# Teacher and Teaching Effects on Students' Academic Performance, Attitudes, and Behaviors 

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Teacher and Teaching Effects on Students’ Academic Performance, Attitudes, and Behaviors:

Extensions of the Literature

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Thesis Presented to the Faculty
of the Graduate School of Education of Harvard University
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## Dedication Page

I thank my advisors, colleagues, family, and friends for all of their help and support throughout graduate school and the dissertation process.

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## Table of Contents

Abstract ..... p. iv
Introduction ..... p. 1
Paper 1 ..... p. 4
Paper 2 ..... p. 52
Paper 3 ..... p. 112
Conclusion ..... p. 160


#### Abstract

Research confirms that teachers have substantial impacts on their students' academic and life-long success. However, little is known about specific dimensions of teaching practice that explain these relationships or whether these effects differ between academic and "non-cognitive" outcomes. Drawing on data from teachers in four urban school districts, I document the relationship between individual teachers and students' math performance, as well as their self-reported self-efficacy in math, happiness in class, and behavior in class. In addition, I estimate the relationship between domains of teaching practice captured by two observation instruments and the set of student outcomes. Finally, I examine the predictive validity of teacher effect estimates on students' attitudes and behaviors amongst a subset of teachers who were randomly assigned to class rosters within schools.

I find that upper-elementary teachers have large effects on a range of students’ attitudes and behaviors in addition to their academic performance. These teacher effect estimates have moderate to strong predictive validity. Further, student outcomes are predicted by teaching practices most proximal to these measures (e.g., between teachers' math errors and students' math achievement, and between teachers' classroom organization and students' behavior in class). However, teachers who are effective at improving some outcomes often are not equally effective at improving others. Together, these findings lend important empirical evidence to well-established theory on the multidimensional nature of teaching and student learning and, thus, the need for policies that account for and incentivize this complexity.


## Introduction

Over the past decade, research has confirmed that teachers have substantial impacts on their students' academic and life-long success (e.g., Chetty, Friedman, \& Rockoff, 2014; Jackson, 2012; Nye, Konstantopoulos, \& Hedges, 2004). Recent investigations also have uncovered some characteristics of effective classroom environments, including teachers' organizational skills and interactions with students (e.g., Grosmman, Loeb, Cohen, \& Wyckoff, 2013; McCaffrey, Miller, \& Staiger, 2013). However, in order to leverage policy tools such as evaluation and professional development that seek to improve the quality of the teacher workforce, additional questions must be answered about the nature of effective teachers and teaching: Which content-specific practices improve student achievement? Are teachers who impact testscores the same as those who impact non-cognitive outcomes? What is the relationship between instructional practices and "non-cognitive" or "non-tested" outcomes? Can these "non-tested" outcomes be used to estimate valid measures of teacher effectiveness?

To answer these questions, I present three papers all drawing on data collected by the National Center for Teacher Effectiveness (NCTE) that includes a broad set of variables rarely available to researchers in one dataset. The sample includes over 300 upper elementary teachers from four school districts during the 2010-11 through 2012-13 school years. Teachers' instruction was scored on two established observation instruments - the Mathematical Quality of Instruction (MQI) and the Classroom Assessment Scoring System (CLASS) - that together capture a range of content-specific and general teaching practices. Further, administrative data and a student survey developed and administered by the project team allow me to capture both self-report and
behavioral measures of student outcomes beyond test scores - which I refer to as "nontested" outcomes - including their behavior in class, self-efficacy in math, happiness in class, and days absent, all of which are linked to long-term life outcomes (Bell, Rosen, \& Dynlacht, 1994; Chetty et al., 2011; Duckworth et al., 2007; Hawkins et al., 1998; John \& Srivastava, 1999; Loeber \& Farrington, 2000; Robins \& Ratcliff, 1980; Schaeffer, Petras, Ialongo, Poduska, \& Kellam, 2003; Tsukayama, Duckworth, \& Kim, 2013). Other student outcomes include student achievement on both high-stakes standardized tests and a project-administered mathematics assessment. Finally, the data include a range of teacher background characteristics that have been shown to contribute both to instructional quality and student outcomes in this and other datasets, thereby allowing me to isolate instructional practices from omitted variables that might bias results. In the third year of the study, the NCTE project engaged in a random assignment study in which teachers were randomly assigned to class rosters within schools. This design allows me to validate teacher effects against potential threats to internal validity.

In the first paper of this dissertation, I estimate the relationship between instructional quality measures captured on the MQI and CLASS instruments and students' academic achievement on the low-stakes math test. In the second paper, I extend this work to the set of non-cognitive outcomes. Further, I examine whether teachers who have large impacts on test-score outcomes are the same teachers who impact non-tested ones. In the third paper of the dissertation, I test the validity of teacher effects on non-tested outcomes by examining whether non-experimental estimates predict student outcomes following random assignment.

Together, these papers can inform ongoing teacher improvement efforts, particularly around evaluation and professional development.

## Paper 1

## Effective Teaching in Elementary Mathematics: Identifying Classroom Practices that Support Student Achievement ${ }^{1}$


#### Abstract

Recent investigations into the education production function have moved beyond traditional teacher inputs, such as education, certification, and salary, focusing instead on observational measures of teaching practice. However, challenges to identification mean that this work has yet to coalesce around specific instructional dimensions that increase student achievement. I build on this discussion by exploiting within-school, betweengrade, and cross-cohort variation in scores from two observation instruments; further, I condition on a uniquely rich set of teacher characteristics, practices, and skills. Findings indicate that inquiry-oriented instruction positively predicts student achievement. Content errors and imprecisions are negatively related, though these estimates are sensitive to the set of covariates included in the model. Two other dimensions of instruction, classroom emotional support and classroom organization, are not related to this outcome. Findings can inform recruitment and development efforts aimed at improving the quality of the teacher workforce.


[^0]
## 1. Introduction

Over the past decade, research has confirmed that teachers have substantial impacts on their students' academic and life-long success (e.g., Nye, Konstantopoulos, \& Hedges, 2004; Chetty, Friedman, \& Rockoff, 2014). Despite concerted efforts to identify characteristics such as experience, education, and certification that might be correlated with effectiveness (for a review, see Wayne \& Youngs, 2003), however, the nature of effective teaching still largely remains a black box. Given that the effect of teachers on achievement must occur at least in part through instruction, it is critical that researchers identify the types of classroom practices that matter most to student outcomes. This is especially true as schools and districts work to meet the more rigorous goals for student achievement set by the Common Core State Standards (Porter, McMaken, Hwang, \& Yang, 2011), particularly in mathematics (Duncan, 2010; Johnson, 2012; U.S. Department of Education, 2010).

Our limited progress toward understanding the impact of teaching practice on student outcomes stems from two main research challenges. The first barrier is developing appropriate tools to measure the quality of teachers' instruction. Much of the work in this area tends to examine instruction either in laboratory settings or in classrooms over short periods of time (e.g., Anderson, Everston, \& Brophy, 1979; Star \& Rittle-Johnson, 2009), neither of which is likely to capture the most important kinds of variation in teachers' practices that occur over the course of a school year. The second is a persistent issue in economics of education research of designing studies that support causal inferences (Murnane \& Willett, 2011). Non-random sorting of students to teachers (Clotfelter, Ladd, \& Vigdor, 2006; Rothstein, 2010) and omitted measures of teachers’
skills and practices limit the success of prior research.
I address these challenges through use of a unique dataset on fourth- and fifthgrade teachers and their students from three anonymous school districts on the East Coast of the United States. Over the course of two school years, the project captured observed measures of teachers' classroom practices on the Mathematical Quality of Instruction (MQI) and Classroom Assessment Scoring System (CLASS) instruments, focusing on mathematics-specific and general teaching practices, respectively. The project also collected data on a range of other teacher characteristics, as well as student outcomes on a low-stakes achievement test that was common across participants.

My identification strategy has two key features that distinguish it from prior work on this topic. First, to account for sorting of students to schools and teachers, I exploit variation in observation scores within schools, across adjacent grades and years. Specifically, I specify models that include school fixed effects and instructional quality scores averaged to the school-grade-year level. This approach assumes that student and teacher assignments are random within schools and across grades or years, which I explore in detail below. Second, to isolate the independent contribution of instructional practices to student achievement, I condition on a uniquely rich set of teacher characteristics, skills, and practices. I expect that there likely are additional factors that are difficult to observe and, thus, are excluded from my data. Therefore, to explore the possible degree of bias in my estimates, I test the sensitivity of results to models that include different sets of covariates. Further, I interpret findings in light of limitations associated with this approach.

Results point to a positive relationship between ambitious or inquiry-oriented mathematics instruction and performance on a low-stakes test of students' math knowledge of roughly 0.10 standard deviations. I also find suggestive evidence for a negative relationship between mathematical errors and student achievement, though estimates are sensitive to the specific set of teacher characteristics included in the model. I find no relationships between two other dimensions of teaching practice - classroom emotional support and classroom organization - and student achievement. Teachers included in this study have value-added scores calculated from state assessment data similar to those of other fourth- and fifth-grade teachers in their respective districts, leading me to conclude that findings likely generalize to these populations beyond my identification sample. I argue that results can inform recruitment and development efforts aimed at improving the quality of the teacher workforce

The remainder of this paper is organized as follows. In the second section, I discuss previous research on the relationship between observational measures of teacher quality and student achievement. In the third section, I describe the research design, including the sample and data. In the fourth section, I present my identification strategy and tests of assumptions. In the fifth section, I provide main results and threats to internal and external validity. I conclude by discussing the implications of my findings for ongoing research and policy on teacher and teaching quality.

## 2. Background and Context

Although improving the quality of the teacher workforce is seen as an economic imperative (Hanushek, 2009), long-standing traditions that reward education and training or offer financial incentives based on student achievement have been met with limited
success (Boyd, Grossman, Lankford, Loeb, \& Wyckoff, 2006; Fryer, 2013; Harris \& Sass, 2011; Springer et al., 2010). One reason for this posed by Murnane and Cohen (1986) almost three decades ago is the "nature of teachers' work" (p. 3). They argued that the "imprecise nature of the activity" makes it difficult to describe why some teachers are good and what other teachers can do to improve (p. 7).

Recent investigations have sought to test this theory by comparing subjective and objective (i.e., "value-added") measures of teacher performance. In one such study, Jacob and Lefgren (2008) found that principals were able to distinguish between teachers in the tails of the achievement distribution but not in the middle. Correlations between principal ratings of teacher effectiveness and value added were weak to moderate: 0.25 and 0.18 in math and reading, respectively ( 0.32 and 0.29 when adjusted for measurement error). Further, while subjective ratings were a statistically significantly predictor of future student achievement, they performed worse than objective measures. Including both in the same regression model, estimates for principal ratings were 0.08 standard deviations (sd) in math and 0.05 sd in reading; comparatively, estimates for value-added scores were 0.18 sd in math and 0.10 sd in reading. This evidence led the authors to conclude that "good teaching is, at least to some extent, observable by those close to the education process even though it may not be easily captured in those variables commonly available to the econometrician" (p. 103).

Two other studies found similar results. Using data from New York City, Rockoff, Staiger, Kane, and Taylor (2012) estimated correlations of roughly 0.21 between principal evaluations of teacher effectiveness and value-added scores averaged across math and reading. These relationships corresponded to effect sizes of 0.07 sd in math and
0.08 sd in reading when predicting future student achievement. Extending this work to mentor evaluations of teacher effectiveness, Rockoff and Speroni (2010) found smaller relationships to future student achievement in math between 0.02 sd and 0.05 sd . Together, these studies suggest that principals and other outside observers understand some but not all of the production function that converts classroom teaching and professional expertise into student outcomes.

In more recent years, there has been a growing interest amongst educators and economists alike in exploring teaching practice more directly. This now is possible through the use of observation instruments that quantitatively capture the nature and quality of teachers' instruction. In one of the first econometric analyses of this kind, Kane, Taylor, Tyler, and Wooten (2011) examined teaching quality scores captured on the Framework for Teaching instrument as a predictor of math and reading test scores. Data came from Cincinnati and widespread use of this instrument in a peer evaluation system. Relationships to student achievement of 0.11 sd in math and 0.14 sd in reading provided suggestive evidence of the importance of general classroom practices captured on this instrument (e.g., classroom climate, organization, routines) in explaining teacher productivity.

At the same time, this work highlighted a central challenge associated with looking at relationships between scores from observation instruments and student test scores. Non-random sorting of students to teachers and non-random variation in classroom practices across teachers means that there likely are unobserved characteristics related both to instructional quality and student achievement. As one way to address this concern, the authors' preferred model included school fixed effects to account for factors
at the school level, apart from instructional quality, that could lead to differences in achievement gains. In addition, they relied on out-of-year observation scores that, by design, could not be correlated with the error term predicting current student achievement. This approach is similar to those taken by Jacob and Lefgren (2008), Rockoff, Staiger, Kane, and Taylor (2012), and Rockoff and Speroni (2010), who use principal/mentor ratings of teacher effectiveness to predict future student achievement. Finally, as a robustness test, the authors fit models with teacher fixed effects to account for timeinvariant teacher characteristics that might be related to observation scores and student outcomes; however, they noted that these estimates were much noisier because of small samples of teachers.

The largest and most ambitious study to date to conduct these sorts of analyses is the Measures of Effective Teaching (MET) project, which collected data from teachers across six urban school districts on multiple observation instruments. By randomly assigning teachers to class rosters within schools and using out-of-year observation scores, Kane, McCaffrey, Miller, and Staiger (2013) were able to limit some of the sources of bias described above. In math, relationships between scores from the Framework for Teaching and prior student achievement fell between 0.09 sd and 0.11 sd. In the non-random assignment portion of the study, Kane and Staiger (2012) found correlations between scores from other observation instruments and prior-year achievement gains in math from 0.09 (for the Mathematical Quality of Instruction) to 0.27 (for the UTeach Teacher Observation Protocol). The authors did not report these as effect size estimates. As a point of comparison, the correlation for the Framework for Teaching and prior-year gains was 0.13 .

Notably, these relationships between observation scores and student achievement from both the Cincinnati and MET studies are equal to or larger in magnitude than those that focus on principal or mentor ratings of teacher quality. This is somewhat surprising given that principal ratings of teacher effectiveness - often worded specifically as teachers' ability to raise student achievement - and actual student achievement are meant to measure the same underlying construct. Comparatively, dimensions of teaching quality included on these instruments are thought to be important contributors to student outcomes but are not meant to capture every aspect of the classroom environment that influence learning (Pianta \& Hamre, 2009). Therefore, using findings from Jacob and Lefgren (2008), Rockoff, Staiger, Kane, and Taylor (2012), and Rockoff and Speroni (2010) as a benchmark, estimates describing the relationship between observed classroom practices and student achievement are, at a minimum, substantively meaningful; at a maximum, they may be viewed as large. Following Murnane and Cohen's intuition, then, continued exploration into the "nature of teachers' work" (1986, p. 3), the practices that comprise high-quality teaching, and their role in the education production function will be a central component of efforts aimed at raising teacher quality and student achievement.

At the same time that work by Kane and his co-authors $(2011,2012,2013)$ has greatly expanded conversation in the economics of education literature to include teaching quality when considering teacher quality, this work has yet to coalesce around specific instructional dimensions that increase student outcomes. Random assignment of teachers to students - and other econometric methods such as use of school fixed effects, teacher fixed effects, and out-of-year observation ratings - likely provide internally valid
estimates of the effect of having a teacher who provides high-quality instruction on student outcomes. This approach is useful when validating different measures of teacher quality, as was the stated goal of many of the studies described above including MET. However, these approaches are insufficient to produce internally valid estimates of the effect of high-quality instruction itself on student outcomes. This is because teachers whose measured instructional practices are high quality might have a true, positive effect on student achievement even though other practices and skills - e.g., spending more time with students, knowledge of students - are responsible for the higher achievement. Kane et al. (2011) fit models with teacher fixed effects in order to "control for all timeinvariant teacher characteristics that might be correlated with both student achievement growth and observed classroom practices" (p. 549). However, it is likely that there are other time-variant skills related both to instructional quality and student achievement.

I address this challenge to identification in two ways. First, my analyses explore an additional approach to account for the non-random sorting of students to teachers. Second, I attempt to isolate the unique contribution of specific teaching dimensions to student outcomes by conditioning on a broad set of teacher characteristics, practices, and skills. Specifically, I include observation scores captured on two instruments (both content-specific and general dimensions of instruction), background characteristics (education, certification, and teaching experience), knowledge (mathematical content knowledge and knowledge of student performance), and non-instructional classroom behaviors (preparation for class and formative assessment) that are thought to relate both to instructional quality and student achievement. Comparatively, in their preferred model, Kane et al. (2011) included scores from one observation instrument, controlling for
teaching experience. While I am not able to capture every possible characteristic, I argue that these analyses are an important advance beyond what currently exists in the field.

## 3. Sample and Data

### 3.1 Sample

Data come from the National Center for Teacher Effectiveness (NCTE), which focused on collection of instructional quality scores and other teacher characteristics in three anonymous districts (henceforth Districts 1 through 3). ${ }^{2}$ Districts 1 and 2 are located in the same state. Data was collected from participating fourth- and fifth-grade math teachers in the 2010-2011 and 2011-2012 school years. Due to the nature of the study and the requirement for teachers to be videotaped over the course of a school year, participants consist of a non-random sample of schools and teachers who agreed to participate. During recruitment, study information was presented to schools based on district referrals and size; the study required a minimum of two teachers at each of the sampled grades. Of eligible teachers, 143 (roughly 55\%) agreed to participate. My identification strategy focuses on school-grade-years in which I have the full sample of teachers who work in non-specialized classrooms (i.e., not self-contained special education or limited English proficient classes) in that school-grade-year. I further restrict the sample to schools that have at least two complete grade-year cells. This includes 111 teachers in 26 schools and 76 school-grade-years; 45 of these teachers, 17 of these schools, and 27 of these school-grade-years are in the sample for both school years.

