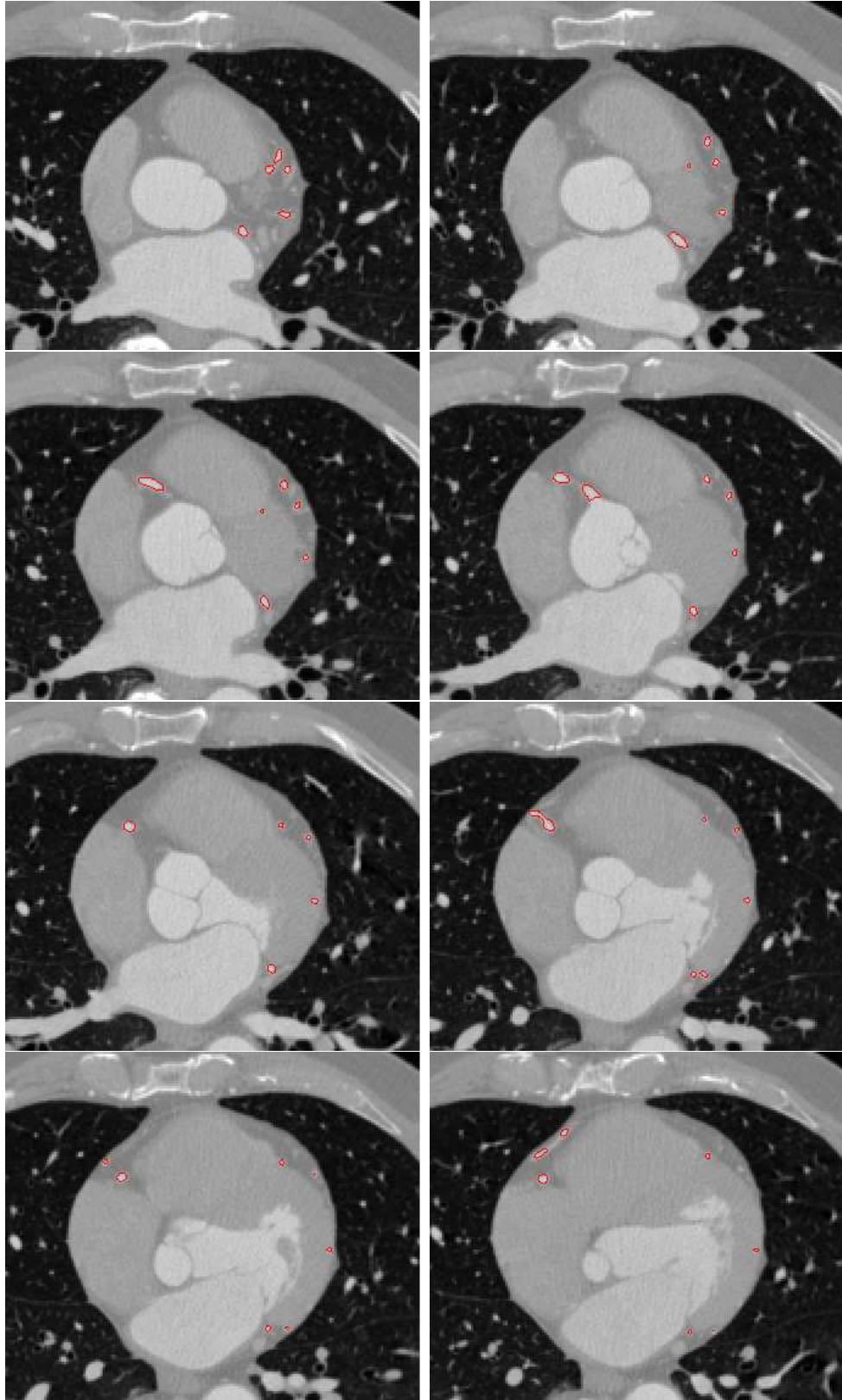


Figure 31: Segmentation results shown in 2D as contours. Dataset #2, Part II.

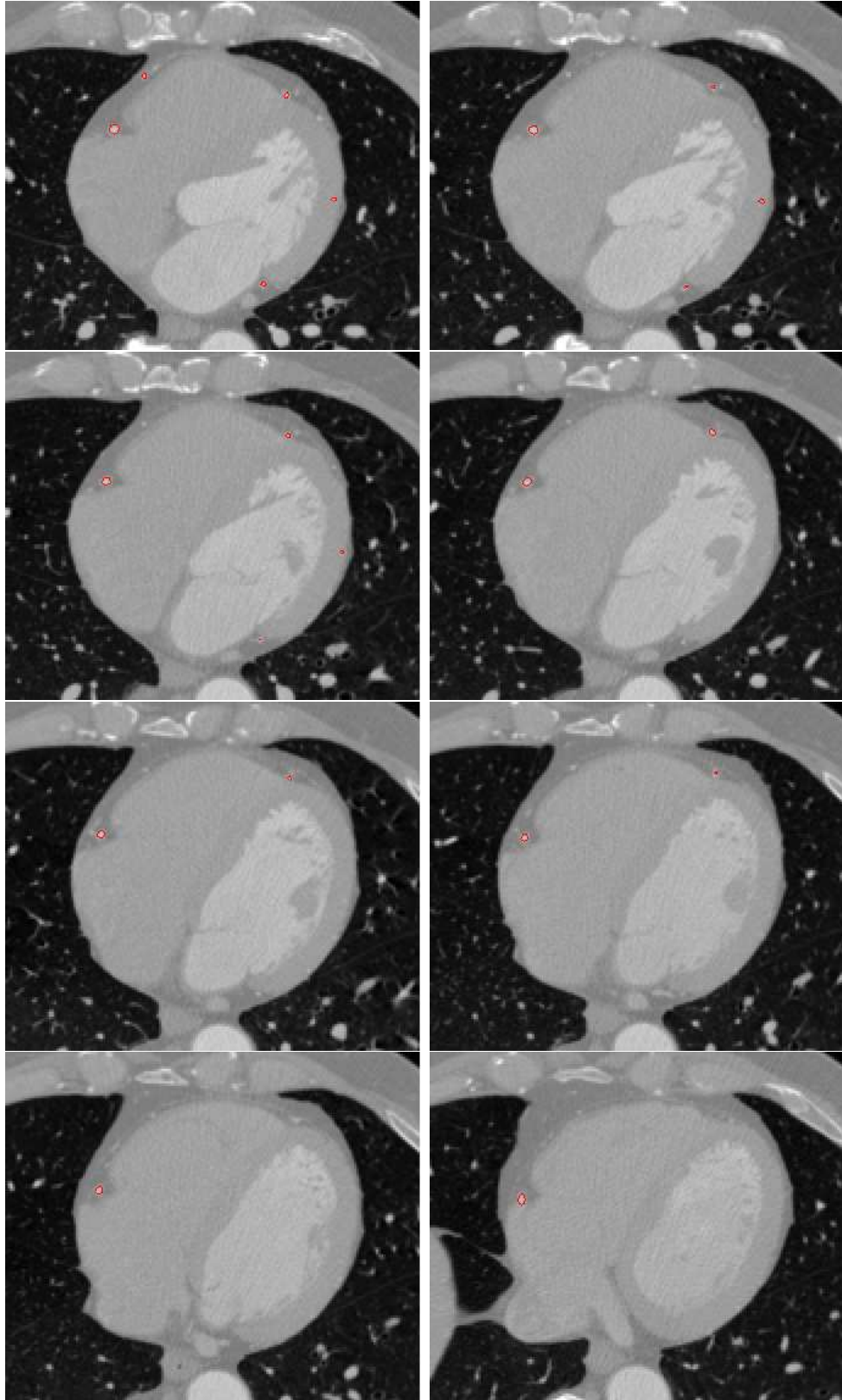


Figure 32: Segmentation results shown in 2D as contours. Dataset #2, Part III.

