# Slip detection and compensation in autonomous tracked micro-vehicles. 

Aaron T. Stewart<br>University of Louisville

Follow this and additional works at: https://ir.library.louisville.edu/etd

## Recommended Citation

Stewart, Aaron T., "Slip detection and compensation in autonomous tracked micro-vehicles." (2010). Electronic Theses and Dissertations. Paper 1385.
https://doi.org/10.18297/etd/1385

By<br>Aaron T. Stewart<br>B.S. University of Louisville

# A Thesis <br> Submitted to the Faculty of the University of Louisville <br> J. B. Speed School of Engineering as Partial Fulfillment of the Requirements for the Professional Degree 

## MASTER OF ENGINEERING

Department of Mechanical Engineering

# SLIP DETECTION AND COMPENSATION IN TRACKED AUTONOMOUS MICRO-VEHICLES 

Submitted by: $\qquad$

Aaron T. Stewart

A Thesis Approved on
by the Following Thesis Committee:

Thesis Director, Dr. Christopher Richards

Dr. William Hnat

Dr. Tamer Inanc

## Acknowledgements

I would like to thank Dr. Chris Richards for his continued commitment to me and the completion of this work, along with the faculty and staff of the University of Louisville who helped me solve problems along the way. Lastly I would like to thank my girlfriend and my family for their love and support and for keeping me focused on the task at hand.


#### Abstract

When tracked vehicles traverse terrain such as sand, soil, or even concrete, they may encounter a variance in density or viscosity of the medium that the vehicle is traveling along. When this happens, one track begins to move faster or slower relative to the ground than its counterpart, causing a change in its orientation and position. Autonomous tracked vehicles must be able to detect how much change occurred in the orientation and position of the vehicle and it must then determine a new path to reach the target location.

This paper focuses on development of the ability for a small tracked vehicle to detect when a slip has occurred, how much the vehicle has slipped and how the autonomous vehicle should correct for the slip that has occurred. Three different algorithms are tested, the Straight Line Slip Method, the Arc Extension Method and the Arc Compensation Method. The Arc Compensation Method returned the best and most predictable results. The Arc Compensation Method averaged 60 mm to the target location from where the vehicle stopped the smallest of the three methods. This method also maintained a smaller standard deviation and range for the distance to the target location than the other two methods.


## Table of Contents

ABSTRACT ..... iv
Nomenclature ..... vi
List of Tables ..... vii
List of Figures ..... viii
I. INTRODUCTION ..... 1
II. PROBLEM STATEMENT ..... 10
III. VEHICLE PLATFORM ..... 15
N. THEORY ..... 19
V. THE ALGORITHMS ..... 25
VI. EXPERIMENT ..... 36
VII. RESULTS, DISCUSSION AND ANALYSIS ..... 42
VIII. CONCLUSIONS ..... 81
IX. FUTURE WORK ..... 83
X. WORKS CITED ..... 84
APPENDIXI ..... 87
APPENDIX II ..... 89
APPENDIX III ..... 102
VITA ..... 124

## Nomenclature

| CEP | Circular Error Probable |
| :---: | :---: |
| 2DRMS | Distance Root Mean Squared |
| COR | Center of Rotation |
| $\mathrm{D}_{\mathrm{pt}}$ | Distance past threshold, distance traveled while slipping only after crossing the slip threshold, in $x$ direction |
| $\mathrm{D}_{\text {s }}$ | Distance to slip in $x$ direction |
| $\mathrm{D}_{\text {st }}$ | Slip travel in $x$ direction |
| $\mathrm{D}_{\mathrm{t}}$ | Total distance traveled in $x$ direction |
| $\mathrm{D}_{\text {trresh }}$ | Distance traveled prior to crossing the slip threshold |
| L | Length of the arc traveled during the slip |
| $L_{p}$ | Partial arc length, length of the arc after crossing the slip threshold |
| $r$ | Radius |
| $\beta$ | Angle of change for the slipping arc |
| $\Delta x$ | Change in $x$ direction |
| $\Delta y$ | Change in $y$ direction |
| $\varepsilon_{x}$ | Distance traveled in the $x$ direction while slipping |
| $\varepsilon_{y}$ | Distance traveled in the y direction while slipping |
| $\theta$ | Change in orientation of the vehicle during the slip |
| $\theta_{\text {t }}$ | Slip threshold |

## List of Tables

TABLE I: VARIABLE MATRIX FOR ALL THREE ALGORITHMS ..... 38
TABLE II: THE AVERAGE, MINIMUM, MAMXIMUM AND STANDARD
DEVIATION FOR MEASURE SLIP (M) AND ACTUAL SLIP (A) AS
ENCOUNTERED BY EACH ALGORITHM ..... 45TABLE III: PERFORMANCE METRICS FOR ALL THREE ALGORITHMSCOMPARING THE DISTNACE TO THE TARGET LOCATION TO THEPOINT THAT THE VEHICLE STOPPED. ALL UNITS IN MM ........................ 77

## List of Figures

FIGURE 1. (a) An example of GraphSLAM as viewed from the side. (b) An Example of GraphSLAM as viewed by a robot (Thurn, et al., 2005). ..... 5
FIGURE 2. Reported GPS location points relative to the absolute position;corrected using WAAS which is GPS supplemented using ground stations(Earth Measurement Consulting).7
FIGURE 3. An example of GPS signal multipath with a GPS receiver mounted to a stable base (Earth Measurement Consulting) ..... 8
FIGURE 4. Autonomous tracked micro-vehicle with major components. ..... 11
FIGURE 5. The ghosted figure represents both the position and orientation ofthe vehicle if a slip did not occur and the autonomous vehicle's presumedposition and orientation when a slip condition is encountered. $\Delta x$ and $\Delta y$ arethe error in the $x$ and $y$ direction and $\theta$ is the change in orientation of thevehicle. A tracked micro-vehicle with (a) traction at each track progresses ina straight line, (b) reduced traction on each track cannot maintain absoluteposition and (c) traction at left track and reduced traction at right track willrotate and travel in an arc in the clockwise direction. ....................................... 13
FIGURE 6. Example of (a) an incremental encoder wheel and optical receiverand (b) incremental encoder and its square wave output. (Pilgrim, 2004) .... 18
FIGURE 7. Slip geometry with constant radius assumption ..... 21
FIGURE 8. Illustration of partial and total arc length. ..... 23
FIGURE 9. An illustration for returning to the target location ..... 24
FIGURE 10. A flow chart describing the secession of events within the algorithms as various stages. ..... 25
FIGURE 11. A flow chart of the three events that are the Baseline DetectionStage. Green indicates a process and orange describes where the data forthat process is acquired........................................................................................ 27
FIGURE 12. Flow diagram for the Slip Monitoring Stage ..... 28
FIGURE 13. Flow Diagram for the Post Slip Localization Stage ..... 30
FIGURE 14. Illustration of the arc, $L_{p}$, as detected by the non slipping track and traveling distances for the Arc Extension Method ..... 31
FIGURE 15. Illustration of how the Straight Line Slip Method treats a slip ..... 33
FIGURE 16. Flow Chart for the structure of the algorithms. Green spaces areprocesses and decisions, orange spaces are information used to control theprocess or decision and the blue box is where each algorithm differs. Eachstage of the algorithm has been boxed in.......................................................... 35
FIGURE 17. Stack of playing cards with an induced shear ..... 37
FIGURE 18. An illustration of the general path taken by the micro-vehicle for
$\qquad$
FIGURE 19. Autonomous tracked vehicle in initial position for testing ..... 40
FIGURE 20. Alignment of playing cards that will become the slip condition. ..... 41
FIGURE 21. The amount of error in the slip angle measurement ..... 43
FIGURE 22. The amount of error in the slip angle measurement aftereliminating trials with a measurement difference of more than three degrees.44
THE AVERAGE, MINIMUM, MAMXIMUM AND STANDARD DEVIATION FOR MEASURE SLIP (M) AND ACTUAL SLIP (A) AS ENCOUNTERED BY EACH ALGORITHM ..... 45
FIGURE 23. Measured angle of slip versus absolute error between actual and target location for the Arc Extension Method. ..... 46
FIGURE 24. Measured angle of slip versus absolute error between actual and target location destination for the Arc Compensation Method ..... 46
FIGURE 25. Measured angle of slip versus absolute error between actual and target location for the Straight Line Slip Method ..... 47
FIGURE 26. Arc length of each trial for the Arc Extension Method compared to where the tracked vehicle stopped relative to the target location before remove outliers. Each ep is equal to 10.89 mm ..... 49
FIGURE 27. Arc length of each trial for the Arc Extension Method compared to where the tracked vehicle stopped relative to the target location with outliers removed. Each ep is equal to 10.89 mm . ..... 51
FIGURE 28. Arc length of each trial for the Arc Compensation Method compared to where the tracked vehicle stopped relative to the target location.52
FIGURE 29. Percentage of arc lengths at each length for the Arc Compensation Method. ..... 53
FIGURE 30. Percentage of arc lengths at each length for the Arc Extension Method. ..... 54
FIGURE 31. The distance from where the tracked vehicle stopped versus thetarget location at point $(0,0)$ for all tests for all three methods. The directionof travel relative to the graph is from right to left.56
FIGURE 32. The distance from where the tracked vehicle stopped versus thetarget location at point $(0,0)$ for all tests of the Arc Compensation Method.The direction of travel relative to the graph is from right to left.57
FIGURE 33. The distance from where the tracked vehicle stopped versus thetarget location at point $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the ArcCompensation Method. The direction of travel relative to the graph is fromright to left.58

FIGURE 34. The distance from where the vehicle stopped versus the target location at point $(0,0)$ for the $121.9 \mathrm{~cm}(4 \mathrm{ft})$ test of the Arc Compensation Method. The direction of travel relative to the graph is from right to left. ....... 59

FIGURE 35. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $182.9 \mathrm{~cm}(6 \mathrm{ft})$ test of the Arc Compensation Method. The direction of travel relative to the graph is from right to left.

FIGURE 36. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for all tests of the Arc Extension Method. The direction of travel relative to the graph is from right to left. 62

FIGURE 37. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the Arc Extension Method. The direction of travel relative to the graph is from right to left. ....... 63

FIGURE 38. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $121.9 \mathrm{~cm}(4 \mathrm{ft})$ test of the Arc Extension Method. The direction of travel relative to the graph is from right to left. ....... 64

FIGURE 39. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $182.9 \mathrm{~cm}(6 \mathrm{ft})$ test of the Arc Extension Method. The direction of travel relative to the graph is from right to left. ....... 65

FIGURE 40. The distance from where the vehicle stopped versus the target location at point $(0,0)$ for all tests of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left. .............................. 67

FIGURE 41. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left. ...

FIGURE 42. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $121.9 \mathrm{~cm}(4 \mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left. ..

FIGURE 43. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for the $182.9 \mathrm{~cm}(6 \mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left. ...

FIGURE 44. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for all tests of the Arc Compensation Method. $5 \%$ of the data lies within 25 mm of the target location, $75 \%$ lies within 75 mm of the target location and $100 \%$ of the data lies within 125 mm of the target location.
FIGURE 45. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for all tests of the Arc Extension Method. 6.7\% of the data lies within 25 mm of the target location, $60 \%$ lies within 75 mm of
the target location and $81.7 \%$ of the data lies within 125 mm of the target location.

FIGURE 46. The distance from where the tracked vehicle stopped versus the target location at point $(0,0)$ for all tests of the Straight Line Slip Method. $10 \%$ of the data lies within 25 mm of the target location, $53.3 \%$ lies within 75 mm of the target location and $78.3 \%$ of the data lies within 125 mm of the target location.
PERFORMANCE METRICS FOR ALL THREE ALGORITHMS COMPARING THE DISTNACE TO THE TARGET LOCATION TO THE POINT THAT THE VEHICLE STOPPED. ALL UNITS IN MM .......................................................... 77
FIGURE 47. Measurements of tracked vehicle position relative to true during a straight line test at $305 \mathrm{~mm}(1 \mathrm{ft})$ increments with best fit line for the data. The equation of the best fit line is $Y=-9 E-05 \times 2+0.0262 x+0.2268$. The line has an $R 2$ value of 0.9599 .

79

## I. INTRODUCTION

Research into autonomous navigation will lead to fewer traffic accidents, faster traveling times, and more efficient highway systems (Thurn, Junior: The Stanford Entry in the Urban Grand Challenge, 2007). On a smaller scale, autonomous robots could perform hazardous missions for the military such as delivering troop supplies to hostile areas, evacuating injured troops and civilians, or even patroling enemy territory. Civilian applications include autonomous mapping of hazardous areas such as mines or caves, factory material management, and search and rescue missions during natural or terrorist induced disasters.

A large amount of research has already been performed in the area of autonomous robots. One of the most well known ventures into this subject matter is the DARPA Grand Challenge. This program was launched by the Defense Advanced Research Project Agency to motivate research into unmanned ground vehicle navigation. The Challenge goal was to build an autonomous robot that is capable of covering a vast distance of rough terrain that had not been previously navigated by the robot. The group that would cross the finish line first would receive a prize worth $\$ 1$ Million. The first challenge took place on March 13, 2004 and required vehicles with no drivers to travel 142 miles
across the Mojave Dessert in less than 10 hours. During the first challenge, 15 teams were selected to compete, yet none of the teams we able to navigate through more than the first $5 \%$ of the course. In 2005, the race was set to take place again. In this year, 23 teams raced across a new course and five of the teams were able to finish (Thurn, Stanley: The Robot that won the DARPA Grand Challenge, 2006).

Another popular robot design competition is the RoboCup World Cup, a competition in which designers develop robots that are capable of playing soccer (The Robocup Federation, 2010). In 2001, the organization developed RoboCup Rescue as a means to increase the awareness of the challenges involved in search and rescue operations. RoboCup Rescue provides an objective evaluation of a robot's design and strategy to negotiate an environment and gives researchers a chance to collaborate. At these events, the robots demonstrate their ability to plan and map their paths, overcome obstacles, and search for victims in simulated disaster environments. Yearly competitions provide direct comparisons of different approaches and stimulate steady advancement in robotic technology that will ultimately save lives (The Robocup Federation, 2010).

Mobile robots must be able to navigate autonomously in any environment to be useful in modern society. One of the key technologies for achieving this is map building and localization. Although GPS is a useful technology that is capable of providing an absolute position and can be used for mobile robot navigation, it is sometimes difficult to estimate precisely an exact location during
outdoor navigation. Due to the availability of signals received from global positioning satellites, the accuracy of measuring the robots location by GPS may vary. To improve the accuracy, simultaneous localization and mapping (SLAM) algorithms are designed for mobile robot navigation. These robots require sensors that are able to detect objects and determine orientation. These systems develop errors when placed in rough terrain due to slipping on obstacles such as loose dirt or pebble. When this happens, a robot will lose its orientation due to accumulated error and ultimately not end up at their target location.

The literature that has been reviewed focused on a variety of topics such as robotic competitions, robotic space endeavors, and the use of autonomous heavy machinery. However, the main focus of the research is on current techniques in navigation, sensors and strategies used to navigate using various sensors. From the information obtained, ideas were generated as to how to enable the robot to perceive its surroundings and determine its absolute position. For modern autonomous robots, there are three major methods that are being implemented as a means to determine the absolute location of the robot. These methods are inertial navigation, vision based navigation such as simultaneous localization and mapping and lastly, odometry based methods

Inertial Navigation Systems (INS) rely heavily in the use of accelerometers and gyroscopes as a means to determine position. These systems use dynamic equations of motion to calculate where a robot should be relative to its starting position. This is accomplished by measuring the acceleration on the $X, Y$ and $Z$ axis and integrating this information into velocity and position data. Yang and

Jianmin discuss the merits and limitations of using Global Positioning Satellites and Inertial Navigation Systems (Yang \& Jianmin, 2007). They present a data analysis technique that combines the use of fuzzy logic and a Kalman filter as a way to combine the data from multiple sensors, detect errors and present the information into a coherent matrix that a computer can use to decipher the data to determine the position of the robot or any other vehicle type. Inertial navigation systems experience large amounts of error due to large amounts of noise in the sensors and from the low resolution of GPS. The majority of the research performed in the area of inertial navigation systems focuses on methods to filter the noise with the creation of adaptive Kalman filters and better fuzzy logic control systems (Bian, Jin, \& Tian, 2005).

A notable disadvantage of Kalman filters and fuzzy logic control systems is that the data is processed and then discarded. The GraphSLAM method offers a way to remember where a robot has been and build a map from this information (Thurn \& Montemerlo, GraphSLAM Algorithm with Applications to Large Scale Mapping of Urban Structures, 2005). SLAM stands for simultaneous localization and mapping and SLAM algorithms use sensors to perceive the environment around the mobile robot. The types of sensors used vary but generally include cameras, laser interfaces, radar, and GPS (Thurn \& Montemerlo, GraphSLAM Algorithm with Applications to Large Scale Mapping of Urban Structures, 2005). GraphSLAM applications include the DARPA Grand Challenge where autonomous vehicles used are to create a digital picture of the robots immediate surroundings so that the robot can use that information to determine how to avoid
obstacles, how fast to go, and how to get to its destination. Figure 1 is visualization of the GraphSLAM algorithm.


FIGURE 1. (a) An example of GraphSLAM as viewed from the side. (b) An Example of GraphSLAM as viewed by a robot (Thurn \& Montemerlo, GraphSLAM Algorithm with Applications to Large Scale Mapping of Urban Structures, 2005).

Odometry based systems, also known as "dead reckoning" systems, are very reliable and accurate on smooth, flat terrain and over short distances. However, when traversing rough terrain, especially soft surfaces like sand or gravel in which the terrain itself can move, dead reckoning based systems are typically not considered useful because wheels slip and the measured rotation does not accurately reflect the distance truly traveled (Ojeda, Cruz, Reina, \& Borenstein, 2006). Much research is being conducted in this field to improve the accuracy and simplify the systems that are being implemented on various platforms.