[^1]In Table 1, I present descriptive statistics on the students and teachers in this sample. Students in District 1 are predominantly African American or Hispanic, with over $80 \%$ eligible for free- or reduced-price lunch (FRPL), $15 \%$ designated as in need of special education (SPED) services, and roughly 24\% designated as limited English proficient (LEP). In District 2, there is a greater percentage of white students (29\%) and fewer FRPL (71\%), SPED (10\%), and LEP students (18\%). In District 3, there is a greater percentage of African-American students (67\%) and fewer FRPL (58\%), SPED (8\%), and LEP students (7\%). Across all districts, teachers have roughly nine years of experience. Teachers in Districts 1 and 2 were certified predominantly through traditional programs ( $74 \%$ and $93 \%$, respectively), while more teachers in District 3 entered the profession through alternative programs or were not certified at all (55\%). Relative to all study participants, teachers in Districts 1 through 3 have above average, average, and below average mathematical content knowledge, respectively.

### 3.2 Main Predictor and Outcome Measures

### 3.2.1 Video-Recorded Lesson of Instruction

Mathematics lessons were captured over a two-year period, with a maximum of three lessons per teacher per year. Capture occurred with a three-camera, unmanned unit and lasted between 45 and 80 minutes. Teachers were allowed to choose the dates for capture in advance, and were directed to select typical lessons and exclude days on which students were taking a test. Although it is possible that these lessons are unique from teachers' general instruction, teachers did not have any incentive to select lessons strategically as no rewards or sanctions were involved with data collection. In addition, analyses from the MET project indicate that teachers are ranked almost identically when
they choose lessons themselves compared to when lessons are chosen for them (Ho \& Kane, 2013).

Trained raters scored these lessons on two established observational instruments: the Mathematical Quality of Instruction (MQI), focused on mathematics-specific practices, and the Classroom Assessment Scoring System (CLASS), focused on general teaching practices. For the MQI, two certified and trained raters watched each lesson and scored teachers' instruction on 17 items for each seven-and-a-half minute segment on a scale from Low (1) to High (3) (see Table 2 for a full list of items). Lessons have different numbers of segments, depending on their length. Analyses of these data (Blazar, Braslow, Charalambous, \& Hill, 2015) show that items cluster into two main factors: Ambitious Mathematics Instruction, which corresponds to many elements contained within the mathematics reforms of the 1990s (National Council of Teachers of Mathematics, 1989, 1991, 2000) and the Common Core State Standards for Mathematics (National Governors Association for Best Practices, 2010); and Mathematical Errors and Imprecisions, which captures any mathematical errors the teacher introduces into the lesson. For Ambitious Mathematics Instruction, higher scores indicate better performance. For Mathematical Errors and Imprecisions, higher scores indicate that teachers make more errors in their instruction and, therefore, worse performance. I estimate reliability for these metrics by calculating the amount of variance in teacher scores that is attributable to the teacher (i.e., the intraclass correlation), adjusted for the modal number of lessons. These estimates are 0.69 and 0.52 for Ambitious Mathematics Instruction and Mathematical Errors and Imprecisions, respectively. Though this latter estimate is lower than conventionally acceptable levels (0.7), it is consistent with those
generated from similar studies (Bell, Gitomer, McCaffrey, Hamre, \& Pianta, 2012; Kane \& Staiger, 2012). ${ }^{3}$

The CLASS instrument captures more general classroom quality. By design, the instrument is split into three dimensions. Based on factor analyses described above, I utilize two: Classroom Emotional Support, which focuses on the classroom climate and teachers' interactions with students; and Classroom Organization, including behavior management and productivity of the lesson. Following the protocol provided by instrument developers, one certified and trained rater watched and scored each lesson on 11 items for each fifteen-minute segment on a scale from Low (1) to High (7). I reverse code one item from the Classroom Organization dimension, "Negative Climate," to align with the valence of the other items. Therefore, in all cases, higher scores indicate better performance. Using the same method as above, I estimate reliabilities of 0.55 for Classroom Emotional Support and 0.65 for Classroom Organization.

In Table 2, I present summary statistics of teacher-level scores that are averaged across raters (for the MQI), segments, and lessons. For the MQI, mean scores are slightly lower than the middle of the scale itself: 1.26 for Ambitious Mathematics Instruction (out of $3 ; \mathrm{sd}=0.12$ ) and 1.12 for Mathematical Errors and Imprecisions (out of 3; $\mathrm{sd}=0.12$ ). For the CLASS, mean scores are centered above the middle of the scale: 4.26 for

[^2]Classroom Emotional Support (out of 7; sd $=0.55$ ) and 6.52 for Classroom Organization (out of 7; sd $=0.44$ ). Pairwise correlations between these teacher-level scores range from roughly zero (between Mathematical Errors and Imprecisions and the two dimensions on the CLASS instrument) to 0.44 between Classroom Emotional Support and Classroom Organization. Ambitious Mathematics Instruction is more consistently related to the other instructional quality dimensions, with correlations between 0.19 and 0.34 . These correlations are high enough to suggest that high-quality teachers who engage in one type of instructional practice may also engage in others, but not too high to indicate that dimensions measure the same construct.

As I discuss below, my identification strategy relies on instructional quality scores at the school-grade-year level. While this strategy loses between-teacher variation, which likely is the majority of the variation in instructional quality scores, I still find substantive variation in instructional quality scores within schools, across grades and years. In Table 3, I decompose the variation in school-grade-year scores into two components: the school-level component, which describes the percent of variation that lies across schools, and the residual component, which describes the rest of the variation that lies within schools. For all four instructional quality dimensions, I find that at least $40 \%$ of the variation in school-grade-year scores lies within schools. This leads me to conclude that there is substantive variation within schools at the school-grade-year level to exploit in this analysis.

In order to minimize noise in these observational measures, I use all available lessons for each teacher (Hill, Charalambous, \& Kraft, 2012). Teachers who participated in the study for one year had three lessons, on average, while those who participated in
the study for two years generally had six lessons. A second benefit of this approach is that it reduces the possibility for bias due to unobserved classroom characteristics that affect both instructional quality and student outcomes (Kane, Taylor, Tyler, \& Wooten, 2011). ${ }^{4}$ This is because, in roughly half of cases, scores represent elements of teachers' instruction from the prior year or future year, in addition to the current year. Specifically, I utilize empirical Bayes estimation to shrink scores back toward the mean based on their precision (see Raudenbush \& Bryk, 2002). To do so, I specify the following hierarchical linear model using all available data, including teachers beyond my identification sample:
(1) OBSERVATION ${ }_{l j}=\mu_{j}+\varepsilon_{l j}$
where the outcome is the observation score for lesson $l$ and teacher $j, \mu_{j}$ is a random effect for each teacher $j$, and $\varepsilon_{l j}$ is the error term. I utilize standardized estimates of the teacher-level random effect as each teacher's observation score. Most distributions of these variables are roughly normal. For identification, I average these scores within each school-grade-year. I do not re-standardize these school-grade-year scores in order to interpret estimates in teacher-level standard deviation units, which are more meaningful than school-grade-year units.

### 3.2.2 Student Demographic and Test-Score Data

[^3]One source of student-level data is district administrative records. Demographic data include gender, race/ethnicity, special education (SPED) status, limited English proficiency (LEP) status, and free- or reduced-price lunch (FRPL) eligibility. I also utilize prior-year test scores on state assessments in both math and reading, which are standardized within district by grade, subject, and year using the entire sample of students in each district, grade, subject, and year.

Student outcomes were measured in both fall and spring on a new assessment developed by researchers who created the MQI in conjunction with the Educational Testing Service (see Hickman, Fu, \& Hill, 2012). Validity evidence indicates internal consistency reliability of 0.82 or higher for each form across the relevant grade levels and school years. Three key features of this test make it ideal for this study. First, the test is common across all districts and students in the sample, which is important given evidence on the sensitivity of statistical models of teacher effectiveness to different achievement tests (Lockwood, McCaffrey, Hamilton, Stecher, Le, \& Martinez, 2007; Papay, 2011). Second, the test is vertically aligned, allowing me to compare achievement scores for students in fourth versus fifth grade. Third, the assessment is a relatively cognitively demanding test, thereby well aligned to many of the teacher-level practices assessed in this study, particularly those captured on the MQI instrument. It likely also is similar to new mathematics assessments administered under the Common Core (National Governors Association for Best Practices, 2010). Lynch, Chin, and Blazar (2015) coded items from this assessment for format and cognitive demand using the Surveys of Enacted Curriculum framework (Porter, 2002). They found that the assessment often asked
students to solve non-routine problems, including looking for patterns and explaining their reasoning. Roughly $20 \%$ of items required short responses.

### 3.2.3 Teacher Survey

Information on teachers' background, knowledge, and skills were captured on a teacher questionnaire administered in the fall of each year. Survey items about teachers' background include whether or not the teacher earned a bachelor's degree in education, amount of undergraduate or graduate coursework in math and math courses for teaching (2 items scored from 1 [No Classes] to 4 [Six or More Classes], internal consistency reliability $(\alpha)=0.66)$, route to certification, and whether or not the teacher had a master's degree (in any subject). Relatedly, the survey also asked about the number of years of teaching experience in math.

Next, I capture teachers' knowledge of content and of their students. Teachers' content knowledge was assessed on items from both the Mathematical Knowledge for Teaching assessment (Hill, Schilling, \& Ball, 2004) and the Massachusetts Test for Educator Licensure. Teacher scores were generated by IRTPro software and were standardized in these models using all available teachers, with a reliability of 0.92 . Second are scores from a test of teachers' knowledge of student performance. These scores were generated by providing teachers with student test items, asking them to predict the percent of students who would answer each item correctly, then calculating the distance between each teacher's estimate and the actual percent of students in their class who got each item correct. Similar to instructional quality scores, I report reliability as adjusted intraclass correlations, which are 0.71 and 0.74 for grades four and five, respectively. To arrive at a final scale, I averaged across items and standardized.

Finally, two items refer to additional classroom behaviors that aim to increase student achievement. The first is teachers' preparation for class, which asks about the amount of time each week that teachers devoted to out-of-class activities such as grading, preparing lesson materials, reviewing the content of the lesson, and talking with parents (4 items scored from 1 [No Time] to 5 [More than Six Hours], $\alpha=0.84$ ). The second construct is formative assessment, which asks how often teachers evaluated student work and provided feedback (5 items scored from 1 [Never] to 5 [Daily or Almost Daily], $\alpha=$ $0.74) .{ }^{5}$

In Table 4, I present correlations between these characteristics and the four instructional quality dimensions. The strongest correlation is between Mathematical Errors and Imprecisions and mathematical content knowledge ( $r=-0.46$ ). This suggests that teachers' knowledge of the content area is moderately to strongly related to their ability to present correct material in class. The sign of this relationship is correct, in that higher scores on Mathematical Errors and Imprecisions means that more errors are made in instruction, while higher scores on the content knowledge test indicate stronger understanding of math. Content knowledge also is related to Ambitious Mathematics Instruction ( $r=0.26$ ). Interestingly, math coursework is related to Classroom Organization, and Mathematical Errors and Imprecisions is related to formative assessment $(r=0.24)$, even though these constructs are not theoretically related. Together, this suggests that the dimensions of instructional quality generally are distinct from other measures often used as a proxy for teacher or teaching quality.

## 4. Identification Strategy and Tests of Assumptions

[^4]In order to estimate the relationship between high-quality instruction and students' mathematics achievement, my identification strategy must address two main challenges: non-random sorting of students to teachers and omitted measures of teachers' skills and practices. I focus on each in turn.

### 4.1 Non-Random Sorting of Students to Teachers

Non-random sorting of students to teachers consists of two possible components: the sorting of students to schools and of students to classes or teachers within schools. In Table 5, I explore the extent to which these types of sorting might bias results by regressing baseline test scores on all four dimensions of instructional quality (see Kane et al., 2011). Comparing teachers within districts, Ambitious Mathematics Instruction is positively related to baseline achievement. This suggests, unsurprisingly, that teachers with higher-quality math instruction tend to be assigned to higher-achieving students. Interestingly, though, only part of this relationship is explained by differences in instructional quality and student achievement across schools. Comparing teachers within schools, the magnitude of the relationship between Ambitious Mathematics Instruction and baseline achievement is substantively smaller but still statistically significant. Further, I now observe a positive relationship between Classroom Organization and baseline test scores. This indicates that within-school sorting and the matching of students to teachers may occur differently than across-school sorting but that it likely serves as an additional source of bias.

In light of non-random sorting, I begin by specifying models that control for a host of observable student and class characteristics, including prior achievement. Further, following Kane, Taylor, Tyler, and Wooten (2011), I include school fixed effects to
account for unobserved differences across schools, other than instructional quality, that also affect student achievement. Finally, to address sorting of students to classes or teachers within schools, I exploit an important logistical and structural constraint of schools - that students may be sorted within but not across grades and years. This is because, in most cases, students advance with a given cohort from one grade to the next. Therefore, similar to Rivkin, Hanushek, and Kain (2005), I exploit between-cohort differences by aggregating teachers' observation scores to the school-grade-year level. They argue that "aggregation to the grade level circumvents any problems resulting from classroom assignment" (p. 426). Doing so restricts identifying variation to that observed across grades - e.g., between fourth-grade teachers in one year and fifth-grade teachers in the same, following, or former school year. In a few instances where grade-level composition changes from one year to the next, there also is identifying variation between the set of fourth-grade teachers in one year and the set of fourth-grade teachers in the following or former school year, and similarly for fifth-grade teachers in one year and fifth-grade teachers in another year

The hypothesized model that describes this relationship is outlined in equation 2 :

$$
\begin{equation*}
A_{i d s g c j t}=\beta \overline{O B S E R V A T I O N}_{d s g t}+\zeta\left(f\left(A_{i d s g c j t-1}\right)\right)+\pi X_{i d s g c j t}+\varphi \bar{X}_{d s g c j t}+ \tag{2}
\end{equation*}
$$ $\sigma_{d g t}+\theta_{s}+\varepsilon_{i d s g c j t}$

where $A_{i d s g c j t}$ is the end-of-year test score for student $i$ in district $d$, school $s$, grade $g$, and class $c$ with teacher $j$ at time $t ; \overline{\text { OBSERVATION }}_{\text {dsgt }}$ is a vector of instructional quality scores that are averaged across teachers within each school-grade-year; $f\left(A_{\text {idsgcjt-1 }}\right)$ is a cubic function of prior achievement on the fall baseline assessment, as well as on the prior-year state assessments in both math and reading; $X_{i}$ is a vector of
observable student-level characteristics; $\bar{X}_{d s g c j t}$ aggregates these and prior achievement measures to the class level. I include district-by-grade-by-year fixed effects, $\sigma_{d g t}$, to account for differences in the scaling of state standardized test scores. As discussed above, I also include fixed effects for schools, $\theta_{s}$, as part of my identification strategy. I calculate standard errors that are clustered at the school-grade-year level to account for heteroskedasticity in the student-level errors, $\varepsilon_{i d s g c j t}$, and non-zero covariance among those students attending the same school in the same grade and year (Kane, Rockoff, \& Staiger, 2008).

The key identifying assumption of this model is that within-school, betweengrade, and cross-cohort differences in average instructional quality scores are exogenous (see Woessmann \& West, 2006 for a discussion of this assumption and strategy as it pertains to class size). While the validity of this assumption is difficult to test directly, I can examine ways that it may play out in practice. In particular, this assumption would be violated by strategic grade assignments in which teachers are shifted across grades due to a particularly strong or weak incoming class, or where students are held back or advanced an additional grade in order to be matched to a specific teacher.

Although these practices are possible in theory, I present evidence that such behavior does not threaten inferences about variation in instructional quality scores. I do observe that 30 teachers were newly assigned to their grade, either because they switched from a different grade in the prior year (before joining the study) or because they moved into the district. In Table 6, I examine differences between switchers and non-switchers on observable characteristics within school-year cells. In addition to comparing teachers on the characteristics listed in Tables 1 and 2, I include average scores on all three
baseline achievement tests; I also include state value-added scores in math. ${ }^{6}$ Here, I find that switchers have students with lower prior-year achievement on state math and reading exams ( $p=0.037$ and 0.002 , respectively). Importantly, though, there are no differences between switchers and non-switchers on any of the observational rubric dimensions, any of the teacher survey constructs, or state value-added scores. Nor can I detect differences between these two groups when all observable traits are tested jointly ( $F=1.159, p=$ $0.315) .{ }^{7}$ This suggests that, even though switchers tend to have lower-achieving students, they are unlikely to be matched to these classes based on observed quality. With regard to sorting of students to grade, fewer than 20 were retained from the previous year or skipped a grade. I drop these from the analytic sample.

A second assumption underlying the logic of this strategy is that identification holds only when all teachers at a given school-grade-year are in the study. If only a portion of the teachers participate, then there may be bias due to the selection of students assigned to these teachers. To address this concern, I limit my final analytic sample to school-grade-years in which I have full participation of teachers. I am able to identify these teachers as I have access to class rosters for all teachers who work in the sample districts. I exclude from these school-grade-year teams teachers who teach self-contained

[^5]special education or bilingual classes, as the general population of students would not be sorted to these teachers' classes. ${ }^{8}$

By dropping certain school-grade-year observations, I limit the sample from which I am able to generalize results. In this sense, I compromise external validity for internal validity. However, below I discuss the comparability of teachers and school-grade-years included in my identification sample to those that I exclude either because they did not participate in data collection through the NCTE project or because they did not meet the sample conditions I describe above.

### 4.2 Omitted Variables Bias

Given non-random sorting of instructional quality to teachers, estimating the effect of these practices on mathematics achievement also requires isolating them from other characteristics that are related both to observation rubric scores and to student test scores. I focus on characteristics that prior research suggests may fit the definition of omitted variables bias in this type of analysis.

