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# Learning Markov Logic Network Structure by Template Constructing

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### Learning Markov logic network structure by template constructing

by

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Ames, Iowa

2017

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### DEDICATION

I would like to thank my family and friends for their loving guidance and financial assistance during the writing of this work.

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### ACKNOWLEDGEMENTS

I would like to take this opportunity to express my thanks to those who helped me with various aspects of conducting research and the writing of this thesis. First and foremost, Dr. Tian for his guidance, patience and support throughout this research and the writing of this thesis. His insights and words of encouragement have often inspired me and renewed my hopes for completing my graduate education. I would also like to thank my committee members for their efforts and contributions to this work: Dr. Chang and Dr. Aduri.

### ABSTRACT

Markov logic networks (MLNs) are a statistical relational model that incorporates firstorder logic and probability by attaching weights to first-order clauses. However, due to the large search space, the structure learning of MLNs is a computationally expensive problem. In this paper, we present a new algorithm for learning the structure of Markov Logic Network by directly utilizing the data to construct the candidate clauses. Our approach makes use of a Markov Network learning algorithm to construct a template network. We then apply the template to guide the candidate clauses construction process. The experimental results demonstrate that our algorithm is promising.

### CHAPTER 1. OVERVIEW

### 1.1 Introduction

In recent years, there has been an increasing interest in methods for unifying the strengths of first-order logic and probabilistic graphical models in machine learning area (Getoor and Taskar, 2007). Markov Logic Networks (MLNs) are a statistical relational model that combine first-order logic and Markov networks. An MLN typically consists of a set of first-order clauses attached with weights, and it can be viewed as a template for features of Markov networks (Richardson and Domingos, 2006). Learning a MLN can be decomposed into two separated parts: structure learning (learning the logical clauses) and weight learning (learning the weight of each clause). Learning the structure of a MLN is the process of generating a set of clauses attached with their weights (Kok and Domingos, 2005), and it allows us to obtain uncertain dependencies underlying the relational data.

The structure learning problem of MLNs is an important but challenging task. With the continuous increasing of the data size, the search space is usually super-exponentially large and the clause evaluation also generates huge amount of groundings. In general, search for all the possible candidate clauses and evaluate them with full groundings may not be a feasible solution. A few practical approaches have been proposed to date, among which the MSL (Kok and Domingos, 2005), BUSL (Mihalkova and Mooney, 2007), ILS (Biba et al., 2008b), LHL (Kok and Domingos, 2009), LSM (Kok and Domingos, 2010), HGSM (Dinh et al., 2010b), GSLP (Dinh et al., 2011) and LNS (Sun et al., 2014). Most of these approaches focus on constraining the search space of the candidate clauses in a top-down or bottom-up manner.

The top-down approaches follow a general-and-test strategy, start from an empty clause, systematically enumerate candidate clauses by greedily adding literals to existing clauses, and evaluate the result clauses' empirical fit to training data by using some scoring models. Such approaches are usually inefficient as they have two shortcomings: searching the explosive space of clauses is computationally expensive; and it is susceptible to result in a local optimum. Bottom-up approaches, however, overcome these limitations by directly utilizing the training data to construct candidate clauses and guide the search.

In this paper, we present a novel MLN structure learning algorithm. This algorithm first constructs a set of template nodes from the database, then creates a set of observations using the data , and utilize the template nodes and observations to learn a "template" Markov networks. This template is then applied to guide the candidate clauses construction process. Candidate clauses are evaluated and reduced to form the final MLN.

We begin the paper by briefly reviewing the necessary background knowledge of first-order logic, Markov networks, and Markov logic networks in chapter 2. We then describe the details of our structure learning algorithms in chapter 3, and report the experimental results in chapter 4. Last, we conclude this paper and discuss future work in chapter 5.

### CHAPTER 2. BACKGROUND

In this chapter, we explain the necessary background knowledge about Markov logic networks. We start with first-order logic and Markov network, then we introduce how Markov logic network incorporates them together. Finally, we demonstrate the structure learning problem of MLNs and review some previous works.