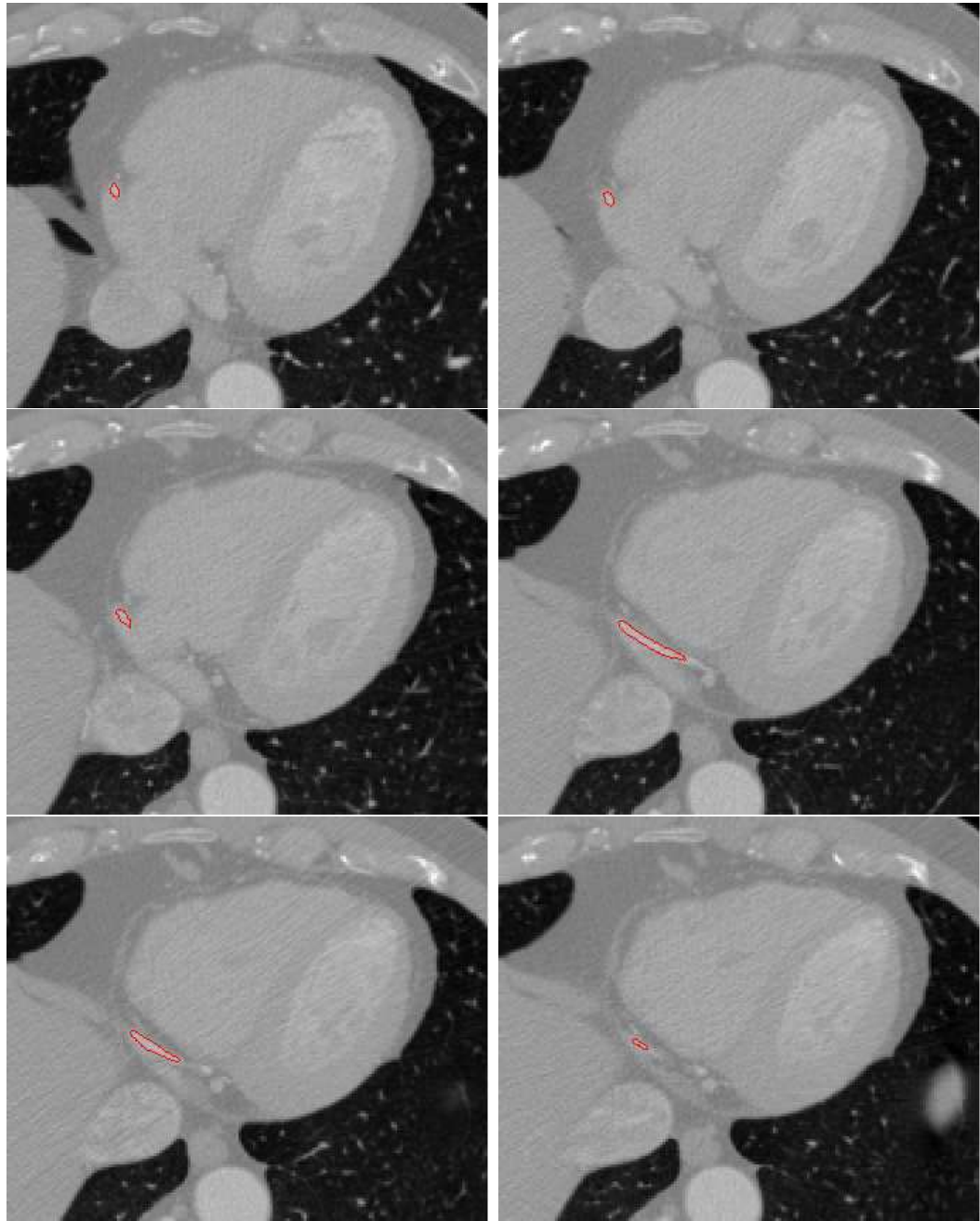


Figure 33: Segmentation results shown in 2D as contours. Dataset #2, Part IV.

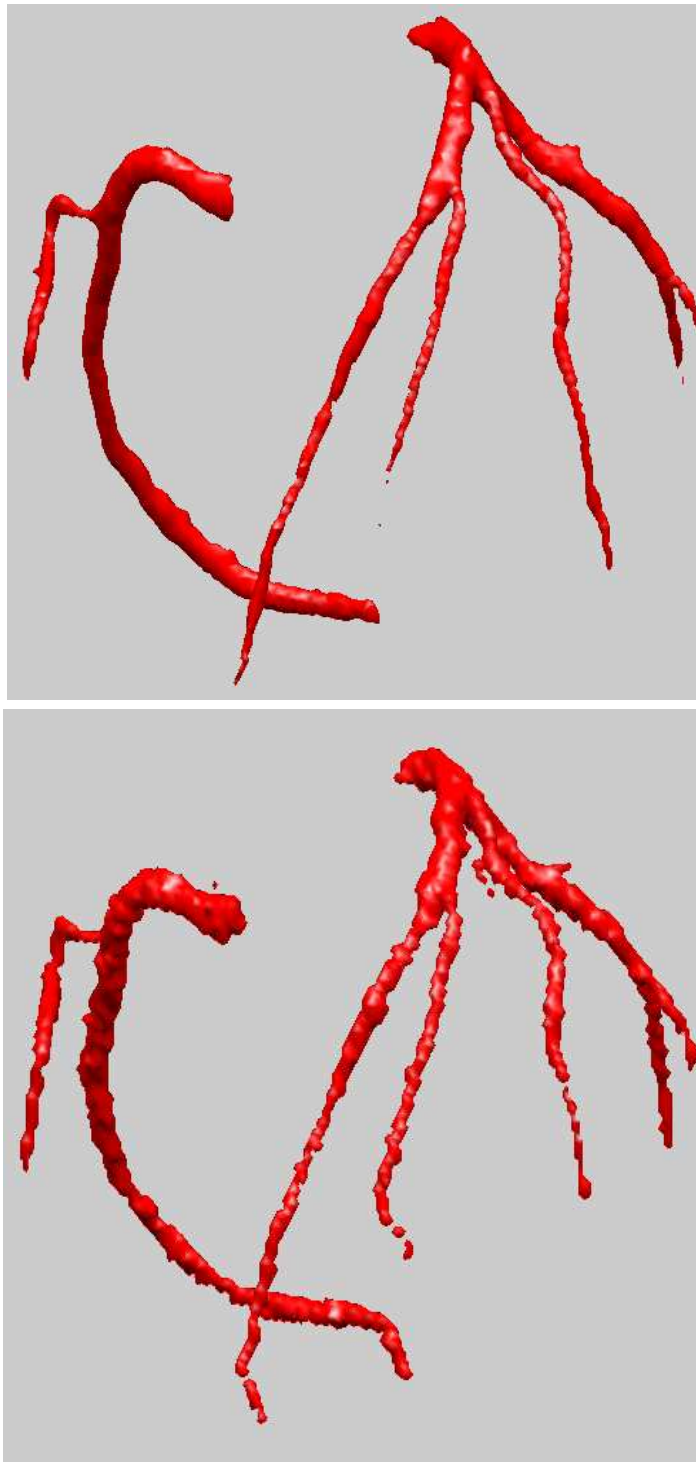


Figure 34: 3D results. Left and right coronary arteries rendered as surfaces. Upper: Automatic BDIS segmentation; Lower: Manual delineated contours rendered as surfaces.