Review of prior research indicates that several observable characteristics are related both to student achievement and instructional quality. Studies indicate that students experience larger test score gains in math from teachers with prior education and coursework in this content area (Boyd, Grossman, Lankford, Loeb, \& Wyckoff, 2009; Wayne \& Youngs, 2003), some forms of alternative certification such as Teach for America relative to traditional certification (Clark et al, 2013; Decker, Mayer, \& Glazerman, 2004), more experience in the classroom (Chetty et al., 2011; Papay \& Kraft, forthcoming; Rockoff, 2004), and stronger content knowledge (Metzler \& Woessmann, 2012). Emerging work also highlights the possible role of additional professional

[^6]competencies, such as knowledge of student performance, in raising student achievement (Kunter, Klusmann, Baumert, Richter, Voss, \& Hachfeld, 2013; Sadler, Sonnert, Coyle, Cook-Smith, \& Miller, 2013). These factors also appear to predict some dimensions of instructional quality in this or other datasets (see Table 3 and Hill, Blazar, \& Lynch, 2015 for further discussion).

Because it is possible that I am missing other important characteristics - namely unobservable ones - I test the sensitivity of results to models that include different sets of teacher-level covariates. I also interpret results cautiously. Despite this limitation, I believe that my ability to isolate instructional practices from a range of other teacher traits and skills is an advance beyond similar studies.

## 5. Results

### 5.1 Main Results

In Table 7a, I present models examining the relationship between instructional quality and student achievement. This first set of models examines the robustness of estimates to specifications that attempt to account for the non-random sorting of students to schools and teachers. I begin with a basic model (Model A) that regresses students' spring test score on teacher-level observation scores. I include a cubic function of fall/prior achievement on the project-administered test and state standardized tests in math and reading; utilizing all three tests of prior achievement allows me to compare students with similar scores on low- and high-stakes tests across both subjects, increasing the precision of my estimates. I also include district-by-grade-by-year dummy variables to account for differences in scaling of tests; and vectors of student-, class-, and schoollevel covariates. Next, I replace school-level covariates with school fixed effects (Model
B). In Model C, I retain the school fixed effects and replace observation scores at the teacher level with those at the school-grade-year level. This model matches equation (2) above. Finally, in order to ensure that school-specific year effects do not drive results, I replace school fixed effects with school-by-year fixed effects in Models D. For all models, I limit the sample to those school-grade-years where all teachers from participating school-grades-years are in the study. Robust standard errors clustered at the school-gradeyear level are reported in parentheses. ${ }^{9}$

In Model C, intended to account for non-random sorting of students to schools and teachers, I find that instructional quality dimensions focused on the mathematics presented in the classroom are related to students' math achievement. Specifically, I find a statistically significant and positive coefficient for Ambitious Mathematics Instruction of 0.10 sd ; the coefficient for Mathematical Errors and Imprecisions of -0.05 sd is marginally significant.

Interestingly, these estimates are larger in magnitude than those from Models A and B. Comparison of estimates to Model A implies that schools and/or classrooms where instruction is higher quality tend to have below-average test-score growth. The fact that estimates in Model C are larger than those in Model B is surprising. By limiting variation to school-grade-years, I expected to calculate lower-bound estimates of the relationship between instructional quality and student achievement (see Rivkin, Hanushek, \& Kain, 2005). One possible explanation for my findings may be that school-grade-year scores are picking up the quality of teaching teams, which also is related to student achievement. At the same time, these differences are not large. Further, standard

[^7]errors are larger in Model C than in Model B, as I would expect given more limited variation in my main predictor variables. Finally, I find that estimates in Model D, which replace school fixed effects with school-by-year fixed effects, are similar in magnitude to those in Model C. This indicates that year effects do not drive results. As before, standard errors are larger than those in Model C given more limited identifying variation. I find no statistically significant relationships for the two other dimensions of instruction.

In Table 7b, I re-estimate results from Model C controlling for different sets of teacher characteristics. I focus on four categories of covariates: education and certification (Model E), teaching experience (Model F), knowledge (Model G), and noninstructional classroom behaviors (Model H). In Model I, I include all four sets of predictors. Similar to instructional quality dimensions, these covariates are averaged to the school-grade-year level. Here, I find that estimates for Ambitious Mathematics Instruction are fairly robust to inclusion of these control variables. In Model G, which controls for two measures of teacher knowledge, I find a marginally significant estimate of 0.08 sd. This slight attenuation makes sense given the positive relationship between mathematical content knowledge and Ambitious Mathematics Instruction noted earlier. Interestingly, coefficients from models that include other sets of covariates are slightly larger than my estimate of 0.10 sd from Model C; in Model I, which controls for all teacher characteristics, the resulting estimate is roughly 0.11 sd . One reason for this may be that be these additional predictors are negatively related either to instructional quality or to student achievement. Earlier, I showed a negative, though not statistically significant, correlation between Ambitious Mathematics Instruction and bachelor's degree in education; here, I observe small but negative relationships to student
achievement for bachelor's degree in education, math coursework, traditional certification, and preparation for class. I am cautious in placing too much emphasis on these differences, as they are not large. However, these patterns suggest that some omitted variables may lead to upward bias while others lead to downward bias.

The relationship between Mathematical Errors and Imprecisions and student achievement is more sensitive to inclusion of control variables. Original estimates from Model C are attenuated most significantly when controlling for teachers' mathematical content knowledge; the resulting estimate of roughly -0.04 sd in Model G is no longer marginally statistically significant. This attenuation is unsurprising given a moderate to strong relationship between Mathematical Errors and Imprecisions and mathematical content knowledge noted earlier ( $r=-0.46$ ). Therefore, it is difficult to tell whether student achievement is negatively impacted by teachers' lack of content knowledge, the way that this lack of knowledge leads to errors and imprecisions in the presentation of material, or a related construct. When I include all sets of predictors in the same model (Model I), the estimate for Mathematical Errors and Imprecisions is -0.03 sd and not statistically significant.

### 5.2 Generalizability of Results Beyond Identification Sample

Finally, in Table 8, I examine whether teachers and schools included in my identification sample are representative of those in their respective districts. Because I do not have instructional quality scores for all district teachers, for this analysis I draw on mathematics value-added scores using state assessment data. I also compare observable characteristics of school-grade-years from my identification sample to those across the rest of the sample districts, looking for differences on each characteristic individually and
as a group. $P$-values testing the difference between sample means are calculated through a regression framework that controls for district, as recruitment of schools and teachers occurred at this level. In both cases of teachers and school-grade-years, I cannot reject the null hypothesis that my identification sample is the same as the rest of the district populations (for differences in teachers' value-added scores: $p=0.123$; for joint differences in observable characteristics of school-grade-years: $F=0.902, p=0.531$ ). Therefore, I conclude that results likely generalizable to these populations.

## 6. Discussion and Conclusion

This study provides some of the strongest evidence to date on the relationship between specific instructional dimensions and students' mathematics achievement. Like others (e.g., Kane et al., 2013; Kane \& Staiger, 2012; Kane et al., 2011), I utilize observation instruments that capture instructional quality within teachers' own classrooms. I also draw on established econometric methods to account for the nonrandom sorting of students to teachers (e.g., Rivkin, Hanushek, \& Kain, 2005). Importantly, I build on past work by examining multiple dimensions of teaching practice, including content-specific elements of instruction and more general pedagogical strategies. Further, I examine the sensitivity of results to models that control for different sets of teacher characteristics. This allows me to isolate dimensions of instructional quality from the most likely observable characteristics that might threaten the internal validity of my results. To my knowledge, no other studies are able to control for this broad set of teaching practices and teacher characteristics. While it is possible that estimates are sensitive to other observed or unobserved characteristics not included in
these data, my findings provide strong suggestive evidence of teaching dimensions that support student achievement.

Results indicate that inquiry-oriented instruction is positively related to student outcomes on a low-stakes math test, with an effect size of roughly 0.10 sd. This finding lends support to decades worth of reform to refocus mathematics instruction toward inquiry and concept-based teaching (National Council of Teachers of Mathematics, 1989, 1991, 2000), as well as positive results of some of these types of activities in laboratory settings (e.g., Star \& Rittle-Johnson, 2009). In some analyses, I also find smaller effect sizes for incorrect presentation of content, though estimates are sensitive to the set of covariates included in the model, particularly teachers' content knowledge. At the same time, even the smallest estimate of roughly 0.03 sd (see Model I in Table 7b) is similar in magnitude to estimates of the relationship between mentor evaluations and student achievement (Rockoff \& Speroni, 2010), suggesting that this finding may still be substantively significant.

Finally, I find no relationship between classroom climate or classroom management and student achievement. These results diverge from recent research highlighting the importance of classroom organization and interactions with students, often above other classroom features (Grossman, Loeb, Cohen, \& Wyckoff, 2013; Stronge, Ward, \& Grant, 2011). In particular, Kane and co-authors (2011, 2012, 2013) found positive relationships between these sorts of classroom practices, as captured on the Framework for Teaching observation instrument, and student achievement; estimates were similar in magnitude to the relationship I find between Ambitious Mathematics Instruction and student outcomes. One reason for these differences may be that these
other studies did not account for additional dimensions of teacher and teaching quality. Therefore, the observed relationship between classroom organization and student achievement may be driven by other practices and skills that are related to this type of instruction. Another reason may be that the outcome used to measure math achievement in this study is a low-stakes test that emphasizes cognitively demanding mathematics practices. Classroom organization and interactions with students may in fact be important contributors to high-stakes achievement tests or non-cognitive outcomes. This is an important topic for future research.

Evidence on the relationship between specific types of teaching and student achievement raises the question of how to get more teachers who engage in these practices into classrooms. Following Murnane and Cohen (1986), I argue that incentives are unlikely to prove effective here, as teachers may not know how to improve their instruction. Therefore, I propose two possible pathways. First, an array of recent literature highlights the potential use of observation instruments themselves to remediate teacher practice. Despite mixed results on the effect of standard professional development programs on teachers' content knowledge, instructional practices, or student achievement (Garet et al., 2011; Yoon, Duncan, Lee, Scarloss, \& Shapley, 2007), new experimental studies highlight positive effects of more intensive coaching programs that utilize observation instruments to improve teacher behaviors and, in some cases, student outcomes (Allen et al., 2011; Blazar \& Kraft, forthcoming; McCollum, Hemmeter, \& Hsieh, 2011; Taylor \& Tyler, 2012). Thus far, this sort of work has focused on use of observation instruments to capture general teaching practices and those specific to
literacy instruction. However, it is possible that findings also extend to inquiry-oriented practices in mathematics.

A second pathway to increase the quality of classroom teaching may also focus on selective recruitment of teachers with content-area expertise. My findings show a moderate to strong relationship between teachers' knowledge of math and the way that this content is enacted in the classroom. Further, I find suggestive evidence of a relationship between incorrect presentation of content and student outcomes. While more research is needed to confirm these relationships, these patterns may inform processes by which education preparation programs and state licensing agencies screen prospective elementary math teachers. A survey of degree pathways indicates minimal requirements for entry and a high degree of variability in the type of training pre-service teachers receive in mathematics. In addition, in all but a few states, elementary teachers can pass their licensing exam without passing the math sub-section (Epstein \& Miller, 2011). It is possible that creating more stringent requirements into the workforce related to math knowledge could lead to more accurate and precise presentation of content and to better student outcomes.

Filling elementary classrooms with teachers who engage in effective mathematics teaching practices will take time. Doing so likely will entail a variety of efforts, including improvements in professional development offerings that engage teachers substantively around their own teaching practices and stronger efforts to hire teachers with deep knowledge of mathematics. Importantly, though, the education community is beginning to gain an understanding of the types of teaching that contribute to student achievement.

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Tables

Table 1
Sample Descriptive Statistics

|  | All Districts | District 1 | District 2 | District 3 |
| :---: | :---: | :---: | :---: | :---: |
| Students |  |  |  |  |
| Male (\%) | 49.7 | 48.8 | 51.1 | 47.6 |
| African-American (\%) | 53.1 | 42.8 | 51.0 | 67.2 |
| Asian (\%) | 4.2 | 7.2 | 3.7 | 2.4 |
| Hispanic (\%) | 17.2 | 37.7 | 12.4 | 8.8 |
| White (\%) | 21.7 | 6.6 | 29.0 | 19.8 |
| FRPL (\%) | 71.0 | 84.1 | 71.3 | 58.3 |
| SPED (\%) | 10.6 | 14.5 | 10.2 | 7.9 |
| LEP (\%) | 16.4 | 23.6 | 17.8 | 6.6 |
| Students | 3203 | 724 | 1692 | 787 |
| Teachers |  |  |  |  |
| Bachelor's Degree in Education (\%) | 45.4 | 33.3 | 57.5 | 42.1 |
| Math Coursework (Likert Scale from 1 to 4) | 2.3 | 2.4 | 2.4 | 2.2 |
| Master's Degree (\%) | 75.0 | 83.3 | 77.5 | 65.8 |
| Traditional Certification (\%) | 70.3 | 74.2 | 92.5 | 45.0 |
| Experience (In Years) | 9.0 | 8.9 | 9.1 | 9.0 |
| Mathematical Content Knowledge (Standardized Scale) | -0.07 | 0.15 | 0.00 | -0.35 |
| Knowledge of Student Performance (Standardized Scale) | 0.05 | 0.32 | 0.16 | -0.28 |
| Preparation for Class (Likert Scale from 1 to 5) | 3.4 | 3.4 | 3.3 | 3.4 |
| Formative Assessment (Likert Scale from 1 to 5) | 3.6 | 3.6 | 3.6 | 3.6 |
| Teachers | 111 | 31 | 40 | 40 |

Table 2

|  | Univariate Statistics |  |  |  |  | Pairwise Correlations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Teacher Level |  | School-Grade-Year Level |  | Reliability | Ambitious Mathematics Instruction | Mathematical Errors and Imprecisions | Classroom <br> Emotional Support | Classroom Organization |
|  | Mean | SD | Mean | SD |  |  |  |  |  |
| Ambitious Mathematics Instruction | 1.26 | 0.12 | 1.27 | 0.10 | 0.69 | 1 |  |  |  |
| Linking and Connections |  |  |  |  |  |  |  |  |  |
| Explanations |  |  |  |  |  |  |  |  |  |
| Multiple Methods |  |  |  |  |  |  |  |  |  |
| Generalizations |  |  |  |  |  |  |  |  |  |
| Math Language |  |  |  |  |  |  |  |  |  |
| Remediation of Student Difficulty |  |  |  |  |  |  |  |  |  |
| Use of Student Productions |  |  |  |  |  |  |  |  |  |
| Student Explanations |  |  |  |  |  |  |  |  |  |
| Student Mathematical Questioning and Reasoning |  |  |  |  |  |  |  |  |  |
| Enacted Task Cognitive Activation |  |  |  |  |  |  |  |  |  |
| Mathematical Errors and Imprecisions | 1.12 | 0.12 | 1.12 | 0.08 | 0.52 | $-0.33^{* * *}$ | 1 |  |  |
| Major Mathematical Errors |  |  |  |  |  |  |  |  |  |
| Language Imprecisions |  |  |  |  |  |  |  |  |  |
| Lack of Clarity |  |  |  |  |  |  |  |  |  |
| Classroom Emotional Support | 4.26 | 0.55 | 4.24 | 0.34 | 0.55 | 0.34*** | -0.01 | 1 |  |
| Positive Climate |  |  |  |  |  |  |  |  |  |
| Teacher Sensitivity |  |  |  |  |  |  |  |  |  |
| Respect for Student Perspectives |  |  |  |  |  |  |  |  |  |
| Classroom Organization | 6.32 | 0.44 | 6.33 | 0.31 | 0.65 | 0.19*** | 0.05 | 0.44*** | 1 |
| Negative Climate |  |  |  |  |  |  |  |  |  |
| Behavior Management |  |  |  |  |  |  |  |  |  |
| Productivity |  |  |  |  |  |  |  |  |  |

Notes: Statistics generated from all available data. MQI items (from Ambitious Mathematics Instruction and Mathematical Errors and Imprecisions) on a scale from 1 to 3. CLASS items (from Classroom Emotional Support and Classroom Organization) on a scale from 1 to 7.

Table 3
Variance Decomposition of School-Grade-Year Instructional Quality Scores

|  | School | Residual |
| :--- | :---: | :---: |
| Ambitious Instruction | 0.59 | 0.41 |
| Mathematical Errors and Imprecisions | 0.46 | 0.54 |
| Classroom Emotional Support | 0.45 | 0.55 |
| Classroom Organization | 0.52 | 0.48 |

Notes: Sample includes 76 school-grade-years.

Table 4
Correlations Between Teacher Practices, Skills, and Background Characteristics

|  | Ambitious <br> Instruction | Mathematical <br> Errors and <br> Imprecisions | Classroom <br> Emotional <br> Support | Classroom <br> Organization |
| :--- | :---: | :---: | :---: | :---: |
| Bachelor's Degree in Education | -0.14 | -0.03 | -0.07 | 0.13 |
| Math Coursework | 0.08 | 0.08 | 0.15 | $0.30^{* * *}$ |
| Master's Degree | 0.10 | -0.05 | 0.00 | -0.12 |
| Traditional Certification | 0.09 | $-0.17 \sim$ | 0.12 | 0.12 |
| Experience | -0.07 | 0.15 | -0.04 | 0.05 |
| Mathematical Content Knowledge | $0.26^{* *}$ | $-0.46^{* * *}$ | 0.03 | 0.01 |
| Knowledge of Student Performance | $0.18 \sim$ | -0.16 | 0.00 | 0.09 |
| Preparation for Class | 0.02 | 0.07 | -0.04 | 0.10 |
| Formative Assessment | -0.01 | $0.24^{* *}$ | 0.14 | $0.17 \sim$ |

Notes: $\sim \mathrm{p}<0.10,{ }^{*} \mathrm{p}<0.05,{ }^{* *} \mathrm{p}<0.01,{ }^{* * *} \mathrm{p}<0.001$

Table 5
Relationships Between Assigned Students' Incoming Achievement and Instructional Quality

|  | Within <br> Districts | Within <br> Schools |
| :--- | :---: | :---: |
| Ambitious Mathematics Instruction | $0.180^{* * *}$ | $0.060^{*}$ |
|  | $(0.026)$ | $(0.028)$ |
| Mathematical Errors and Imprecisions | -0.022 | -0.034 |
|  | $(0.021)$ | $(0.022)$ |
| Classroom Emotional Support | -0.013 | -0.018 |
|  | $(0.018)$ | $(0.023)$ |
| Classroom Organization | -0.003 | $0.087 * *$ |
|  | $(0.024)$ | $(0.029)$ |

Notes: $\sim \mathrm{p}<.10,{ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<.01,{ }^{* * *} \mathrm{p}<.001$. Columns contain estimates from separate regressions. Robust standard errors in parentheses. All models control for district-by-grade-by-year fixed effects. Sample includes 3,203 students, 111 teachers, and 76 school-grade-years.