### 2.1 First-order logic

A first-order knowledge base (KB) is a set of formulas or sentences in first-order logic (Genesereth and Nilsson, 1987). There are four types of symbols in first-order logic: constants, variables, functions and predicates. Constant symbols represent objects in a domain and can have types (e.g., person: *alice, bob, carl,*etc.). Variable symbols range over the objects in a domain. Function symbols represent functions that map tuples of objects to objects(e.g., MotherOf). Predicate symbols describe attributes of objects (e.g., Student(clice)) or relations between objects in the domain (e.g., workedUnder(alice, bob)). Constants and variables are often typed, that is, constants can only represent objects of the corresponding type and variables can only range over objects in the corresponding type. In this paper, we assume no functions in the domains. We denote constants by lower-cased strings, variables by single upper-case letters and predicates by strings that start with upper-case letters.

**Example:** We use the IMDB database as the domain for this example: This dataset contains *facts* that describe the profession of individuals in the movie business, *relationships* that indicate the connection between people, and the *movies* represent which person works for which movie. Actor(alice) means *alice* is an actor and Director(bob) indicates that *bob* is a director. The predicate *workedUnder*(A, B) specifies that person A works on a movie under the supervision of person B, and the predicate Movie(T, C) specifies that person C works on

movie T. Here both A, B, and T are variables, A and B range over objects in type *Person* and T range over objects in type *Movie*.

A term is any expression that represents an object in the domain. It can be a constant, a variable, or a function that is applied to terms. For example, *alice*, A, and *MotherOf(alice)* are terms. Ground terms contain no variables. An *atomic formula* or *atom* is a predicate applied to a tuple of terms(e.g., *workedUnder(alice, MotherOf(alice))*). A ground atom is a predicate replaces all variables with constants. We call an atom *variable atom* if it only contains variables. Formulas are constructed from atoms using logical connectives and quantifiers. A positive literal is an atom and a negative literal is a negated atom. A clause is a disjunction of positive and negative literals. The number of literals in the disjunction is the *length* of the clause. A *database* is a partial specification of a world, that is, each atom in it is true, false or unknown. In this paper, we make a closed-world assumption: a ground atom in the database is assumed to be true, a ground atom that is not in the database is considered false. A world is an assignment of truth values to all the possible ground atoms in a domain.

To conclude, first-order logic is a helpful tool that widely used in Artificial Intelligence area for the purpose of knowledge representation. Its expressiveness allows us to describe the complexity of the world in a more succinct way. However, first-order logic can not handle the uncertainty of the world, thus, pure first-order logic has restricted applicability to practical AI problems.

### 2.2 Markov networks

A Markov network (or Markov random field) is an undirected graphical model for the joint distribution of a set of random variables  $X = (X_1, X_2, ..., X_n) \in \mathcal{X}$  (Pearl, 1988). It consists of an undirected graph G = (V, E) with a list of potential function  $\phi_k$ . The graph G has a set of nodes, each of them represents one of the random variable. Nodes are connected by edges, which describe the dependency of nodes. A clique is a set of nodes, where each pair of nodes in the clique is connected by an edge. For each clique in the graph there is a potential function. Each potential function is a real-valued non-negative function, represents the state of the corresponding clique. Figure 2.1 gives an example of a Markov network. There are four nodes A, B, C and D in the figure, which represent the random variables, and they form two cliques. The corresponding potential functions of the cliques are  $\Phi(A, B)$  and  $\Phi(B, C, D)$ .

Given a set of random variables  $X = (X_1, X_2, ..., X_n) \in \mathcal{X}$ , let P(X = x) be the probability of finding that random variable X takes on the particular value configuration x. Because X is a set of variables, then P(X = x) can be understood to be the *joint distribution* of X. The *joint distribution* for a Markov network is given by the following formula (Richardson and Domingos, 2006):

$$P(X = x) = \frac{1}{Z} \prod_{k} \phi_k(x_{\{k\}})$$
(2.1)

where  $x_{\{k\}}$  is the state of variables that appear in the *k*th clique. Here *Z* is the normalizing partition function given by:  $Z = \sum_{x \in \mathcal{X}} \prod_k \phi_k(x_{\{k\}})$ . Markov networks can also equivalently written as *log-linear models*, which is given by:

$$P(X = x) = \frac{1}{Z} exp(\sum_{k} w_k f_k(x_{\{k\}}))$$
(2.2)

where  $f_k(x_{\{k\}})$  is the feature corresponding to  $x_{\{k\}}$  with its weight  $w_k$  being  $\log \phi_k(x_{\{k\}})$ . Each feature can be any real-valued function of the state, but in this paper we will only focus on binary features, that is, it is either 0 or 1, depends on whether it is satisfied or not.