Mobile robots are increasingly being used to explore rough terrain situations such as planetary exploration and military applications. Current control and localization algorithms are not well suited for rough terrain and do not consider the physical characteristics of the vehicle and its environment. Little research has
been performed on the effects of wheel slip which will affect odometry accuracy, traction and performance and could lead to the failure of a localization routine and ultimately the failure of the robot to meet its objective (Reina, Ojeda, Milella, \& Borenstein, 2006). Current methods to detect wheel slippage make use of encoders, gyroscopes and a current indicator to monitor the speed of rotation in the wheels and the resistance incurred (Ojeda, Cruz, Reina, \& Borenstein, 2006).

To many, the obvious solution to keep track of the exact or absolute position of an autonomous vehicle is through the use of GPS. However, GPS has many limitations; the most relevant for this application is the precision of the GPS. GPS manufacturers us a statistic known as CEP or Circular Error Probable and are usually tested under ideal conditions (Earth Measurement Consulting). The CEP is the radius of the circle that will contain approximately 50 percent of the position measurements reported by the GPS receiver. This also means that $50 \%$ of the positions reported by a GPS will be outside of this circle. Another way to measure the accuracy of the GPS is the Distance Root Mean Squared method (2DRMS). 2DRMS is the $95-98 \%$ probability that the position will be within the stated 2 dimensional accuracy. The probability varies between $95-98 \%$ because the standard deviation of latitude and longitude may not always match. Figure 2 illustrates the Circular Error Probable for GPS.


FIGURE 2. Reported GPS location points relative to the absolute position; corrected using WAAS which is GPS supplemented using ground stations (Earth Measurement Consulting).

The accuracy and precision of GPS is not reliable enough for small scale robotic applications. Micro-vehicles will maneuver in areas not much larger than a few square meters and will need to know their location to within a few millimeters depending on the application. Other limitations include area obstructions above $5^{\circ}$ of elevation and can include trees, buildings, fences and cables. These obstructions have the effect of reducing the number of satellites that the GPS can "see," reducing the strength of the signal, creating satellite signal multipath, resulting in the delay of the satellite signal and corrupting the GPS measurements (Earth Measurement Consulting). Figure 3 illustrates how a GPS device can receive incorrect signals through signal multipath.


FIGURE 3. An example of GPS signal multipath with a GPS receiver mounted to a stable base (Earth Measurement Consulting).

Multipath can reduce accuracy up to a few meters (Byun, Hajj, \& Young, 2002). To improve the accuracy of GPS, Real Time Kinematic, or RTK GPS, has been introduced. RTK is a process where GPS signal corrections are transmitted in real time from a reference receiver at a known location to a remote receiver. RTK capable GPS can compensate for atmospheric delay, orbital errors and other variables in GPS geometry, increasing positioning accuracy up to within a centimeter. However, these systems often cost tens of thousands of dollars to purchase and setup (Ashtech Technology, 2010).

Due to the limitations of standard GPS devices and the projected uses of these autonomous micro-vehicles, standard GPS should not be used as a means to precisely locate an autonomous micro-vehicle; thus, a new system must be used as a way to determine absolute position. These strategies include the development of a wide array of sensors, localization techniques, and course planning strategies. When these strategies are employed on tracked vehicles as
they move across landscapes, the vehicles may encounter obstructions that may not be detected as an obstacle that requires avoidance by the array of sensors. These obstacles such as gravel, sand piles, or loose dirt can cause changes in orientation as they shift when being traversed by small vehicles. The change in orientation must be detected and accounted for so that autonomous vehicles will continuously know their location relative to a starting location within a small operating area. This research can be applied to various robotic applications such as extra-planetary exploration and underground mapping, where GPS localization is not available, or other applications in which precision beyond the capability of GPS required such as autonomous air duct cleaning or lawn care.

## II. PROBLEM STATEMENT

Consider an autonomous two track micro-vehicle designed to travel a straight trajectory towards a target location. If the vehicle encounters a change in surface friction, a loss of traction, or slip, occurs. For this research, a slip is defined when a reduction in surface friction results in relative motion between one or both tracks and the surface traveled. The objective of this project is to measure the change in position and orientation of an autonomous two track vehicle which experiences a slip and corrects for the error associated with the slip that has occurred. The primary motivation for this objective is to direct a tracked vehicle to move autonomously to a desired location from a known starting location. Figure 4 is the autonomous tracked micro-vehicle used as the test vehicle for this research. This vehicle is discussed in detail in the section titled "Vehicle Platform." In Figure 4, the major components used for navigation, the compass, the microcontroller along with the encoder wheel and receiver, are shown.


FIGURE 4. Autonomous tracked micro-vehicle with major components.

In the event that the autonomous two track vehicle does not encounter a slip, the vehicle will continue along its original trajectory to the target location (Figure 5(a)). Simultaneous slippage of both tracks, which results in relative motion between both tracks and the surface traveled, will not be considered since the position of the vehicle relative to its starting location is lost. The absolute position of the vehicle is lost because both tracks continue to move and the encoders continue to measure the rotation and translate that information to linear travel when in reality, only the tracks are moving, not the entire vehicle (Figure 5(b)). This case will not be considered because it is outside the scope of the project and must be handled using other localization methods such as those used by
inertial navigation systems. During a single track slip, the vehicle experiences a loss of absolute position in one track due to a loss of traction on that track, while still retaining absolute position in the other track. This changes both the position and orientation of the vehicle from the continued forward motion (Figure 5(c)). Of the cases presented in Figure 5, only Figure 5(c) will be considered for this project. Preliminary thought suggests that GPS localization should be the primary method for locating the autonomous micro-vehicle. However, as discussed in section I, when GPS is available it is not accurate enough because of signal multipath (Figure 3) nor is the level of precision of the GPS measurements great enough (Figure 2) for small scale applications.
a.

b.

c.


FIGURE 5. The ghosted figure represents both the position and orientation of the vehicle if a slip did not occur and the autonomous vehicle's presumed position and orientation when a slip condition is encountered. $\Delta x$ and $\Delta y$ are the error in the $x$ and $y$ direction and $\theta$ is the change in orientation of the vehicle. A tracked micro-vehicle with (a) traction at each track progresses in a straight line, (b) reduced traction on each track cannot maintain absolute position and (c) traction at left track and reduced traction at right track will rotate and travel in an arc in the clockwise direction.

Estimation of the vehicle's new position and orientation is generated using information from a pair of optical encoders and an electronic compass on the vehicle. A process that has been designed to control the autonomous vehicle will determine a new trajectory for the vehicle to travel to the target location. The
process used in this research is limited to only being able to detect one slip per trial, or test of the vehicle.

## III. VEHICLE PLATFORM

The vehicle platform consists of a modified version of the Parallax® Boe-Bot (Parallax, 2010) as seen in Figure 4. Modifications include the use of a tank tread kit from Parallax® that has been fitted to custom wheels that reduce track/wheel separation. These modifications include the addition of spiked guide wheels, pinions used as track tensioners, and a custom encoder wheel. Three components reside onboard the vehicle for navigation: a microcontroller, a compass, and a pair of optical incremental encoders and corresponding light emitter/detector sensors (Parallax, 2010). The microcontroller receives data from the encoders' sensors and compass, which indicate the vehicle's absolute position and orientation with respect to the coordinate system illustrated in Figure 5. Algorithms encoded on the microcontroller then resolve the error associated with an encountered slip condition. The microcontroller is a single processor unit with limited processing speed of 20 MHz that allows only one process to execute at a time. Consequently, the microcontroller cannot simultaneously control the direction and speed of the motors driving the tracks while monitoring the compass and encoder sensors. Therefore a ServoPAL from Parallax® (Parallax, 2010) is utilized for controlling the two Parallax® continuous rotation servo-
motors. The ServoPAL is sent instructions by the microcontroller each time the vehicle needs to start or stop motion. The ServoPAL then executes the instructions independently of the microprocessor until new instructions are received.

The compass, a Hitachi HM55B compass module, has a typical sensitivity of $1.0 \mu \mathrm{~T}$ (microtesla) and a maximum sensitivity of $1.6 \mu \mathrm{~T}$ (Parallax, Inc, 2005). Due to the sensitivity of the compass, small external magnetic fields can alter the compass reading. A range of up to 9 degrees has been experienced with the compass with the vehicle at rest. Also, due to the sensitivity of the compass, testing could not be completed in the presence of other electrical machinery or near metallic objects, both of which would alter the reading of the compass. These limitations are particular only to the device used on this autonomous micro-vehicle which was chosen for compatibility with the microcontroller. Other digital compass devices have increased sensitivity and precision for more accurate and consistent results.

Encoders and sensors are utilized on the vehicle, one on each track, as the rear track guide wheel and are in line with the gears that drive each track. The encoder wheel has 9 holes cut into its surface allowing for 18 instances when the signal of the encoder sensor will change polarity during one revolution of the encoder wheel. The distance the vehicle travels during two polarity changes of the signal to the receiver, is known as an encoder period (ep) (Pilgrim, 2004), which is the equivalent of 1.089 cm of travel (Figure 6). The length of the ep was determined by instructing the vehicle to move a known number of eps and
measuring the resulting distance. Once the distance had been measured, the number of eps was divided by the distance, resulting in one ep being the equivalent of 1.089 cm . This procedure was performed throughout the testing process to ensure its reliability.


FIGURE 6. Example of (a) an incremental encoder wheel and optical receiver and (b) incremental encoder and its square wave output.
(Pilgrim, 2004)

## IV. THEORY

To develop an algorithm to correct for the change in orientation due to a slip, the following factors must be known: 1) the distance from the starting location to the target location, 2) the direction (clockwise or counter clockwise) and magnitude of the change in orientation and 3) how far the track that did not slip traveled during the slip. At the beginning of each trial, the distance to the target destination is provided. The process controlling the vehicle will also determine its beginning orientation using the compass module before initiating movement to the target location. Establishing this baseline, or original orientation, is the first step in detecting the amount of slip that occurs. Once the autonomous tracked vehicle begins traveling to the target location, the controlling process continuously accesses the compass to check the vehicles current orientation and continuously compares it to the original orientation. If the current orientation exceeds the slip threshold, which is the amount of orientation variation allowed within the process, the process will determine that the tracked vehicle is experiencing a slip.

Preceding the detection of a slip, the process continuously monitors the distance traveled by the micro-vehicle. Once the slip threshold has been
exceeded, the process records the distance already traveled and the encoders are reset so that the distance traveled only during the slip can be recorded. While the vehicle is slipping, it will be assumed that vehicle will travel in an arc of constant radius (Figure 7). During the slip, current and previous compass readings are compared. To indicate that the tracked vehicle is no longer in a rotational state, matching orientation readings must be received consecutively from the compass module, signifying that the vehicle is no longer slipping. Once the slip has been completed, the compass is accessed to obtain the current orientation which is then be compared to the original orientation. This allows the process to determine the change in orientation during the slip. The change in orientation combined with the distance that the vehicle traveled will allow the algorithm to determine the vehicles new absolute position based upon the arc length and constant radius assumption. By assuming that the radius of the arc is constant, the parallel, $\varepsilon_{x}$, and perpendicular, $\varepsilon_{y}$, position coordinates can be determined allowing for the absolute position to be calculated. This is illustrated in Figure 7 where COR is the center or rotation, $r$ is the radius of the arc, $L$ is the length of the arc that was traveled during the slip and $\theta$ is the change in orientation due to the slip.


FIGURE 7. Slip geometry with constant radius assumption.

The primary variables from this figure are the lengths $\varepsilon_{x}$ and $\varepsilon_{y}$, which are the position change that the tracked vehicle experiences due to the slip. Appendix I shows the calculations used to find $\varepsilon_{\mathrm{x}}$ and $\varepsilon_{\mathrm{y}}$.

There are three different methods that have been developed to resolve the error associated with an encountered slip condition. Each method, the Arc Compensation Method, the Arc Extension Method and the Line Slip Method, will be tested individually and compared to each other to see which produced the most desirable results. The experiments have been designed to test the algorithms ability to adjust to each variation without further input from the user. The Arc Compensation Method resolves errors associated with slip conditions by
detecting the distance that the non slipping track moved once the algorithm detected a slip after crossing the slip threshold. This differs from the Arc Extension Method through the use of an equation that, once the vehicle has finished slipping, is used to extrapolate how far the vehicle traveled while experiencing slip conditions but prior to crossing the slip threshold. The third method, the Line Slip Method, assumes that when the vehicle encounters a slip condition that no change in position along the $y$ axis occurs. This is discussed in detail in the section titled "The Algorithms." The key difference between the Arc Compensation Method and the Arc Extension Method is how the arc length is calculated. For the Arc Compensation Method, the arc length that is detected by the encoder after crossing the threshold is the length that is used. For the Arc Extension Method, the length of the arc prior to crossing the compass threshold is calculated using

$$
\begin{equation*}
L=L_{p}+\theta_{t}\left(\frac{L_{p}}{\theta-\theta_{t}}\right) \tag{1}
\end{equation*}
$$

where $L_{p}$ is the partial arc length as detected by the encoders and $\theta_{t}$ is the slip threshold and is equal to $15^{\circ}$ for this project. Figure 8 illustrates the different arc lengths.


FIGURE 8. Illustration of partial and total arc length.

The process is designed to power the vehicle on a straight trajectory to its target location and monitor if a slip occurs. If a slip occurs the controlling process will then calculate the vehicles new position and orientation. Once the current position has been determined, the distance from the vehicles current location to the target location is calculated. The vehicle is then oriented to the target destination and then directed to move in a straight trajectory to the target location. The use of triangles to find the distance and the angle to the destination is illustrated in Figure 9.


FIGURE 9. An illustration for returning to the target location.

## V. THE ALGORITHMS

The algorithms are encoded on the microcontroller and are used to resolve the error associated with an encountered slip condition. The microcontroller has 32 bytes of RAM memory and 2 Kbytes of memory dedicated to the EEPROM which is used for the storage of the algorithm. Figure 11 is a flow chart categorizing the algorithm into different stages.


FIGURE 10. A flow chart describing the secession of events within the algorithms as various stages.

The algorithm begins in the Baseline Detection Stage by running an autoalignment routine. The routine checks the encoders to see if a high or low signal
is being received. If the encoder returns a high signal, the algorithm directs the vehicle to rotate the track until the signal from the encoder becomes low. The transition from high to low is seen in Figure 6. This routine is applied to both the left and right tracks to ensure that the encoders are always in the same starting position for each side of the vehicle. Each encoder should begin on an edge so that the first encoder period is 10.89 mm like each encoder period preceding it. Potentially, this could cause a displacement error of up to 10.89 mm if the encoder begins just past the edge of the encoder period. For example, if the encoders begin at two different locations for a 10 ep move, one track may move 108.9 mm and the other track may move 112 mm because of the extra distance to cover before a signal change occurred and would still read the move as 10 eps. This auto-alignment routine is run prior to placing the robot at the origin. After the vehicle has been aligned and placed at the origin, a loop that reads the compass output is executed that makes 10 orientation readings and then determines an average of these 10 values, which then becomes the nominal orientation. An average is needed to deal with the flux the compass experiences, most fluxes are no more than 2 degrees. The distance from the origin to the target location is then provided. A flow chart detailing the steps of the Baseline Detection Stage is presented in Figure 12.


FIGURE 11. A flow chart of the three events that are the Baseline Detection Stage. Green indicates a process and orange describes where the data for that process is acquired.

The autonomous tracked vehicle will begin to move forward from the origin and the algorithm will enter the Slip Monitoring Stage. This stage continuously monitors the compass and the encoders so that the distance traveled and the orientation of the vehicle is always known. The algorithm will stay in this loop unless one of two conditions is met. The first condition is if the amount of encoder pulses equals the desired distance to travel. If this condition is met then the autonomous tracked vehicle has arrived at its destination without experiencing any slip. When this occurs, the algorithm will move to the Target Achievement Stage, as seen in Figure 11, where the vehicle is told to stop forward motion. The second condition for the algorithm to exit the loop is if the compass returns an orientation that is outside of the limits of the given orientation threshold. The slip threshold, $\theta_{\mathrm{t}}$, for this system is 15 degrees from the nominal orientation. If the compass returns a reading outside of these limits, it is assumed that the vehicle is slipping. As the vehicle begins to slip, the algorithm saves the
distance that has already been traveled and resets the counter for the encoders so that the distance traveled during the slip is recorded. The algorithm will then move into the Slip Monitoring Stage which continuously monitors the compass and the encoders. The Slip Monitoring Stage is illustrated in Figure 13.


FIGURE 12. Flow diagram for the Slip Monitoring Stage.

The order in which this loop acquires information is significant due to the way the information is compiled and compared. If the order is changed, the value assigned to the variable for the previous angle reading will always be equal to the value assigned to the variable for the current angle reading and cause only a single cycle through the loop. First the loop checks the encoders to keep track of distance and then the loop compares the previous angle reading from the compass to the current angle reading. If the two angles are different, the loop saves the new angle as the previous angle for comparison in the next time through the loop. The loop then pauses for 0.1 seconds to allow for any change
in orientation that is occurring and then accesses the compass to get a new angle reading and begins the loop again. This loop will continue until the compass provides two consecutive readings at the same orientation.

When two consecutive readings occur, the algorithm will know that the slipping has ceased and will exit the Slip Monitoring Stage and move into the Post Slip Localization Stage which signals a stop in forward motion for the tracked vehicle. The algorithm then takes 10 orientation readings and averages the values to get a final orientation after the slip. The algorithm then enters a routine to find out if the vehicle rotated clockwise or counter clockwise. From this information, the appropriate encoder information can be selected and the angle change can be measured for use later in the algorithm. If the vehicle rotated CW then the data from the left encoder is used, otherwise the information from the right encoder is used. The Post Slip Localization Stage is illustrated in Figure 14.