Table 6
Differences Between Teachers Who Switch Grade Assignments and Those Who Do Not

|  | Switchers | Non-Switchers | $P$-value on <br> Difference |
| :--- | :---: | :---: | :---: |
| Instructional Quality Dimensions |  |  |  |
| Ambitious Instruction | -0.05 | 0.03 | 0.660 |
| Mathematical Errors and Imprecisions | -0.07 | -0.20 | 0.463 |
| Classroom Emotional Support | -0.18 | -0.25 | 0.752 |
| Classroom Organization | -0.22 | -0.11 | 0.596 |
| Other Measures of Teacher Quality |  |  |  |
| Bachelor's Degree in Education | 63.0 | 42.7 | 0.169 |
| Math Coursework | 2.2 | 2.4 | 0.259 |
| Master's Degree | 74.4 | 77.4 | 0.781 |
| Traditional Certification | 69.7 | 74.7 | 0.613 |
| Experience | 7.8 | 10.1 | 0.208 |
| Mathematical Content Knowledge | -0.19 | -0.01 | 0.558 |
| Knowledge of Student Performance | 0.20 | 0.06 | 0.519 |
| Preparation for Class | 3.3 | 3.3 | 0.981 |
| Formative Assessment | 3.5 | 3.7 | 0.318 |
| Student Achievement Measures |  |  |  |
| Fall Project-Administered Math Test | -0.35 | -0.12 | 0.318 |
| Prior-Year State Math Test | -0.05 | 0.08 | 0.037 |
| Prior-Year State Reading Test | -0.09 | 0.10 | 0.002 |
| State Value-Added in Math | -0.03 | -0.01 | 0.646 |
| Join Test |  | $F$-statistic | 1.098 |
| Teacher-Year Observations | $p$-value | 0.367 |  |
| Nan Ma | 126 |  |  |

Notes: Means and $p$-values estimated from individual regressions that control for schoolyear, which is absorbed in the model.

Table 7a
Relationships Between Students' Mathematics Achievement and Instructional Quality, Accounting for Non-Random Sorting

|  | Model A | Model B | Model C | Model D |
| :--- | :---: | :---: | :---: | :---: |
| Ambitious Instruction | 0.061 | $0.095^{*}$ | $0.097^{*}$ | $0.109^{*}$ |
|  | $(0.038)$ | $(0.037)$ | $(0.042)$ | $(0.052)$ |
| Mathematical Errors and Imprecisions | -0.033 | $-0.040 \sim$ | $-0.050 \sim$ | $-0.053 \sim$ |
|  | $(0.022)$ | $(0.023)$ | $(0.026)$ | $(0.029)$ |
| Classroom Emotional Support | -0.028 | -0.001 | -0.032 | -0.026 |
|  | $(0.021)$ | $(0.023)$ | $(0.035)$ | $(0.037)$ |
| Classroom Organization | 0.026 | -0.002 | -0.003 | -0.015 |
|  | $(0.025)$ | $(0.024)$ | $(0.034)$ | $(0.037)$ |
| Student Covariates | X | X | X | X |
| Class Covariates | X | X | X | X |
| District-by-Grade-by-Year Fixed Effects | X | X | X | X |
| School Covariates | X |  |  |  |
| School Fixed Effects |  | X | X | X |
| Instructional Quality at School-Grade-Year Level |  |  | X | X |
| School-by-Year Fixed Effects |  |  |  |  |

Notes: $\sim \mathrm{p}<0.10,{ }^{*} \mathrm{p}<0.05,{ }^{* *} \mathrm{p}<0.01,{ }^{* * *} \mathrm{p}<0.001$. Columns contain estimates from separate regressions. Robust standard errors clustered at the school-grade-year level in parentheses. Sample includes 3,203 students, 111 teachers, and 76 school-grade-years.

Table 7b
Relationships Between Students' Mathematics Achievement and Instructional Quality, Accounting for Omitted Variables Bias

|  | Model E | Model F | Model G | Model H | Model I |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ambitious Mathematics Instruction | 0.124** | 0.096* | 0.083~ | $0.121^{* *}$ | 0.114* |
|  | (0.042) | (0.039) | (0.045) | (0.041) | (0.044) |
| Mathematical Errors and Imprecisions | -0.049~ | -0.049~ | -0.035 | -0.038 | -0.028 |
|  | (0.027) | (0.029) | (0.026) | (0.027) | (0.035) |
| Classroom Emotional Support | -0.038 | -0.031 | -0.025 | -0.044 | -0.041 |
|  | (0.031) | (0.036) | (0.036) | (0.034) | (0.036) |
| Classroom Organization | 0.010 | -0.002 | -0.009 | -0.002 | -0.002 |
|  | (0.035) | (0.033) | (0.034) | (0.035) | (0.039) |
| Bachelor's Degree in Education | 0.010 |  |  |  | -0.004 |
|  | (0.065) |  |  |  | (0.072) |
| Math Coursework | -0.027 |  |  |  | -0.019 |
|  | (0.021) |  |  |  | (0.028) |
| Master's Degree | 0.086 |  |  |  | 0.022 |
|  | (0.070) |  |  |  | (0.075) |
| Traditional Certification | -0.013 |  |  |  | -0.019 |
|  | (0.068) |  |  |  | (0.077) |
| Experience |  | -0.001 |  |  | -0.000 |
|  |  | (0.004) |  |  | (0.005) |
| Mathematical Content Knowledge |  |  | 0.017 |  | 0.008 |
|  |  |  | (0.020) |  | (0.031) |
| Knowledge of Student Performance |  |  | 0.035 |  | 0.038 |
|  |  |  | (0.041) |  | (0.044) |
| Preparation for Class |  |  |  | -0.054~ | -0.044 |
|  |  |  |  | (0.030) | (0.038) |
| Formative Assessment |  |  |  | 0.028 | 0.027 |
|  |  |  |  | (0.032) | (0.037) |

Notes: $\sim \mathrm{p}<.10,{ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<.01,{ }^{* * *} \mathrm{p}<.001$. Columns contain estimates from separate regressions.
Robust standard errors clustered at the school-grade-year level in parentheses. All models control for student and class covariates, as well as district-by-grade-by-year and school fixed effects. Instructional quality and background characteristics are averaged at the school-grade-year level. Sample includes 3,203 students, 111 teachers, and 76 school-grade-years.

Table 8
Differences Between Identification Sample and District Populations

|  | In <br> Identification <br> Sample | Out of <br> Identification <br> Sample | $p$-value on <br> Difference |
| :--- | :---: | :---: | :---: |
| Teacher Characteristic |  |  |  |
| State Value-Added | -0.02 | 0.00 | 0.123 |
| Teacher-Year Observations | 156 | 1,334 |  |
| School Characteristics |  |  |  |
| Male | 49.1 | 50.1 | 0.361 |
| African-American | 53.7 | 55.3 | 0.659 |
| Asian | 4.6 | 3.9 | 0.404 |
| Hispanic | 26.6 | 26.0 | 0.833 |
| White | 11.6 | 11.6 | 0.996 |
| FRPL | 74.2 | 76.3 | 0.504 |
| SPED | 17.1 | 15.7 | 0.240 |
| LEP | 21.3 | 20.8 | 0.810 |
| Prior-Year State Math Test | -0.02 | 0.04 | 0.299 |
| Prior-Year State Reading Test | 0.00 | 0.05 | 0.409 |
| Joint Test |  | $F$-statistic | 0.902 |
|  | $p$-value | 0.531 |  |
| School-Grade-Year Observations | 76 | 511 |  |
| Notes |  |  |  |

Notes: Means and $p$-values calculated from individual regressions that control for district.

## Appendices

Table A1
Relationships Between Instructional Quality and Class Composition

|  | Ambitious <br> Instruction | Mathematical <br> Errors and <br> Imprecisions | Classroom <br> Emotional <br> Support | Classroom <br> Organization |
| :--- | :---: | :---: | :---: | :---: |
| Class Size | -0.069 | 0.020 | -0.114 | -0.029 |
| Male | $(0.069)$ | $(0.059)$ | $(0.077)$ | $(0.061)$ |
|  | 0.016 | -0.013 | -0.002 | -0.021 |
| African American | $(0.012)$ | $(0.013)$ | $(0.014)$ | $(0.016)$ |
|  | 0.005 | 0.005 | -0.038 | 0.022 |
| Asian | $(0.023)$ | $(0.026)$ | $(0.034)$ | $(0.029)$ |
|  | -0.015 | -0.016 | -0.037 | 0.060 |
| Hispanic | $(0.037)$ | $(0.038)$ | $(0.052)$ | $(0.039)$ |
|  | 0.002 | 0.003 | -0.036 | 0.030 |
| White | $(0.022)$ | $(0.024)$ | $(0.034)$ | $(0.026)$ |
|  | -0.017 | 0.012 | 0.005 | 0.035 |
| FRPL | $(0.035)$ | $(0.035)$ | $(0.043)$ | $(0.036)$ |
| SPED | -0.014 | 0.000 | 0.012 | 0.016 |
|  | $(0.011)$ | $(0.013)$ | $(0.013)$ | $(0.011)$ |
| LEP | -0.009 | 0.006 | $-0.035^{*}$ | -0.018 |
|  | $(0.010)$ | $(0.012)$ | $(0.013)$ | $(0.012)$ |
| Fall Project-Administered Math Test | -0.003 | 0.004 | 0.004 | 0.014 |
|  | 0.439 | $(0.017)$ | $(0.018)$ | $(0.019)$ |
| Prior-Year State Math Test | 1.739 | $-2.384^{*}$ | 0.085 |  |
| Prior-Year State Reading Test | $(0.666)$ | $(1.090)$ | $(0.880)$ | $(0.859)$ |
|  | -0.005 | 0.099 | -0.984 | -0.523 |
| Joint Test | $(0.630)$ | $(0.834)$ | $(0.877)$ | $(1.028)$ |
|  | $0.475^{*}$ | -0.401 | $1.186^{* *}$ | -0.366 |
|  | $(0.224)$ | $(0.462)$ | $(0.368)$ | $(0.421)$ |

Notes: $\sim \mathrm{p}<0.10,{ }^{*} \mathrm{p}<0.05$, ${ }^{* *} \mathrm{p}<0.01,{ }^{* * *} \mathrm{p}<0.001$. Columns contain estimates from separate regressions. Robust standard errors clustered at the school-grade-year level in parentheses. All models include teacher fixed effects. Sample includes 45 teachers who were in the study for two years.

## Paper 2

# Teacher and Teaching Effects on Students' Attitudes and Behaviors ${ }^{10}$ 


#### Abstract

Research has focused predominantly on how teachers affect students’ achievement on tests despite evidence that a broad range of attitudes and behaviors are equally important to their long-term success. We find that upper-elementary teachers have large effects on self-reported measures of students' self-efficacy in math, and happiness and behavior in class. Students' attitudes and behaviors are predicted by teaching practices most proximal to these measures, including teachers' emotional support and classroom organization. However, teachers who are effective at improving math test scores often are not equally effective at improving students' attitudes and behaviors. These findings lend evidence to well-established theory on the multidimensional nature of teaching and the need to identify strategies for improving the full range of teachers' skills.


[^8]
## 1. Introduction

Empirical research on the education production function traditionally has examined how teachers and their background characteristics contribute to students’ performance on standardized tests (Todd \& Wolpin, 2003; Hanushek \& Rivkin, 2010). However, a substantial body of evidence indicates that student learning is multidimensional, with many factors beyond their core academic knowledge as important contributors to both short- and long-term success. ${ }^{11}$ For example, psychologists find that emotion and personality influence the quality of one's thinking (Baron, 1982) and how much a child learns in school (Duckworth, Quinn, \& Tsukayama, 2012). Longitudinal studies document the strong predictive power of measures of childhood self-control, emotional stability, persistence, and motivation on health and labor market outcomes in adulthood (Borghans, Duckworth, Heckman, \& Ter Weel, 2008; Chetty et al., 2011; Moffitt et. al., 2011). In fact, these sorts of attitudes and behaviors are stronger predictors of some long-term outcomes than test scores (Chetty et al., 2011).

Consistent with these findings, decades worth of theory also have described teaching as multidimensional. High-quality teachers are thought and expected not only to raise test scores but also to provide emotionally supportive environments that contribute to students' social and emotional development, to manage classroom behaviors, to deliver accurate content, and to support critical thinking (Cohen, 2011; Lampert, 2001; Pianta \& Hamre, 2009). In recent years, two research traditions have emerged to test this theory using empirical evidence. The first tradition has focused on observations of classrooms as

[^9]a means of identifying unique domains of teaching practice (Blazar, Braslow, Charalambous, \& Hill, 2015; Hamre et al., 2013). Several of these domains, including teachers' interactions with students, classroom organization, and emphasis on critical thinking within specific content areas, aim to support students' development in areas beyond their core academic skill. The second research tradition has focused on estimating internally valid estimates of teachers' contribution to student outcomes, often referred to as "teacher effects" (Chetty et al., 2011; Hanushek \& Rivkin, 2010). These studies have found that, as with test scores, teachers vary considerably in their ability to impact students' social and emotional development and a variety of observed school behaviors (Backes \& Hansen, 2015; Gershenson, 2016; Jackson, 2012; Jennings \& DiPrete, 2010; Kraft \& Grace, 2016; Koedel, 2008; Ladd \& Sorensen, 2015; Ruzek et al., 2014). Further, weak to moderate correlations between teacher effects on different student outcomes suggest that test scores alone cannot identify teachers' skill in the classroom (Gershenson, 2016; Jackson, 2012; Jennings \& DiPrete, 2010; Kraft \& Grace, 2016).

Our study is among the first to integrate these two research traditions, which largely have developed in isolation. Working at the intersection of these traditions, we aim both to maximize internal validity and to open up the "black box" of teacher effects by examining whether certain dimensions of teaching practice predict students' attitudes and behaviors. We refer to these relationships between teaching practice and student outcomes as "teaching effects." Specifically, we ask three research questions:
(1) To what extent do teachers impact students' attitudes and behaviors in class?
(2) To what extent do specific teaching practices impact students' attitudes and behaviors in class?
(3) Are teachers who are effective at raising test-score outcomes equally effective at developing positive attitudes and behaviors in class?

To answer our research questions, we draw on a rich dataset from the National Center for Teacher Effectiveness (NCTE) of upper-elementary teachers' math instruction that collected teacher-student links, observations of teaching practice on two established observation instruments, students' math performance on both high- and low-stakes tests, and a student survey that captured their attitudes and behaviors in class. We used this survey to construct our three primary outcomes: students' self-reported self-efficacy in math, happiness in class, and behavior in class. Although the specific attitudes and behaviors we examine are limited to those available in NCTE data, they are important outcomes of interest to researchers, policymakers, and parents (Borghans et al., 2008; Chetty et al., 2011; Farrington et al., 2012). They also align with theories linking teachers and teaching practice to outcomes beyond students' core academic skills (Bandura, Barbaranelli, Caprara, \& Pastorelli, 1996; Pianta \& Hamre, 2009), allowing us to test these theories explicitly.

We find that upper-elementary teachers in our sample have substantive impacts on students' self-reported attitudes and behaviors in addition to their math performance. We estimate that the variation in teacher effects on students' self-efficacy in math and behavior in class is of similar magnitude to the variation in teacher effects on math test scores. Teacher effects on students' happiness in class are even larger than those for testbased outcomes. Further, these outcomes are predicted by teaching practices most
proximal to these measures, thus aligning with theory and providing important face and construct validity to these measures. Specifically, teachers' emotional support for students is related both to their self-efficacy in math and their happiness in class. Teachers' classroom organization predicts students' reports of their own behavior in class. Errors in teachers' presentation of mathematical content are negatively related to students' self-efficacy in math and happiness in class, as well as students' math performance. Finally, we find that teachers are not equally effective at improving all outcomes. Compared to an unadjusted correlation between teacher effects on our two math achievement tests of 0.64 , the strongest unadjusted correlation between teacher effects on students' math achievement and effects on their attitudes or behavior is 0.19.

Together, these findings add further evidence for the multidimensional nature of teaching and, thus, the need for researchers, policymakers, and practitioners to identify strategies for improving these skills. In our conclusion, we discuss several instances in which policymakers and practitioners may start to do so, including the design and implementation of teacher evaluation systems, teacher recruitment policies, and strategic teacher assignments. We situate this discussion within existing resource constraints and challenges associated with outcome-based accountability, both of which make this a complicated task.

## 2. Review of Related Research

Theories of teaching and learning have long emphasized the important role teachers play in supporting students' development in areas beyond their core academic skill. For example, in their conceptualization of high-quality teaching, Pianta and Hamre (2009) describe a set of emotional supports and organizational techniques that are equally
important to learners as teachers' instructional methods. They posit that, by providing "emotional support and a predictable, consistent, and safe environment" (p. 113), teachers can help students become more self-reliant, motivated to learn, and willing to take risks. Further, by modeling strong organizational and management structures, teachers can help build students' own ability to self-regulate. Content-specific views of teaching also highlight the importance of teacher behaviors that develop students' attitudes and behaviors in ways that may not directly impact test scores. In mathematics, which is the focus of this paper, researchers and professional organizations have advocated for teaching practices that emphasize critical thinking and problem solving around authentic tasks (Lampert, 2001; National Council of Teachers of Mathematics [NCTM], 1989, 2014). Understanding the considerable stresses that this content can create for students, others have pointed to teachers' equally important role of developing students' self-efficacy and decreasing their anxiety in math (Bandura et al., 1996; Usher \& Pajares, 2008; Wigfield \& Meece, 1988).