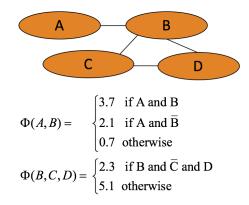


Figure 2.1 An example Markov network

Markov network is a probabilistic model that handles the uncertainty of the world. However, it is not expressiveness and can not describe the complexity of the world.

### 2.3 Markov logic networks

Markov Logic network is a statistical relational learning model that unifies first-order logic and Markov network, takes the advantages from both of them. It consists of a set of weighted first-order clauses. If we consider a first-order KB as a set of hard constraints on the possible worlds, then a MLN can be seen as an approach to soften these constraints: a world that violates some clauses is less likely to be possible, but not impossible. The fewer clauses a world violates, the more probable it is. The weight attached to a clause shows how strong the constraint is. A higher weight indicates the greater difference between a world satisfies the clauses and the world that does not. Table 2.1 shows an example of a simple MLN. The formal definition of MLNs is defined as follows:

**Definition 1** (Richardson and Domingos, 2006) A Markov logic network L is a set of pairs  $(f_i, w_i)$ , where  $f_i$  is a formula in first-order logic and  $w_i$  is a real number. Together with a finite set of constants  $C = \{c_1, c_2, ..., c_{|C|}\}$ , it defines a Markov network  $M_{L,C}$  (2.1 and 2.2) as follows:

1.  $M_{L,C}$  contains one binary node for each possible grounding of each atom appearing in L. The value of the node is 1 if the grounding atom is true, and 0 otherwise.

2.  $M_{L,C}$  contains one feature for each possible grounding of each formula  $f_i$  in L. The value of this feature is 1 if the ground formula is true, and 0 otherwise. The weight of the feature is the  $w_i$ , attached with  $f_i$  in L.

Two nodes in  $M_{L,C}$  are connected by an edge if and only if the corresponding ground atoms appear together in some ground formulas in L. Thus the atoms in each ground formula form a clique in  $M_{L,C}$ . For example, figure 2.2 shows the graph of the ground Markov network defined by giving the MLN in table 2.1 with constants Tim, Frank, and Shawshank. This graph contains a node for each ground atom and an edge for each pair of atoms that appear together in one of the ground formula. Its features include  $Actor(Tim) \Rightarrow \neg Director(Tim)$ ,  $Director(Frank) \Rightarrow \neg WorkedUnder(Frank, Tim)$ , etc.

An MLN can be seen as a *template* for generating Markov networks, given different sets of constants, it will construct different ground Markov networks. Let X be the set of all ground atoms,  $\mathcal{F}$  be the set of all clauses in the MLN,  $w_i$  be the weight attached with clause  $f_i \in \mathcal{F}$ ,

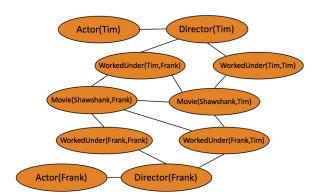


Figure 2.2 Ground Markov network

 $\mathcal{G}_{f_i}$  be the set of all possible groundings of clause  $f_i$  with the constants in the domain. Then the probability of a possible world x specified by the ground Markov network  $M_{L,C}$  is defined as:

$$P(X=x) = \frac{1}{Z} exp(\sum_{f_i \in \mathcal{F}} w_i \sum_{g \in \mathcal{G}_{f_i}} g(x)) = \frac{1}{Z} exp(\sum_{f_i \in \mathcal{F}} w_i n_i \{x\})$$
(2.3)

The value of g(x) is 1 if g is satisfied and 0 otherwise. Then, given a truth assignment to X, the quantity  $\sum_{g \in \mathcal{G}_{f_i}} g(x)$  counts the number of groundings of  $f_i$  that are true. Thus  $n_i\{x\}$  is the number of true groundings of  $f_i$  in x.