FIGURE 13. Flow Diagram for the Post Slip Localization Stage.

Up to this point in the algorithm, all versions are the same. For the Arc Compensation Method, the distance traveled during the slip, but prior to the threshold is treated as if the vehicle only travels in the $x$ direction and there is no displacement in the $y$ direction. The distance that the non slipping track traveled is saved as $\varepsilon_{x}$. The displacement in the $y$ direction, $\varepsilon_{y}$, is only accounted for after the slip exceeds the slip angle. Equation 2 is not applied in this version of the algorithm. Figure 15 illustrates that only $L_{d}$ is accounted for in this algorithm and is found simply from encoder information on the non slipping track.


FIGURE 14. Illustration of the arc, $L_{p}$, as detected by the non slipping track and traveling distances for the Arc Extension Method.

For the Arc Extension Method, the distance that the vehicle travels during the slip is estimated using Equation 1 to compensate for the unmeasured arc length. Finding the $x$ position requires more manipulation in this algorithm because the distance traveled during the slip but prior to reaching the threshold has already
been accounted for and just adding the $x$ distance for the entire slip would be the equivalent of

$$
\begin{equation*}
D_{t}=\mathrm{D}_{\mathrm{s}}+\mathrm{D}_{\text {thresh }}+\mathrm{D}_{\mathrm{st}} \tag{2}
\end{equation*}
$$

where $D_{t}$ is the total distance traveled prior to slipping and after the slip, $D_{s}$ is the distance to the slip, $\mathrm{D}_{\text {thresh }}$ is the distance traveled prior to reaching the threshold and $D_{\text {st }}$ is the slip travel, or the distance traveled during the entire slip as illustrated in Figure 14. The total distance equation should not account for $\mathrm{D}_{\text {thresh }}$ and look like

$$
\begin{equation*}
D_{t}=\mathrm{D}_{\mathrm{s}}+\mathrm{D}_{\mathrm{st}} \tag{3}
\end{equation*}
$$

To find the unknown distance of how far the tracked vehicle traveled during the slip but prior to reaching the threshold, the distance traveled during the slip after the threshold can be subtracted from the estimated distance traveled during the entire slip. Equation 7 then becomes

$$
\begin{equation*}
D_{t}=\mathrm{D}_{\mathrm{s}}+\mathrm{D}_{\mathrm{st}}+\mathrm{D}_{\text {thresh }}-\left(\mathrm{D}_{\mathrm{st}}-\mathrm{D}_{\mathrm{pt}}\right) \tag{4}
\end{equation*}
$$

where $D_{p t}$ is the distance traveled while slipping only after crossing the threshold and

$$
\begin{equation*}
D_{\text {thres } h}=\left(\mathrm{D}_{\mathrm{st}}-\mathrm{D}_{\mathrm{pt}}\right) \tag{5}
\end{equation*}
$$

From Figure $15, \varepsilon_{x}$ is equal to $D_{\text {st }}$ for the Arc Extension Method. After cancellation, Equation 4 becomes Equation 3 and allows $D_{t}$ to be found.

The third algorithm, the Straight Line Slip Method, treats the slip as no displacement along the $y$ axis for the entire slip. The distance that is recorded by the encoders during the slip is treated as travel only in the $x$ direction. Figure 16 is an illustration of the Straight Line Slip Method.


FIGURE 15. Illustration of how the Straight Line Slip Method treats a slip.

From this point forward, all three algorithms use the same equations and methods to arrive at the target location. Once the algorithm determines the position of the tracked vehicle after the slip, the algorithm enters the Slip Condition Escape Stage where vehicle precedes 30.5 cm on the post slip
orientation in order to clear the slip condition. The algorithm then enters the Target Location Acquirement Stage and finds the $\varepsilon_{x}$ and $\varepsilon_{y}$ distances traveled, and the orientation required to proceed to its target location is determined. The tracked vehicle then rotates to that orientation and moves forward to the destination. Once the tracked vehicle arrives at the target location a nd enters the Target Location Achievement Stage and the vehicle rotates back to the initial orientation. Figure 17 is an illustration of the decision making process for the complete algorithm.


FIGURE 16. Flow Chart for the structure of the algorithms. Green spaces are processes and decisions, orange spaces are information used to control the process or decision and the blue box is where each algorithm differs. Each stage of the algorithm has been boxed in.

## VI. EXPERIMENT

Many external conditions can cause an autonomous tracked vehicle to deviate from a straight trajectory. In order to simulate a slip condition with a high level of repeatability and control, a deck of new plastic coated playing cards was used. Thirty playing cards are stacked and given a horizontal shear at an angle of $30^{\circ}$ from the ground as shown in Figure 18.


FIGURE 17. Stack of playing cards with an induced shear.

Each trial was setup so that the autonomous tracked micro-vehicle always rotated clockwise and followed a path similar to the one illustrated in Figure 19.


FIGURE 18. An illustration of the general path taken by the microvehicle for each trial.

The experiment was completed in a series of trials that were designed to test the autonomous tracked vehicles capabilities in various situations. Three different
variables were tested: distance to the destination from the origin, distance to the slip and the version of the algorithm that is controlling the tracked vehicle. Table I shows the variables tested during each trial for all three algorithms.

## TABLE I

## VARIABLE MATRIX FOR ALL THREE ALGORITHMS

## Distance to Destination



Each different combination of the variables as marked above with an " $X$ " was tested 10 times on a large wooden table measuring 3 meters by 1.2 meters, resulting in 180 tests for the 18 different combinations. The 1.8 m test substituted a 5 cm slip distance for a 25.4 cm slip distance; the tests for 91.5 cm and 122 cm distances will not have a 25.4 cm distance to slip. This is due to the arctangent (ATN) command in the algorithm which has is limited to a range of -127 to +127 (Martin, Williams, Gracey, Alvarez, \& Lindsay, 2005).This command can be seen on line 222 of the source code for Arc Compensation Method in Appendix IlpI. If the distance after the slip exceeds 127 eps the command will overflow. For example, if the distance remaining after the slip is 132 eps , the algorithm will
calculate this as -122 eps. The algorithm then believes that it has exceeded its destination by 122 eps and will perform later calculations under this assumption which will lead to extremely poor test results. This cause for error was found during testing and leads to a new distance limitation for the tracked vehicle. The new limitation is the traveling distance after recovering from the slip cannot exceed 127 eps or 138 cm .

Testing begins by pressing the reset button on the tracked vehicle, this runs the automatic encoder alignment routine to ensure that the encoders are in the same position. The tracked vehicle is placed on a sheet of one inch grid paper and aligned so that the tracks of the vehicle is parallel with the lines on the grid paper and that the measuring point on the vehicle is consistently in the same position. The distance to the slip is measured from the lower front axle of the vehicle to the center of the set of 30 stacked playing cards which are in line with the trajectory of the tracked vehicle as shown in Figure 20. All distance measurements were taken with a standard steel tape measure to the nearest $1 / 8$ inch and converted to metric.


FIGURE 19. Autonomous tracked vehicle in initial position for testing.

The cards that will become the slip condition are placed in the vehicles paths and visually aligned so that they form a 45 degree angle to the grid paper as shown in Figure 21.


FIGURE 20. Alignment of playing cards that will become the slip condition.

Once the Autonomous tracked vehicle has been aligned and placed at the origin and the cards have been placed in the path of the tracked vehicle, the vehicle sets off on its trajectory. The robot continues until a slip is encountered and after the slip condition is cleared, the vehicle pauses 15 seconds to allow physical measurement of the actual slip angle with a protractor. The vehicle then reorients itself toward the target destination and again pauses for 15 seconds for another measurement with the protractor. Finally, the vehicle continues along its new path to the target destination. Upon completion of the algorithm, the $x$ and $y$ distances from the target location to the place where the robot stopped are recorded.

## VII. RESULTS, DISCUSSION AND ANALYSIS

For each trial of the algorithm, the algorithm detected the angle of slip that it encountered during the trial and reported the angle in degrees to the nearest whole number to the computer interface, the computer only received data, it did not externally control the vehicle. Concurrently, each slip was measured to the nearest whole number using a protractor and recorded in a separate spreadsheet. Both readings were taken as a means to record any error related to the compass as reported by the algorithm with the measurements taken with the protractor being the definitive measure. All measurements taken from the compass are considered measured readings; all measurements taken from the protractor are considered actual readings. The average difference between the actual and measured slip angle is 2 degrees for all the algorithms. The maximum difference is 14 degrees and the minimum is no error between the measurements. The standard deviation between the actual and measured values is 2 degrees. Figure 21 breaks down the amount of difference, by percent, between the actual and measured angles of occurrences.


FIGURE 21. The amount of error in the slip angle measurement.

From Figure 21, 82.2\% of the readings reported by the algorithm experience a difference of 3 degrees or less when compared to the actual value. Figure 21 validate that even though the compass is prone to error; the readings are consistently similar to the actual value and are reliable for use in the algorithm as a means to detect changes in orientation. However, in an effort to reduce the amount of error that propagates in the results, only trials that have a difference of three degrees between the actual reading and the measured reading where considered. All of the following figures represent this change. Figure 22 breaks
down the amount of difference, by percent, between the actual and measured angles of occurrences with a difference of three degrees or less.


FIGURE 22. The amount of error in the slip angle measurement after eliminating trials with a measurement difference of more than three degrees.

This reduces the compasses level of uncertainty to $+/-3^{\circ}$. The protractor has a level of uncertainty of $+/-0.5^{\circ}$.

Table II highlights the metrics for the amount of slip for each algorithm as measured with the protractor (Actual) and as measured by the algorithm (Measured).

## TABLE II

THE AVERAGE, MINIMUM, MAMXIMUM AND STANDARD DEVIATION FOR MEASURED SLIP (M) AND ACTUAL SLIP (A) AS ENCOUNTERED BY EACH ALGORITHM. ALL UNITS IN MM.

|  | Avg. |  |  | Min |  |  | Max |  |  | StdDev |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M | A | M | A | M | A | M | A |  |  |  |
| Arc Extension Method | 16 | 15 | 10 | 8 | 29 | 28 | 4 | 5 |  |  |  |
| Arc Compensation Method | 16 | 16 | 7 | 8 | 23 | 24 | 4 | 5 |  |  |  |
| Straight Line Slip Method | 18 | 19 | 9 | 12 | 33 | 31 | 4 | 5 |  |  |  |

Table II shows that the characteristics of slipping are similar for each algorithm as measured by the algorithm. Because the amount of slip is not a controlled variable, the results of each slip are monitored and recorded to ensure that there are no biases between each algorithm.

Another point of interest is if the amount of slip the tracked vehicle encountered would have any impact on the vehicles ability to reach its target location. Figures $23-25$ are the final destination results versus the amount of slip measured by the compass the vehicle experienced for each trial and each method.


FIGURE 23. Measured angle of slip versus absolute error between actual and target location for the Arc Extension Method.


FIGURE 24. Measured angle of slip versus absolute error between actual and target location destination for the Arc Compensation Method.


FIGURE 25. Measured angle of slip versus absolute error between actual and target location for the Straight Line Slip Method.

Figures 23-25 show a trend that is independent of each method. As the angle of slip increases, the distance to the target location from the point that the robot stopped decreases. This result was unexpected since greater orientation changes are associated with larger arc lengths and lower accuracy in achieving the target destination. This is not the case. The change in orientation is found to be independent of the arc length.

Along with being able to detect changes in orientation, the algorithms must be able to determine the vehicles new position that results from the slip. The algorithms combine orientation information and position information from the compass and the encoder, from which the algorithm can determine the new position of the vehicle. A key component to finding the position after a slip is determining the arc length that the tracked vehicle traveled during the slip. The
three algorithms employ three different methods to determining the vehicle's post-slip position.

The simplest method to determine the arc length is employed by the Straight Line Slip Method. This algorithm makes the assumption that the tracked vehicle did not travel in an arc during the slip, but rather slipped along a straight line and did not change position along the y axis. The most involved method to determine the arc length is the Arc Extension Method. This algorithm uses Equation 1 to account for the arc that the tracked vehicle traveled prior to crossing the slip threshold of 15 degrees. The Arc Compensation Method is similar to the Arc Extension Method but does not account for any slip prior to crossing the slip threshold.

Figure 26 shows the variations in the length of the arc for each slip.


FIGURE 26. Arc length of each trial for the Arc Extension Method compared to where the tracked vehicle stopped relative to the target location before remove outliers. Each ep is equal to 10.89 mm .

From Figure 26, the arc length is sometimes equal to zero and ranges to 80 eps ( 37.1 cm ). Based on observation, it is known that the case of zero arc length and the case of 80 eps arc length are untrue. From observation, a normal slip is between 1 and 16 cm . From the data recorded, only $51.7 \%$ of the values for the arc length when measured by the Arc Extension Method fall into this range. Also from the data, $21.7 \%$ of the values where measured to be zero. The reasons for these calculations is due to the compass; as soon as the compass reports that it has surpassed the 15 degree threshold it exits the loop and begins to wait for the compass to report back that the tracked vehicle is no longer slipping. The precision of the compass declines while the tracked vehicle is in motion, which is why the algorithm takes the orientation measurements used for calculations while
the tracked vehicle is stopped and why the 15 degree threshold is in place and not a lower amount. If the tracked vehicle was never slipping when the compass reported back the measurement or if the tracked vehicle was slipping but never changed orientation by more than 15 degrees then the arc was measured as zero. This is confirmed by the data which reports that for each occurrence of a zero arc length, the compass reported an angle change of 15 degrees or less $69 \%$ ( 9 of 13 instances) of the time.

The error resulting in large erroneous arc lengths originates in the assumption that the radius of the arc is constant and is manifested through Equation 2 which relies on a continuous change in orientation in order to be applicable. If the tracked vehicle changed orientation gradually up until the 15 degree threshold and then drastically changed orientation after crossing the threshold, Equation 1 assumes that the drastic change occurred throughout the entire slip and calculates the position information as if this were true.

In order to gain a better perspective on the Arc Extension Method's ability to measure the arc length, the erroneous data points were eliminated. All arc lengths that were greater than or equal to 25 eps have been eliminated, as have all data points equal to zero arc length. Figure 27 is the same as Figure 26 with the outliers removed.


FIGURE 27. Arc length of each trial for the Arc Extension Method compared to where the tracked vehicle stopped relative to the target location with outliers removed. Each ep is equal to 10.89 mm .

From Figure 27, as the arc length increases during each slip, the distance to the target location from where the vehicle stopped also increases. The same trend can be seen for the Arc Compensation Method as illustrated in Figure 28.


FIGURE 28. Arc length of each trial for the Arc Compensation Method compared to where the tracked vehicle stopped relative to the target location.

The results from Figures 27 and 28 are expected. The longer the arc length, the greater the displacement during a slip, which this requires more correction to the tracked vehicles path. Another result that can be seen in Figures 27 and 28 is the distribution of slip lengths. Figure 29 illustrates the percentage of occurrences at each arc length for the Arc Compensation Method.


FIGURE 29. Percentage of arc lengths at each length for the Arc Compensation Method.

From Figure 29, the percentage of arc lengths is greater for the smaller arc lengths for the Arc Compensation Method. Figure 30 is the percentage of occurrences at each arc length for the Arc Extension Method.


FIGURE 30. Percentage of arc lengths at each length for the Arc Extension Method.

From Figure 30, the distribution in arc lengths shifts for the Arc Extension Method. This is expected since this method calculates a longer arc because it considers the arc prior to crossing the slip threshold. Figures 29 and 30 also show a significant amount of slips resulting in and arc length of one ep (10.89 mm ). This may is a result of both methods ability to detect when the tracked vehicle has finished slipping. Currently, the algorithm requires the compass to return two identical readings consecutively while slipping. If the vehicle is not rotating quickly enough between readings, the algorithms may prematurely signal that the vehicle is done slipping. Figures 27 and 28 support this theory, they illustrate that the tracked vehicle stops at highly varying distances from the target
location when the arc length is equal to one ep for both methods. It seems to me that if the slip was measured less that actual, the vehicle would fall short of the target. Figures 27 and 28 do not show this, but all of your figures later (those showing xy plots from destination) do. Indicate that as shown later, these two methods almost always (use percentage rather than my relative grammar here) fall short of the destination.

After each trial, the distance to the target location to the point that the vehicle stopped was measured in the $x$ and $y$ direction and recorded using a standard tape measure. From this data, information and statistics for each algorithm were tabulated and modeled with scatter plots. For each series of test, the distance that the vehicle had to travel was varied from $0.9 \mathrm{~m}(3 \mathrm{ft}), 1.2 \mathrm{~m}(4 \mathrm{ft})$ and 1.8 mm (6 ft). Overall, the Arc Compensation Method averaged a radial distance of 60 mm from the target location to the point that the vehicle stopped. Figure 31 plots where the tracked vehicle stopped for each trial relative to the target location for all three methods.


FIGURE 31. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for all test data and for all three methods. The direction of travel relative to the graph is from right to left.

From Figure 31, each method displays varying levels of precision and accuracy. The Line Slip Method has a wide range of data points whereas the Arc Compensation Method has a more concentrated grouping of data points. The Arc Extension Method tends to be concentrated in the first quadrant. Figure 32 plots where the tracked vehicle stopped for each trial relative to the target location for the Arc Compensation Method alone.


FIGURE 32. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for all tests of the Arc Compensation Method. The direction of travel relative to the graph is from right to left.

From this figure, the tracked vehicle consistently came short of the target location and never stopped at the coordinate $(0,0)$ which is the target location. The Arc Compensation method had an average distance to the target location from the point that the vehicle stopped of 53 mm . Figure 33 illustrates the distance to the target location for the short range test.