In recent years, development and use of observation instruments that capture the quality of teachers' instruction have provided a unique opportunity to examine these theories empirically. One instrument in particular, the Classroom Assessment Scoring System (CLASS), is organized around "meaningful patterns of [teacher] behavior...tied to underlying developmental processes [in students]" (Pianta \& Hamre, 2009, p. 112). Factor analyses of data collected by this instrument have identified several unique aspects of teachers' instruction: teachers' social and emotional interactions with students, their ability to organize and manage the classroom environment, and their instructional supports in the delivery of content (Hafen et al., 2015; Hamre et al., 2013). A number of
studies from developers of the CLASS instrument and their colleagues have described relationships between these dimensions and closely related student attitudes and behaviors. For example, teachers' interactions with students predicts students' social competence, engagement, and risk-taking; teachers' classroom organization predicts students' engagement and behavior in class (Burchinal et al., 2008; Downer, RimmKaufman, \& Pianta, 2007; Hamre, Hatfield, Pianta, \& Jamil, 2014; Hamre \& Pianta, 2001; Luckner \& Pianta, 2011; Mashburn et al., 2008; Pianta, La Paro, Payne, Cox, \& Bradley, 2002). To date, these studies have focused predominantly on pre-kindergarten settings (for a few exceptions, see Downer et al., 2007; Hamre \& Pianta, 2001; Luckner \& Pianta, 2011). Further, none of the studies can rule out the possibility of omitted variables bias - that is, that teachers who have strong interactions with students or behavior management techniques might also engage in additional practices that are responsible for higher student outcomes.

Additional content-specific observation instruments highlight several other teaching competencies with links to students' attitudes and behaviors. For example, in this study we draw on the Mathematical Quality of Instruction (MQI) to capture mathspecific dimensions of teachers' classroom practice. Factor analyses of data captured both by this instrument and the CLASS identified two teaching skills in addition to those described above: the cognitive demand of math activities that teachers provide to students and the precision with which they deliver this content (Blazar et al., 2015). To date, validity evidence for the MQI has focused on the relationship between these teaching practices and students' math test scores (Blazar, 2015; Kane \& Staiger, 2012), which makes sense given the theoretical link between teachers' content knowledge, delivery of
this content in the classroom, and students' own understanding of the content (Hill et al., 2008). However, as noted above, professional organizations and researchers also describe theoretical links between the sorts of teaching practices captured on the MQI and student outcomes beyond test scores (e.g., critical thinking, self-efficacy in math; Bandura et al., 1996; Lampert, 2001; NCTM, 1989, 2014; Usher \& Pajares, 2008; Wigfield \& Meece, 1988) that, to our knowledge, have not been tested.

In a separate line of research, several recent studies have borrowed from the literature on teachers' "value-added" to student test scores in order to document the magnitude of teacher effects on a range of other outcomes. Consistent with the teacher effectiveness literature more broadly, these studies attempt to isolate the unique effect of teachers on non-tested outcomes from factors outside of teachers' control (e.g., students' prior achievement, race, gender, socioeconomic status) and to limit any bias due to nonrandom sorting. In one of the first studies of this kind, Jennings and DiPrete (2010) used the Early Childhood Longitudinal Study - Kindergarten Cohort (ECLS-K) to estimate the role that teachers play in a composite measure of kindergarten and first-grade students' social and behavioral outcomes. They found teacher effects on social and behavioral outcomes that were even larger ( 0.35 standard deviations [sd]) than effects on academic achievement. In a study of 35 middle school math teachers, Ruzek et al. (2014) found small but meaningful teacher effects on motivation between 0.03 sd and 0.08 sd among seventh graders. Kraft and Grace (2016) found teacher effects on students' self-reported measures of grit, growth mindset and effort in class ranging between 0.14 and 0.17 sd . Additional studies identified teacher effects on observed school behaviors, including
absences, suspensions, grades, grade progression, and graduation (Backes \& Hansen, 2015; Gershenson, 2016; Jackson, 2012; Koedel, 2008; Ladd \& Sorensen, 2015).

To date, evidence is mixed on the extent to which teachers who improve test scores also improve other outcomes. Four of the studies described above found weak relationships between teacher effects on students' academic performance and effects on other outcome measures. Compared to a correlation of 0.42 between teacher effects on math achievement versus effects on reading achievement, Jennings and DiPrete (2010) found correlations of 0.15 between teacher effects on students' social and behavioral outcomes and effects on either math or reading achievement. Kraft and Grace (2016) found correlations between teacher effects on achievement outcomes and multiple socialemotional competencies were sometimes non-existent and never greater than 0.23. Similarly, Gershenson (2016) and Jackson (2012) found weak or null relationships between teacher effects on students' academic performance and effects on observed schools behaviors. However, correlations from two other studies were larger. Ruzek et al. (2014) estimated a correlation of 0.50 between teacher effects on achievement versus effects on students' motivation in math class. Drawing on data from the MET project, Mihaly, McCaffrey, Staiger, and Lockwood (2013) found a correlation of 0.57 between middle school teacher effects on students' self-reported effort versus effects on math test scores.

Our analyses extend this body of research in several ways. First, we estimate teacher effects on additional attitudes and behaviors captured by students in upperelementary grades. We also are able to leverage data that offer the unique combination of a moderately sized sample of teachers and students with lagged survey measures. Second,
we utilize similar econometric approaches to test the relationship between teaching practice and these same attitudes and behaviors. These analyses allow us to examine the face and construct validity of our teacher effect estimates and the extent to which they align with theory. Finally, we examine teacher and teaching effects in the context of mathematics, which is essential for policy given a growing focus of education reform on STEM education (Duncan, 2010; U.S. Department of Education, 2010).

## 3. Data and Sample

Beginning in the 2010-2011 school year, the NCTE engaged in a three-year data collection process. Data came from participating fourth- and fifth-grade teachers ( $\mathrm{N}=$ 310) in four anonymous, urban school districts on the East coast of the United States who agreed to have their classes videotaped, complete a teacher questionnaire, and help collect a set of student outcomes. Teachers were clustered within 52 schools, with an average of six teachers per school. Teacher-student links were verified for all study participants based on class rosters provided by teachers. While this study focused on teachers' math instruction, participants were generalists who taught all subject areas. This is important, as it allowed us to consider the contribution of individual teachers to students' attitudes and behaviors that was not confounded by the influence of multiple teachers in the same year. Despite having a non-random sample of teachers, evidence from these same data indicated that teachers who participated in the study did not differ on their effectiveness at improving students' math test scores as those who did not participate (Blazar, Litke, \& Barmore, in press). We describe this sample in more depth below.

### 3.1. Students' Attitudes and Behaviors

As part of the expansive data collection effort, researchers administered a student survey with items $(\mathrm{N}=18)$ that were adapted from other large-scale surveys including the TRIPOD survey project, the MET project, the National Assessment of Educational Progress (NAEP), and the Trends in International Mathematics and Science Study (TIMSS) (see Appendix Table 1 for a full list of items). Items were selected based on a review of the research literature and identification of constructs thought most likely to be influenced by upper-elementary teachers and math-specific teaching practices. Students rated all items on a five-point Likert scale where $1=$ Totally Untrue and $5=$ Totally True. We reverse coded items with negative valence in order to form composites with other items.

Researchers and policymakers have raised several concerns about the use of selfreported survey data to capture students' underlying attitudes and behaviors. Students and elementary students in particular - may not be accurate reporters of their own attitudes and behaviors. Their responses can be prone to "social desirability bias," in which students "provide answers that are desirable but not accurate" (Duckworth \& Yeager, 2015, p. 239). Different frames of reference also can bias responses. For example, school-wide norms around behavior and effort may change the implicit standards of comparison that students use to judge their own behavior and effort (West et al., 2016). In response to these concerns, we describe validity evidence both from our own and other studies as we present each of our student outcomes below. We also attempted to minimize the potential threat posed by reference bias through our modeling strategy. Specifically, we restricted comparisons to teachers and students in the same
school, which helps limit potential differences in reference groups and social norms across schools that could confound our analyses.

We identified a parsimonious set of three outcome measures based on a combination of theory and exploratory factor analyses (see Appendix Table 1). ${ }^{12}$ The first outcome, which we call Self-Efficacy in Math (10 items), is a variation on well-known constructs related to students' effort, initiative, and perception that they can complete tasks. In other datasets focused on elementary students, academic self-efficacy is correlated with math achievement around 0.21 (Multon, Brown, \& Lent, 1991), which is quite close to the correlation we find between Self-Efficacy in Math and the two math test scores ( $r=0.25$ and 0.22 ; see Table 1 ). These similarities provide important validity evidence for our construct. The second related outcome measure is Happiness in Class (5 items), which was collected in the second and third years of the study. Exploratory factor analyses suggested that these items clustered together with those from Self-Efficacy in Math to form a single construct. However, post-hoc review of these items against the psychology literature from which they were derived suggests that they can be divided into a separate domain. As above, this measure is a school-specific version of wellknown scales that capture students' affect and enjoyment (Diener, 2000). Both SelfEfficacy in Math and Happiness in Class have relatively high internal consistency reliabilities ( 0.76 and 0.82 , respectively) that are similar to those of self-reported attitudes

[^10]and behaviors explored in other studies (Duckworth et al., 2007; John \& Srivastava, 1999; Tsukayama et al., 2013). Further, self-reported measures of similar constructs have been linked to long-term outcomes, including academic engagement and earnings in adulthood, even conditioning on cognitive ability (King, McInerney, Ganotice, \& Villarosa, 2015; Lyubomirsky, King, \& Diener, 2005).

The third and final construct consists of three items that were meant to hold together and which we call Behavior in Class (internal consistency reliability is 0.74 ). Higher scores reflect better, less disruptive behavior. Teacher reports of students' classroom behavior have been found to relate to antisocial behaviors in adolescence, criminal behavior in adulthood, and earnings (Chetty et al., 2011; Segal, 2013; Moffitt et al., 2011; Tremblay et al., 1992). Our analysis differs from these other studies in the selfreported nature of behavior outcomes. That said, other studies also drawing on elementary school students found correlations between self-reported and either parent- or teacher-reported measures of behavior that were similar in magnitude to correlations between parent and teacher reports of student behavior (Achenbach, McConaughy, \& Howell, 1987; Goodman, 2001). Further, other studies have found correlations between teacher-reported behavior of elementary school students and either reading or math achievement ( $r=0.22$ to 0.28 ; Miles \& Stipek, 2006; Tremblay et al., 1992) similar to the correlation we find between students' self-reported Behavior in Class and our two math test scores ( $r=0.24$ and 0.26 ; see Table 1). Together, this evidence provides both convergent and consequential validity evidence for this outcome measure. For all three of these outcomes, we created final scales by averaging raw student responses across all available items and standardizing measures to have a mean of zero and a standard
deviation of one within each school year. ${ }^{13}$ We standardized within years, given that, for some measures, the set of survey items varied across years.

### 3.2. Student Demographic and Test Score Information

Student demographic and achievement data came from district administrative records. Demographic data include gender, race/ethnicity, free- or reduced-price lunch (FRPL) eligibility, limited English proficiency (LEP) status, and special education (SPED) status. These records also included current- and prior-year test scores in math and English Language Arts (ELA) on state assessments, which we standardized within districts by grade, subject, and year using the entire sample of students in each district, grade, subject, and year.

The project also administered a low-stakes mathematics assessment to all students in the study. Validity evidence indicates internal consistency reliability of 0.82 or higher for each form across grade levels and school years (Hickman, Fu, \& Hill, 2012). We used this assessment in addition to high-stakes tests given that teacher effects on two outcomes that aim to capture similar underlying constructs (i.e., math achievement) provide a unique point of comparison when examining the relationship between teacher effects on student outcomes that are less closely related (i.e., math achievement versus attitudes and behaviors). Indeed, students' high- and low-stake math test scores are correlated more strongly $(r=0.70)$ than any other two outcomes (see Table 1 ). Coding of items from both the low- and high-stakes tests also identify a large degree of overlap in terms of content coverage and cognitive demand (Lynch, Chin, \& Blazar, 2015). All tests focused most on numbers and operations ( $40 \%$ to $60 \%$ ), followed by geometry (roughly $15 \%$ ), and algebra

[^11]( $15 \%$ to $20 \%$ ). By asking students to provide explanations of their thinking solve nonroutine problems such as identifying patterns, the low-stakes test also was similar to the high-stakes tests in two districts; in the other two districts, items often asked students to execute basic procedures.

### 3.3. Mathematics Lessons

Teachers' mathematics lessons were captured over a three-year period, with an average of three lessons per teacher per year. ${ }^{14}$ This number corresponds to recommendations by Hill, Charalambous, and Kraft (2012) to achieve sufficiently high levels of predictive reliability. Trained raters scored these lessons on two established observational instruments, the CLASS and the MQI. Analyses of these same data show that items cluster into four main factors (Blazar et al., 2015). The two dimensions from the CLASS instrument capture general teaching practices: Emotional Support focuses on teachers' interactions with students and the emotional environment in the classroom, and is thought to increase students' social and emotional development; and Classroom Organization focuses on behavior management and productivity of the lesson, and is thought to improve students' self-regulatory behaviors (Pianta \& Hamre, 2009). ${ }^{15}$ The two dimensions from the MQI capture mathematics-specific practices: Ambitious

Mathematics Instruction focuses on the complexity of the tasks that teachers provide to

[^12]their students and their interactions around the content, thus corresponding to the set of professional standards described by NCTM $(1989,2014)$ and many elements contained within the Common Core State Standards for Mathematics (National Governors Association Center for Best Practices, 2010); Mathematical Errors identifies any mathematical errors or imprecisions the teacher introduces into the lesson. Both dimensions from the MQI are linked to teachers' mathematical knowledge for teaching and, in turn, to students' math achievement (Blazar, 2015; Hill et al., 2008; Hill, Schilling, \& Ball, 2004).

We estimate reliability for these metrics by calculating the amount of variance in teacher scores that is attributable to the teacher (the intraclass correlation [ICC]), adjusted for the modal number of lessons. These estimates are: $0.53,0.63,0.74$, and 0.56 for Emotional Support, Classroom Organization, Ambitious Mathematics Instruction, and Mathematical Errors, respectively (see Table 2). Though some of these estimates are lower than conventionally acceptable levels (0.7), they are consistent with those generated from similar studies (Kane \& Staiger, 2012). Correlations between dimensions range from roughly 0 (between Emotional Support and Mathematical Errors) to 0.46 (between Emotional Support and Classroom Organization). Given that teachers contributed different number of lessons to the project, which could lead to noise in these observational measures, we utilized empirical Bayes estimation to shrink scores back to the mean based on their precision (see below for more details). We standardized final scores within the full sample of teachers to have a mean of zero and a standard deviation of one.

### 3.4. Sample Restrictions

In choosing our analysis sample, we faced a tradeoff between precision and internal validity. Including all possible teachers would maximize the precision of our estimates. At the same time, we lacked critical data for some students and teachers that could have been used to guard against potential sources of bias. Thus, we chose to make two important restrictions to our original sample of teachers in order to strengthen the internal validity of our findings. First, for all analyses predicting students' attitudes and behaviors, we only included fifth grade teachers who happened to have students who also had been part of the project in the fourth grade and, therefore, took the survey in the prior year. This group included between 51 and 111 teachers and between 548 and 1,529 students. For analyses predicting test score outcomes, we were able to maintain the full sample of 310 teachers, whose 10,575 students all had test scores in the previous year. Second, in analyses relating domains of teaching practice to student outcomes, we further restricted our sample to teachers who themselves were part of the study for more than one year, which allowed us to use out-of-year observation scores that were not confounded with the specific set of students in the classroom. This reduced our analysis samples to between 47 and 93 teachers and between 517 and 1,362 students when predicting students' attitudes and behaviors, and 196 teachers and 8,660 students when predicting math test scores. We describe the rationale for these restrictions in more detail below.

In Table 3, we present descriptive statistics on teachers and their students in the full sample (column 1), as well as those who were ever in any of our analyses predicting students' attitudes and behaviors (column 2). ${ }^{16}$ We find that teachers look relatively

[^13]similar across these two analytic samples, with no statistically significant differences on any observable characteristics. ${ }^{17}$ Sixteen percent of teachers were male and $65 \%$ were white. Eight percent received their teaching certification through an alternative pathway. The average number of years of teaching experience was roughly 10 . Value-added scores on state math tests were right around the mean for each district ( 0.01 sd ). Blazar et al. (in press) tested formally for differences in these value-added scores between project teachers and the full population of teachers in each district and found none, lending important external validity to our findings

We do observe some statistically significant differences between student characteristics in the full sample versus the subsample. For example, the percentage of students identified as limited English proficient was 20\% in the full sample compared to $14 \%$ in the sample of students who ever were part of analyses drawing on our survey measures. Average prior achievement scores were 0.10 sd and 0.09 sd in math and ELA in the full sample, respectively, compared to 0.18 sd and 0.20 sd in the subsample. Although variation in samples could result in dissimilar estimates across models, the overall character of our findings is unlikely to be driven by these modest differences. Further, students in our samples look similar to those in many urban districts in the United States, where roughly $68 \%$ are eligible for free or reduced-price lunch, $14 \%$ are classified as in need of special education services, and $16 \%$ are identified as limited English proficient; roughly $31 \%$ are African American, $39 \%$ are Hispanic, and $28 \%$ are
construct capturing teachers' mathematics coursework. Further, the survey included a test of teachers' mathematical content knowledge, with items from both the Mathematical Knowledge for Teaching assessment (Hill, Schilling, \& Ball, 2004), which captures math-specific pedagogical knowledge, and the Massachusetts Test for Educator Licensure. Teacher scores were generated by IRTPro software and standardized in these models, with a reliability of 0.92 . (For more information about these constructs, see Hill, Blazar, \& Lynch, 2015.)
${ }^{17}$ Descriptive statistics and formal comparisons of other samples show similar patterns and are available upon request.
white. Comparatively, in the country as a whole, a much higher percentage of students are white (roughly 52\%), and lower percentages are eligible for free or reduced-price lunch (49\%) or classified as limited English proficient (9\%) (Council of the Great City Schools, 2013).