For example, consider an MLN that contains exactly one formula  $Actor(A) \Rightarrow \neg Director(A)$ with its weight w, and  $C = \{Bob\}$ . This results in four possible worlds:  $\{Actor(Bob), Director(Bob)\}, \{\neg Actor(Bob), Director(Bob)\}, \{Actor(Bob), \neg Director(Bob)\}, and \{\neg Actor(Bob), \neg Director(Bob)\}.$ From 2.3 we can obtain  $P(\{Actor(Bob), Director(Bob)\}) = \frac{1}{3e^w+1}$  and the probability of the other three worlds is  $\frac{e^w}{3e^w+1}$ . Here  $3e^w + 1$  is the value of partition function Z. Thus, any w > 0will make the world  $P(\{Actor(Bob), Director(Bob)\})$  less possible than the others.

Table 2.1 Example of a MLN

First-order logic	Weight
$Actor(A) \Rightarrow \neg Director(A)$	0.8
$Director(A) \Rightarrow \neg WorkedUnder(A, B)$	1.2
$WorkedUnder(A, B) \land Movie(T, A) \Rightarrow Movie(T, B)$	1.5

#### **2.3.1** Inference

To perform inference over a given MLN, one needs to ground it to its corresponding Markov network (Pearl, 1988). As described by Richardson and Domingos (2006), this process can be done as follows. First, all the possible ground atoms in the domain are constructed, and they are used as the nodes of the Markov network. The edges in the Markov network are decided by the groundings of the first-order clauses, that is, two ground atoms are connected if they are both in a grounding of a clause. Thus, nodes that participate together in a ground clause will form cliques.

### 2.3.2 Structure learning

Given a database, the problem of learning a MLN can be separated into two parts: weight learning and structure learning, where structure learning referred to learning the formulas and weight learning referred to learning the weights. In this paper we only focus on the structure learning problem, because given a structure learned, a weight learning algorithm called L - BFGS (Liu and Nocedal, 1989) has been developed to learn the weights. The main task in learning the structure of MLNs is to find a set of potentially good clauses. Clauses are evaluated using a weighted pseudo log-likelihood (WPLL) measure, introduced in (Kok and Domingos, 2005), defined as:

$$log P_w(X = x) = \sum_{r \in R} c_r \sum_{k=1}^{g_r} log P_w(X_{r,k} = x_{r,k} | MB_x(X_{r,k}))$$
(2.4)

where R is the set of first-order predicates,  $g_r$  is the number of groundings of predicate r,  $x_{r,k}$ is the truth value (either 0 or 1) of the kth ground atom of r,  $c_r = 1/g_r$ .

Some previous works on structure learning are: MSL, BUSL, listed as follows:

**MSL:** This algorithm is proposed by Kok and Domingos (2005), it uses beam search to search from all possible clauses. In each iteration, MSL uses beam search to find the best clause, and add it to the MLN: starting with all the unit clauses, it applies each possible operator (addition and deletion) to each clause, keep the n best ones, apply the operator to those, and repeat until no new clause improves the WPLL. The best clause is the one with highest WPLL score and it will be added to the MLN. MSL terminates when no more clause can be added to the MLN, and it then returns the MLN.

**BUSL:** This algorithm makes use of relational path-finding to find a path of ground atoms in the data. It variabilizes each ground atom in the path and creates a Markov network with the paths as nodes and the boolean value matrix as training data. It utilizes the Grow-Shrink Markov network structure learning algorithm to connect the nodes. After construction of Markov network template, it creates candidate clauses by making disjunctions of the atoms in each clique's node. Finally, it uses WPLL to evaluate the candidates and discards those candidates that do not increase the overall WPLL.

# CHAPTER 3. TEMPLATE CONSTRUCTING STRUCTURE LEARNING

In this chapter, we explain the details of our algorithms: learning Markov logic network structure by template constructing (TCSL).