FIGURE 33. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the Arc Compensation Method. The direction of travel relative to the graph is from right to left.

From Figure 33, the algorithm generally directed the tracked vehicle not to travel as far as necessary to reach the target location along the $x$ axis and directed the tracked vehicle to travel too far along the $y$ axis. From this information, it can be suggested that that algorithm over calculated the return angle in conjunction with operating within a 10 degree range (+/-5 degrees from measured) when obtaining the return angle, (this range does not include the up to three degree error of the compass) causing the vehicle to underperform. The 10 degree range is necessary because of the low resolution of the compass.

Figure 34 plots the distance to the target location for the 121.9 cm total distance tests.


FIGURE 34. The distance from where the vehicle stopped with respect to the target location at coordinate $(0,0)$ for the $121.9 \mathrm{~cm}(4 \mathrm{ft})$ test of the Arc Compensation Method. The direction of travel relative to the graph is from right to left.

From the above figure, the algorithm again consistently did not direct the vehicle to travel far enough in the parallel direction. However, the algorithm equally missed the target along the perpendicular axis by traveling both too far and too short. From this information, it can be determined that the algorithm does not consistently over calculate or under calculate the return angle or that the compass operating range that is allowed is too much. It is thought that methods for determining how far the tracked vehicle traveled during the slip may not be
accurate enough to achieve extremely high resolution results but are very good at low resolution estimation.

Figure 35 plots the distance to the target location for the 182.9 cm total distance tests.


FIGURE 35. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the 182.9 cm (6 ft ) test of the Arc Compensation Method. The direction of travel relative to the graph is from right to left.

From Figure 35 , the suggestion that the algorithm always over calculates the return angle can be completely ruled out. Another factor may be the distance traveled. The short range test consistently over calculated the angle giving
results in the fourth quadrant, the medium range was centered along the $y$ axis and the long range test consistently under calculated the angle and gave results in the first quadrant. Figures $33-35$ show that in each series of tests, the tracked vehicle did not travel the correct distance in the $x$ direction. The error does not lie in the angle calculation but in the algorithms ability to measure for how far the vehicle traveled in the $x$ direction during a slip. The long range test added more distance to travel and therefore resulted in smaller return angles, where as the short range test had shorter distance to travel and produced larger return angles. Therefore it is the algorithms ability to measure slip travel in the x direction that is in error and not the algorithms ability to place the vehicle on the correct return trajectory. This can also be seen in the series of test in which the Arc Extension Method is used to control the tracked autonomous vehicle.

The series of test with the autonomous tracked vehicle running the Arc Extension Method performed much more poorly than the Arc Compensation Method at achieving the target location. Overall, the Arc Extension Method averaged a radial distance of 80 mm from the target location to the point that the tracked vehicle stopped. After eliminating the outliers, the averaged dropped to 70 mm which is $32 \%$ farther than the Arc Extension Method. Figure 36 plots the distance to the target location for all of the tests using the Arc Extension Method.


FIGURE 36. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for all tests of the Arc Extension Method. The direction of travel relative to the graph is from right to left.

The values for the Arc Extension Method are less consistent than the Arc Compensation Method. The tracked vehicle most often ended up in the first quadrant and generally stopped short of the target location. However, the algorithm did stop at the $(0,0)$ coordinate. Figure 37 plots the distance to the target location for the 91.4 cm total distance tests for the Arc Extension Method.


FIGURE 37. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the Arc Extension Method. The direction of travel relative to the graph is from right to left.

From Figure 37, the tracked vehicle consistently did not travel far enough along the $x$ direction. For the series of tests in which the vehicle traveled the short initial distance under control of the Arc Extension Method, the vehicle stopped an average of 65 mm away from the target location in the $x$ direction and 46 mm away in the $y$ direction. Comparatively, when the autonomous tracked vehicle was controlled by the Arc Compensation Method, the tracked vehicle stopped and average of 34 mm away from the target location in the $x$ direction and 25 mm away in the $y$ direction. The tracked vehicle stopped an average of 83 mm radial distance from the target location when under control of the Arc Extension

Method. By comparison, the autonomous tracked vehicle when controlled by the Arc Compensation Method stopped an average of 46 mm radial distance from the target location, an 80\% difference.

Figure 38 plots the distance to the target location for the 121.9 cm total distance tests for the Arc Extension Method..


FIGURE 38. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the 121.9 cm (4 $\mathrm{ft})$ test of the Arc Extension Method. The direction of travel relative to the graph is from right to left.

From Figure 38, the tracked vehicle stopped an average of 46 mm from the target location in the $x$ direction and an average of 54 mm in the $y$ direction. An average radial distance less than 74 mm was recorded for this series of test, with a range of 165 mm and a standard deviation of 51 mm . The standard deviation
for the Arc Compensation Method during the 121.9 cm series of test is 30 mm , a 70\% difference to the respective Arc Extension Method series of testing.

Figure 39 plots the distance to the target location for the 182.9 cm total distance tests for the Arc Extension Method.


FIGURE 39. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the 182.9 cm (6 ft ) test of the Arc Extension Method. The direction of travel relative to the graph is from right to left.

For the series of tests, the Arc Extension Method averaged a radial distance of 55 mm , which is smaller than the 62 mm average for the respective series of test for the Arc Compensation Method. The range and the standard deviation for the Arc Extension Method and the Arc Compensation Method are very similar for the 182.9 cm total distance test. The range for the Arc Extension Method is 112 mm,
doing better than the Arc Compensation Method by 10 mm . The standard deviation is 33 mm for both methods.

The Straight Line Slip Method had an average radial distance from where the vehicle stopped to the target location of 78 mm . This is only 8 mm further than the Arc Extension Method and is 25 mm further than the Arc Compensation Method. The Straight Line Slip Method is also the simplest of the three methods. Being the simplest, the Line Slip Method has no ability to measure change in the y direction during a slip. Figure 40 plots the distance to the target location for all of the tests using the Straight Line Slip Method.


FIGURE 40. The distance from where the vehicle stopped with respect to the target location at coordinate $(0,0)$ for all tests of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left.

The consistency of the Straight Line Slip Method is poorer than the Arc Compensation Method and the Arc Extension Method. One of the most notable aspects of these results is how often the algorithm directed the tracked vehicle to travel the appropriate distance in the $x$ direction, this could because the method does not perform any numerical calculation in relation to the distance traveled in the $x$ direction that would shorten that distance such as sine and cosine operations. The average distance in the $x$ direction that the tracked vehicle traveled when controlled by the Straight Line Slip Method is 21 mm compared to the 32 mm of the Arc Compensation Method. Although the Straight Line Slip

Method performed very well in directing the tracked vehicle to travel the appropriate distances in the $x$ direction, the algorithm performed the worst in determining the distance to travel in the $y$ direction. The algorithm had an average distance to the target location in the $y$ direction of 71 mm compared to the 37 mm average of the Arc Compensation Method, a 56\% difference. The Arc Extension Method averaged 45 mm in the $y$-direction, a $37 \%$ difference compared to the Straight Line Slip Method.

Figure 41 plots the distance to the target location for the 91.4 cm total distance tests for the Straight Line Slip Method.


FIGURE 41. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the $91.4 \mathrm{~cm}(3 \mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left.

The Straight Line Slip Method differs the most with its results by having more results in quadrant N than the other two algorithms. During the 91.4 cm total distance series of test, $100 \%$ of the data is in quadrants III and IV indicating that the Straight Line Slip Method routinely measured a larger return angle than was necessary. The reason for this is because the algorithm does not consider how far it travels in the $y$ direction during a slip.

Figure 42 plots the distance to the target location for the 121.9 cm total distance tests for the Straight Line Slip Method.


FIGURE 42. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the 121.9 cm (4 $\mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left.

From Figure 42, the majority of the results are in quadrants III and N. For all the series of tests with the Straight Line Slip Method controlling the tracked vehicle, $66 \%$ of the results are in quadrants III and N . For the test series with a total travel distance of $121.9 \mathrm{~cm}, 60 \%$ of the data are in quadrants III and IV. One of the most notable pieces of information from Figure 42 is the fact that the vehicle stopped at the coordinate $(0,0)$ during one of its test while under the control of this method.

Figure 43 plots the distance to the target location for the 182.9 cm total distance tests for the Straight Line Slip Method.


FIGURE 43. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0,0)$ for the $182.9 \mathrm{~cm}(6$ $\mathrm{ft})$ test of the Straight Line Slip Method. The direction of travel relative to the graph is from right to left.

The assumption that the Straight Line Slip Method usually calculates the angle of return as larger than necessary is incorrect. The variance along the $y$ axis is due to not measuring or calculating the change in position along the $y$ axis during a slip.

From the Arc Extension Method, it was discovered that attempting to interpolate how far the tracked vehicle slipped under the assumption that the radius of the slipping arc is constant will result in inconsistent results. The Straight Line Slip Method generated good insight to estimating the how far the tracked vehicle needs to travel in the $x$ direction to reach the target location. This
insight is that it may be better to not tamper with the slip in the $x$ direction measurement. From the Arc Compensation Method, consistent and high accuracy results were produced, but showed the need for better estimating the distance to travel in the $x$ direction. All the results demonstrated the need for a higher resolution compass so that the tolerances for the compass could be tightened.

From this data, information and statistics for each algorithm were tabulated and modeled. The following figures document the precision and accuracy of the algorithms by generating circles for varying levels of accuracy. The smaller circles represent a higher level of accuracy. This type of figure will be referenced as a bull's-eye plot. Figures 42-44 plot the distance from the target location to the point that the tracked vehicle stopped within a bull's-eye plot. The plots document the percentage of data that lies within each level of accuracy. The Arc Compensation Method is represented in Figure 44, the Arc Extension Method is represented in Figure 45 and the Straight Line Slip Method is represented in Figure 46.

FIGURE 44. The distance from where the tracked vehicle stopped with respect to the target location at coordinate $(0$,
0) for all tests of the Arc Compensation Method. Five percent of the data lies within 25 mm of the target location,
$75 \%$ lies within 75 mm of the target location and $100 \%$ of the data lies within 125 mm of the target location.



FIGURE 46. The distance from where the tracked vehicle stopped with respect to the target location at coordinate ( 0,0 ) within 75 mm of the target location and $78.3 \%$ of the data lies within 125 mm of the target location.

The Arc Compensation Method performed the best of the three algorithms at directing the tracked vehicle to the target location. Although the algorithm had the least amount of data points within the circle for the highest level of accuracy, only $7.1 \%$ of the data points, the algorithm had $100 \%$ of its data points within the circle for the lowest level of accuracy and $83 \%$ of its data points within the circle for the middle level of accuracy.

Comparatively from Figure 45, the Arc Extension Method had the same amount data points within the circle for the highest level of accuracy as the Arc Compensation Method. However, the algorithm had only $66 \%$ of its data points within the circle for the middle range of accuracy, $18 \%$ less than the Arc Compensation Method. When all three tiers of accuracy are considered, 87.5\% of the data points lie within this region on the bull's-eye plot. This is a less percentage than the Arc Compensation Method.

The Straight Line Slip Method had the most results in the region for the highest accuracy with $9.6 \%$ of the data points at this level. However, this algorithm produced the fewest data points at the two subsequent levels of accuracy with $51.9 \%$ of the data points within the circle for the middle level and $78.8 \%$ within the circle for the lowest level of accuracy. The level of performance for the Straight Line Slip Method was only slightly lower than the performance level of the Arc Extension Method.

The single most informative statistic that can be measured about each algorithm is the distance to the target location from the point that the tracked
vehicle stopped during each trial. Table III compares each algorithm on the basis of the average, the minimum, the maximum and standard deviation for the distance to the target location from the point that the vehicle stopped.

## TABLE III

PERFORMANCE METRICS FOR ALL THREE ALGORITHMS COMPARING THE DISTNACE TO THE

TARGET LOCATION TO THE POINT THAT THE VEHICLE STOPPED. ALL UNITS IN MM

|  | Avg. | Min | Max | StdDev |
| :--- | :---: | :---: | :---: | :---: |
| Arc Extension Method | 70 | 0 | 165 | 43 |
| Arc Compensation Method | 53 | 6 | 123 | 27 |
| Straight Line Slip Method | 78 | 0 | 173 | 46 |

The Arc Compensation Method has a smaller number in each category, indicating a higher level of performance than the other algorithms except for the minimum distance to the target location from the point that the vehicle stopped.

Although the algorithms are able to meet their objectives, and the tracked vehicle and its instruments provide a very capable platform, all still experience some sources of error. The first notable source of error is the tendency to the tracked vehicle to bear right when traversing a straight trajectory. This is due to the mechanical setup of the tracked vehicle and will vary for each setup. There are two primary drivers to the tendency of bearing right for the tracked vehicle.

The first is the variation in the servo motors that drive each track of the vehicle. Although great care was taken to make them as similar as possible, they cannot be identical and will not drive each track equally. This will also change based on the power level of the batteries driving the servos. The second driver is the track of the vehicle itself. The guide wheels for each track are attached to the chassis by two nuts, a bolt and a washer. The amount of torque on each bolt affects how freely the guide wheels rotate. Each wheel was setup to rotate as freely as possible, however, the freedom of rotation for each wheel varies.

To measure how much this affected the tracked vehicle, a series of 10 test where run in which the vehicle traveled a distance of 182.9 cm and it was recorded how far the vehicle had varied from the straight trajectory at 305 mm increments. Figure 47 documents this tendency by plotting the amount of deviation from a straight line for each measurement during each test.


FIGURE 47. Measurements of tracked vehicle position relative to true during a straight line test at 305 mm (1 ft) increments with best fit line for the data. The equation of the best fit line is $\mathrm{Y}=$-9E$05 x 2+0.0262 x+0.2268$. The line has an $R 2$ value of 0.9599 .

The tracked vehicle's tendency to bear right is slight up to $915 \mathrm{~mm}(3 \mathrm{ft})$, where according to the best line equation; the variance is at 51 mm . At the 1219 mm mark, the variance doubles to 102 mm of variance. At $1830 \mathrm{~mm}(6 \mathrm{ft})$, the best fit equation predicts a variance of 253 mm . This information suggests that the tracked vehicle is subject to extreme straight line variations when traveling long distances. However, if the tracked vehicle is limited to distances of less than 1 meter during straight line travel, then variances will be slight. These figures will not be the same for each vehicle setup and the results for this project have not been adjusted to account for any straight line variance.

The second notable source of error is the tolerance limits that are built into the algorithm and are the result of a combination of two sources. The compass provides acceptable results but is not precise enough to provide high levels of accuracy. Therefore tolerances had to be built into the algorithms to allow for the
variations resulting from the degree changes that the compass measured and the true amount of change in orientation actually existed. For each algorithm, the tolerance is +/- 5 degrees, which allows for a 10 degree range in which the tracked vehicle can operate in. It is thought that this source of error is the primary limitation on improving the accuracy of the algorithms.

A third source of error is due to the microcontroller used for the tracked vehicle. The Basic Stamp 2, which has its limitations stated above, only allows for whole number math and therefore cannot perform division and multiplication that results in parts of number. The microcontroller will perform the math and then round down to the next whole number and report that number as its result. This will affect such calculations as determining how far the tracked vehicle must travel and cause small errors while covering distances.

Overall, all three algorithms met the objective of directing the tracked vehicle to the target location. The Arc Compensation Method proved to be the most capable algorithm for directing the tracked vehicle to the target location. The tracked vehicle has a length dimension of 210 mm . For the Arc Compensation Method, $92.8 \%$ of the trials resulted with at least $50 \%$ of the length of the tracked vehicle being within a half body length radius $(105 \mathrm{~mm})$ of the target location.

## VIII. CONCLUSIONS

Three methods were created and tested to find which method was better able to direct a robot to the target location, detect changes in position and orientation as a result of a slip condition and correct for changes associate with a slip. The Arc Compensation Method produced the best results at achieving the target destination. The Line Slip Method produced the worst results at achieving the target location but was the most capable at calculating the correct distance to travel in the $x$-direction. The Arc Extension Method produced results that were in between the other two methods; however, this method produced more realistic results for detecting the arc length.

As the arc increases, the vehicles ability to achieve the target destination decreases. This applies to both the Arc Extension Method and the Arc Compensation Method and was expected since the greater the arc length, the greater the displacement of the slip. The Straight Line Slip Method does not consider the arc length to determine the amount of slip incurred.

As the change in orientation increases for a slip, the ability to achieve the target location will increase. This proves that the initial assumption of a constant
radius arc formed during a slip is incorrect. Therefore, the use of this assumption results in poor arc length estimations for slips with varying rates of rotation.

With the elimination of arc length outliers, the Arc Extension Method gives a more realistic distribution of arc lengths. The Arc Compensation Method tends to report shorter arc lengths; this was expected since the Arc Extension Method includes the arc length prior to crossing the slip threshold. Without the elimination of arc length outliers, the Arc Extension Method produces many values that exceed expectation and are not realistic. These results that exceed expectation are due to the initial assumption of a constant radius arc. Both methods produced a significant amount of zero length arc lengths and is a result of each methods ability to determine when the tracked vehicle has ceased to slip.

## IX. FUTURE WORK

For future applications of the Arc Compensation Method, the platform should include a compass with significantly better resolution than the one used for this project. This is so the orientation tolerances can have a smaller operating range and provide greater accuracy in orientation measurement, especially when the autonomous tracked vehicle is moving. In conjunction with this recommendation, the ability for the compass to operate in a noisy environment with multiple strong magnetic fields should be increased with shielding or by some other method. One of the most difficult aspects of this project was to find a suitable testing place that was void of a lot of electronics and far from large quantities of metal that altered the Earth's magnetic field. Another suggested implementation is the use of a microcontroller that is capable of math using partial numbers to reduce any error associated with not being able to use partial numbers. A method of detecting slip should be created that does not rely on the constant radius arc assumption to improve the accuracy of the arc length detection. Lastly, a method should be created from the best components of the three methods presented.