## 4. Empirical Strategy

### 4.1. Estimating Teacher Effects on Students' Attitudes and Behaviors

Like others who aim to examine the contribution of individual teachers to student outcomes, we began by specifying an education production function model of each outcome for student $i$ in district $d$, school $s$, grade $g$, class $c$ with teacher $j$ at time $t$ :

$$
\begin{equation*}
\text { OUTCOME }_{\text {idsgjct }}=\alpha f\left(A_{i t-1}\right)+\pi X_{i t}+\varphi \bar{X}_{i t}^{c}+\tau_{d g t}+\left(\mu_{j}+\delta_{j c}+\varepsilon_{i d s g j c t}\right) \tag{1}
\end{equation*}
$$

OUTCOME idsgjct is used interchangeably for both math test scores and students'
attitudes and behaviors, which we modeled in separate equations as a cubic function of students' prior achievement, $A_{i t-1}$, in both math and ELA on the high-stakes district tests ${ }^{18}$; demographic characteristics, $X_{i t}$, including gender, race, FRPL eligibility, SPED status, and LEP status; these same test-score variables and demographic characteristics averaged to the class level, $\bar{X}_{i t}^{c}$; and district-by-grade-by-year fixed effects, $\tau_{d g t}$, that account for scaling of high-stakes test scores at this level. The error structure consists of both teacher- and class-level random effects, $\mu_{j}$ and $\delta_{j c}$, respectively, and a studentspecific error term, $\varepsilon_{\text {idsg } j c t}$. Given our focus on elementary teachers, over $97 \%$ of

[^14]teachers in our sample worked with just one set of students in a given year. Thus, class effects are estimated by observing teachers in multiple years and are analogous to teacher-by-year effects.

The key identifying assumption of this model is that estimates are not biased by non-random sorting of students to teachers. Recent experimental (Kane, McCaffrey, Miller, \& Staiger, 2013) and quasi-experimental (Chetty et al., 2014) analyses provide strong empirical support for this claim when student achievement is the outcome of interest. However, much less is known about bias and sorting mechanisms when other outcomes are used. For example, it is quite possible that students were sorted to teachers based on their classroom behavior in ways that were unrelated to their prior achievement. To address this possibility, we made two modifications to equation (2). First, we included school fixed effects, $\sigma_{s}$, to account for sorting of students and teachers across schools. This means that estimates rely only on between-school variation, which has been common practice in the research literature when estimating teacher effects on student achievement. In their review of this literature, Hanushek and Rivkin (2010) propose ignoring the between-school component because it is "surprisingly small" and because including this component leads to "potential sorting, testing, and other interpretative problems" (p. 268). Other recent studies estimating teacher effects on student outcomes beyond test scores have used this same approach (Backes \& Hansen, 2015; Gershenson, 2016; Jackson, 2012; Ladd \& Sorensen, 2015). Another important benefit of withinschool comparisons is that it minimizes the possibility of reference bias in our selfreported measures (Duckworth \& Yeager, 2015; West et al., 2016). As a second modification for models that predict each of our three student survey measures, we
included $O U T C O M E_{i t-1}$ on the right-hand side of the equation in addition to prior achievement - that is, when predicting students' Behavior in Class, we controlled for students' self-reported Behavior in Class in the prior year. ${ }^{19}$ This strategy helps account for within-school sorting on factors other than prior achievement.

Using equation (1), we estimated the variance of $\mu_{j}$, which is the stable component of teacher effects. We report the standard deviation of these estimates across outcomes. This parameter captures the magnitude of the variability of teacher effects. With the exception of teacher effects on students' Happiness in Class, where survey items were not available in the first year of the study, we included $\delta_{j c}$ in order to separate out the time-varying portion of teacher effects, combined with peer effects and any other class-level shocks. The fact that we are able to separate class effects from teacher effects is an important extension of prior studies examining teacher effects on outcomes beyond test scores, many of which only observed teachers at one point in time. Because $\mu_{j}$ is measured imprecisely given typical class sizes, unadjusted estimates would overstate the true variation in teacher effects. Thus, we utilized empirical Bayes estimation to shrink each score for teacher $j$ back toward the mean based on its precision (Raudenbush \& Bryk, 2002), where precision is a function of the number of students attributed to each teacher or class. Like others interested in the variance of teacher effects (e.g., Chetty et al.,

[^15]2011), we specified this parameter as a random effect, which provides unbiased modelbased estimates of the true population variance of teacher effects. ${ }^{20}$

### 4.2. Estimating Teaching Effects on Students' Attitudes and Behaviors

We examined the contribution of teachers' classroom practices to our set of student outcomes by estimating a variation of equation (1):

$$
\begin{gather*}
\text { OUTCOME }_{i d s g j c t}=\beta \text { OBSER } \widehat{\operatorname{VATION}}  \tag{2}\\
l j,-t \\
\\
\\
\pi X_{i t}+\varphi \bar{X}_{i t}^{c}+\sigma_{s}+\tau_{d g t}+\left(\mu_{j}+\delta_{j c}+\varepsilon_{i d s g j c t}\right)+\gamma \text { OUTCOME }
\end{gather*}
$$

This multi-level model includes the same set of control variables as above in order to account for the non-random sorting of students to teachers and for factors beyond teachers' control that might influence each of our outcomes. We further included a vector of their teacher $j$ 's observation scores, $O B S E R \widehat{V A T} I O N_{l j,-t}$. The coefficients on these variables are our main parameters of interest and can be interpreted as the change in standard deviation units for each outcome associated with exposure to teaching practice one standard deviation above the mean. ${ }^{21}$

One concern when relating observation scores to student survey outcomes is that they may capture the same behaviors. For example, teachers may receive credit on the Classroom Organization domain when their students demonstrate orderly behavior. In this case, we would have the same observed behaviors on both the left and right side of

[^16]our equation relating instructional quality to student outcomes, which would inflate our teaching effect estimates. A related concern is that the specific students in the classroom may influence teachers' instructional quality (Hill, Blazar, \& Lynch, 2015; Steinberg \& Garrett, in press; Whitehurst, Chingos, \& Lindquist, 2014). ${ }^{22}$ While the direction of bias is not as clear here - as either lesser- or higher-quality teachers could be sorted to harder to educate classrooms - this possibility also could lead to incorrect estimates. To avoid these sources of bias, we only included lessons captured in years other than those in which student outcomes were measured, denoted by $-t$ in the subscript of OBSER $\widehat{V A T I O N} N_{l,-t}$. As noted above, these are predicted estimates that aim to reduce measurement error in our observation measures. ${ }^{23}$ To the extent that instructional quality varies across years, using out-of-year observation scores creates a lower-bound estimate of the true relationship between instructional quality and student outcomes. We consider this an important tradeoff to minimize potential bias.

An additional concern for identification is the endogeneity of observed classroom quality. Our preferred analytic approach attempted to account for potential sources of bias by conditioning estimates of the relationship between one dimension of teaching

[^17]The outcome is the observation score for lesson $l$ from teacher $j$ in years other than $t ; \gamma_{j}$ is a random effect for each teacher, and $\varepsilon_{l j t}$ is the residual. For each domain of teaching practice and school year, we utilized standardized estimates of the teacher-level residual as each teacher's observation score in that year. Thus, scores vary across time. In the main text, we refer to these teacher-level residual as OBSER $\widehat{\operatorname{VATION}}{ }_{l j,-t}$ rather than $\widehat{\gamma_{J}}$ for ease of interpretation for readers.
practice and student outcomes on the three other dimensions. ${ }^{24}$ An important caveat here is that we only observed teachers' instruction during math lessons and, thus, may not capture important pedagogical practices teachers used with these students when teaching other subjects. Including dimensions from the CLASS instrument, which are meant to capture instructional quality across subject areas (Pianta \& Hamre, 2009), helps account for some of this concern. However, given that we were not able to isolate one dimension of teaching quality from all others, we consider this approach as providing suggestive rather than conclusive evidence on the underlying causal relationship between teaching practice and students' attitudes and behaviors.

### 4.3. Estimating the Relationship Between Teacher Effects Across Multiple Student

## Outcomes

In our third and final set of analyses, we examined whether teachers who are effective at raising math test scores are equally effective at developing students' attitudes and behaviors. To do so, we drew on equation (1) to estimate $\hat{\mu}_{j}$ for each outcome and teacher $j$. These estimates capture the residual variation in each outcome attributable to each teacher, or their "value-added" score. Then, we generated a correlation matrix of these teacher effect estimates. For consistency, we continued to specify this parameter as a random effect rather than fixed effects.

[^18]Despite attempts to increase the precision of these estimates through empirical Bayes estimation, estimates of individual teacher effects are measured with error that will attenuate these correlations (Spearman, 1904). Thus, if we were to find weak to moderate correlations between different measures of teacher effectiveness, this could identify multidimensionality or could result from measurement challenges, including the validity and reliability of individual constructs (Chin \& Goldhaber, 2015). For example, prior research suggests that different tests of students' academic performance can lead to differences in teacher rankings, even when those tests measure similar underlying constructs (Lockwood et al., 2007; Papay, 2011). To address this concern, we focus our discussion on relative rankings in correlations between teacher effect estimates rather than their absolute magnitudes. Specifically, we examine how correlations between teacher effects on two closely related student outcomes (e.g., two math achievement tests) compare with correlations between teacher effects on outcomes that aim to capture different underlying constructs. In light of research highlighted above, we did not expect the correlation between teacher effects on high- and low-stakes math tests to be 1 (or, for that matter, close to 1). However, we hypothesized that these relationships should be stronger than the relationship between teacher effects on students' math performance and effects on their attitudes and behaviors. We also present disattenuated correlations in an online appendix to confirm that the conclusions we draw from these comparisons are not a product of differential measurement properties across outcomes.

## 5. Results

5.1. Do Teachers Impact Students' Attitudes and Behaviors?

We begin by presenting results of the magnitude of teacher effects in Table 4. Here, we observe sizable teacher effects on students' attitudes and behaviors that are similar to teacher effects on students' academic performance. Starting first with teacher effects on students' academic performance, we find that a one standard deviation difference in teacher effectiveness is equivalent to a 0.17 sd or 0.18 sd difference in students' math achievement. In other words, relative to an average teacher, teachers at the $84^{\text {th }}$ percentile of the distribution of effectiveness move the medium student up to roughly the $57^{\text {th }}$ percentile of math achievement. Notably, these findings are similar to those from other studies that also estimate within-school teacher effects in large administrative datasets (Hanushek \& Rivkin, 2010). This suggests that our use of school fixed effects with a more limited number of teachers observed within a given school does not appear to overly restrict our identifying variation. Estimated teacher effects on students' selfreported Self-Efficacy in Math and Behavior in Class are 0.14 sd and 0.15 sd, respectively. The largest teacher effects we observe are on students' Happiness in Class, of 0.31 sd. Given that we do not have multiple years of data to separate out class effects for this measure, we interpret this estimate as the upward bound of true teacher effects on Happiness in Class. Rescaling this estimate by the ratio of teacher effects with and without class effects for Self-Efficacy in Math $(0.14 / 0.19=0.74)$ produces an estimate of stable teacher effects on Happiness in Class of 0.23 sd, still larger than effects for other outcomes. ${ }^{25}$

### 5.2. Do Specific Teaching Practices Impact Students' Attitudes and Behaviors?

[^19]Next, we examine whether certain characteristics of teachers' instructional practice help explain the sizable teacher effects described above (see Table 5). We present unconditional estimates in Panel A, where the relationship between one dimension of teaching practice and student outcomes is estimated without controlling for the other three dimensions. Thus, cells contain estimates from separate regression models. In Panel B, we present conditional estimates, where all four dimensions of teaching quality are included in the same regression model. Here, columns contain estimates from separate regression models. In all models, we control for student and class characteristics, and school fixed effects. We present all estimates as standardized effect sizes, which allows us to make comparisons across models and outcome measures. Unconditional and conditional estimates generally are quite similar. Therefore, we focus our discussion on our preferred conditional estimates.

We find that students' attitudes and behaviors are predicted by both general and content-specific teaching practices in ways that generally align with theory. For example, teachers' Emotional Support is positively associated with the two closely related student constructs, Self-Efficacy in Math and Happiness in Class. Specifically, a one standard deviation increase in teachers' Emotional Support is associated with a 0.14 sd increase in students' Self-Efficacy in Math and a 0.37 sd increase in students' Happiness in Class. These finding makes sense given that Emotional Support captures teacher behaviors such as their sensitivity to students, regard for students' perspective, and the extent to which they create a positive climate in the classroom. We also find that Classroom Organization, which captures teachers' behavior management skills and productivity in delivering content, is positively related to students' reports of their own Behavior in

Class ( 0.08 sd ). This suggests that teachers who create an orderly classroom likely create a model for students' own ability to self-regulate. Despite this positive relationship, we find that Classroom Organization is negatively associated with Happiness in Class ( -0.23 sd), suggesting that classrooms that are overly focused on routines and management are negatively related to students' enjoyment in class. At the same time, this is one instance where our estimate is sensitive to whether or not other teaching characteristics are included in the model. When we estimate the relationship between teachers' Classroom Organization and students' Happiness in Class without controlling for the three other dimensions of teaching quality, this estimate is roughly 0 sd and is not statistically significant. Similarly, in our unconditional models, Ambitious Mathematics Instruction is positively related to students' Self-Efficacy in Math. However, this estimate is much smaller and no longer statistically significant once we control for other teaching practices, suggesting that other related teaching practices likely are responsible for higher outcomes. Finally, we find that the degree to which teachers commit Mathematical Errors is negatively related to students' Self-Efficacy in Math ( -0.09 sd ) and Happiness in Class ( -0.18 sd ). These findings illuminate how a teacher's ability to present mathematics with clarity and without serious mistakes is related to their students' perceptions that they can complete math tasks and their enjoyment in class. ${ }^{26}$

Comparatively, when predicting scores on both math tests, we only find one marginally significant relationship - between Mathematical Errors and the high-stakes math test (-0.02 sd). For two other dimensions of teaching quality, Emotional Support

[^20]and Ambitious Mathematics Instruction, estimates are signed in the way we would expect and with similar magnitudes, though they are not statistically significant. Given the consistency of estimates across the two math tests and our restricted sample size, it is possible that non-significant results are due to limited statistical power. ${ }^{27}$ At the same time, even if true relationships exist between these teaching practices and students' math test scores, they are likely weaker than those between teaching practices and students’ attitudes and behaviors. For example, we find that the $95 \%$ confidence intervals relating Classroom Emotional Support to Self-Efficacy in Math [0.068, 0.202] and Happiness in Class $[0.162,0.544]$ do not overlap with the $95 \%$ confidence intervals for any of the point estimates predicting math test scores. This suggests that, still, very little is known about how specific classroom teaching practices are related to student achievement in math.

### 5.3. Are Teachers Equally Effective at Raising Different Student Outcomes? <br> In Table 6, we present correlations between teacher effects on each of our student

 outcomes. The fact that teacher effects are measured with error makes it difficult to estimate the precise magnitude of these correlations. Instead, we describe relative differences in correlations, focusing on the extent to which teacher effects within outcome type - i.e., teacher effects on the two math achievement tests or effects on students' attitudes and behaviors - are similar or different from correlations between teacher effects across outcome type. We illustrate these differences in Figure 1, where[^21]Panel A presents scatter plots of these relationships between teacher effects within outcome type and Panel B does the same across outcome type. Recognizing that not all of our survey outcomes are meant to capture the same underlying construct, we also describe relative differences in correlations between teacher effects on these different measures. We also note that even an extremely conservative adjustment that scales correlations by the inverse of the square root reliabilities lead to a similar overall pattern of results (see Appendix Table 2 for reliabilities and Appendix Table 3 for disattenuated correlations). ${ }^{28}$

Examining the correlations of teacher effect estimates reveals that individual teachers vary considerably in their ability to impact different students outcomes. As hypothesized, we find the strongest correlations between teacher effects within outcome type. Similar to Corcoran, Jennings, and Beveridge (2012), we estimate a correlation of 0.64 between teacher effects on our high- and low-stakes math achievement tests. We

[^22]also observe a strong correlation of 0.49 between teacher effects on two of the student survey measures, students' Behavior in Class and Self-Efficacy in Math. Comparatively, the correlations between teacher effects across outcome type are much weaker. Examining the scatter plots in Figure 1, we observe much more dispersion around the best-fit line in Panel B than in Panel A. The strongest relationship we observe across outcome types is between teacher effects on the low-stakes math test and effects on SelfEfficacy in Math $(r=0.19)$. The lower bound of the $95 \%$ confidence interval around the correlation between teacher effects on the two achievement measures [0.56, 0.72 ] does not overlap with the $95 \%$ confidence interval of the correlation between teacher effects on the low-stakes math test and effects on Self-Efficacy in Math $[-0.01,0.39]$, indicating that these two correlations are substantively and statistically significantly different from each other. Using this same approach, we also can distinguish the correlation describing the relationship between teacher effects on the two math tests from all other correlations relating teacher effects on test scores to effects on students' attitudes and behaviors. We caution against placing too much emphasis on the negative correlations between teacher effects on test scores and effects on Happiness in Class ( $r=-0.09$ and -0.21 for the highand low-stakes tests, respectively). Given limited precision of this relationship, we cannot reject the null hypothesis of no relationship or rule out weak, positive or negative correlations among these measures.

Although it would be useful to make comparisons between teacher effects on different measures of students' attitudes and behaviors, error in these estimates makes us less confident in our ability to do so. At face value, we find correlations between teacher effects on Happiness in Class and effects on the two other survey measures ( $r=0.26$ for

Self-Efficacy in Math and 0.21 for Behavior in Class) that are weaker than the correlation between teacher effects on Self-Efficacy in Math and effects on Behavior in Class described above $(r=0.49)$. One possible interpretation of these findings is that teachers who improve students' Happiness in Class are not equally effective at raising other attitudes and behaviors. For example, teachers might make students happy in class in unconstructive ways that do not also benefit their self-efficacy or behavior. At the same time, these correlations between teacher effects on Happiness in Class and the other two survey measures have large confidence intervals, likely due to imprecision in our estimate of teacher effects on Happiness in Class. Thus, we are not able to distinguish either correlation from the correlation between teacher effects on Behavior in Class and effects on Self-Efficacy in Math.