As we mentioned in chapter 2, MLNs can be viewed as templates for generating Markov networks, given different sets of constants, different ground Markov networks are constructed. Thus, we want to create a Markov network template similar to the one in figure 3.1 to restrict the search space and guide the construction of candidate clauses. Algorithm 1 gives the skeleton of TCSL. Let  $\mathcal{P}$  be the set of all predicates in the domain. Each predicate P is considered in sequence. For each P, the algorithm first constructs a set of template nodes, and creates a set of observations using the data. A Markov network template is then learned using the template nodes and the observations. Finally, we focus on each maximal clique in the template network and generate a set of candidate clauses. We evaluate the candidates with the WPLL score, add these candidates which increase the overall WPLL score to the final MLN.

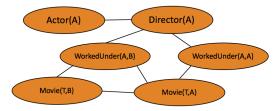


Figure 3.1 An example Markov network template

### 3.1 Construct template nodes

To learn a Template network using Markov network structure learning algorithm, we first need to construct a set of template nodes. A template node is basically a literal that only

Algorithm :	1	TCSL(	DB .	, MLN .	, Ma	xFree	Variable	)
-------------	---	-------	------	---------	------	-------	----------	---

- 1: Initialization, add all unit clauses to MLN
- 2: for each  $P \in \mathcal{P}$  do
- 3: Construct template nodes for predicate P
- 4: Generate observations for the template nodes
- 5: Use the template nodes and the observations to learn the Markov network template
- 6: Use the template to build candidate clauses
- 7: end for
- 8: Remove duplicate candidates clauses
- 9: Evaluate candidates, add the best ones to MLN

10: return MLN

contains variables. We use predicate P to create the first template node, referred to as the *headNode*. Other template nodes are then created by searching for constant-shared ground atoms in the database and constructing a corresponding variable literal. Thus, template nodes are actually atoms that have true groundings in the data. The output of template nodes construction process for predicate P is an array, which contains a set of template nodes. Algorithm 2 displays how the template nodes are created. It makes use of the following definition:

**Definition 2** Two ground atoms are *constant-shared* or *connected* if there is at least one constant that is an argument of both.

Let P be the predicate currently under consideration in this iteration, m be the maximum number of free variable that can be allowed in the *templateNodeArray*. The algorithm first creates the variable atom of P as the *headNode* in line 1, and add it to the position 0 of *templateNodeArray*. Each argument in *headNode* is assigned a unique variable. In line 2, we set *variableNum* to the number of variables in *headNode*. Next, from line 3 to 15, the algorithm iterates over each possible ground atom  $G_P$  of P. In line 4, it finds the set of all the true ground atoms in the data that are constant-shared with  $G_P$ , denoted as  $C_{G_P}$ . Then for each  $c \in C_{\mathcal{G}_{\mathcal{P}}}$ , it constructs a new template node. If the *newNode* was not created previously and did not violate the limitation of variable number, then it will be added to *templateNodeArray* (line 9-10). However, note that some nodes will be ignored if there already exists m variables, thus some useful information may be lost.

**Example:** Assume we are given the database shown in table 3.1 as the domain of our running example. The ground atoms listed in the database are *true* and all the other atoms

Algorithm 2 TemplateNodesConstruction(P, m)

### Input:

P: the predicate being considered in this loop

m: maximum free variable number allowed in the array

### Output:

templateNodeArray: the array contains template nodes

- 1: Use P to create the *head* template node, called *headNode*, and add it to the place 0 of *templateNodeArray*.
- 2: variableNum = number of variables in headNode

```
3: for each G_P, ground atom of P do
```

4: let  $\mathcal{C}_{G_P}$  be the set of all the true ground atoms that are constant-shared with  $G_P$ 

```
5: for each c \in C_{G_P} do
```

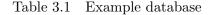
```
6: newNode = Create a new template node
```

- 7: variableNum + = new variable introduced in newNode
- 8: Index = templateNodeArray.find(newNode)

```
9: if Index < 0\&\&variableNum <= m then
```

- 10: add newNode to templateNodeArray
- 11: else
- 12: variableNum = new variable introduced in newNode
- 13: end if
- 14: **end for**
- 15: end for

are *false*:



Actor(Tim) Director(Frank) WorkedUnder(Tim, Frank) Movie(Shawshank, Tim) Movie(ShawShank, Frank)

Suppose the predicate currently under consideration is P = Actor. Then the headNode is Actor(A). We need to consider each ground atom of P and let's start with Actor(Tim). The constant-shared ground atoms of Actor(Tim) in the database are WorkedUnder(Tim, Frank) and Movie(Shawshank, Tim). Thus we can create template nodes WorkedUnder(A, B) and Movie(C,A), add them to templateNodeArray. Next we consider the other ground atom Ac-tor(Frank): the constant-shared ground atoms in the database are Director(Frank), WorkedUnder(Tim, Frank) and Movie(Shawshank, Frank). Template nodes constructed are Director(A).