## X. WORKS CITED

Ashtech Technology. (2010). RTK (Real Time Kinematic). Retrieved April 20, 2010, from Magellangps.com:
http://pro.magellangps.com/en/products/aboutgps/rtk.asp

Bian, H., Jin, Z., \& Tian, W. (2005). Study on GPS attitude determination system aided INS using adaptive Kalman filter. Measurement Science and Technology, 2072-2079.

Byun, S., Hajj, G., \& Young, L. (2002). Assessment of GPS Signal Multipath Interface. San Diego, CA: Jet Propulsion Laboratory, California Institute of Technology.

Earth Measurement Consulting. (n.d.). GPS Accuracy and Limitations.
Retrieved Feb 16, 2010, from Earth Measurement and Cooling: www.earthmeasurement.com/GPS_accuracy.html

Martin, J., Williams, J., Gracey, K., Alvarez, A., \& Lindsay, S. (2005). BASIC Stamp Syntax and Reference Manual Version 2.2. Rocklin, CA: Parallax.

Ojeda, L., Cruz, D., Reina, G., \& Borenstein, J. (2006). Current-Based Slippage Detection and Odometry Correction for Mobile Robots and Planetary Rovers. IEEE Transactions on Robotics , 366-378.

Parallax. (2010). Parallax.com. Retrieved March 21, 2010, from www.parallax.com

Parallax, Inc. (2005, May). Hitachi® HM55B Compass Module (\#29123). Retrieved April 11, 2010, from Parallax.com: http://www.parallax.com/Portals/O/Downloads/docs/prod/compshop/HM55BModD ocs.pdf

Pilgrim, P. C. (2004, April 11). Applying the Boe-Bot Digital Encoder Kit (\#28107). Retrieved April 11, 2010, from Parallax.com:
http://www.parallax.com/Portals/0/Downloads/docs/prod/datast/ApplyEncoder.pdf

Reina, G., Ojeda, L., Milella, A., \& Borenstein, J. (2006). Wheel Slippage and Sinkage Detection for Planetary Rovers. IEEE/ASME Transactions on Mechatronics, 185-195.

The Robocup Federation. (2010). RoboCup. Retrieved April 11, 2010, from www.robocup.org

The Robocup Federation. (2010). RoboCup Rescue. Retrieved March 7, 2010, from http://www.robocuprescue.org/

Thurn, S. (2007). Junior: The Stanford Entry in the Urban Grand Challenge. Stanford Artifical Intelligence Lab, Stanford University.

Thurn, S. (2006). Stanley: The Robot that won the DARPA Grand Challenge. Journal of Field Robotics .

Thurn, S., \& Montemerlo, M. (2005). GraphSLAM Algorithm with Applications to Large Scale Mapping of Urban Structures. The Internation Journal of Robotics Research (25), 403-429.

Yang, Q., \& Jianmin, S. (2007, Nov 3). A Location Method for Autonomous Vehicle Based on Integrated GPS/INS. IEEE Xplore .

## APPENDIX I

## FIND ING $\varepsilon_{X}$ AND $\varepsilon_{Y}$ LENGTHS

$$
\begin{equation*}
\beta=\theta \tag{I1}
\end{equation*}
$$

where $\beta$ is the arc angle and $\theta$ is measured from the compass readings. The radius of the arc in degrees is found using

$$
\begin{equation*}
r=\left(\frac{L}{\theta}\right)\left(\frac{180}{\pi}\right) \tag{I2}
\end{equation*}
$$

where $L$ can be either the total arc length as used by the Arc Extension Method or the partial arc length, $L_{p}$, as used by the Arc Compensation Method. The length is calculated using

$$
\begin{equation*}
z=r \cos \theta \tag{I3}
\end{equation*}
$$

Since the radius of the arc is already known, $\varepsilon_{x}$ and $\varepsilon_{y}$ lengths are found using

$$
\begin{equation*}
\varepsilon_{\mathrm{y}}=r-z=r-r \cos \theta \tag{14}
\end{equation*}
$$

$$
\begin{equation*}
\varepsilon_{x}=r \sin \theta \tag{15}
\end{equation*}
$$

The resultant is seen in Figure 7. By subtracting $\varepsilon_{x}$ and the distance traveled before the slip from the distance from the origin to the destination, the distance to the target location in the $x$ direction is determined. Using Equation 5 and the distance to the destination in the $x$ direction, a new orientation to the destination is set and a new traveling distance is calculated using Pythagorean's Theorem.

## APPENDIX II

## Test Data

|  |  | Equation 1 ? | Distance to Slip (mm) | Distance from Origin | Nominal Angle (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Test \# | 1 | Y | 50.8 | 3' (84 eps) | 82 |
| Test \# | 2 | Y | 50.8 | 3' (84 eps) | 76 |
| Test \# | 3 | Y | 50.8 | 3' (84 eps) | 76 |
| Test \# | 4 | Y | 50.8 | 3' (84 eps) | 78 |
| Test \# | 5 | Y | 50.8 | 3' (84 eps) | 79 |
| Test \# | 6 | Y | 50.8 | $3^{\prime}$ (84 eps) | 80 |
| Test \# | 7 | Y | 50.8 | 3' (84 eps) | 80 |
| Test \# | 8 | Y | 50.8 | 3' (84 eps) | 77 |
| Test \# | 9 | Y | 50.8 | 3' (84 eps) | 79 |
| Test \# | 10 | Y | 50.8 | 3' (84 eps) | 79 |
| Test \# | 11 | Y | 50.8 | 4' (112 eps) | 78 |
| Test \# | 12 | Y | 50.8 | 4' (112 eps) | 79 |
| Test \# | 13 | Y | 50.8 | 4' (112 eps) | 79 |
| Test \# | 14 | Y | 50.8 | 4' (112 eps) | 80 |
| Test \# | 15 | Y | 50.8 | 4' (112 eps) | 76 |
| Test \# | 16 | Y | 50.8 | 4' (112 eps) | 82 |
| Test \# | 17 | Y | 50.8 | 4' (112 eps) | 77 |
| Test \# | 18 | Y | 50.8 | 4' (112 eps) | 77 |
| Test \# | 19 | Y | 50.8 | 4' (112 eps) | 79 |
| Test \# | 20 | Y | 50.8 | 4' (112 eps) | 79 |
| Test \# | 21 | Y | 152.4 | 6' (168 eps) | 77 |
| Test \# | 22 | Y | 152.4 | 6' (168 eps) | 81 |
| Test \# | 23 | Y | 152.4 | 6' (168 eps) | 78 |
| Test \# | 24 | Y | 152.4 | 6' (168 eps) | 79 |
| Test \# | 25 | Y | 152.4 | 6' (168 eps) | 78 |
| Test \# | 26 | Y | 152.4 | $6{ }^{\prime}$ (168 eps) | 79 |
| Test \# | 27 | Y | 152.4 | 6' (168 eps) | 78 |
| Test \# | 28 | Y | 152.4 | 6' (168 eps) | 79 |
| Test \# | 29 | Y | 152.4 | 6' (168 eps) | 79 |
| Test \# | 30 | Y | 152.4 | 6' (168 eps) | 78 |
| Test \# | 31 | Y | 152.4 | 3' (84 eps) | 81 |
| Test \# | 32 | Y | 152.4 | 3' (84 eps) | 79 |
| Test \# | 33 | Y | 152.4 | 3' (84 eps) | 78 |
| Test \# | 34 | Y | 152.4 | 3' (84 eps) | 79 |
| Test \# | 35 | Y | 152.4 | 3' (84 eps) | 78 |
| Test \# | 36 | Y | 152.4 | 3' (84 eps) | 78 |
| Test \# | 37 | Y | 152.4 | 3' (84 eps) | 77 |
| Test \# | 38 | Y | 152.4 | 3' (84 eps) | 78 |
| Test \# | 39 | Y | 152.4 | 3' (84 eps) | 80 |
| Test \# | 40 | Y | 152.4 | 3' (84 eps) | 80 |
| Test \# | 41 | Y | 152.4 | 4' (112 eps) | 82 |
| Test \# | 42 | Y | 152.4 | 4' (112 eps) | 82 |
| Test \# | 43 | Y | 152.4 | 4' (112 eps) | 80 |


| Test \# | 44 | Y | 152.4 | 4' (112 eps) | 80 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Test \# | 45 | Y | 152.4 | 4' (112 eps) | 75 |
| Test \# | 46 | Y | 152.4 | 4' (112 eps) | 76 |
| Test \# | 47 | Y | 152.4 | 4' (112 eps) | 74 |
| Test \# | 48 | Y | 152.4 | 4' (112 eps) | 76 |
| Test \# | 49 | Y | 152.4 | 4' (112 eps) | 73 |
| Test \# | 50 | Y | 152.4 | 4' (112 eps) | 76 |
| Test \# | 51 | Y | 254 | 6' (168 eps) | 76 |
| Test \# | 52 | Y | 254 | 6' (168 eps) | 77 |
| Test \# | 53 | Y | 254 | 6' (168 eps) | 79 |
| Test \# | 54 | Y | 254 | 6' (168 eps) | 75 |
| Test \# | 55 | Y | 254 | 6' (168 eps) | 75 |
| Test \# | 56 | Y | 254 | 6' (168 eps) | 74 |
| Test \# | 57 | Y | 254 | 6' (168 eps) | 75 |
| Test \# | 58 | Y | 254 | 6' (168 eps) | 75 |
| Test \# | 59 | Y | 254 | 6' (168 eps) | 74 |
| Test \# | 60 | Y | 254 | 6' (168 eps) | 74 |
| Test \# | 61 | N | 50.8 | 3' (84 eps) | 78 |
| Test \# | 62 | N | 50.8 | 3' (84 eps) | 80 |
| Test \# | 63 | N | 50.8 | 3' (84 eps) | 77 |
| Test \# | 64 | N | 50.8 | 3' (84 eps) | 78 |
| Test \# | 65 | N | 50.8 | 3' (84 eps) | 77 |
| Test \# | 66 | N | 50.8 | 3' (84 eps) | 80 |
| Test \# | 67 | N | 50.8 | 3' (84 eps) | 78 |
| Test \# | 68 | N | 50.8 | 3' (84 eps) | 77 |
| Test \# | 69 | N | 50.8 | 3' (84 eps) | 80 |
| Test \# | 70 | N | 50.8 | 3' (84 eps) | 78 |
| Test \# | 71 | N | 50.8 | 4' (112 eps) | 81 |
| Test \# | 72 | N | 50.8 | 4' (112 eps) | 77 |
| Test \# | 73 | N | 50.8 | 4' (112 eps) | 80 |
| Test \# | 74 | N | 50.8 | 4' (112 eps) | 81 |
| Test \# | 75 | N | 50.8 | 4' (112 eps) | 78 |
| Test \# | 76 | N | 50.8 | 4' (112 eps) | 80 |
| Test \# | 77 | N | 50.8 | 4' (112 eps) | 78 |
| Test \# | 78 | N | 50.8 | 4' (112 eps) | 81 |
| Test \# | 79 | N | 50.8 | 4' (112 eps) | 77 |
| Test \# | 80 | N | 50.8 | 4' (112 eps) | 81 |
| Test \# | 81 | N | 152.4 | 6' (168 eps) | 80 |
| Test \# | 82 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 83 | N | 152.4 | 6' (168 eps) | 80 |
| Test \# | 84 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 85 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 86 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 87 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 88 | N | 152.4 | 6' (168 eps) | 79 |
| Test \# | 89 | N | 152.4 | 6' (168 eps) | 81 |
| Test \# | 90 | N | 152.4 | 6' (168 eps) | 78 |


| Test \# | 91 | N | 152.4 | 3' (84 eps) | 77 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Test \# | 92 | N | 152.4 | 3' (84 eps) | 78 |
| Test \# | 93 | N | 152.4 | 3' (84 eps) | 79 |
| Test \# | 94 | N | 152.4 | 3' (84 eps) | 78 |
| Test \# | 95 | N | 152.4 | 3' (84 eps) | 78 |
| Test \# | 96 | N | 152.4 | 3' (84 eps) | 78 |
| Test \# | 97 | N | 152.4 | 3' (84 eps) | 81 |
| Test \# | 98 | N | 152.4 | 3' (84 eps) | 81 |
| Test \# | 99 | N | 152.4 | 3' (84 eps) | 78 |
| Test \# | 100 | N | 152.4 | 3' (84 eps) | 79 |
| Test \# | 101 | N | 152.4 | 4' (112 eps) | 78 |
| Test \# | 102 | N | 152.4 | 4' (112 eps) | 79 |
| Test \# | 103 | N | 152.4 | 4' (112 eps) | 78 |
| Test \# | 104 | N | 152.4 | 4' (112 eps) | 79 |
| Test \# | 105 | N | 152.4 | 4' (112 eps) | 79 |
| Test \# | 106 | N | 152.4 | 4' (112 eps) | 78 |
| Test \# | 107 | N | 152.4 | 4' (112 eps) | 78 |
| Test \# | 108 | N | 152.4 | 4' (112 eps) | 76 |
| Test \# | 109 | N | 152.4 | 4' (112 eps) | 77 |
| Test \# | 110 | N | 152.4 | 4' (112 eps) | 78 |
| Test \# | 111 | N | 254 | 6' (168 eps) | 78 |
| Test \# | 112 | N | 254 | 6' (168 eps) | 79 |
| Test \# | 113 | N | 254 | 6' (168 eps) | 78 |
| Test \# | 114 | N | 254 | 6' (168 eps) | 77 |
| Test \# | 115 | N | 254 | 6' (168 eps) | 77 |
| Test \# | 116 | N | 254 | 6' (168 eps) | 77 |
| Test \# | 117 | N | 254 | 6' (168 eps) | 78 |
| Test \# | 118 | N | 254 | 6' (168 eps) | 79 |
| Test \# | 119 | N | 254 | 6' (168 eps) | 77 |
| Test \# | 120 | N | 254 | 6' (168 eps) | 77 |
| Test \# | 121 | Straight | 50.8 | 3' (84 eps) | 79 |
| Test \# | 122 | Straight | 50.8 | 3' (84 eps) | 79 |
| Test \# | 123 | Straight | 50.8 | 3' (84 eps) | 82 |
| Test \# | 124 | Straight | 50.8 | 3' (84 eps) | 82 |
| Test \# | 125 | Straight | 50.8 | 3' (84 eps) | 79 |
| Test \# | 126 | Straight | 50.8 | 3' (84 eps) | 80 |
| Test \# | 127 | Straight | 50.8 | 3' (84 eps) | 82 |
| Test \# | 128 | Straight | 50.8 | 3' (84 eps) | 79 |
| Test \# | 129 | Straight | 50.8 | 3' (84 eps) | 80 |
| Test \# | 130 | Straight | 50.8 | 3' (84 eps) | 78 |
| Test \# | 131 | Straight | 50.8 | 4' (112 eps) | 80 |
| Test \# | 132 | Straight | 50.8 | 4' (112 eps) | 79 |
| Test \# | 133 | Straight | 50.8 | 4' (112 eps) | 80 |
| Test \# | 134 | Straight | 50.8 | 4' (112 eps) | 81 |
| Test \# | 135 | Straight | 50.8 | 4' (112 eps) | 76 |
| Test \# | 136 | Straight | 50.8 | 4' (112 eps) | 78 |
| Test \# | 137 | Straight | 50.8 | 4' (112 eps) | 80 |


| Test \# | 138 | Straight | 50.8 | 4' (112 eps) | 79 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Test \# | 139 | Straight | 50.8 | 4' (112 eps) | 82 |
| Test \# | 140 | Straight | 50.8 | 4' (112 eps) | 79 |
| Test \# | 141 | Straight | 152.4 | 6' (168 eps) | 79 |
| Test \# | 142 | Straight | 152.4 | 6' (168 eps) | 81 |
| Test \# | 143 | Straight | 152.4 | 6' (168 eps) | 80 |
| Test \# | 144 | Straight | 152.4 | 6' (168 eps) | 79 |
| Test \# | 145 | Straight | 152.4 | 6' (168 eps) | 81 |
| Test \# | 146 | Straight | 152.4 | 6' (168 eps) | 81 |
| Test \# | 147 | Straight | 152.4 | 6' (168 eps) | 81 |
| Test \# | 148 | Straight | 152.4 | 6' (168 eps) | 80 |
| Test \# | 149 | Straight | 152.4 | 6' (168 eps) | 80 |
| Test \# | 150 | Straight | 152.4 | 6' (168 eps) | 77 |
| Test \# | 151 | Straight | 152.4 | 3' (84 eps) | 78 |
| Test \# | 152 | Straight | 152.4 | 3' (84 eps) | 78 |
| Test \# | 153 | Straight | 152.4 | 3' (84 eps) | 77 |
| Test \# | 154 | Straight | 152.4 | 3' (84 eps) | 78 |
| Test \# | 155 | Straight | 152.4 | 3' (84 eps) | 78 |
| Test \# | 156 | Straight | 152.4 | 3' (84 eps) | 78 |
| Test \# | 157 | Straight | 152.4 | 3' (84 eps) | 79 |
| Test \# | 158 | Straight | 152.4 | 3' (84 eps) | 79 |
| Test \# | 159 | Straight | 152.4 | 3' (84 eps) | 77 |
| Test \# | 160 | Straight | 152.4 | 3' (84 eps) | 76 |
| Test \# | 161 | Straight | 152.4 | 4' (112 eps) | 76 |
| Test \# | 162 | Straight | 152.4 | 4' (112 eps) | 82 |
| Test \# | 163 | Straight | 152.4 | 4' (112 eps) | 80 |
| Test \# | 164 | Straight | 152.4 | 4' (112 eps) | 78 |
| Test \# | 165 | Straight | 152.4 | 4' (112 eps) | 78 |
| Test \# | 166 | Straight | 152.4 | 4' (112 eps) | 78 |
| Test \# | 167 | Straight | 152.4 | 4' (112 eps) | 79 |
| Test \# | 168 | Straight | 152.4 | 4' (112 eps) | 78 |
| Test \# | 169 | Straight | 152.4 | 4' (112 eps) | 78 |
| Test \# | 170 | Straight | 152.4 | 4' (112 eps) | 77 |
| Test \# | 171 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 172 | Straight | 254 | 6' (168 eps) | 79 |
| Test \# | 173 | Straight | 254 | 6' (168 eps) | 75 |
| Test \# | 174 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 175 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 176 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 177 | Straight | 254 | 6' (168 eps) | 76 |
| Test \# | 178 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 179 | Straight | 254 | 6' (168 eps) | 77 |
| Test \# | 180 | Straight | 254 | 6' (168 eps) | 78 |