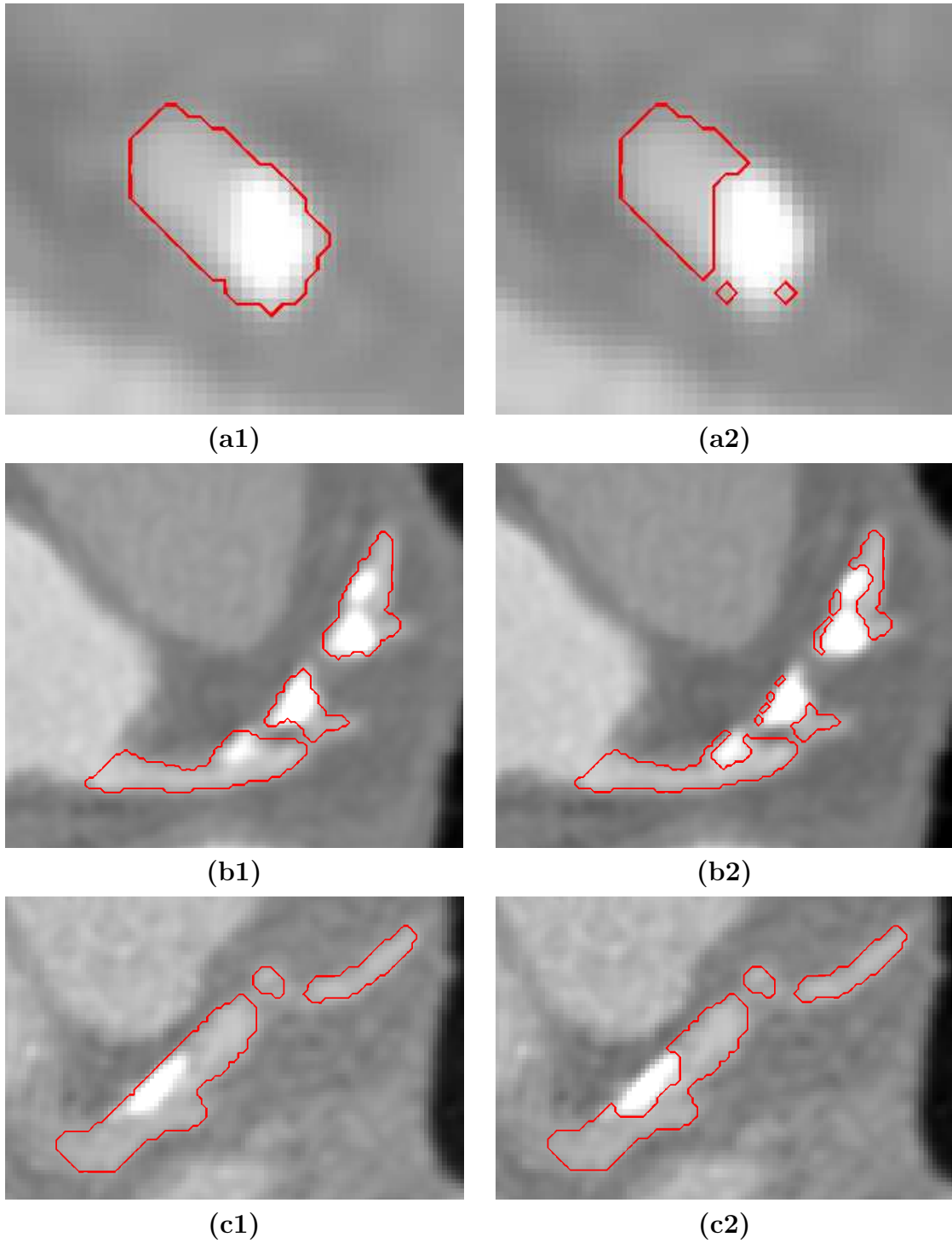


Figure 35: Removing calcified plaques from the segmentation. (a1) and (a2): before and after removing the calcium on Slice #34 of Dataset #8; (b1) and (b2): Slice #8 of Dataset #15; (c1) and (c2): Slice #6 of Dataset #16.

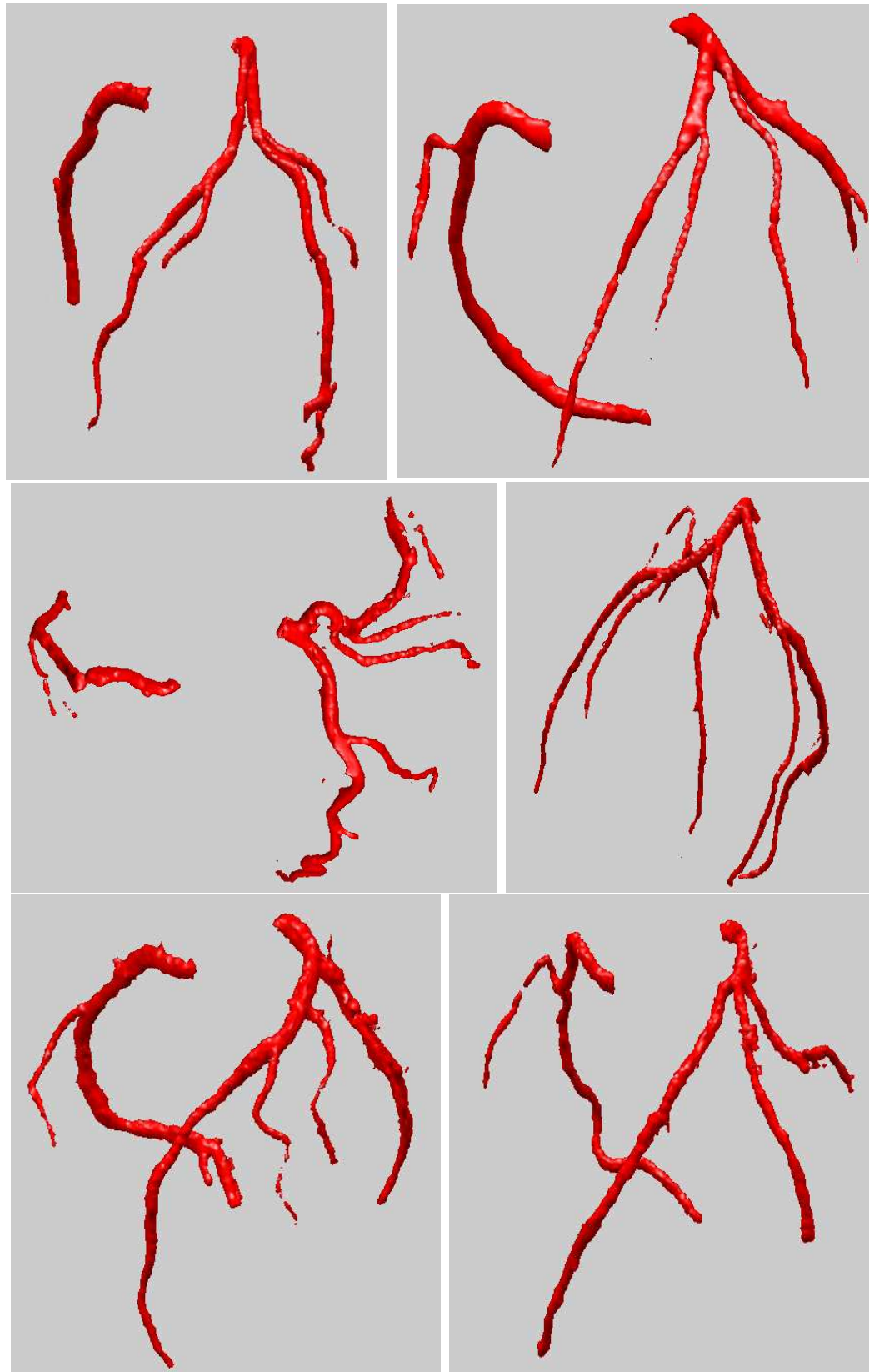


Figure 36: BDIS segmentation results shown as surfaces. Part I. Datasets #1 - #6.