WorkedUnder(D,A) and Movie(E,A). Movie(E,A) is ignored because Movie(C,A) already exists, the rest two nodes are added to templateNodeArray. Table 3.2 lists the set of template nodes constructed. There are four free variables in the array: A, B, C and D.

Table 3.2 Template nodes constructed

Actor(A) $WorkedUnder$	$(A,B) \mid Movie(C,A)$	Director(A)	WorkedUnder(D, A)
------------------------	-------------------------	-------------	-------------------

### **3.2** Generate observations

We have constructed a list of template nodes and added them to the array. Next we will generate a set of observations for the template nodes. We have limited the number of free variables in templateNodeArray by setting the parameter m. Algorithm 3 lists the procedure.

Algorithm 3 Generate Observations
Input:
templateNodeArray: the array of template nodes
m: max free variable number in $templateNodeArray$
Output:
M: a matrix contains the observations generated
1: let $\mathcal{S}$ be the set of all possible assignments to the variables of the template nodes.
2: for each $s_i \in \mathcal{S}$ do
3: append a new array $M[i]$ to $M$
4: for each node $n_j \in templateNodeArray$ do
5: <b>if</b> the ground atom of $n_j$ under the assignment $s_i$ is <i>true</i> <b>then</b>
6:    M[i][j] = true
7: else
8: $M[i][j] = false$
9: end if
10: end for
11: end for

Let S be the set of all possible assignments for the variables in the *templateNodeArray*, M be the result matrix containing a column for each template node and a row for each possible assignment. The algorithm considers each assignment  $s_i \in S$ , it first add a new empty array to M, then, in line 4-8, it checks the ground atom of each template node given variable assignment  $s_i$ , set the corresponding value in M to true if the ground atom exists in the data and false otherwise. The larger number of variables in *templateNodeArray*, the greater size of S will

Actor(A)	WorkedUnder(A, B)	Movie(C, A)	Director(A)	WorkedUnder(D, A)
1	0	1	0	0
1	0	1	0	0
1	1	1	0	0
1	1	1	0	0
0	0	1	1	1
0	0	1	1	0
0	0	1	1	1
0	0	1	1	0

Table 3.3 An example of observations generated

be. A greater size of S could help generate more observations. However, generate too many observations may result in an extremely long run time. We set m = 5 to control the number of observations generated.

Table 3.3 shows the observations we generate for the template node in table 3.2. Both A, B and D can take two possible constants, while C can only be Shawshank. So the total number of observations created is  $2 \times 2 \times 2 = 8$ .

### **3.3** Alternative approach to create template nodes and observations

As we pointed out in section 3.1, some of the template nodes will be filtered out with limited number of free variable in *templateNodeArray*. We have to set m to limit the number of variable, this is because we generated S which contains all possible assignment of variables in *templateNodeArray*. Without the restriction of variable number, the size of S could be exponentially large. However, this restriction may also result in loss of some template nodes. Here we present an alternative approach to relax the restriction: we still add these template nodes to the *templateNodeArray*, but create their observations in a different way. The details of the algorithms are listed as follows:

Algorithm 4 displays the details of template nodes construction. The only difference here is that we remove the variable number restriction m, others remain the same. By removing restriction, more template nodes will be introduced, thus more information may be gained.