## 6. Discussion and Conclusion

The teacher effectiveness literature has profoundly shaped education policy over the last decade and has served as the catalyst for sweeping reforms around teacher recruitment, evaluation, development, and retention. However, by and large, this literature has focused on teachers' contribution to students' test scores. Even research studies such as the MET project and new teacher evaluation systems that focus on "multiple measures" of teacher effectiveness (Center on Great Teachers and Leaders, 2013; Kane et al., 2013) generally attempt to validate other measures, such as observations of teaching practice, by examining their relationship to students' academic performance.

Our study extends an emerging body of research examining the effect of teachers on student outcomes beyond test scores. In many ways, our findings align with
conclusions drawn from previous studies that also identify teacher effects on students' attitudes and behaviors (Jennings \& DiPrete, 2010; Kraft \& Grace, 2016; Ruzek et al., 2014), as well as weak relationships between different measures of teacher effectiveness (Gershenson, 2016; Jackson, 2012; Jennings \& DiPrete, 2010; Kane \& Staiger, 2012). Although our study focuses on a small to moderate sample of teachers, our rich dataset builds on prior work in several ways. To our knowledge, this study is the first to identify teacher effects on measures of students' self-efficacy in math and happiness in class, as well as on a self-reported measure of student behavior. By interpreting teacher effects alongside teaching effects, we also provide strong face and construct validity for our teacher effect estimates. Specifically, we find that improvements in upper-elementary students' attitudes and behaviors are predicted by general teaching practices in ways that align with hypotheses laid out by instrument developers (Pianta \& Hamre, 2009).

Findings linking errors in teachers' presentation of math content to students' self-efficacy in math, in addition to their math performance, also are consistent with theory (Bandura et al., 1996). Finally, the broad data collection effort from NCTE allows us to examine relative differences in relationships between measures of teacher effectiveness, thus avoiding some concerns about how best to interpret correlations that differ substantively across studies (Chin \& Goldhaber, 2015). Indeed, correlations between teacher effects on student outcomes that aim to capture different underlying constructs (e.g., math test scores and behavior in class) are weaker than correlations between teacher effects on two outcomes that are much more closely related (e.g., math achievement).

Our findings can help inform policy and practice in several key ways. Beginning first with policy, our evidence may generate interest among some policymakers to
incorporate teacher effect estimates on students' attitudes and behaviors into high-stakes personnel decisions. This may be particularly true after passage of the Every Student Succeeds Act (ESSA) in December of 2015, which mandates that states select one nonacademic indicator with which to assess students' success in school (ESSA, 2015). Our findings suggest that teachers can and do help develop attitudes and behaviors among their students that are important for success in life. Including measures of students' attitudes and behaviors in accountability or evaluation systems, even with very small associated weights, could serve as a strong signal that schools and educators should value and attend to developing these skills in the classroom. But, like other researchers (Duckworth \& Yeager, 2015), we caution against a rush to incorporate these measures into high-stakes decisions. Despite growing attention to these metrics, the science behind developing measures of students' attitudes and behaviors is relatively new compared to the long history of developing valid and reliable assessment of cognitive aptitude and content knowledge. Most existing measures, including those used in this study, were developed for research purposes rather than large-scale testing with repeated administrations. In particular, open questions remain about whether reference bias substantially distorts comparisons across schools and the susceptibility of these measures to "survey" coaching when high-stakes incentives are attached. Such incentives likely would render teacher assessments of their students' attitudes and behaviors inappropriate. Thus, there is a clear need for additional research on the reliability and validity of students' attitudes and behaviors, as well as the development of objective performance measures that can capture these outcomes.

In light of these concerns, we make three specific recommendations for the design and implementation of teacher performance evaluation. First, it is possible that measures of teachers' effectiveness at improving students' attitudes and behaviors may be suitable for low-stakes decision-making in schools. For example, these metrics could be used for early intervention efforts that diagnose areas of weakness and connect teachers to targeted professional development, which many argue should be the primary focus of teacher evaluation (Darling-Hammond, 2013; Hill \& Grossman, 2013; Papay, 2012). Second, an alternative approach to incorporating teacher effects on students' attitudes and behaviors into teacher evaluation may be through observations of teaching practice. Our findings suggest that specific domains captured on classroom observation instruments (i.e., Emotional Support and Classroom Organization from the CLASS and Mathematical Errors from the MQI) may serve as indirect proxy measures of improvements in students' attitudes and behaviors. One benefit of this approach is that districts commonly collect related measures as part of teacher evaluation systems (Center on Great Teachers and Leaders, 2013), and such measures are not restricted to teachers who work in tested grades and subjects. Third, performance evaluations - whether formative or summative - should avoid placing teachers into a single performance category whenever possible. Although many researchers and policymakers argue for creating a single weighted composite of different measures of teachers' effectiveness (Center on Great Teachers and Leaders, 2013; Kane et al., 2013), doing so likely oversimplifies the complex nature of teaching. For example, a teacher who excels at developing students' core math content knowledge but struggles to promote joy in learning or students' own self-efficacy in math is a very different teacher than one who is
middling across all three measures. Looking at these two teachers' composite scores would suggest they are similarly effective. A single overall evaluation score can facilitate a systematized process for making binary decisions such as whether to grant teachers tenure, but the decisions informed by teacher evaluations should reflect the complexity of classroom practice.

Next, we consider the implications of our findings for the teaching profession more broadly. While our findings lend empirical support to research on the multidimensional nature of teaching (Cohen, 2011; Lampert, 2001; Pianta \& Hamre, 2009), we also identify tensions inherent in this sort of complexity and potential tradeoffs between some teaching practices. In our primary analyses, we find that high-quality instruction around classroom organization is positively related to students' self-reported behavior in class but negatively related to their happiness in class. Our results here are not conclusive, as the negative relationship between classroom organization and students' happiness in class is sensitive to model specification. However, if there indeed is a causal relationship, further research will be critical to gain a better understanding of how teachers can develop classroom environments that engender both constructive classroom behavior and students' happiness in class. Our findings also demonstrate a need to integrate general and more content-specific perspectives on teaching, a historical challenge in both research and practice (Grossman \& McDonald, 2008; Hamre et al., 2013). We find that both math-specific and general teaching practices predict a range of student outcomes. Yet, particularly at the elementary level, teachers' math training often is overlooked. Prospective elementary teachers often gain licensure without taking college-level math classes; in many states, they do not need to pass the math sub-section
of their licensure exam in order to earn a passing grade overall (Epstein \& Miller, 2011). Striking the right balance between general and content-specific teaching practices is not a trivial task, but it likely is a necessary one.

Finally, we see opportunities to maximize students' exposure to the range of teaching skill we examine through strategic teacher assignments. Creating a teacher workforce skilled in all or most areas of teaching practice is, in our view, the ultimate goal. However, this goal likely will require substantial changes to teacher preparation programs and curriculum materials, as well as new policies around teacher recruitment, evaluation, and development. In middle and high schools, content-area specialization or departmentalization often is used to ensure that students have access to teachers with skills in distinct content areas. Some, including the National Association of Elementary School Principals, also see this as a viable strategy at the elementary level (Chan \& Jarman, 2004). Similar approaches may be taken to expose students to a collection of teachers who together can develop a range of academic skills, attitudes and behaviors. For example, when configuring grade-level teams, principals may pair a math teacher who excels in her ability to improve students' behavior with an ELA or reading teacher who excels in his ability to improve students' happiness and engagement. Viewing teachers as complements to each other may help maximize outcomes within existing resource constraints.

For decades, efforts to improve the quality of the teacher workforce have focused on teachers' abilities to raise students' academic achievement. Our work further illustrates the potential and importance of expanding this focus to include teachers'
abilities to promote students' attitudes and behaviors that are equally important for students' long-term success.

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## Figures

Panel A: Within Outcome Type


Panel B: Across Outcome Type


Figure 1. Scatter plots of teacher effects across outcomes. Solid lines represent the bestfit regression line.

## Tables

Table 1
Descriptive Statistics for Students' Attitudes, Behavior, and Academic Performance

|  | Univariate Statistics |  |  | Pairwise Correlations |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | SD | Internal Consistency Reliability | HighStakes Math Test | Low- <br> Stakes <br> Math Test | SelfEfficacy in Math | Happiness in Class | Behavior in Class |
| High-Stakes Math Test | 0.10 | 0.91 | -- | 1.00 |  |  |  |  |
| Low-Stakes Math Test | 0.61 | 1.1 | 0.82 | 0.70*** | 1.00 |  |  |  |
| Self-Efficacy in Math | 4.17 | 0.58 | 0.76 | 0.25*** | 0.22*** | 1.00 |  |  |
| Happiness in Class | 4.10 | 0.85 | 0.82 | 0.15*** | 0.10*** | 0.62*** | 1.00 |  |
| Behavior in Class | 4.10 | 0.93 | 0.74 | 0.24*** | 0.26 *** | 0.35*** | 0.27*** | 1.00 |

Notes: ${ }^{* * *} \mathrm{p}<.001$. For high-stakes math test, reliability varies by district; thus, we report the lower bound of these estimates. Behavior in Class, Self-Efficacy in Math, and Happiness in Class are measured on a 1 to 5 Likert Scale. Statistics were generated from all available data.

Table 2
Descriptive Statistics for CLASS and MQI Dimensions

|  | Univariate Statistics |  |  | Pairwise Correlations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | SD | Adjusted Intraclass Correlation | Emotional Support | Classroom Organization | Ambitious Mathematics Instruction | Mathematical Errors |
| Emotional Support | 4.28 | 0.48 | 0.53 | 1.00 |  |  |  |
| Classroom Organization | 6.41 | 0.39 | 0.63 | 0.46*** | 1.00 |  |  |
| Ambitious Mathematics Instruction | 1.27 | 0.11 | 0.74 | 0.22*** | 0.23*** | 1.00 |  |
| Mathematical Errors | 1.12 | 0.09 | 0.56 | 0.01 | 0.09 | $-0.27^{* * *}$ | 1.00 |

Notes: ${ }^{* * *}$ p<.001. Intraclass correlations were adjusted for the modal number of lessons. CLASS items (from Emotional Support and Classroom Organization) were scored on a scale from 1 to 7. MQI items (from Ambitious Instruction and Errors) were scored on a scale from 1 to 3. Statistics were generated from all available data.

Table 3
Participant Demographics

|  | Full Sample | Attitudes and <br> Behaviors <br> Sample | $P$-Value on <br> Difference |
| :--- | :---: | :---: | :---: |
| Teachers |  |  |  |
| Male | 0.16 | 0.16 | 0.949 |
| African-American | 0.22 | 0.22 | 0.972 |
| Asian | 0.03 | 0.00 | 0.087 |
| Hispanic | 0.03 | 0.03 | 0.904 |
| White | 0.65 | 0.66 | 0.829 |
| Mathematics Coursework (1 to 4 Likert scale) | 2.58 | 2.55 | 0.697 |
| Mathematical Content Knowledge (standardized scale) | 0.01 | 0.03 | 0.859 |
| Alternative Certification | 0.08 | 0.08 | 0.884 |
| Teaching Experience (years) | 10.29 | 10.61 | 0.677 |
| Value Added on High-Stakes Math Test (standardized scale) | 0.01 | 0.00 | 0.505 |
| Observations | 310 | 111 |  |
| Students |  |  |  |
| Male | 0.50 | 0.49 | 0.371 |
| African American | 0.40 | 0.40 | 0.421 |
| Asian | 0.08 | 0.07 | 0.640 |
| Hispanic | 0.23 | 0.20 | 0.003 |
| White | 0.24 | 0.28 | $<0.001$ |
| FRPL | 0.64 | 0.59 | 0.000 |
| SPED | 0.11 | 0.09 | 0.008 |
| LEP | 0.20 | 0.14 | $<0.001$ |
| Prior Score on High-Stakes Math Test (standardized scale) | 0.10 | 0.18 | $<0.001$ |
| Prior Score on High-Stakes ELA Test (standardized scale) | 0.09 | 0.20 | $<0.001$ |
| Observations | 10,575 | 1,529 |  |

Table 4
Teacher Effects on Students' Attitudes, Behavior, and Academic Performance

|  | Observations |  | SD of <br> Teacher- <br> Level |
| :--- | :---: | :---: | :---: |
| Variance |  |  |  |.

Notes: Cells contain estimates from separate multi-level regression models.
All non-zero effects are statistically significant at the 0.05 level.

Table 5
Teaching Effects on Students' Attitudes, Behavior, and Academic Performance

|  | High- <br> Stakes <br> Math Test | Low- <br> Stakes <br> Math Test | Behavior in <br> Class | Self- <br> Efficacy in <br> Math | Happiness <br> in Class |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Panel A: Unconditional Estimates |  |  |  |  |  |
| Emotional Support | 0.012 | 0.018 | 0.039 | $0.142^{* * *}$ | $0.279^{* * * *}$ |
|  | $(0.013)$ | $(0.014)$ | $(0.027)$ | $(0.031)$ | $(0.082)$ |
| Classroom Organization | -0.017 | -0.010 | $0.081^{*}$ | $0.065 \sim$ | 0.001 |
|  | $(0.014)$ | $(0.014)$ | $(0.033)$ | $(0.038)$ | $(0.090)$ |
| Ambitious Mathematics Instruction | 0.017 | 0.021 | 0.004 | $0.077^{*}$ | 0.082 |
|  | $(0.015)$ | $(0.015)$ | $(0.032)$ | $(0.036)$ | $(0.068)$ |
| Mathematical Errors | $-0.027^{*}$ | -0.009 | -0.027 | $-0.107^{* * *}$ | $-0.164^{*}$ |
|  | $(0.013)$ | $(0.014)$ | $(0.027)$ | $(0.030)$ | $(0.076)$ |
| Panel B: Conditional Estimates |  |  |  |  |  |
| Emotional Support | 0.015 | 0.020 | 0.030 | $0.135^{* * *}$ | $0.368^{* * *}$ |
| Classroom Organization | $(0.014)$ | $(0.015)$ | $(0.030)$ | $(0.034)$ | $(0.090)$ |
| Ambitious Mathematics Instruction | -0.022 | -0.018 | $0.077^{*}$ | -0.020 | $-0.227^{*}$ |
|  | $(0.014)$ | $(0.015)$ | $(0.036)$ | $(0.042)$ | $(0.096)$ |
| Mathematical Errors | 0.014 | 0.019 | -0.034 | -0.006 | 0.079 |
|  | $(0.015)$ | $(0.016)$ | $(0.036)$ | $(0.040)$ | $(0.068)$ |
| Teacher Observations | $-0.024 \sim$ | -0.005 | -0.009 | $-0.094^{* *}$ | $-0.181^{*}$ |
| Student Observations | $(0.013)$ | $(0.014)$ | $(0.029)$ | $(0.033)$ | $(0.081)$ |

Notes: $\sim \mathrm{p}<0.10,{ }^{*} \mathrm{p}<0.05,{ }^{* * *} \mathrm{p}<0.001$. In Panel A, cells contain estimates from separate regression models. In Panel B, columns contain estimates from separate regression models, where estimates are conditioned on other teaching practices. All models control for student and class characteristics, and include school fixed effects and teacher random effects. Models predicting all outcomes except for Happiness in Class also include class random effects.

Table 6
Correlations Between Teacher Effects on Students' Attitudes, Behavior, and Academic Performance

|  | High-Stakes <br> Math Test | Low-Stakes <br> Math Test | Self- <br> Efficacy in <br> Math | Happiness <br> in Class | Behavior in <br> Class |
| :--- | :---: | :---: | :---: | :---: | :---: |
| High-Stakes Math Test | 1.00 |  |  |  |  |
| Low-Stakes Math Test | $0.64^{* * *}$ | 1.00 |  |  |  |
| Self-Efficacy in Math | $(0.04)$ | -- |  |  |  |
|  | $0.16 \sim$ | $0.19^{*}$ | 1.00 |  |  |
| Happiness in Class | $(0.10)$ | $(0.10)$ | -- |  |  |
|  | -0.09 | -0.21 | $0.26 \sim$ | 1.00 |  |
| Behavior in Class | $(0.14)$ | $(0.14)$ | $(0.14)$ | -- |  |
|  | 0.10 | 0.12 | $0.49^{* * *}$ | $0.21 \sim$ | 1.00 |
|  | $(0.10)$ | $(0.10)$ | $(0.08)$ | $(0.14)$ | -- |

Notes: $\sim \mathrm{p}<0.10, * \mathrm{p}<0.05, * * * \mathrm{p}<0.001$. Standard errors in parentheses. See Table 4 for sample sizes used to calculate teacher effect estimates. The sample for each correlation is the minimum number of teachers between the two measures.
Appendices
Appendix Table 1
Factor Loadings for Items from the Student Survey

|  | Year 1 |  | Year 2 |  | Year 3 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Factor 1 | Factor 2 | Factor 1 | Factor 2 | Factor 1 | Factor 2 |
| Eigenvalue | 2.13 | 0.78 | 4.84 | 1.33 | 5.44 | 1.26 |
| Proportion of Variance Explained | 0.92 | 0.34 | 0.79 | 0.22 | 0.82 | 0.19 |
| Behavior in Class |  |  |  |  |  |  |
| My behavior in this class is good. | 0.60 | -0.18 | 0.47 | -0.42 | 0.48 | -0.37 |
| My behavior in this class sometimes annoys the teacher. | -0.58 | 0.40 | -0.35 | 0.59 | -0.37 | 0.61 |
| My behavior is a problem for the teacher in this class. | -0.59 | 0.39 | -0.38 | 0.60 | -0.36 | 0.57 |
| Self-Efficacy in Math |  |  |  |  |  |  |
| I have pushed myself hard to completely understand math in this class | 0.32 | 0.18 | 0.43 | 0.00 | 0.44 | -0.03 |
| If I need help with math, I make sure that someone gives me the help I need. | 0.34 | 0.25 | 0.42 | 0.09 | 0.49 | 0.01 |
| If a math problem is hard to solve, I often give up before I solve it. | -0.46 | 0.01 | -0.38 | 0.28 | -0.42 | 0.25 |
| Doing homework problems helps me get better at doing math. | 0.30 | 0.31 | 0.54 | 0.24 | 0.52 | 0.18 |
| In this class, math is too hard. | -0.39 | -0.03 | -0.38 | 0.22 | -0.42 | 0.16 |
| Even when math is hard, I know I can learn it. | 0.47 | 0.35 | 0.56 | 0.05 | 0.64 | 0.02 |
| I can do almost all the math in this class if I don't give up. | 0.45 | 0.35 | 0.51 | 0.05 | 0.60 | 0.05 |
| I'm certain I can master the math skills taught in this class. |  |  | 0.53 | 0.01 | 0.56 | 0.03 |
| When doing work for this math class, focus on learning not time work takes. |  |  | 0.58 | 0.09 | 0.62 | 0.06 |
| I have been able to figure out the most difficult work in this math class. |  |  | 0.51 | 0.10 | 0.57 | 0.04 |
| Happiness in Class |  |  |  |  |  |  |
| This math class is a happy place for me to be. |  |  | 0.67 | 0.18 | 0.68 | 0.20 |
| Being in this math class makes me feel sad or angry. |  |  | -0.50 | 0.15 | -0.54 | 0.16 |
| The things we have done in math this year are interesting. |  |  | 0.56 | 0.24 | 0.57 | 0.27 |
| Because of this teacher, I am learning to love math. |  |  | 0.67 | 0.26 | 0.67 | 0.28 |
| I enjoy math class this year. |  |  | 0.71 | 0.21 | 0.75 | 0.26 |

Notes: Estimates drawn from all available data. Loadings of roughly 0.4 or higher are highlighted to identify patterns.