| Arc Length <br> (eps) | Measured | Measured <br> Radius | Measured <br> x length | Actual Slip <br> y length | Measured Slip <br> Angle (deg) | Difference <br> Angle (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| btwn A/M |  |  |  |  |  |  |


| 16 | 38 | 35 | 22 | 18 | 24 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 29 | 62 | 59 | 44 | 22 | 27 | 5 |
| 16 | 57 | 16 | 2 | 15 | 16 | 1 |
| 25 | 57 | 8 | 1 | 22 | 25 | 3 |
| 48 | 120 | 101 | 56 | 21 | 23 | 2 |
| 1 | 4 | 2 | 0 | 15 | 13 | 2 |
| 2 | 5 | 1 | 0 | 22 | 25 | 3 |
| 14 | 28 | 18 | 7 | 28 | 29 | 1 |
| 12 | 24 | 16 | 6 | 25 | 29 | 4 |
| 16 | 46 | 42 | 27 | 18 | 20 | 2 |
| 0 | 0 | 0 | 0 | 15 | 15 | 0 |
| 32 | 92 | 84 | 54 | 18 | 20 | 2 |
| 14 | 73 | 73 | 73 | 9 | 11 | 2 |
| 0 | 0 | 0 | 0 | 15 | 17 | 2 |
| 3 | 12 | 12 | 11 | 14 | 14 | 0 |
| 12 | 28 | 4 | 0 | 23 | 25 | 2 |
| 33 | 59 | 33 | 10 | 28 | 32 | 4 |
| 0 | 0 | 0 | 0 | 16 | 14 | 2 |
| 6 | 18 | 3 | 0 | 20 | 19 | 1 |
| 1 | 7 | 7 | 6 | 16 | 8 | 8 |
| 0 | 0 | 0 | 0 | 19 | 14 | 5 |
| 12 | 33 | 27 | 15 | 24 | 21 | 3 |
| 1 | 3 | 0 | 0 | 20 | 19 | 1 |
| 0 | 0 | 0 | 0 | 19 | 18 | 1 |
| 4 | 18 | 7 | 2 | 15 | 13 | 2 |
| 3 | 9 | 1 | 0 | 21 | 19 | 2 |
| 6 | 29 | 15 | 4 | 14 | 12 | 2 |
| 1 | 4 | 1 | 0 | 19 | 16 | 3 |
| 1 | 3 | 0 | 0 | 22 | 22 | 0 |
| 21 | 33 | 33 | 29 | 32 | 36 | 4 |
| 0 | 0 | 0 | 0 | 16 | 14 | 2 |
| 8 | 29 | 8 | 1 | 16 | 16 | 0 |
| 0 | 0 | 0 | 0 | 12 | 9 | 3 |
| 2 | 7 | 2 | 0 | 18 | 16 | 2 |
| 5 | 24 | 13 | 4 | 16 | 12 | 4 |
| 0 | 0 | 0 | 0 | 11 | 12 | 1 |
| 1 | 4 | 4 | 4 | 17 | 14 | 3 |
| 5 | 24 | 13 | 4 | 15 | 12 | 3 |
| 0 | 0 | 0 | 0 | 15 | 16 | 1 |
| 2 | 6 | 5 | 2 | 16 | 18 | 2 |
| 0 | 0 | 0 | 0 | 15 | 12 | 3 |
| 4 | 13 | 13 | 10 | 15 | 17 | 2 |
| 2 | 5 | 0 | 0 | 21 | 22 | 1 |
| 1 | 4 | 1 | 0 | 18 | 16 | 2 |
| 1 | 4 | 2 | 1 | 15 | 15 | 0 |
| 6 | 25 | 24 | 21 | 14 | 14 | 0 |
| 0 | 0 | 0 | 0 | 8 | 7 | 1 |


| 5 | 13 | 0 | 0 | 21 | 22 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 14 | 8 | 2 | 14 | 12 | 2 |
| 8 | 23 | 21 | 14 | 19 | 20 | 1 |
| 4 | 19 | 10 | 3 | 11 | 12 | 1 |
| 1 | 8 | 5 | 2 | 12 | 7 | 5 |
| 4 | 11 | 10 | 7 | 18 | 20 | 2 |
| 2 | 7 | 2 | 0 | 16 | 16 | 0 |
| 8 | 22 | 18 | 10 | 23 | 21 | 2 |
| 11 | 33 | 5 | 0 | 19 | 19 | 0 |
| 2 | 9 | 4 | 1 | 15 | 13 | 2 |
| 1 | 14 | 11 | 5 | 15 | 4 | 11 |
| 4 | 29 | 28 | 24 | 11 | 8 | 3 |
| 2 | 38 | 5 | 0 | 9 | 3 | 6 |
| 7 | 22 | 17 | 8 | 22 | 18 | 4 |
| 1 | 14 | 11 | 5 | 9 | 4 | 5 |
| 10 | 26 | 0 | 0 | 24 | 22 | 2 |
| 10 | 20 | 13 | 5 | 24 | 29 | 5 |
| 2 | 8 | 5 | 2 | 15 | 15 | 0 |
| 0 | 0 | 0 | 0 | 15 | 8 | 7 |
| 10 | 34 | 32 | 24 | 19 | 17 | 2 |
| 2 | 7 | 2 | 0 | 14 | 16 | 2 |
| 2 | 13 | 5 | 1 | 11 | 9 | 2 |
| 3 | 10 | 10 | 7 | 20 | 17 | 3 |
| 0 | 0 | 0 | 0 | 11 | 9 | 2 |
| 0 | 0 | 0 | 0 | 11 | 9 | 2 |
| 0 | 0 | 0 | 0 | 15 | 14 | 1 |
| 4 | 21 | 21 | 21 | 11 | 11 | 0 |
| 16 | 40 | 34 | 19 | 21 | 23 | 2 |
| 2 | 11 | 6 | 2 | 11 | 10 | 1 |
| 1 | 14 | 11 | 5 | 9 | 4 | 5 |
|  |  |  |  | 20 | 20 | 0 |
|  |  |  |  | 26 | 24 | 2 |
|  |  |  |  | 22 | 20 | 2 |
|  |  |  |  | 18 | 17 | 1 |
|  |  |  |  | 20 | 23 | 3 |
|  |  |  |  | 22 | 21 | 1 |
|  |  |  |  | 13 | 11 | 2 |
|  |  |  |  | 23 | 23 | 0 |
|  |  |  |  | 20 | 21 | 1 |
|  |  |  |  | 30 | 37 | 7 |
|  |  |  |  | 25 | 25 | 0 |
|  |  |  |  | 26 | 25 | 1 |
|  |  |  |  | 16 | 16 | 0 |
|  |  |  |  | 20 | 17 | 3 |
|  |  |  |  | 14 | 14 | 0 |
|  |  |  |  | 12 | 9 | 3 |
|  |  |  |  | 18 | 16 | 2 |


| 17 | 16 | 1 |
| :---: | :---: | :---: |
| 18 | 17 | 1 |
| 20 | 17 | 3 |
| 20 | 19 | 1 |
| 23 | 25 | 2 |
| 11 | 10 | 1 |
| 15 | 13 | 2 |
| 15 | 16 | 1 |
| 15 | 14 | 1 |
| 15 | 12 | 3 |
| 25 | 22 | 3 |
| 18 | 16 | 2 |
| 18 | 17 | 1 |
| 16 | 15 | 1 |
| 14 | 13 | 1 |
| 20 | 20 | 0 |
| 20 | 20 | 0 |
| 18 | 20 | 2 |
| 20 | 21 | 1 |
| 25 | 26 | 1 |
| 15 | 16 | 1 |
| 16 | 14 | 2 |
| 20 | 19 | 1 |
| 15 | 12 | 3 |
| 23 | 25 | 2 |
| 17 | 15 | 2 |
| 17 | 17 | 0 |
| 19 | 17 | 2 |
| 21 | 17 | 4 |
| 18 | 11 | 7 |
| 15 | 13 | 2 |
| 15 | 14 | 1 |
| 12 | 15 | 3 |
| 24 | 24 | 0 |
| 26 | 12 | 14 |
| 20 | 18 | 2 |
| 17 | 14 | 3 |
| 28 | 29 | 1 |
| 31 | 33 | 2 |
| 19 | 14 | 5 |
| 17 | 14 | 3 |
| 13 | 13 | 0 |
| 14 | 11 | 3 |


| Actual Final Orientation (deg) | Measured Final Orientation (deg) | Difference btwn A/M | $\begin{gathered} \text { x-cord } \\ (\mathrm{mm}) \end{gathered}$ | $\begin{gathered} y \text {-cord } \\ (\mathrm{mm}) \end{gathered}$ | Radius (mm) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 4 | 1 | 25 | -6 | 26 |
| 7 | 8 | 1 | 102 | 108 | 148 |
| 11 | 11 | 0 | 76 | 57 | 95 |
| 11 | 11 | 0 | 76 | 51 | 92 |
| 22 | 22 | 0 | 25 | 38 | 46 |
| 6 | 4 | 2 | 25 | 32 | 41 |
| 11 | 12 | 1 | 95 | 127 | 159 |
| 12 | 16 | 4 | 102 | 140 | 173 |
| 11 | 14 | 3 | 92 | 76 | 120 |
| 13 | 14 | 1 | 64 | 51 | 81 |
| 5 | 5 | 0 | 51 | 108 | 119 |
| 5 | 4 | 1 | 105 | 127 | 165 |
| 6 | 4 | 2 | 51 | 102 | 114 |
| 13 | 12 | 1 | 127 | 200 | 237 |
| 8 | 5 | 3 | 105 | 89 | 137 |
| 9 | 2 | 7 | 105 | 76 | 130 |
| 9 | 4 | 5 | 51 | 102 | 114 |
| 8 | 7 | 1 | 44 | 60 | 75 |
| 5 | 4 | 1 | 29 | 25 | 38 |
| 6 | 7 | 1 | 44 | 0 | 44 |
| 4 | 2 | 2 | 76 | 60 | 97 |
| 5 | 5 | 0 | 25 | 44 | 51 |
| 6 | 5 | 1 | 70 | -44 | 83 |
| 3 | 2 | 1 | 76 | 83 | 112 |
| 5 | 4 | 1 | 22 | 51 | 55 |
| 2 | 2 | 0 | 38 | -19 | 43 |
| 8 | 2 | 6 | 102 | 191 | 216 |
| 4 | 5 | 1 | 48 | 25 | 54 |
| 3 | 2 | 1 | 57 | 6 | 58 |
| 4 | 2 | 2 | 0 | 0 | 0 |
| 20 | 25 | 5 | 70 | -25 | 74 |
| 10 | 9 | 1 | 38 | -13 | 40 |
| 6 | 8 | 2 | 44 | -25 | 51 |
| 8 | 5 | 3 | 25 | 0 | 25 |
| 17 | 16 | 1 | 64 | -16 | 65 |
| 7 | 7 | 0 | 95 | -25 | 99 |
| 20 | 15 | 5 | 51 | 25 | 57 |
| 15 | 12 | 3 | 25 | -6 | 26 |
| 5 | 7 | 2 | 54 | 29 | 61 |
| 10 | 7 | 3 | 57 | -3 | 57 |
| 7 | 5 | 2 | 38 | -13 | 40 |
| 8 | 8 | 0 | 41 | -10 | 42 |
| 3 | 4 | 1 | 102 | 0 | 102 |


| 10 | 12 | 2 | 175 | -19 | 176 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18 | 18 | 0 | 213 | -51 | 219 |
| 10 | 8 | 2 | -6 | -3 | 7 |
| 15 | 16 | 1 | 0 | 0 | 0 |
| 17 | 15 | 2 | 48 | 35 | 59 |
| 7 | 5 | 2 | 13 | -51 | 52 |
| 11 | 9 | 2 | 19 | 19 | 27 |
| 8 | 8 | 0 | 13 | 76 | 77 |
| 9 | 8 | 1 | 6 | -29 | 29 |
| 7 | 5 | 2 | 3 | 64 | 64 |
| 3 | 2 | 1 | 3 | 6 | 7 |
| 8 | 9 | 1 | 32 | 51 | 60 |
| 5 | 4 | 1 | 51 | -32 | 60 |
| 2 | 5 | 3 | 10 | 60 | 61 |
| 5 | 4 | 1 | 13 | 48 | 49 |
| 7 | 7 | 0 | 22 | -25 | 34 |
| 14 | 12 | 2 | 95 | 117 | 151 |
| 9 | 7 | 2 | 41 | 0 | 41 |
| 12 | 12 | 0 | 29 | -73 | 78 |
| 7 | 5 | 2 | 0 | -64 | 64 |
| 7 | 7 | 0 | 19 | -70 | 72 |
| 10 | 18 | 8 | 64 | -76 | 99 |
| 13 | 11 | 2 | 25 | -6 | 26 |
| 8 | 8 | 0 | 51 | 0 | 51 |
| 8 | 8 | 0 | 32 | -64 | 71 |
| 12 | 11 | 1 | 32 | -13 | 34 |
| 9 | 8 | 1 | 25 | -25 | 36 |
| 7 | 5 | 2 | 38 | -38 | 54 |
| 8 | 8 | 0 | -13 | -13 | 18 |
| 21 | 19 | 2 | -38 | -114 | 120 |
| 5 | 4 | 1 | 22 | -70 | 73 |
| 7 | 7 | 0 | 64 | 38 | 74 |
| 2 | 2 | 0 | 38 | 117 | 123 |
| 7 | 7 | 0 | -10 | -29 | 30 |
| 6 | 5 | 1 | 13 | -102 | 102 |
| 6 | 4 | 2 | 25 | -25 | 36 |
| 8 | 5 | 3 | 0 | 41 | 41 |
| 5 | 2 | 3 | 64 | 67 | 92 |
| 3 | 2 | 1 | 41 | -19 | 45 |
| 3 | 4 | 1 | 38 | -13 | 40 |
| 6 | 1 | 5 | 38 | 51 | 64 |
| 6 | 4 | 2 | 25 | -25 | 36 |
| 6 | 4 | 2 | 25 | -29 | 38 |
| 5 | 2 | 3 | 25 | 95 | 99 |
| 6 | 2 | 4 | 51 | 95 | 108 |
| 4 | 2 | 2 | 25 | 64 | 68 |
| 3 | 0 | 3 | 41 | 102 | 110 |


| 15 | 15 | 0 | 25 | 29 | 38 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 11 | 2 | 32 | -29 | 43 |
| 22 | 19 | 3 | 25 | -13 | 28 |
| 8 | 8 | 0 | 48 | -19 | 51 |
| 6 | 4 | 2 | 51 | -3 | 51 |
| 13 | 15 | 2 | 25 | 0 | 25 |
| 10 | 12 | 2 | 38 | 0 | 38 |
| 23 | 21 | 2 | 38 | -29 | 48 |
| 21 | 19 | 2 | 48 | -57 | 74 |
| 6 | 5 | 1 | 25 | 41 | 48 |
| 6 | 0 | 6 | 48 | 73 | 87 |
| 6 | 4 | 2 | 0 | -70 | 70 |
| 1 | 0 | 1 | 0 | -102 | 102 |
| 9 | 8 | 1 | 51 | 51 | 72 |
| 6 | 0 | 6 | 38 | 13 | 40 |
| 10 | 11 | 1 | 25 | 13 | 28 |
| 13 | 14 | 1 | 0 | 51 | 51 |
| 9 | 5 | 4 | 48 | 25 | 54 |
| 2 | 1 | 1 | 38 | -79 | 88 |
| 9 | 8 | 1 | 25 | 25 | 36 |
| 6 | 4 | 2 | 51 | 6 | 51 |
| 1 | 1 | 0 | -6 | 0 | 6 |
| 6 | 4 | 2 | 32 | 41 | 52 |
| 4 | 1 | 4 | 41 | 64 | 76 |
| 5 | 1 | 2 | 51 | 64 | 81 |
| 4 | 2 | 2 | 41 | 114 | 122 |
| 2 | 11 | 9 | 25 | -25 | 36 |
| 7 | 7 | 0 | 22 | 3 | 22 |
| 1 | 1 | 0 | 35 | 57 | 67 |
| 5 | 0 | 5 | 32 | 48 | 57 |
| 11 | 13 | 2 | -19 | -19 | 27 |
| 15 | 15 | 0 | 51 | -83 | 97 |
| 14 | 19 | 5 | 25 | -6 | 26 |
| 7 | 6 | 1 | 0 | -127 | 127 |
| 8 | 9 | 1 | 38 | -25 | 46 |
| 7 | 9 | 2 | 25 | -152 | 155 |
| 5 | 4 | 1 | 0 | -152 | 152 |
| 16 | 14 | 2 | 13 | -114 | 115 |
| 8 | 7 | 1 | 0 | -102 | 102 |
| 19 | 19 | 0 | 0 | -51 | 51 |
| 8 | 7 | 1 | 44 | 13 | 46 |
| 8 | 7 | 1 | 25 | 64 | 68 |
| 4 | 5 | 1 | -19 | -51 | 54 |
| 6 | 5 | 1 | 44 | 6 | 45 |
| 4 | 4 | 0 | 13 | -152 | 153 |
| 5 | 2 | 3 | -25 | -64 | 68 |
| 6 | 4 | 2 | 13 | -89 | 90 |