Algorithm 5 describes the alternative way for generating observations. If a template node only contains the first mth variables, we use the same way in algorithm 3 to assign its value in

Algorithm 4 TemplateNodesConstruction2(P)
Input:
P: the predicate being considered in this loop
Output:
templateNodeArray: the array contains template nodes
1: Use $P$ to create the <i>head</i> template node, called <i>headNode</i> , and add it to the place 0 of
templateNodeArray.
2: $variableNum =$ number of variables in $headNode$
3: for each $G_P$ , ground atom of $P$ do
4: let $\mathcal{C}_{G_P}$ be the set of all the true ground atoms that are constant-shared with $G_P$
5: for each $c \in \mathcal{C}_{G_P}$ do
$6: \qquad newNode = CreateNode(c, headNode, G_P)$
7: $variableNum + =$ new variable introduced in $newNode$
8: $Index = templateNodeArray.find(newNode)$
9: <b>if</b> $Index < 0$ <b>then</b>
10: add $newNode$ to $templateNodeArray$
11: $else$
12: $variableNum - =$ new variable introduced in $newNode$
13: end if
14: end for
15: end for

M; otherwise, we make use of an idea in BUSL (Mihalkova and Mooney, 2007), that is, if this node has a true grounding that is constant-shared with the current grounding of *headNode*, then its value in M will be set to true. Other things remain the same.

This alternative approach allows more variables to be introduced, thus more template nodes are added to the *templateNodeArray*, while the size of S remains the same.

### 3.4 Learn the template and build candidate clauses

Finally, to construct the Markov network template, we need to know how the template nodes are connected by edges. Consider the template nodes as the nodes in the Markov network, and the observation matrix M as the training data, we can find the edges by applying a Markov network structure learning algorithm. Any Markov network structure learning algorithm can be applied here, and we chose the Grow-Shrink Markov Network (GSMN) algorithm by Bromberg et al. (2006). GSMN decides whether two nodes are conditionally independent of each other by using  $\chi^2$  statistical tests.

Algorithm 5	5	Generate	Observation	s2
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### Input:

templateNodeArray: the array of template nodes m: max free variable number in templateNodeArray

### **Output:**

M: a matrix contains the observations generated

1: let  $\mathcal{S}$  be the set of all possible assignments to the first *m*th variables of the template nodes.

```
2: for each s_i \in \mathcal{S} do
      append a new array M[i] to M
 3:
      for each node n_j \in templateNodeArray do
 4:
        if n_j only contains first mth variables then
 5:
 6:
           if the ground atom of n_i under the assignment s_i is true then
             M[i][j] = true
 7:
 8:
           else
9:
             M[i][j] = false
           end if
10:
        else
11:
           if there exists a true grounding of n_j that is constant-shared with the grounding of
12:
           headNode then
             M[i][j] = true
13:
           else
14:
             M[i][j] = false
15:
           end if
16:
        end if
17:
      end for
18:
19: end for
```

After the template network is constructed for predicate P, we then use it to build a set of candidate clauses. We consider each clique contains *headNode* in the Markov network template, generate all possible clauses from length 1 to the size the of the clique by making disjunctions from the template nodes in the clique, and we try all possible negation/nonnegation combinations. Note that we only construct clauses from those template nodes which form cliques in the template; i.e., for any two template nodes in a clause, there must exist an edge between them. Every candidate clause must contain the *headNode*.

Finally, we remove duplicates in the candidates, and evaluate them using the WPLL. Each clause need to be assigned a weight in order to learn the WPLL score. To learn the weight, we use L - BFGS as Richardson and Domingos did (2006). After all the scores are learned, all the candidate clauses are considered for addition to the MLN in order of decreasing score. To speed up the inference and decrease over fitting, we only evaluate candidates with its weight greater than minWeight. Candidates that do not increase the overall WPLL score are discarded, and the rest are appended to the MLN.

### CHAPTER 4. EXPERIMENTAL EVALUATION

#### 4.1 Experimental setup

In this section we describe how we setup our experiment. We implement our algorithm using the Alchemy package available at http:// alchemy.cs.washington.edu.

### 4.1.1 Datasets

We use a publicly available dataset IMDB database to evaluate our approach. It's available at http://alchemy.cs.washington.edu. The statistics are shown in Table 4.1

Table 4.1 Details of dataset

Dataset	Types	Constants	Predicates	True Atoms	Total Atoms
IMDB	4	316	10	1540	32615

**IMDB.** The IMDB dataset is created by Mihalkova and Mooney (2007) from the imdb.com database, describes a domain about movie. Its predicates describing directors, actors, movies, and their relationships (e.g, Director(person), WorkedUnder(person, person), etc.) It is divided into 5 independent folds. Each fold contains four movies, their directors and actors, etc. We omitted 4 equality predicates (e.g, SamePerson(person, person), SameMovie(movie, movie), etc.) since they are true if and only if their arguments are the same.