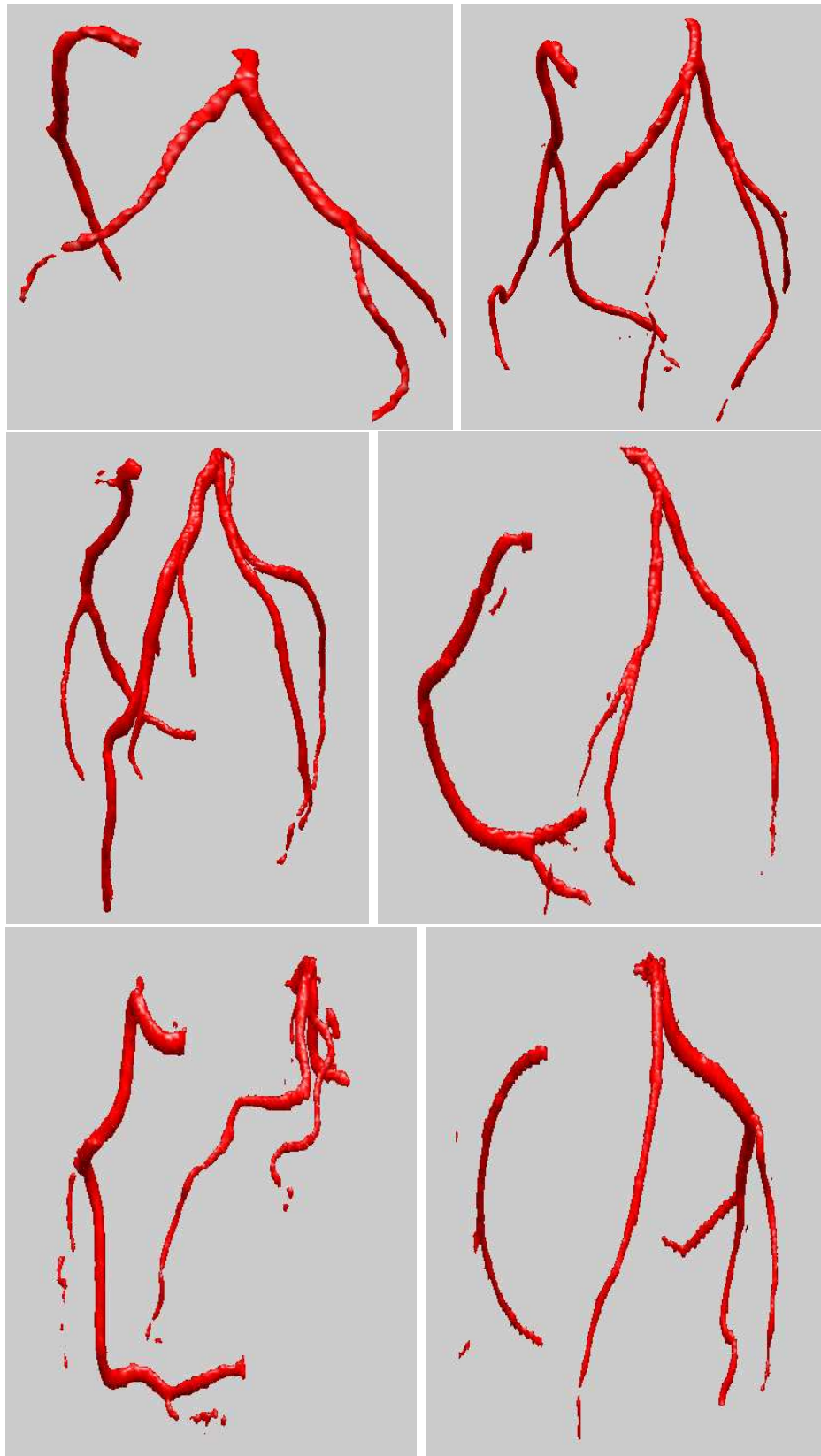


Figure 37: BDIS segmentation results shown as surfaces. Part II. Datasets #7 - #12.

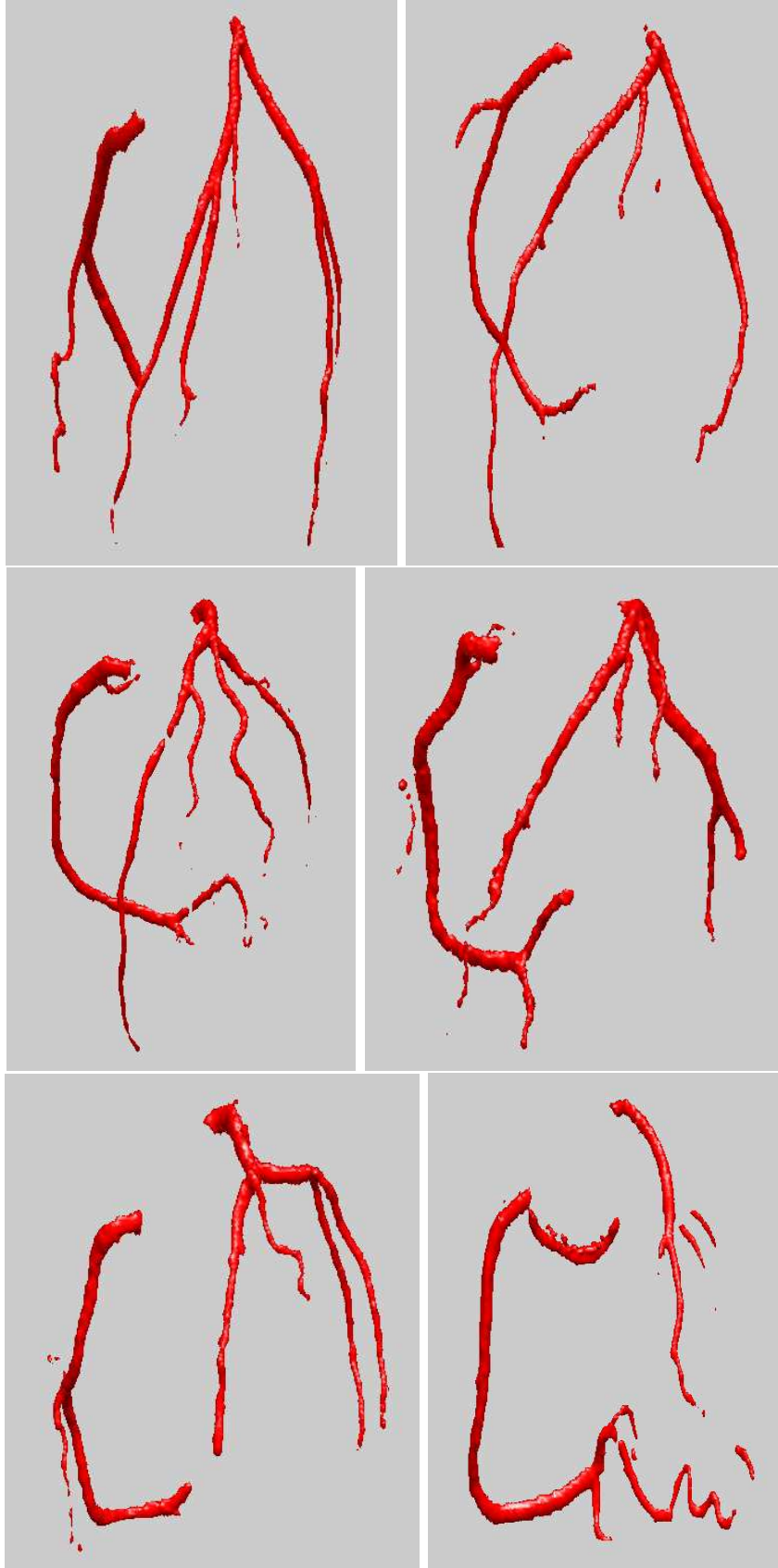


Figure 38: BDIS segmentation results shown as surfaces. Part III. Datasets #13 - #18.

CHAPTER V

CENTERLINE EXTRACTION AND STENOSIS EVALUATION FOR CORONARY ARTERIES

In this chapter, we present a centerline extraction (skeletonization) approach for triangulated surfaces of 3D tubular structures. In our application of coronary artery analysis, we use the segmented surfaces obtained in the previous chapter as the input to the skeletonization method presented in this chapter. These two chapters bind naturally to provide a complete tool set for coronary CTA analysis. In addition, the “harmonic skeletonization” approach proposed here also provides orthogonal cutting planes located at each centerline point, and thus offers a convenient way to measure cross-sectional areas of the vessels, which is an important indicator of coronary stenosis.

We first describe and explain the algorithms in Sections 5.1 and 5.2, and then further test and validate the method using a digital phantom and real clinical datasets in Section 5.3.

5.1 Harmonic Skeletonization

The harmonic skeletonization is a centerline extraction method based on the solution of the Laplace equation with boundary conditions of the first kind (Dirichlet problem) on the surface of a tubular structure. Since the solution of the Laplace equation is a harmonic function, the skeleton extracted using this method is called the *harmonic skeleton* [110]. The harmonic skeleton is easy to compute, is guaranteed to be smooth, and can automatically give a viewing vector when used as a guidance for fly-throughs for virtual endoscopy. Moreover, the space of harmonic functions is linear (as opposed

to that of the distance transform on which the ordinary skeleton is founded).