| 7 | 4 | 3 | -13 | -19 | 23 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 9 | 2 | -13 | -83 | 84 |
| 4 | 5 | 1 | -38 | -95 | 103 |
| 6 | 2 | 4 | 25 | -95 | 99 |
| 5 | 4 | 1 | 0 | -102 | 102 |
| 4 | 0 | 4 | 13 | 25 | 28 |
| 4 | 2 | 2 | 32 | -140 | 143 |
| 5 | 2 | 3 | 0 | 83 | 83 |
| 1 | 2 | 1 | -38 | -76 | 85 |
| 3 | 1 | 2 | 0 | -127 | 127 |
| 3 | 4 | 1 | 0 | -178 | 178 |
| 3 | 2 | 1 | 25 | -57 | 63 |
| 3 | 2 | 1 | 13 | 152 | 153 |
| 5 | 7 | 2 | 13 | -64 | 65 |
| 5 | 7 | 2 | 13 | -38 | 40 |
| 10 | 10 | 0 | 25 | -19 | 32 |
| 13 | 12 | 1 | 0 | -38 | 38 |
| 13 | 11 | 2 | 19 | -64 | 66 |
| 12 | 11 | 1 | 6 | -13 | 14 |
| 13 | 16 | 3 | 0 | -38 | 38 |
| 7 | 9 | 2 | 0 | -44 | 44 |
| 7 | 10 | 3 | 13 | -51 | 52 |
| 10 | 12 | 2 | 0 | -108 | 108 |
| 7 | 4 | 3 | 108 | 64 | 125 |
| 8 | 8 | 0 | 0 | 38 | 38 |
| 5 | 4 | 1 | 32 | -38 | 50 |
| 8 | 5 | 3 | 0 | -25 | 25 |
| 6 | 5 | 1 | 0 | 0 | 0 |
| 6 | 5 | 1 | 13 | 0 | 13 |
| 3 | 2 | 1 | 6 | -127 | 127 |
| 5 | 4 | 1 | 3 | -51 | 51 |
| 4 | 4 | 0 | 6 | -25 | 26 |
| 6 | 4 | 2 | 13 | 70 | 71 |
| 6 | 5 | 1 | 70 | 133 | 151 |
| 5 | 1 | 4 | 16 | -140 | 141 |
| 7 | 4 | 3 | 0 | 6 | 6 |
| 4 | 2 | 2 | 19 | 95 | 97 |
| 4 | 5 | 1 | 13 | 0 | 13 |
| 4 | 5 | 1 | 98 | 51 | 111 |
| 3 | 2 | 1 | 19 | 25 | 32 |
| 3 | 2 | 1 | 25 | 92 | 96 |
| 4 | 2 | 2 | 51 | 64 | 81 |
| 2 | 1 | 1 | 38 | 133 | 139 |

## APPENDIX III

## Source Code



```
'TotalDist = 100
PAUSE 1000
PULSOUT nInp, 500
    'Pulse both servos to move forward
PULSOUT nInp, 1000
    '(left servo)
DO UNTIL ((angle > nomAngle + thresh) OR (angle < nomAngle - thresh)) 'Allows a small variance
from nominal.
    GOSUB Compass
    GOSUB CheckEnco
    'DEBUG DEC ? RCounter
    IF Rcounter = TotalDist THEN GOTO ending 'If the robot encounters no slip and reaches
destination then quit moving.
LOOP
Dist = Rcounter
    'Distance robot has traveled so far.
DEBUG "Distance to Slip: ", DEC Dist,CR
RCounter = 0
LCounter = 0
DEBUG "slipping...",CR
slipping:
DO UNTIL (angle = prevAngle) 'Do untill repeated results.
    GOSUB CheckEnco
    'DEBUG DEC ? RCounter, DEC ? LCounter
    IF (angle <> prevAngle) THEN 'Save old angle as new angle for comparison.
    prevAngle = angle
    ENDIF
    'DEBUG DEC ? prevAngle
    PAUSE 100
in orientation
    GOSUB Compass
LOOP
PULSOUT nInp, 2000 'Stop Servos
PULSOUT nInp, 2000
FOR i = 0 TO 9
        GOSUB Compass
        Sigma = Sigma + angle
NEXT
angle = sigma/10
'Doing some math for the slip...
IF angle > nomAngle THEN 'Slipped and rotated CW
    angle = angle - nomAngle
    arcLength = (LCounter)
    dir = CW
ELSEIF angle < nomAngle THEN 'Slipped and rotated CCW
    angle = nomAngle - angle
    arcLength = (RCounter)
    dir = CCW
ENDIF
DEBUG SDEC ? angle, DEC ? arcLength
'arcLength = arcLength + ((thresh * arcLength)/ (angle - thresh)) 'Arc modification
'DEBUG DEC ? arcLength
sigma = arcLength * 1800 / (angle * 31) 'Here, sigma is the radius of the arc.
angle = angle * 32/45
ycord = sigma - (sigma*(COS angle) / 127)
xcord = sigma*(SIN angle) / 127
Totaldist = TotalDist - xcord - Dist
remmaining.
```

DEBUG "Radius= ", SDEC sigma, CR, SDEC ? ycord, SDEC ? xCord, "Dist remaining= ", SDEC TotalDist,
CR
196 RCounter = 0
RCounter $=0$
LCounter $=0$
PULSOUT nInp, 500 'Move forward
PULSOUT nInp, 1000
'DEBUG "Clearing slip.", CR
DO UNTIL (RCounter = 28) 'Move forward 12 inches to clear slip.
GOSUB CheckEnco
LOOP
PULSOUT nInp, 2000
'Stop Servos
PULSOUT nInp, 2000
DEBUG "Take slip angle measurement.", CR
PAUSE 15000
'Pause for 15 seconds to take measurements.
'DEBUG "Slip cleared.",CR
'Doing some math for the clearance...
ycord $=((28 *$ SIN angle) / 127) + ycord 'In brads
xcord $=(28 * \operatorname{COS}$ angle) / 127
DEBUG SDEC ? ycord, SDEC ? xcord
Totaldist $=$ Totaldist - xcord
'Total distance left in the $x$-dir.
DEBUG SDEC ? TotalDist
sigma = TotalDist ATN ycord 'Redefine sigma to be the angle (in brads) that
robot must rotate from nominal to correct from slip.
'DEBUG "Degree of slip (brad): ", SDEC sigma,CR
sigma = sigma */ 360 'Convert sigma to degrees.
Totaldist $=$ Totaldist HYP ycord 'Total distance from current position.
DEBUG "Degree of Correction: ", SDEC sigma,CR, SDEC ? TotalDist
'DEBUG "Aligning to original destination.", CR
IF dir = CW THEN
PULSOUT nInp, 700 'Rotate CCW to recover from CW slip.
PULSOUT nInp, 700
sigma = nomAngle - sigma 'Redefine sigma to be the complete angle that the
robot must rotate to go to destination.
ELSEIF dir = CCW THEN
PULSOUT nInp, 800 'Rotate CW to recover from CCW slip.
PULSOUT nInp, 800
sigma = nomAngle + sigma 'Redefine sigma to be the complete angle that the
robot must rotate to go to destination.
ENDIF
IF sigma.BIT15 = 1 THEN 'Allows it to calculate across 360 degree boundary.
sigma $=360+$ sigma
DEBUG "Sigma neg.", CR
ENDIF
DEBUG "Angle to Destination: ", SDEC sigma,CR
DO UNTIL ( (sigma + 5) >= angle) AND (angle >= (sigma - 5) )
GOSUB Compass
'DEBUG "Compass angle: ", DEC angle,CR
LOOP
PULSOUT nInp, 2000
'Stop Servos
PULSOUT nInp, 2000
253
254 DEBUG "Take final orientation measurement.",CR

```
PAUSE 15000
                'Pause for 15 seconds to take measurements.
PAUSE 100
RCounter = 0
'Reset encoders
LCounter = 0
DEBUG "Go to original destination.",CR, DEC ? TotalDist
PULSOUT nInp, 500
PULSOUT nInp, 1000
DO UNTIL (Rcounter = TotalDist)
'Go to original destination.
        GOSUB CheckEnco
LOOP
'DEBUG "Arrived.",CR
ending:
PULSOUT nInp, 2000 'Stop Servos
PULSOUT nInp, 2000
PAUSE 150
IF dir = CCW THEN
PULSOUT nInp, }70
'Rotate CCW to begining orientation.
PULSOUT nInp, }70
ELSEIF dir = CW THEN
PULSOUT nInp, 800 'Rotate CW to begining orientation.
PULSOUT nInp, 800
ENDIF
DO UNTIL (nomAngle + 5 > angle) AND (nomAngle - 5 < angle)
        GOSUB Compass
        'DEBUG "Compass angle: ", DEC angle,CR
LOOP
DEBUG "Robot has arrived.",CR
PULSOUT nInp, 2000 'Stop Servos
PULSOUT nInp, 2000
END
'------[Subroutines]--------------------------------------------------------------------
CheckEnco:
'Checks both encoders
REncoValue = INS.LOWBIT(REnco)
IF REncoValue ^ PrevR THEN
RCounter = Rcounter + 1
PrevR = REncoValue
ENDIF
LEncoValue = INS.LOWBIT(LEnco)
IF LEncoValue ^ PrevL THEN
LCounter = LCounter + 1
PrevL = LEncoValue
ENDIF
RETURN
Compass:
GOSUB Compass_Get_Axes
GOSUB Compass_Correct_Offsets
angle = x ATN -y
GOSUB Compass_Interpolate
angle = angle */ 360
'DEBUG DEC ? angle
RETURN
```

321
-----[ Subroutine - Compass_Get_Axes ]----------------------------------------------1
' This subroutine handles BASIC Stamp - HM55B communication and stores the
' magnetic field strength measurements returned by the device in the x and
y axis variables.

```
Compass_Get_Axes: ' Compass module subroutine
    HIGH En: LOW En ' Send reset command to HM55B
    SHIFTOUT DinDout,clk,MSBFIRST,[Reset\4]
    HIGH En: LOW En ' HM55B start measurement command
    SHIFTOUT DinDout,clk,MSBFIRST,[Measure\4]
    status = 0 ' Clear previous status flags
    DO ' Status flag checking loop
    HIGH En: LOW En ' Measurement status command
    SHIFTOUT DinDout,clk,MSBFIRST,[Report\4]
    SHIFTIN DinDout,clk,MSBPOST,[Status\4] ' Get Status
    LOOP UNTIL status = Ready ' Exit loop when status is ready
    SHIFTIN DinDout,clk,MSBPOST,[x\11,y\11] ' Get x & y axis values
    HIGH En ' Disable module
    IF (y.BIT10 = 1) THEN y = y | NegMask ' Store 11-bits as signed word
    IF (x.BIT10 = 1) THEN x = x | NegMask ' Repeat for other axis
```

    RETURN
    
' This subroutine corrects cumulative magnetic field interference that can
' come from sources such as the PCB, jumper wires, a nearby battery, or a
' nearby current source. This subroutine relies on values stored in
' the EEPROM space that was reserved by the CompassOffsets DATA directive.
' These EEPROM values were written by CalibrateHM55BCompass.bs2.
Compass_Correct_Offsets:
READ CompassOffsets, Word axisOffset ' Get x-axis offset
x = x - axisOffset ' Correct x-axis
READ CompassOffsets + 2, Word axisOffset
' Get y-axis offset
y = y - axisOffset ' Correct y-axis
RETURN

This subroutine applies linear interpolation to the refine the compass
measurement. This second level of refinement can be performed after the
Compass_Correct_Offsets subroutine, and it can correct axis skew and other
errors inherent to the HM55B chip.
'
' The subroutine relies on sixteen actual compass measurements that were stored
' in the sixteen EEPROM locations reserved by the CompassCal DATA directive.
' These measurements were stored by CalibrateHM55BCompass.bs2, and they
' represent the actual compass measurements for $0,22.5,45,90, \ldots, 337.5$
' degrees. The subroutine finds the two EEPROM measurements that the current
' angle measurement falls between. It then updates the angle measurement
' based on where the angle measurement falls between the two known table values.
Compass_Interpolate:
' Start with the lowest value in the CompassCal table.
READ CompassLowVal, index
' Load current and previous table values.
READ CompassCal + index, table(current)
READ (CompassCal + (index - 1 \& \$F)), table(previous)
' The IF...ELSEIF...ELSE...ENDIF code block finds the two EEPROM CompassCal
' table values that the current angle measurement falls between and calculates
' the difference between the current angle measurement and the lower of the
' two table values. The IF and ELSEIF blocks deal with values that are
' greater than the highest or less than the lowest table values. The ELSE
' block everything between the highest and lowest table values.
IF (angle >= table(previous)) THEN
span $=(255-$ table(previous)) + table(current)
angleOffset = angle - table(previous)
ELSEIF (angle <= table(current)) THEN
span $=$ table(current) $+(255-$ table(previous))
angleOffset $=$ angle $+(255-$ table(previous))
ELSE
index = index - 1
READ CompassCal + index, table(current)
DO
table(previous) = table(current)
index $=$ index +1
READ CompassCal + index, table(current)
IF (angle <= table(current)) AND (angle > table(previous)) THEN
span = table(current) - table(previous)
angleOffset = angle - table(previous)
EXIT
ENDIF
LOOP
ENDIF
' After the offset between the current angle measurement and the next lower
' table measurement has been determined, this code block uses it along with
' the span between the table entries above and below the angle measurement
' to solve for: angle(corrected) = angle(offset) * $16 / \mathrm{span}$.
' This code block also rounds up or down by comparing the remainder of
' the angleOffset / span division to the value of (span / 2).
angleOffset $=$ angleOffset * 16

angle $=(($ index $-1 \& \$ F) * 16)+$ angle
angle $=$ angle \& \$ff
RETURN


```
'TotalDist = 100
PAUSE 1000
PULSOUT nInp, 500
'Pulse both servos to move forward
PULSOUT nInp, 1000
    '(left servo)
DO UNTIL ((angle > nomAngle + thresh) OR (angle < nomAngle - thresh)) 'Allows a small variance
from nominal.
    GOSUB Compass
    GOSUB CheckEnco
    'DEBUG DEC ? RCounter
    IF Rcounter = TotalDist THEN GOTO ending 'If the robot encounters no slip and reaches
destination then quit moving.
LOOP
Dist = Rcounter
DEBUG "Distance to Slip: ", DEC Dist,CR
RCounter = 0
LCounter = 0
DEBUG "slipping...",CR
slipping:
DO UNTIL (angle = prevAngle) 'Do unitll repeated results.
GOSUB CheckEnco
'DEBUG DEC ? RCounter, DEC ? LCounter
IF (angle <> prevAngle) THEN 'Save old angle as new angle for comparison.
prevAngle = angle
ENDIF
'DEBUG DEC ? prevAngle
PAUSE 100
in orientation
    GOSUB Compass
LOOP
PULSOUT nInp, 2000 'Stop Servos
PULSOUT nInp, 2000
FOR i = 0 TO 9
        GOSUB Compass
        Sigma = Sigma + angle
NEXT
angle = sigma/10
'Doing some math for the slip...
IF angle > nomAngle THEN 'Slipped and rotated CW
    angle = angle - nomAngle
    arcLength = (LCounter)
    dir = CW
ELSEIF angle < nomAngle THEN 'Slipped and rotated CCW
    angle = nomAngle - angle
    arcLength = (RCounter)
    dir = CCW
ENDIF
DEBUG SDEC ? angle, DEC ? arcLength
sigma = arcLength * 1800 / (angle * 31) 'Here, sigma is the measured radius of the arc.
xcord = sigma*(SIN angle) / 127
arcLength = arcLength + ((thresh * arcLength)/ (angle - thresh)) 'Arc modification
DEBUG DEC ? arcLength
sigma = arcLength * 1800 / (angle * 31) 'Here, sigma is the radius of the arc.
angle = angle * 32/45
ycord = sigma - (sigma*(COS angle) / 127)
```

```
1 9 4 ~ x c o r d ~ = ~ ( s i g m a * ( S I N ~ a n g l e ) ~ / ~ 1 2 7 ) ~ - ~ x c o r d ~ ' D i s t a n c e ~ t r a v e l e d ~ w h i l e ~ s l i p p i n g ~ p r i o r ~ t o ~ b r e a k i n g ~
    threshold.
1 9 5 \text { xcord = (sigma*(SIN angle) / 127) - xcord 'Distance traveled during entire slip.}
1 9 6
    Totaldist = TotalDist - xcord - Dist 'Convert total distance to travel to distance
    remmaining.
198
1 9 9 \text { DEBUG "Radius= ", SDEC sigma,CR, SDEC ? ycord, SDEC ? xcord, "Dist remaining= ", SDEC TotalDist,}
    CR
200
RCounter = 0
LCounter = 0
PULSOUT nInp, 500 'Move forward
PULSOUT nInp, 1000
'DEBUG "Clearing slip.",CR
DO UNTIL (RCounter = 28)
        GOSUB CheckEnco
    LOOP
    PULSOUT nInp, 2000 'Stop Servos
    PULSOUT nInp, 2000
    DEBUG "Take slip angle measurement.",CR
    PAUSE 15000
    'DEBUG "Slip cleared.",CR
    'Doing some math for the clearance...
ycord = ((28 * SIN angle) / 127) + ycord 'In brads
xcord = (28 * COS angle) / 127
DEBUG SDEC ? ycord, SDEC ? xcord
Totaldist = Totaldist - xcord
DEBUG SDEC ? TotalDist
sigma = TotalDist ATN ycord 'Redefine sigma to be the angle (in brads) that
robot must rotate from nominal to correct from slip.
228 'DEBUG "Degree of slip (brad): ", SDEC sigma,CR
2 2 9 ~ s i g m a ~ = ~ s i g m a ~ * / ~ 3 6 0 ~ ' C o n v e r t ~ s i g m a ~ t o ~ d e g r e e s . ~
2 3 0 ~ T o t a l d i s t ~ = ~ T o t a l d i s t ~ H Y P ~ y c o r d ~ ' T o t a l ~ d i s t a n c e ~ f r o m ~ c u r r e n t ~ p o s i t i o n . ~
2 3 1 ~ D E B U G ~ " D e g r e e ~ o f ~ C o r r e c t i o n : ~ " , ~ S D E C ~ s i g m a , C R , ~ S D E C ~ ? ~ T o t a l D i s t ~
2 3 2
'DEBUG "Aligning to original destination.",CR
IF dir = CW THEN
PULSOUT nInp, }70
PULSOUT nInp, }70
sigma = nomAngle - sigma
robot must rotate to go to destination.
239 ELSEIF dir = CCW THEN
2 4 0 \text { PULSOUT nInp, 800}
PULSOUT nInp, 800
sigma = nomAngle + sigma
robot must rotate to go to destination.
243 ENDIF
2 4 4 ~ I F ~ s i g m a . B I T 1 5 ~ = ~ 1 ~ T H E N ~ ' A l l o w s ~ i t ~ t o ~ c a l c u l a t e ~ a c r o s s ~ 3 6 0 ~ d e g r e e ~ b o u n d a r y . ~
sigma = 360 + sigma
DEBUG "Sigma neg.",CR
ENDIF
DEBUG "Angle to Destination: ", SDEC sigma,CR
DO UNTIL ( (sigma + 5) >= angle) AND (angle >= (sigma - 5) )
GOSUB Compass
'DEBUG "Compass angle: ", DEC angle,CR
```

```
angle = x ATN -y
' Convert x and y to brads
GOSUB Compass_Interpolate
' Linear interpolation
angle = angle */ 360
' Convert brads to degrees
'DEBUG DEC ? angle
RETURN
' -----[ Subroutine - Compass_Get_Axes ]
' This subroutine handles BASIC Stamp - HM55B communication and stores the
' magnetic field strength measurements returned by the device in the x and
' y axis variables.
Compass_Get_Axes: ' Compass module subroutine
HIGH En: LOW En ' Send reset command to HM55B
SHIFTOUT DinDout,clk,MSBFIRST,[Reset\4]
HIGH En: LOW En
SHIFTOUT DinDout,clk,MSBFIRST, [Measure\4]
status = 0 ' Clear previous status flags
DO ' Status flag checking loop
HIGH En: LOW En ' Measurement status command
DO 
SHIFTIN DinDout,clk,MSBPOST,[Status\4] ' Get Status
LOOP UNTIL status = Ready ' Exit loop when status is ready
SHIFTIN DinDout,clk,MSBPOST,[x\11,y\11] ' Get x & y axis values
HIGH En ' Disable module
IF (y.BIT10 = 1) THEN y = y | NegMask ' Store l1-bits as signed word
IF (x.BIT10 = 1) THEN x = x | NegMask ' Repeat for other axis
' HM55B start measurement command
```