### 4.1.2 Methodology

We compared our algorithms with MSL and BUSL. Both of them are implemented in the Alchemy package. We measured the performance using the metrics used by Kok and Domingos (2005), the area under the precision-recall curve (AUC). AUC is helpful because it displays how good an algorithm predicts the positive atoms in the data, and it is insensitive to a large number of true negative atoms in the data. In order to calculate the AUC of a given MLN, we performed inference over it, tested the prediction for each predicate by providing the rest predicates in the data as evidence. Exception is the predicates Actor(person) and Director(person), we have to evaluate them together because the groundings of them for the same constant are mutually exclusive, that is, one person can only be either a actor or a director. We set MSL's parameters as default setting and set BUSL's parameters as in Mihalkova and Mooney (2007). We set TCSL's minWeight = 0.5 in our experiments. We performed all runs on the same machine.

### 4.2 Experimental results

Table 4.2 reports the average AUCs and the AUCs of three different types of predicates for each algorithm. Higher number of AUC indicates better performance.

Let TCSL be the first algorithm we proposed and TCSL-Alter be the alternative approach to create template nodes and observations. First, we compare our algorithms with MSL and BUSL. Our algorithms' average AUCs are higher than both MSL and BUSL. For predicate Director(person) and Actor(person), our algorithms significantly outperform MSL, and also improve over BUSL. For predicate WorkedUnder(person, person), our algorithms have higher AUCs than BUSL, but lower than MSL. For predicate Movie(movie, person), all the four algorithms' AUCs are very close. This result suggests that our algorithms outperform BUSL for both types of the predicates, but compare to MSL, our algorithms did worse on the relationship predicate WorkedUnder(person, person) and much better on predicating unary predicate. Next we compare TCSL with TCSL-Alter. The average AUCs of TCSL and TCSL-Alter are almost the same. TCSL has a higher AUC for predicate Director(person) and Actor(person), and also slightly better for predicate Movie(movie, person), but performs worse for predicate WorkedUnder(person, person). This result indicates that, since TCSL-Alter introduced more variables and more template nodes than TCSL, that may be the reason it performs better on WorkedUnder(person, person) predicate, but assign the values in M matrix in two different ways may also lead to the decreasing of AUC on Director(person) and Actor(person).

Table 4.3 shows the average training time overall for each system. Both TCSL and TCSL-Alter are trained much slower than BUSL and MSL. This is because our algorithms spend most

System	Average AUC	Director and Actor	WorkedUnder	Movie
MSL	0.414	0.603	0.381	0.259
BUSL	0.468	0.911	0.249	0.245
TCSL	0.511	0.981	0.296	0.256
TCSL-Alter	0.506	0.968	0.312	0.238

Table 4.2Experimental results of AUCs

Table 4.3Experimental running time

System	$\operatorname{runTimes}(\min)$
MSL	6.91
BUSL	1.42
TCSL	14.67
TCSL-Alter	15.55

of their training time on generating the observations. That's also the reason that TCSL's and TCSL-ALter's run time are very close, although TCSL-Alter introduced more template nodes.

### CHAPTER 5. CONCLUSION AND FUTURE WORK

In this paper, we have presented a novel algorithm for the Markov logic network structure learning problem. This approach directly makes use of the data to restrict the search space and guide the construction of candidate clauses, it also generates a set of observations to help construct reliable Markov network templates. Our experiments with a real-world domain have shown the effectiveness of our approach. One bottleneck of this approach is that, it is pretty slow currently because the observation generation algorithm is not very efficient.

Directions for future work includes: improve the efficiency of observation generation process (the significant limitation in our approach); apply our algorithms to larger, richer domains; instead of only consider the ground atoms that is constant-shared with *headNode*, introduce multiple hops (e.g., variabilize the ground atoms which are constant-shared with template nodes already obtained) of template nodes in the template nodes construction part .

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