An effective way to determine the boundary conditions for solving the appropriate Laplace equation is proposed here, so that the points that form the final skeleton are evenly distributed, without being too dense or too sparse, thus guaranteeing the connectivity of the skeleton. Then, the cross-sectional area at a certain location on the artery can be conveniently measured using the least squares plane that fits all the points on the iso-value contour of the solution of the Laplace equation. This means that we can acquire the cross-sectional areas throughout the artery in order to identify stenoses.

The harmonic skeleton can be obtained by solving the Laplace equation on the surface of the artery. Let Σ denote the surface, which is topologically a branched tube. Each branch has a boundary σ_i ($i = 0, \dots, N - 1$), which is a closed contour, as shown in Figure 39 in blue. Here N denotes the total number of boundaries including the root σ_0 , which can be selected arbitrarily or selected based on physiological considerations. We have chosen the root σ_0 to be at the proximal section of the left main (LM) coronary artery. Note that the initial segmented surface is normally a closed surface and here we use these boundary contours to cut the branches in order to create open-ended tubes for our computation.

Next we can calculate the harmonic function u by solving the Laplace equation on $\Sigma \setminus \sigma_i$ ($i = 0, \dots, N - 1$):

$$\Delta u = 0, \tag{34}$$

with proper boundary conditions. To find these boundary conditions, we assign the values at the boundaries in the following manner:

1. Set the boundary value of u at the root σ_0 to be zero, and set *StepNumber* = θ ;
2. Label all the points on σ_0 as “visited”;
3. Label all the neighbors of the “visited” points as “visited”;

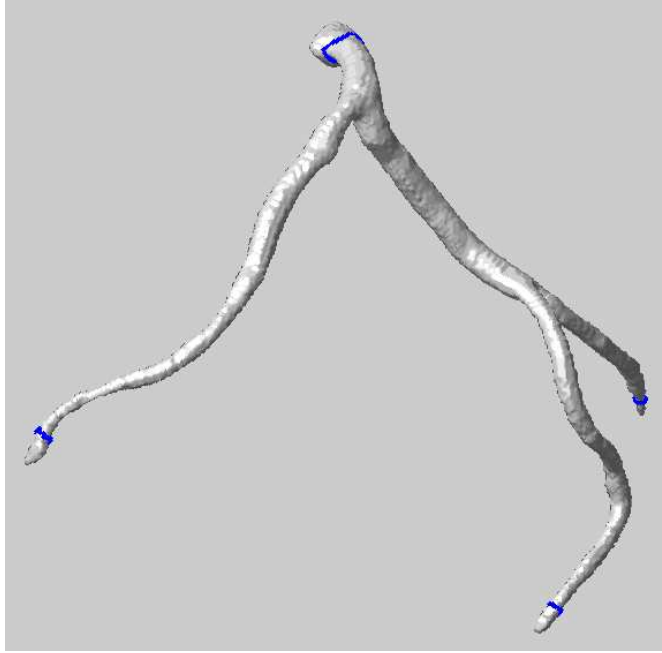


Figure 39: The segmented surface of left coronary arteries with boundary contours shown in blue at each end. Dataset #7.

4. $StepNumber ++$;
5. Repeat steps 3. and 4. until “visited” points reached another boundary σ_i ;
6. Set the value at the current boundary σ_i to be the current value of $StepNumber$.

In other words, we set the boundary value of σ_i to be the number of triangle strips between σ_i and the root boundary σ_0 . In coronary arteries, there are several branches, some of which are long and some of which are short. Note that if we used standard Dirichlet boundary conditions in which $u(\sigma_0) = 0$ and $u(\sigma_i) = 1$ for all i 's, as for example, is done in [104], the resulting points that form the skeleton will be denser for the short branches, and sparser for the longer ones. Hence, we employ the boundary conditions stated above to obtain more evenly distributed skeleton points.

Having obtained the boundary conditions for the Dirichlet problem, we can solve the Laplace equation $\Delta u = 0$ on the surface using finite element techniques [31, 39]. From the standard theory [22], u exists and is unique, with the maximum and minimum values on the boundaries. In Figure 40, the surface of the artery is painted

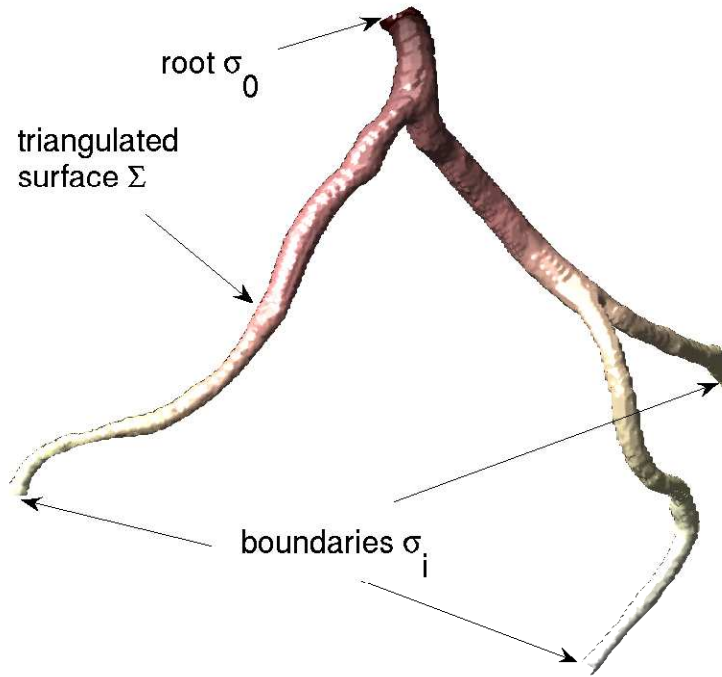


Figure 40: The coronary artery surface is color-painted with solved harmonic function u , where dark color means lower u , and light color means higher u . Dataset #7.

with the solved u , where brighter color indicates higher u , and darker color indicates lower u .

Using the harmonic function u , we can now build the harmonic skeleton. We first find the level sets of u on the surface, i.e., sets $\{x|u(x) = \nu\}$ for values of ν ranging from 0 to $\max(u)$. Each level set corresponds to a group of points on the surface which have the value of a certain ν . These points are not necessarily located on the vertices of our original triangulation of the surface, so we obtain these level points by linearly interpolating the coordinates of the vertices according to the values of u .

We also check the change in the topology of the level contours as we proceed, and further partition these contours into sub-contours if not all the points are connected to form a single contour. This means there is a bifurcation and one contour splits into two at the current level of u . We assume one contour cannot split into more than

two contours, which is true for coronary arteries in most cases. The centroid of each contour or sub-contour is then calculated:

$$\frac{1}{M} \sum_{i=1}^M \mathbf{x}_i,$$

where $\mathbf{x}_i = (x_i, y_i, z_i)'$ is a point on the contour, and M is the total number of points on the current contour. Each centroid contributes a point to the final harmonic skeleton. By increasing ν from 0 to the maximum value of u , we can find a series of centroids that can finally be connected to build a structured tree, which is the harmonic skeleton.

Figure 41 demonstrates the above procedure by showing a series of level contours (in blue) on the surface and the centerline (in red) achieved from the centroids of these level contours. As the algorithm runs, the contours and center points are generated from a lower level of u to a higher level, which is equivalent to the situation from top to bottom in this example. Notice that only a portion of the level contours are shown here for visualization. In fact, if all the contours are visualized, the surface will be covered completely with these contours.

5.2 Cross-sectional Area Measurement and Stenosis Detection

The harmonic skeleton obtained using the above method can be used as a guide in calculating cross-sectional areas at specific locations along the vessels, and the cross-sectional areas can in turn be used to precisely evaluate stenoses in the coronaries. Cross-sectional areas are better than diameters because atherosclerotic plaques are usually eccentric and asymmetric as we have introduced in Chapter 1, and the cross-sections of the narrowed vessel lumen may not be circular. The stenosis may be underestimated if one uses only diameters for stenosis evaluation. Cross-sectional areas, on the other hand, provide more information about the stenosis, and are directly related to the flow rate of blood through the cross-section.