RETURN

' This subroutine corrects cumulative magnetic field interference that can
' come from sources such as the PCB, jumper wires, a nearby battery, or a
' nearby current source. This subroutine relies on values stored in
' the EEPROM space that was reserved by the CompassOffsets DATA directive.
' These EEPROM values were written by CalibrateHM55BCompass.bs2.
Compass_Correct_Offsets:
READ CompassOffsets, Word axisOffset
$x=x$ - axisOffset
READ CompassOffsets +2 , Word axisOffset
$y=y$ - axisOffset
' Get x-axis offset
' Correct $x$-axis
' Get y-axis offset
' Correct y-axis
RETURN
[ Subroutine - Compass_Interpolate ]
' This subroutine applies linear interpolation to the refine the compass
' measurement. This second level of refinement can be performed after the
' Compass_Correct_Offsets subroutine, and it can correct axis skew and other
' errors inherent to the HM55B chip.
' The subroutine relies on sixteen actual compass measurements that were stored
' in the sixteen EEPROM locations reserved by the CompassCal DATA directive.
' These measurements were stored by CalibrateHM55BCompass.bs2, and they
' represent the actual compass measurements for $0,22.5,45,90, \ldots, 337.5$
' degrees. The subroutine finds the two EEPROM measurements that the current
' angle measurement falls between. It then updates the angle measurement
' based on where the angle measurement falls between the two known table values.
' Start with the lowest value in the CompassCal table.
READ CompassLowVal, index
' Load current and previous table values.
READ CompassCal + index, table(current)
READ (CompassCal + (index - $1 \& \$$ )), table(previous)
' The IF...ELSEIF...ELSE...ENDIF code block finds the two EEPROM CompassCal
' table values that the current angle measurement falls between and calculates
' the difference between the current angle measurement and the lower of the
' two table values. The IF and ELSEIF blocks deal with values that are
' greater than the highest or less than the lowest table values. The ELSE
' block everything between the highest and lowest table values.
IF (angle >= table(previous)) THEN
span $=(255-$ table(previous) $)+$ table(current)
angleOffset = angle - table(previous)
ELSEIF (angle <= table(current)) THEN
span = table(current) $+(255-$ table(previous))
angleOffset $=$ angle $+(255$ - table(previous))
ELSE
index = index - 1
READ CompassCal + index, table(current)
DO
table(previous) = table(current)
index $=$ index +1
READ CompassCal + index, table(current)
IF (angle <= table(current)) AND (angle > table(previous)) THEN
span = table(current) - table(previous)
angleOffset = angle - table(previous)
EXIT
ENDIF
LOOP
ENDIF
' After the offset between the current angle measurement and the next lower
' table measurement has been determined, this code block uses it along with
' the span between the table entries above and below the angle measurement
' to solve for: angle(corrected) = angle(offset) * $16 / \mathrm{span}$.
' This code block also rounds up or down by comparing the remainder of
' the angleOffset / span division to the value of (span / 2).
angleOffset $=$ angleOffset * 16

angle $=((i n d e x-1 \& \$ F) * 16)+$ angle
angle = angle \& \$ff
RETURN


```
'TotalDist = 100
PAUSE 1000
PULSOUT nInp, 500
    'Pulse both servos to move forward
PULSOUT nInp, 1000
    '(left servo)
DO UNTIL ((angle > nomAngle + thresh) OR (angle < nomAngle - thresh)) 'Allows a small variance
from nominal.
    GOSUB Compass
    GOSUB CheckEnco
    'DEBUG DEC ? RCounter
    IF Rcounter = TotalDist THEN GOTO ending 'If the robot encounters no slip and reaches
destination then quit moving.
LOOP
Dist = Rcounter
DEBUG "Distance to Slip: ", DEC Dist,CR
RCounter = 0
LCounter = 0
'DEBUG "slipping...",CR
slipping:
DO UNTIL (angle = prevAngle)
    GOSUB CheckEnco
    'DEBUG DEC ? RCounter, DEC ? LCounter
    IF (angle <> prevAngle) THEN
    prevAngle = angle
    ENDIF
    'DEBUG DEC ? prevAngle
    PAUSE 100
in orientation
    GOSUB Compass
LOOP
PULSOUT nInp, 2000
PULSOUT nInp, 2000
FOR i = 0 TO 9
        GOSUB Compass
        Sigma = Sigma + angle
NEXT
angle = sigma/10
'Doing some math for the slip...
IF angle > nomAngle THEN
    angle = angle - nomAngle
    arcLength = (LCounter)
    dir = CW
ELSEIF angle < nomAngle THEN 'Slipped and rotated CCW
    angle = nomAngle - angle
    arcLength = (RCounter)
    dir = CCW
ENDIF
DEBUG SDEC ? angle
arcLength = 0
Dist = Dist + RCounter
DEBUG DEC ? arcLength
sigma = arcLength * 1800 / (angle * 31)
angle = angle * 32/45
ycord = sigma - (sigma*(COS angle) / 127)
xcord = sigma*(SIN angle) / 127
xcord = 4
```

```
1 9 4
```

Totaldist = TotalDist + xcord - Dist
'Convert total distance to travel to distance
remmaining.
CR
198
199 RCounter = 0
LCounter $=0$
PULSOUT nInp, 500 'Move forward
PULSOUT nInp, 1000
'DEBUG "Clearing slip.",CR
DO UNTIL (RCounter = 28) 'Move forward 12 inches to clear slip.
GOSUB CheckEnco
LOOP
PULSOUT nInp, 2000 'Stop Servos
PULSOUT nInp, 2000
'Pause for 15 seconds to take measurements.
'DEBUG "Slip cleared.",CR
'Doing some math for the clearance...
ycord $=((28 *$ SIN angle) / 127) + ycord 'In brads
xcord $=(28 * \operatorname{COS}$ angle) / 127
DEBUG SDEC ? ycord, SDEC ? xcord
Totaldist = Totaldist - xcord Total distance left in the x-dir.
DEBUG SDEC ? TotalDist
sigma $=$ TotalDist ATN ycord 'Redefine sigma to be the angle (in brads) that
robot must rotate from nominal to correct from slip.
'DEBUG "Degree of slip (brad): ", SDEC sigma,CR
sigma = sigma */ 360 'Convert sigma to degrees.
Totaldist $=$ Totaldist HYP ycord 'Total distance from current position.
DEBUG "Degree of Correction: ", SDEC sigma,CR, SDEC ? TotalDist
'DEBUG "Aligning to original destination.", CR
IF dir = CW THEN
PULSOUT nInp, 700 'Rotate CCW to recover from CW slip.
PULSOUT nInp, 700
sigma = nomAngle - sigma 'Redefine sigma to be the complete angle that the
robot must rotate to go to destination.
ELSEIF dir = CCW THEN
PULSOUT nInp, 800 'Rotate CW to recover from CCW slip.
PULSOUT nInp, 800
sigma = nomAngle + sigma 'Redefine sigma to be the complete angle that the
robot must rotate to go to destination.
ENDIF
IF sigma.BIT15 = 1 THEN 'Allows it to calculate across 360 degree boundary.
sigma $=360+$ sigma
DEBUG "Sigma neg.", CR
ENDIF
DEBUG "Angle to Destination: ", SDEC sigma,CR
DO UNTIL ( (sigma + 3) >= angle) AND (angle >= (sigma - 3) )
GOSUB Compass
'DEBUG "Compass angle: ", DEC angle,CR
LOOP
254

```
255 PULSOUT nInp, 2000
PULSOUT nInp, 2000
DEBUG "Take final orientation measurement.",CR
PAUSE 15000
'Pause for 15 seconds to take measurements.
PAUSE 100
RCounter = 0 'Reset encoders
LCounter = 0
DEBUG "Go to original destination.",CR, DEC ? TotalDist
PULSOUT nInp, 500
'Move forward
PULSOUT nInp, 1000
DO UNTIL (Rcounter = TotalDist)
'Go to original destination.
        GOSUB CheckEnco
    LOOP
    'DEBUG "Arrived.",CR
    ending:
    PULSOUT nInp, 2000 'Stop Servos
    PULSOUT nInp, 2000
    PAUSE 150
    IF dir = CCW THEN
    PULSOUT nInp, }70
    'Rotate CCW to begining orientation.
    PULSOUT nInp, }70
    ELSEIF dir = CW THEN
    PULSOUT nInp, 800 'Rotate CW to begining orientation.
PULSOUT nInp, }80
    ENDIF
    DO UNTIL (nomAngle + 3 > angle) AND (nomAngle - 3 < angle)
        GOSUB Compass
        'DEBUG "Compass angle: ", DEC angle,CR
    LOOP
    DEBUG "Robot has arrived.",CR
    PULSOUT nInp, 2000 'Stop Servos
    PULSOUT nInp, 2000
    END
    '----- [Subroutines]------------------------------------------------------------------------
    CheckEnco:
                                    'Checks both encoders
    REncoValue = INS.LOWBIT(REnco)
IF REncoValue ^ PrevR THEN
RCounter = Rcounter + 1
PrevR = REncoValue
ENDIF
LEncoValue = INS.LOWBIT(LEnco)
IF LEncoValue ^ PrevL THEN
    LCounter = LCounter + 1
    PrevL = LEncoValue
    ENDIF
    RETURN
    Compass:
    GOSUB Compass_Get_Axes
    GOSUB Compass_Correct_Offsets
    angle = x ATN -y
GOSUB Compass_Interpolate
'Checks Compass
' Get x, and y values
' Correct axis offsetes
' Convert x and y to brads
' Linear interpolation
```

angle $=$ angle */ 360
Convert brads to degrees
322 'DEBUG DEC ? angle

```
HIGH En: LOW En
SHIFTOUT DinDout,clk,MSBFIRST,[Measure\4]
```

status $=0$ ' Clear previous status flags
DO ' Status flag checking loop
HIGH En: LOW En ' Measurement status command
SHIFTOUT DinDout,clk, MSBFIRST, [Report\4]
SHIFTIN DinDout, clk,MSBPOST,[Status $\backslash 4]$ ' Get Status
LOOP UNTIL status = Ready ' Exit loop when status is ready
SHIFTIN DinDout, clk, MSBPOST, $[x \backslash 11, y \backslash 11]$ ' Get $x \& y$ axis values
HIGH En ' Disable module
IF (y.BIT10 = 1) THEN $y=y$ | NegMask ' Store 11-bits as signed word
IF (x.BIT10 = 1) THEN $x=x \quad \mid$ NegMask ' Repeat for other axis
RETURN

This subroutine corrects cumulative magnetic field interference that can
come from sources such as the PCB, jumper wires, a nearby battery, or a
nearby current source. This subroutine relies on values stored in
the EEPROM space that was reserved by the CompassOffsets DATA directive.
These EEPROM values were written by CalibrateHM55BCompass.bs2.
Compass_Correct_Offsets:
READ CompassOffsets, Word axisOffset ' Get x-axis offset
$\mathrm{x}=\mathrm{x}$ - axisOffset ' Correct x-axis
READ CompassOffsets + 2, Word axisOffset ' Get y-axis offset
$y=y$ - axisOffset ' Correct y-axis
RETURN

This subroutine applies linear interpolation to the refine the compass
measurement. This second level of refinement can be performed after the
Compass_Correct_Offsets subroutine, and it can correct axis skew and other
errors inherent to the HM55B chip.
The subroutine relies on sixteen actual compass measurements that were stored
in the sixteen EEPROM locations reserved by the CompassCal DATA directive.
These measurements were stored by CalibrateHM55BCompass.bs2, and they
represent the actual compass measurements for $0,22.5,45,90, \ldots, 337.5$
degrees. The subroutine finds the two EEPROM measurements that the current
angle measurement falls between. It then updates the angle measurement
based on where the angle measurement falls between the two known table values.
386 Compass_Interpolate:
' Start with the lowest value in the CompassCal table.
READ CompassLowVal, index
' Load current and previous table values.
READ CompassCal + index, table(current)
READ (CompassCal + (index - 1 \& \$F)), table(previous)
' The IF...ELSEIF...ELSE...ENDIF code block finds the two EEPROM CompassCal
' table values that the current angle measurement falls between and calculates
' the difference between the current angle measurement and the lower of the
' two table values. The IF and ELSEIF blocks deal with values that are
' greater than the highest or less than the lowest table values. The ELSE
' block everything between the highest AND lowest table values.
IF (angle >= table(previous)) THEN
span $=(255-$ table(previous)) + table(current)
angleOffset = angle - table(previous)
ELSEIF (angle <= table(current)) THEN
$\operatorname{span}=$ table(current) $+(255-$ table(previous))
angleOffset $=$ angle $+(255$ - table(previous))
ELSE
index = index - 1
READ CompassCal + index, table(current)
DO
table(previous) = table(current)
index $=$ index +1
READ CompassCal + index, table(current)
IF (angle <= table(current)) AND (angle > table(previous)) THEN
span = table(current) - table(previous)
angleOffset $=$ angle - table(previous)
EXIT
ENDIF
LOOP
ENDIF
' After the offset between the current angle measurement and the next lower
' table measurement has been determined, this code block uses it along with
' the span between the table entries above and below the angle measurement
' to solve for: angle(corrected) = angle(offset) * $16 / \mathrm{span}$.
' This code block also rounds up or down by comparing the remainder of
' the angleOffset / span division to the value of (span / 2).
angleOffset $=$ angleOffset * 16
angle $=($ angleOffset $/ \operatorname{span})+((a n g l e O f f s e t / / s p a n) /(s p a n ~ / ~ 2)) ~$
angle $=(($ index $-1 \& \$ F) * 16)+$ angle
angle = angle \& \$ff
RETURN

## VITA

Aaron Stewart graduated with his Bachelor's Degree in Mechanical Engineering from the University of Louisville in the fall of 2008 and received his Masters Degree in Mechanical Engineering in the spring of 2010, also from the University of Louisville. While at the university Aaron was very active in various intramural sports including soccer, flag football, kickball, dodge ball and volleyball and was an intramural champion in both soccer and volleyball. While at the University of Louisville, Aaron worked as a Guest Service Supervisor at the Louisville Marriott Downtown and as the Senior Wedding Videographer for Complete Video where he and his team received a Best of Weddings award for the city of Louisville. Upon graduation Aaron will begin work for SABIC Innovative Plastics as an engineer in the Operational Development Program.