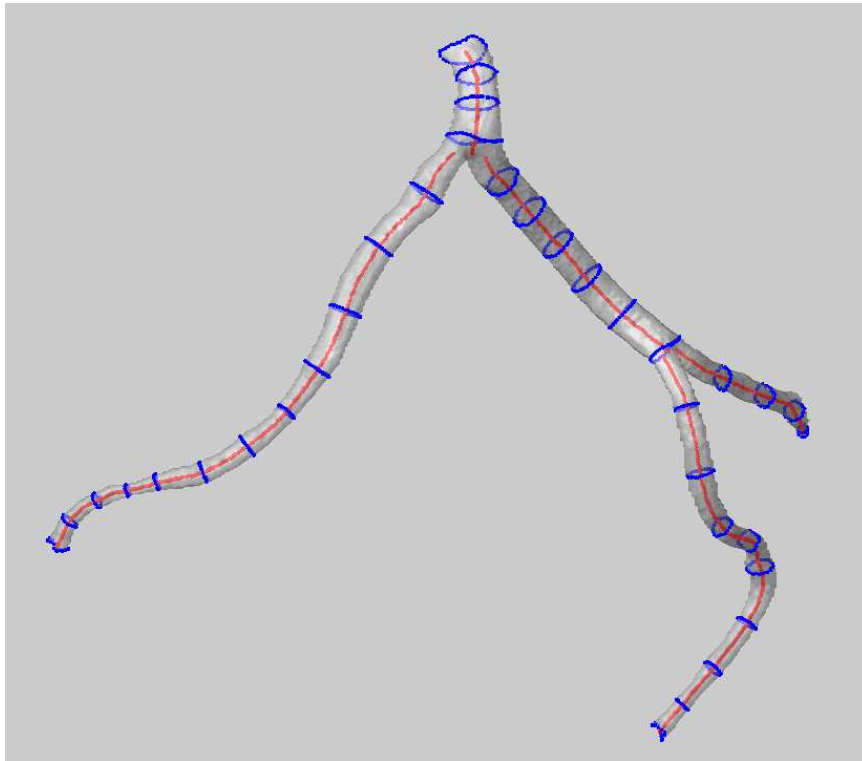


Figure 41: In blue: level contours of the harmonic function u . In red: vessel centerline formed by a series of centroids of the level contours. Dataset #7.

One straightforward way of obtaining the cross-sections of the artery is by looking for a plane that is perpendicular to the skeleton to cut the tube at a certain location. But this strongly depends on the local properties of the skeleton, and a plane that is perpendicular to the skeleton locally may not be perpendicular to the vessel itself. What we do here is to start with the contours or sub-contours obtained in the above section, and measure the cross-sectional area at the same time as we calculate the centroid. It can be seen from Figure 41 that the level contours already exhibit an orthogonal appearance to the vessels.

The first step is to find the cross-sectional plane. We have many more points (about 50 points, somewhat more for wider contours and somewhat less for narrower contours) on a level contour than are necessary (3 points) for determining a plane. Hence we need to use least squares to solve this over-determined problem. Suppose we have a set of points $X = (\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N)'$, where $\mathbf{x}_i = (x_i, y_i, z_i)'$, $i = 1, \dots, M$ is a point on the level contour, and we build a matrix $A = X - \mathbf{x}_0$, where $\mathbf{x}_0 = (x_0, y_0, z_0)'$ is the centroid of all the points on the contour. Calculating the Singular Value Decomposition (SVD) [71] of matrix A , we get $A = USV^T$, where U and V are orthogonal matrices and S is a diagonal matrix with non-negative diagonal entries in decreasing order. The singular vector in V that corresponds to the smallest singular value in S is the cosine of the direction of the normal to the best-fit plane. The centroid and the normal vector can now be used to uniquely determine the least squares plane.

We now use this plane to cut the surface of the vessel and obtain a series of points on the surface which also belong to the least squares plane. Again, these points may not coincide with the vertices of the triangulated surface, so we find the points on the triangle edges, and connect them to form a polygon. We then calculate the area of the polygon, and the result is the desired cross-sectional area at the current location on the vessel.

5.3 Results and Validation

In this section we present the results of applying the proposed method to a digital phantom and all clinical datasets which have been presented in the previous chapter. The results are validated quantitatively on the digital phantom to show the accuracy of our approach. On real clinical datasets, we first show the skeletonization results on the 18 clinical datasets, and then present two methods to visualize the cross-sectional area measuring results.

5.3.1 Digital Phantoms

We first test and validate our skeletonization and area measuring algorithm using a digital phantom simulating a stenosed vessel. The phantom is constructed from a series of images with a circle located at the center of each image. The radius of the circles is composed of five segments of 40 slices, first being a larger value (10 in pixel space), then gradually changing to a smaller value (5 in the pixel space) according to a sinusoid function, keeping the smaller value for 40 slices, gradually changing back to the larger value, and finally keeping the larger value for another 40 slices.

Each individual slice is added with Gaussian noise, and further blurred with a Gaussian kernel of size 7×7 with a standard deviation of 2. The volume rendering of the phantom images is shown in Figure 42 (Left).

Using Matlab function *isosurface* we generate a triangulated surface of the phantom, and the Laplace equation is then solved on this open-ended surface. Figure 42 (Middle) shows the solution u by representing different u values with different colors. The harmonic skeleton is then obtained and the cross-sectional areas are measured at the same time. Figure 42 (Right) is a similar figure to Figure 41 showing selected level contours of u (in blue) and the skeleton (in red).

We compared both the skeleton and the cross-sectional areas to the ground truth parameters, with which we have constructed the phantom. To compare the skeleton,

we calculate the distance from each skeleton point to the ground truth skeleton. The average distance error is 0.0788 pixel, which is 0.788% of the larger radius and 1.58% of the smaller radius.

We also compared the cross-sectional areas measured with our approach against the ground truth. The mean error over the whole phantom is 6.1842 *pixel*², which is 1.97% of the normal area, and 7.87% of the stenosed area. To further detail the quantification, we compared the difference at the normal area, which is 3.36%, and the stenosed area, which is 6.46%. In terms of vessel radius, the error is 0.1665 *pixel* at the normal site (with a true radius of 10 *pixel*) and 0.1643 *pixel* at the stenosed site (with a true radius of 5 *pixel*). Interestingly, we have observed that the automatic algorithm tends to overestimate the area of the normal segment of the vessel, but underestimate the area of the stenosed segment, which in turn will overestimate the degree of stenosis. This error is mostly due to the Gaussian smoothing of the original images and the isosurface step that follows.

5.3.2 Clinical Data

The proposed harmonic skeletonization and cross-sectional area measuring method is applied to all clinical datasets used in Chapter 4. The input is the triangulated surfaces obtained from the results of BDIS segmentation of the vessels. For the attributes of all datasets, see Table 2.

5.3.3 Generation of Harmonic Skeletons

We first present the results of harmonic skeletons of all 18 datasets. Figure 43, 44 and 45 show both semi-transparent surfaces of the vessels and the skeletons. The results are visually satisfying except for a few tiny isolated branches whose skeletons are missing in the results. This is due to the fact that our method is based on a singly connected genus zero triangulated surface, and these tiny branches are not topologically connected to the major vessels.

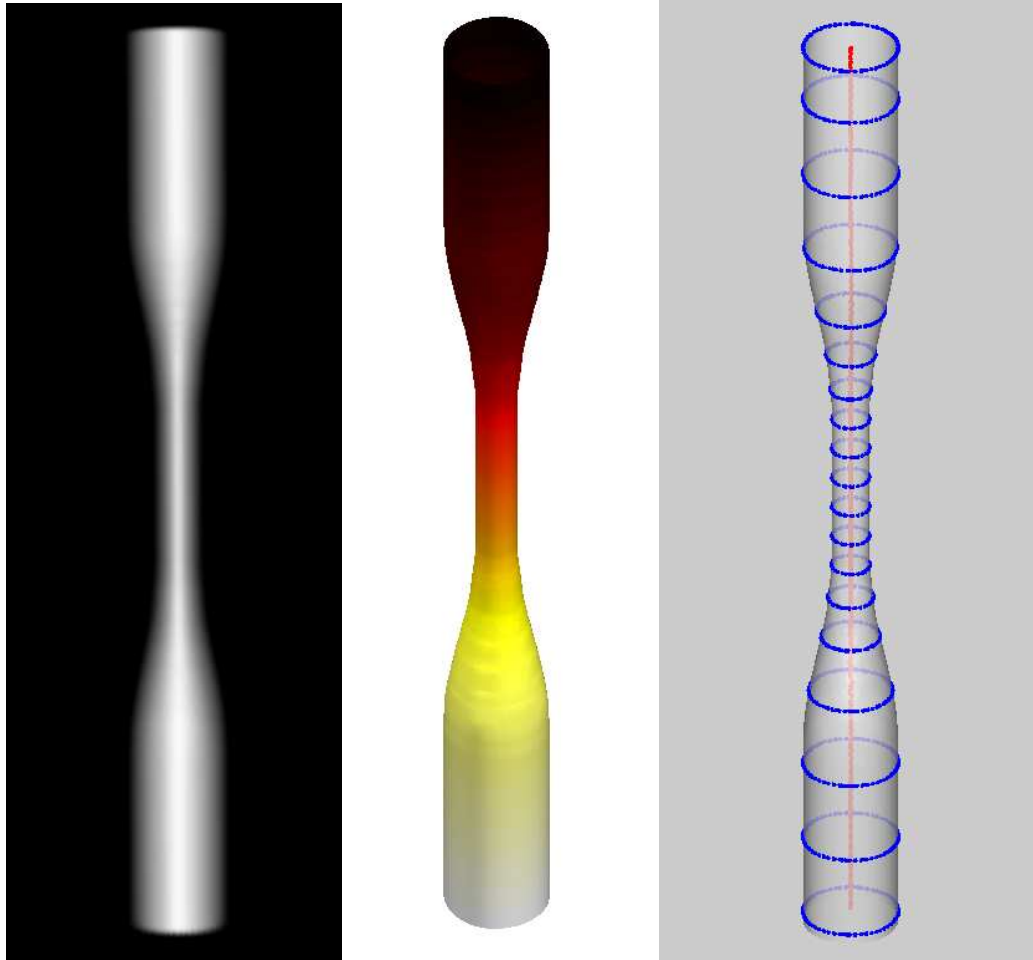


Figure 42: Digital phantom of a stenosed vessel. Left: volume rendering of the phantom; Middle: solved harmonic function u colored-painted on the surface; Right: selected level contours of u (in blue) and harmonic skeleton (in red).

At the bifurcation sites, some post-processing was performed to keep the skeleton smooth and natural. Increasing the value of u and tracking the topology change of the level contours, one contour will split into two at a certain u level, and there will be a jump between the centroid of the single parent contour and the centroids of the two daughter contours. If we connect the centroids directly, the resulting skeleton may not be smooth where it bifurcates. To solve this problem, we start from the daughter branches, and trace back until they reach the bifurcation site, and then extend the branches further until they meet the parent branch. After the post-processing, the skeleton is visually more natural at the bifurcation sites.

5.3.4 Stenosis Evaluation

The cross-sectional areas were calculated along the vessel with a resolution of $\delta u = 0.5$, which means we measure the cross-sectional area once we increase the harmonic function u by 0.5. For each coronary artery, there are roughly 400 levels of cross-sectional areas, and at each level, there are one or several cross-sectional areas measured according to the number of branches at this level.

We propose two methods to visualize the quantitative measurements and illustrate using two examples. The first is to specify a u value, which is equivalent to specifying a location on the vessel, and show the cross-sectional areas at this u level, as demonstrated in Figure 47, where three sub-contours at the same u level are shown along with the cross-sectional areas at these locations.

The second way is to create a color map of the cross-sectional area values, and paint the surface with the color of these values. This provides an intuitive way to localize the stenosis, by showing different colors where the cross-sectional area has an apparent change along the vessels, as demonstrated in Figure 48. In this figure, lighter color indicates normal sized vessel lumen, and darker color means the lumen is narrowed, thus implying stenosis.

Figure 49 is a plot of u versus cross-sectional area along the LAD of Figure 48. The left y-axis shows the cross-sectional areas in mm^2 , and the right y-axis shows the stenosis percentage, which is an important measure for the evaluation of stenosis. We can see from this plot that this LAD has two stenosis sites, one mild (a little less than 40% blockage) and another more severe (60% blockage). This is in consistent with what is shown in Figure 48.

With these results we conclude this chapter, in which we proposed a skeletonization approach for the segmented surface of branched vessels. This approach gives a straightforward way to measure cross-sectional areas of the vessels, thus provides useful references for stenosis detection and evaluation. We should mention that since the cross-sectional area measuring process is performed on the segmented surface, the result is essentially determined by the segmentation result. The algorithms proposed in this chapter were applied to the segmented vessel surfaces obtained from the previous chapter using the BDIS method, which has been validated in the previous chapter as well. In this chapter, we quantitatively validated our skeletonization method using a digital phantom.

The skeletons provide an abstract yet informative representation of the vessel tree, which leads to many possibilities of visualizing the vessels, such as MPRs and fly-throughs. These visualization methods are very often used clinically nowadays for 3D tubular structure, including airways, colons and vessels. The essential step is to acquire a reliable and accurate skeleton of these tubular structures with minimal user input. The skeletonization method proposed in this chapter is an automatic approach given a segmented surface, and the phantom study also shows a good centeredness of the skeleton. The stenosis estimation presented here is based on local cross-sectional areas, which is theoretically better than the ones based on the diameter. However, there are clinicians who prefer to use minimum/maximum diameter in the stenosis

evaluation or surgical planning procedures for stent implantation, and these parameters can also be acquired following the harmonic skeletonization method, since we essentially extract the cross-sectional boundary of the vessels, which is a closed contour in 2D. For further visualization, these 2D contours can be overlaid onto the original image data that are re-sampled in the corresponding location and direction. Hence, there are many ways to use the skeletons in a clinical setting, according to the preference of clinicians who actually use them. The algorithm would show more value if it is integrated to a friendly graphical user interface (GUI), which allows more flexibility in visualizing and exploring the datasets; however, the design and implementation of GUI is beyond the scope of this thesis.



Figure 43: Skeletonization results. Part I. Datasets #1 - #6.



Figure 44: Skeletonization results. Part II. Datasets #7 - #12.



Figure 45: Skeletonization results. Part III. Datasets #13 - #16.



Figure 46: Skeletonization results. Part IV. Datasets #17 - #18.

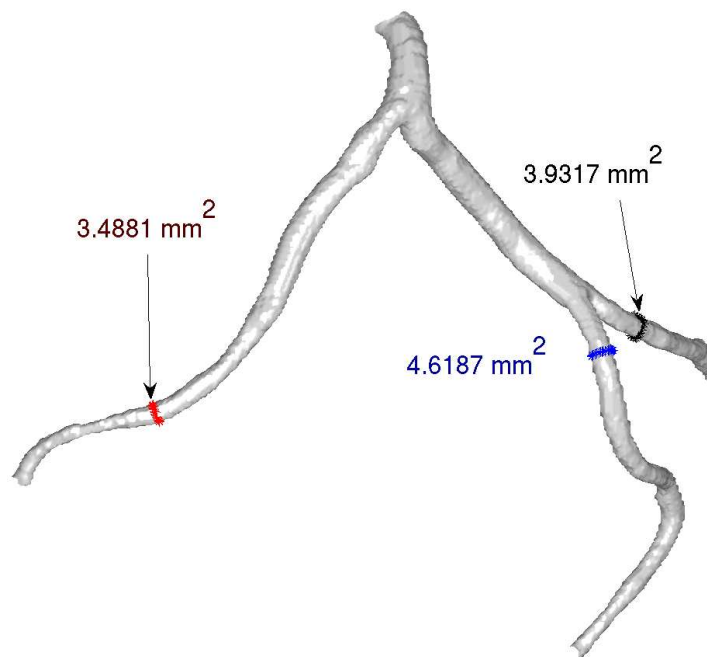


Figure 47: Cross-sectional area visualization #1. The cross-sectional area of each branch of the coronaries for a certain u . Dataset #7.

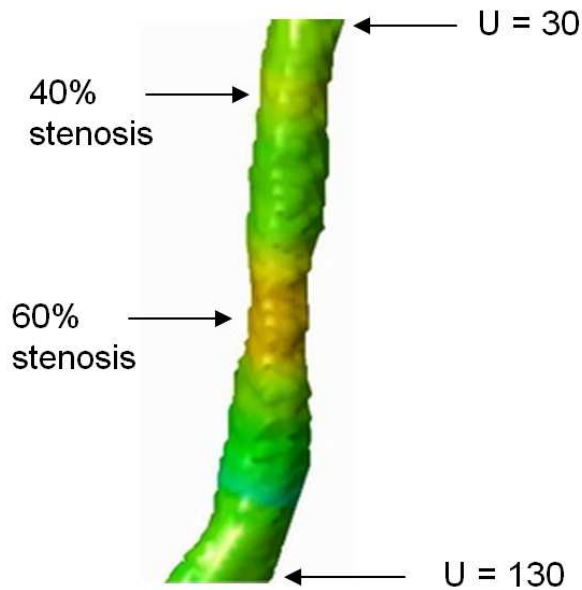


Figure 48: Cross-sectional area visualization #2. Color-painted LAD indicates an obvious stenosis site in the vessel. Dataset #1.

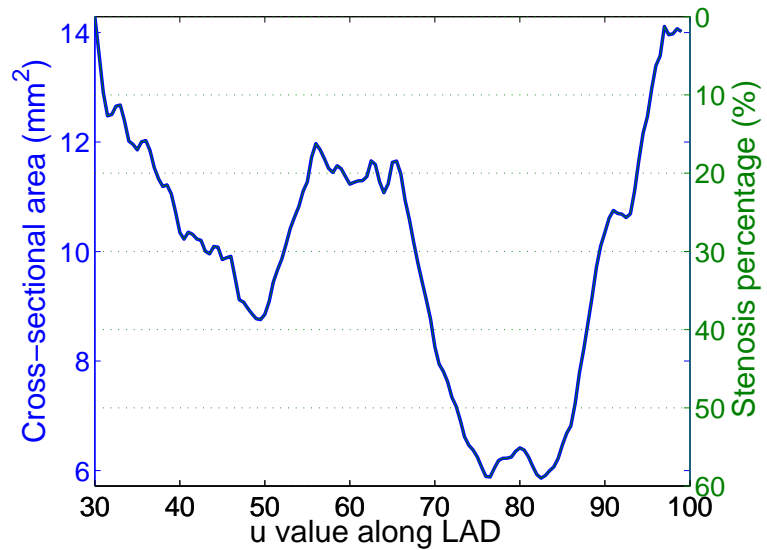


Figure 49: Cross-sectional area along the LAD shown in Figure 48. The left y-axis shows the cross-sectional area in mm^2 , and the right y-axis shows the stenosis percentage.

CHAPTER VI

CONCLUSIONS AND FUTURE RESEARCH

In this final chapter, we conclude the thesis and mention some possible extensions and future directions. This thesis has focused on the 3D image analysis of coronary arteries using CTA images. We first proposed a general image segmentation approach called BDIS in Chapter 3, which is based on Bayesian pixel processing and the level set image segmentation framework. The algorithm can be easily extended to 3D, with which we segmented coronary arteries from CTA images in Chapter 4. In order to generate an initial segmentation to start the BDIS process, we adopted a multi-scale Hessian based 3D line filtering technique to isolate the vessels and eliminate other structures in the images. The algorithm was applied to 18 real clinical datasets and was validated using manual segmentation of the same datasets. In Chapter 5 we further proposed shape analysis methods based on the segmented surface of the vessels. First, a skeletonization algorithm is explored using the solution of the Laplace equation on the surface in order to extract the centerlines of the branched vessels. Then a convenient way to measure cross-sectional areas of the vessel lumen is proposed to assist the detection and evaluation of stenosis.

The automatic image processing techniques have the potential to change the routinely clinical work-flow of a radiologist fundamentally. In stead of viewing the 2D axial image slice by slice to look for interested structures such as coronary arteries which only occupy a small number of voxels, the automatic approach proposed in this thesis takes the 3D dataset as a whole and output the structure of interest with minimal user input or interaction, with clinical significant parameters measured in

addition. Commercial software systems are now incorporating more and more automatic techniques to assist the clinical work-flow; however, higher level of automation and better accuracy are always desirable and critical. To our knowledge, so far there is no commercial systems which provide algorithms with the level of automation presented in this thesis. Normally the user still needs a great amount of manual work such as mouse clicking or parameter tuning to achieve a result similar to the results presented here. In order for the algorithms to be used clinically in a more efficient manner, a friendly GUI is desirable to visualize the results in multiple intuitive ways, as we have discussed at the end of the previous chapter. This needs more software engineering work including interface design, usability testing, speed optimization and more.

The validation of the proposed methods is performed quantitatively by comparing with the manual segmentation in this thesis. However, this is not a clinical validation, since the datasets are anonymous and the diagnoses were not available with the datasets. To strictly validate the proposed methods for clinical use, one should compare the results acquired here with the real diagnosis on each patient, especially for calcium identification and stenosis evaluation, to see how much difference there is between the automatic approach and the real diagnosis.

Also notice that the vessel analysis discussed in this thesis is essentially “lumen” analysis, since we have been aiming at segmenting regions filled with the contrast agent which is the blood-filled region. However, more information of atherosclerotic plaques is, in fact, hidden in the vessel wall, which can be composed of stable cores or vulnerable ones. Vulnerable plaques are prone to rupture, thus are more dangerous to patients. However, they are usually the ones which are more difficult to image. CTA is capable of revealing calcified plaques which may or may not be vulnerable plaques, and we have proposed a method to analyze this (see Chapter 4, Section 4.3.2). More challenges lie in the image post-processing and analysis of the vessel wall, which

normally do not have a good contrast with other tissues, but may contain valuable information about the plaques themselves. In order to reveal more information, one can explore texture analysis approaches (e.g., based on wavelets) which have been used to analyze the image of myocardium, cartilage and bones, and apply these methods on the vessel walls. With the hope that certain measures developed from the texture features of the vessel wall may differentiate stable and vulnerable plaques, texture analysis of the plaques can be an interesting future direction of this line of research. The segmentation of the lumen presented here can provide an ideal starting point for the texture analysis, which can be applied along the inner boundary of the vessel wall.

In the automatic segmentation work (Chapter 4), we have observed that the Hessian-based vessel filtering offers a slightly better sensitivity in the distal end of the vessels than the final BDIS segmentation results. This might be due to the poor diffusion of contrast agent at the distal end, which makes the image intensity lower than the proximal end. One alternative process would be to generate a centerline from the Hessian-based filter response to preserve the better sensitivity. This centerline, however, can hardly be smooth or well connected, since the filter response gives quite ragged isosurface and in many places are disjointed. Hence, the harmonic skeletonization is still essential in generating a smooth centerline which also has better connectivity.

In this thesis, the harmonic skeletonization work (Chapter 5) is based on the surface of a 3D tubular structure, which is a quite general model. This method hence has the potential to be applied to other structures such as airways, colons, elongated bones, and even other non-medical structures, generated either from tomography images such as the one used in this thesis, or any other imaging or modeling methods. Since the harmonic skeletonization method is completely surface-based, we have not used the original images in this step once we have obtained the surface from image

segmentation. However, one interesting extension would be to go back to the original CTA images, and use the generated centerline to guide a fly-through of the gray scale images, where the vessels can be viewed in either longitudinal or orthogonal directions, by re-sampling the 3D CTA images using oblique or curved planes following the centerline. In this way, the vessels and their segmentation can be examined in a more intuitive manner, and stenoses can be detected more straightforwardly.

Some works (e.g. Chalopin *et al.* [13]) have considered the problem of automatic labeling of different branches in a vessel tree by fitting the geometry of the vessels to a pre-defined model. The harmonic skeletons generated in this thesis can certainly serve as a good representation of the vessel tree for labeling purposes.

In the past few decades, medical imaging has grown rapidly and made tremendous contributions to the diagnosis and treatment to different diseases, such as atherosclerosis studied in this thesis. We hope the automatic image processing techniques explored here can provide a convenient way for radiologist and physicians to extract useful information from the large amount of images acquired by modern scanners more efficiently and accurately. The image segmentation technique also provides *patient-specific* models of coronary arteries, which can in turn be used to simulate blood flow patterns specifically for these patients, with the hope that the flow patterns and other bio-fluid mechanical properties of the blood may reveal more information about disease formation and development.

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