## Appendix Table 2

Signal-to-Noise Ratio of Teacher Effect Estimates

|  | Original <br> Sample | Common <br> Sample |
| :--- | :---: | :---: |
| High-Stakes Math Test | 0.67 | 0.54 |
| Low-Stakes Math Test | 0.64 | 0.50 |
| Self-Efficacy | 0.53 | 0.50 |
| Happiness in Class | 0.56 | 0.56 |
| Behavior in Class | 0.55 | 0.52 |

Notes: See Table 4 for sample sizes across outcomes in the original samples. The common sample includes 51 teachers and 548 students.
\(\left.$$
\begin{array}{l}\begin{array}{l}\text { Appendix Table 3 } \\
\text { Disattenuated Correlations Between Teacher Effects on Students' Attitudes, Behavior, and } \\
\text { Academic Performance }\end{array} \\
\hline\end{array}
$$ $$
\begin{array}{ccccc}\text { High- } \\
\text { Stakes } \\
\text { Math Test }\end{array}
$$ \quad $$
\begin{array}{ccccc}\text { Low- } \\
\text { Stakes } \\
\text { Math Test }\end{array}
$$ \quad $$
\begin{array}{c}\text { Self- } \\
\text { Efficacy in } \\
\text { Math }\end{array}
$$ \quad $$
\begin{array}{c}\text { Happiness } \\
\text { in Class }\end{array}
$$ \quad \begin{array}{c}Behavior in <br>

Class\end{array}\right]\)|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| High-Stakes Math Test | 1.00 |  |  |  |
| Low-Stakes Math Test | 0.98 | 1.00 |  |  |
| Self-Efficacy in Math | 0.27 | 0.33 | 1.00 |  |
| Happiness in Class | -0.15 | -0.35 | 0.48 | 1.00 |
| Behavior in Class | 0.17 | 0.20 | 0.91 | 0.38 |

## Paper 3

# Validating Teacher Effects on Students' Attitudes and Behaviors through Random 

## Assignment


#### Abstract

There is growing interest among researchers, policymakers, and practitioners in identifying teachers who are skilled at improving student outcomes beyond test scores. However, it is not clear whether the key identifying assumption underlying the estimation of teacher effects - that estimates are not biased by non-random sorting of students to teachers - holds when test scores are replaced with other student outcomes. Leveraging the random assignment of teachers to students, I find that teachers have causal effects on their students' self-reported behavior in class, self-efficacy in math, and happiness in class that are similar in magnitude to effects on test scores. At the same time, value-added approaches to estimating these teacher effects often are insufficient to account for bias. One exception is teacher effects on students' behavior in class, where predicted differences come close to actual differences following random assignment. Therefore, it likely will be necessary to continue to rely on random assignment in order to identify teachers who are effective at improving students' attitudes and behaviors, as well as to find ways to help teachers improve in these areas.


## 1. Introduction

Decades worth of research on education production have narrowed in on the importance of teachers to student outcomes (Hanushek \& Rivkin, 2010; Murnane \& Phillips, 1981; Todd \& Wolpin, 2003). Over the last several years, these studies have coalesced around two key findings. First, teachers vary considerably in their ability to improve students' academic performance (Hanushek \& Rivkin, 2010; Nye, Konstantopoulos, \& Hedges, 2004), which in turn influences a variety of long-term outcomes including teenage pregnancy rates, college attendance, and earnings in adulthood (Chetty, Friedman, \& Rockoff, 2014b). Second, experimental and quasiexperimental studies indicate that "value-added" approaches to estimating teachers' contribution to student test scores are valid ways to identify effective teachers (BacherHicks, Chin, Kane, \& Staiger, 2015; Chetty, Friedman, \& Rockoff, 2014a; Glazerman \& Pratik, 2015; Kane, McCaffrey, Miller, \& Staiger, 2013; Kane \& Staiger, 2008). In other words, these teacher effect estimates are not confounded with the non-random sorting of teachers to students, the specific set of students in the classroom, or factors beyond teachers' control. Policymakers have taken notice of these important findings, leading to widespread changes in teacher evaluation (Dee \& Wyckoff, 2015), compensation (Podgursky \& Springer, 2011), and promotion (Loeb, Miller, \& Wyckoff, 2015).

While the studies described above have focused predominantly on teachers' contribution to students' academic performance, the research community is starting to have evidence that teachers also impact a variety of other student outcomes in ways that are only weakly related to their effects on test scores (Blazar \& Kraft, 2015; Gershenson, 2016; Jackson, 2012; Jennings \& DiPrete, 2010; Kraft \& Grace, 2016). For example, in
earlier work drawing on the same dataset used in this paper, Blazar and Kraft (2015) found that teacher effects on students' self-reported behavior in class, self-efficacy in math, and happiness in class were similar in magnitude to effects on math test scores. However, teachers who were effective at improving test scores often were not equally effective at improving students' attitudes and behaviors, with correlations between measures no higher than 0.19. Similarly, Jackson (2012) found that teacher effects on a composite measure of observed school behaviors, including suspensions, absences, grade point average, and on-time grade progression, explained five percent or less of the variation in teacher effects on students' academic performance. Together, these findings lend empirical evidence to the multidimensional nature of teaching and, thus, the need for policymakers and researchers to account for this sort of complexity.

Given that the research base examining teachers' contributions to student outcomes beyond test scores is relatively new, important questions remain about the validity of these measures. In particular, it is not clear whether the key identifying assumption underlying the estimation of teacher effects - that estimates are not biased by non-random sorting of students to teachers - holds when test scores are replaced with other student outcomes. Researchers who estimate value-added to students' test scores typically control for prior achievement because it captures many of the pre-determined factors that also affect current achievement, including the schools they attend, the neighborhoods they live in, and the family members with whom they interact (Chetty et al., 2014a; Kane et al., 2013). However, it is quite possible that there are additional factors not captured by prior test scores that influence students' attitudes or behaviors, which, in turn, could bias teacher effects on these outcomes.

In this paper, I examine this concern by drawing on a unique dataset from the National Center for Teacher Effectiveness in which participating students completed a survey that asked about a range of attitudes and behaviors in class. In the third year of the study, a subset of participating teachers were randomly assigned to class rosters within schools. Together, these data allow me to examine the extent to which teachers vary in their contribution to students' attitudes and behaviors, even after random assignment; the sensitivity of teacher effects on students' attitudes and behaviors to different model specifications, including those that control for students' prior academic performance versus prior attitudes and behaviors; and, ultimately, whether non-experimental estimates of teacher effects on these attitudes and behaviors predict these same outcomes following random assignment, which produces a measure of forecast bias.

Findings indicate that teachers have causal effects on their students' self-reported behavior in class, self-efficacy in math, and happiness in class. The magnitude of the teacher-level variation on these outcomes is similar to that on test scores. However, value-added approaches to estimating these teacher effects are insufficient to account for bias in many cases. One exception is teacher effects on students' behavior in class, where predicted differences come close to actual differences following random assignment. Interestingly, teacher effects are not particularly sensitive to models that control from students' prior achievement, student demographic characteristics, or prior survey responses. Given that these are the tools and data typically available to the econometrician, it likely will be necessary to continue to rely on random assignment in order to identify teachers who are effective at improving students' attitudes and behaviors, as well as to find ways to help teachers improve in these areas.

Several caveats about the sample and data should guide readers' interpretation of these findings. First and foremost, student surveys where administered under low-stakes conditions where individual student responses were not visible either to the teacher or to other students in the classroom. Thus, it is possible that estimates of bias might differ under high-stakes settings where survey responses could be coached or influenced by other pressures. Second, the fact that teachers were randomly assigned to class rosters within schools means that these findings cannot inform between-school comparisons. Finally, in light of a small sample of teachers in the experimental portion of the study ( N $=41$ ), additional studies are necessary to estimate magnitudes of bias more precisely. As the first random assignment study to focus specifically on teacher effects on students' attitudes and behaviors, though, these findings can serve as a benchmark for future work and contribute to the evidence base validating measures of teacher effectiveness.

## 2. Background

### 2.1. The Importance of Schools and Teachers in Improving Student Outcomes Beyond

 Test ScoresA growing body of research highlights the importance of student outcomes beyond test scores to short- and long-term success, including earnings, health, and community engagement (Chetty et al., 2011; Duckworth, Quinn, \& Tsukayama, 2013; Lindqvist \& Vestman, 2011; Moffit et. al., 2011; Mueller \& Plug, 2006; Murayama et al., 2012). In turn, this work has led to investigations of the specific factors that improve these outcomes, many of which have focused on schools and teachers. For example, in some of the earliest work on this topic, Heckman, Stixrud, and Urzua (2006) analyzed
longitudinal data from the National Longitudinal Survey of Youth 1979 and found relationships between additional years of high school and students' locus of control and self-esteem. Re-analyzing data from the HighScope Perry preschool experiment, Heckman, Pinto, and Savelyev (2013) demonstrated how externalizing behavior and academic motivation drove large increases in employment and earnings, as well as reductions in criminal behavior for students randomly assigned to attend the preschool. In a related re-analysis of the Tennessee STAR experiment, in which kindergarten students were randomly assigned to small or large classes, Chetty et al. (2011) found that effort, initiative, and disruptive behavior mediated the relationship between kindergarten class quality and college attendance and adult earnings.

Several recent studies have borrowed from the literature on teachers' "valueadded" to student test scores (e.g., Hanushek \& Rivkin, 2010; Nye et al., 2004; Sanders, Wright, \& Horn, 1997) in order to document the magnitude of teacher effects on a range of other outcomes. Without experimental designs, these studies have attempted to isolate the unique effect of teachers on these outcomes and to limit bias due to non-random sorting of students to teachers. To do so, they primarily control for prior measures of students' academic performance and basic demographic characteristics (e.g., gender, race, socioeconomic status). In a few instances (Blazar \& Kraft, 2015; Backes \& Hansen, 2015; Gershenson, 2016), studies also controlled for prior measures of the outcome variable when these measures were available at more than one point in time. Findings suggest substantive teacher effects on students' motivation, self-control, and interpersonal skills (Blazar \& Kraft, 2015; Jennings \& DiPrete, 2010; Ruzek et al., 2014), as well as on a range of observed school behaviors, including absences, suspensions,
grades, grade progression, and graduation, that are thought be proxies for students' underlying social and emotional development (Backes \& Hansen, 2015; Gershenson, 2016; Jackson, 2012; Koedel, 2008; Ladd \& Sorenson, 2015). Drawing on the same data as in this paper, Blazar and Kraft (2015) also found intuitive relationships between teachers' classroom practices and closely related student outcomes - e.g., between the climate teachers created in the classroom and students' self-efficacy in math and happiness in class - thus providing strong face validity to these teacher effect estimates.

In the one experimental study of this kind, where teachers were randomly assigned to class rosters within schools as part of the Measures of Effective Teaching (MET) project, Kraft and Grace (2016) found teacher effects on students' grit, growth mindset, and effort in class similar in magnitude to teacher effects from non-experimental studies. Specifically, they found that teachers identified as 1 standard deviation (sd) above the mean in the distribution of effectiveness improved these outcomes by roughly 0.10 sd to 0.17 sd. However, there was considerable attrition of students who moved out of their randomly assigned teachers' classroom, thus limiting the conclusions of this study. Further, given that measures of students' grit, growth mindset, and effort in class were collected in only one year, this study was not able to relate teacher effects calculated under experimental conditions to effects calculated under non-experimental ones. Below, I describe why this sort of validity evidence is crucial to inform use of these metrics.

### 2.2. Validating Teacher Effects on Student Outcomes

Over the last decade, several experimental and quasi-experimental studies have tested the validity of non-experimental methods for estimating teacher effects on student
achievement. In the first of these, Kane and Staiger (2008) described the rationale and set up for such a study: "Non-experimental estimates of teacher effects attempt to answer a very specific question: If a given classroom of students were to have teacher A rather than teacher B , how much different would their average test scores be at the end of the year?" (p.1). However, as these sorts of teacher effects estimates are derived from conditions where non-random sorting is the norm (Clotfelter, Ladd, \& Vigdor, 2006; Rothstein, 2010), these models assume that statistical controls (e.g., students' prior achievement, demographic characteristics) are sufficient to isolate the talents and skills of individual teachers rather than "principals' preferential treatment of their favorite colleagues, ability-tracking based on information not captured by prior test scores, or the advocacy of engaged parents for specific teachers" (Kane \& Staiger, 2008, p. 1). ${ }^{29}$

Random assignment of teachers to classes offers a way to test this assumption. If non-experimental teacher effects are causal estimates that capture true differences in quality between teachers, then these non-experimental or predicted differences should be equal, on average, to actual differences following the random assignment of teachers to classes. In other words, a 1 sd increase in predicted differences in achievement across classrooms should result in a 1 sd increase in observed differences, on average. Estimates greater than 0 sd would indicate that non-experimental teacher effects contain some information content about teachers' underlying talents and skills. However, deviations from the 1:1 relationship would signal that these scores also are influenced by factors beyond teachers' control, including students' background and skill, the composition of

[^23]students in the classroom, or strategic assignment policies. These deviations often are referred to as "forecast bias."

Results from Kane and Staiger (2008) and other experimental (Bacher-Hicks et al., 2015; Glazerman \& Pratik, 2015; Kane et al., 2013) studies have accumulated to provide strong evidence against bias in teacher effects on students' test scores. In a meta-analysis of the three experimental studies with the same research design, where teachers were randomly assigned to class rosters within schools, ${ }^{30}$ Bacher-Hicks et al. (2015) found a pooled estimate of 0.95 sd relating predicted teacher effects on students' math achievement to actual differences in this same outcome. In all cases, predicted teacher effects were calculated from models that controlled for students' prior achievement. Given the nature of their meta-analytic approach, the standard error around this estimate (0.09) was much smaller than in each individual study and the corresponding $95 \%$ confidence interval included 1 sd, thus indicting very little bias. This result was quite similar to findings from three quasi-experimental studies in much larger administrative datasets, which leveraged plausibly exogenous variation in teacher assignments due to staffing changes at the school-grade level (Bacher-Hicks et al., 2014; Chetty et al, 2014a; Rothstein, 2014).

Following a long line of inquiry around the sensitivity of value-added models to different model specifications and which may be most appropriate for policy (Aaronson,

[^24]Barrow, \& Sander, 2007; Blazar, Litke, \& Barmore, 2016; Goldhaber \& Theobald, 2012;
Hill, Kapitula, \& Umland, 2011; Newton, Darling-Hammond, Haertel, \& Thomas, 2010), many of these studies also examined the predictive validity of alternative methods for estimating teacher effects. For example, some have advocated for controlling for the composition of students in the classroom, which is thought to influence test scores beyond teachers themselves (Hanushek, Kain, Markman \& Rivkin, 2003; Kupermintz, 2003; Thum \& Bryk, 1997). Others have specified models that only compare teachers within schools in order to limit bias due to sorting of teachers and students across schools (Rivkin, Hanushek, \& Kain, 2005); however, this approach can lead to large differences in teacher rankings relative to models that compare teachers across schools (Goldhaber \& Theobald, 2012). The general conclusion across validation studies - both experimental and quasi-experimental - is that controlling for students' prior achievement is sufficient to account for the vast majority of bias in teacher effect estimates on achievement (Chetty et al., 2014a; Kane et al., 2013; Kane \& Staiger, 2008). In other words, non-experimental teacher effects on achievement that only control for students' prior achievement come closest to a 1:1 relationship when predicting current student outcomes.

To my knowledge, only one study has examined the validity of teacher effects on student outcomes beyond test scores. ${ }^{31}$ Drawing on the quasi-experimental design described by Chetty et al. (2014), Backes and Hansen (2015) examined the validity of teacher effects on a range of observed school behaviors captured in administrative records, including unexcused absences, suspensions, grade point average, percent of

[^25]classes failed, grade progression, and graduation from high school. Their study focused specifically on teachers certified through Teach for America in Miami-Dade County. Findings supported the validity of teacher effects on students' suspensions and percent of classes failed when looking across elementary, middle, and high schools, with estimates that could be distinguished from 0 sd and could not be distinguished from 1 sd. Teacher effects on unexcused absences, grade point average, and grade progression were valid at some grade levels but biased at others. Interestingly, for both unexcused absences and grade progression, predicted differences in student outcomes at the elementary level overstated actual differences (i.e., coefficient less than 1 sd ), likely due to sorting of "better" students (i.e., those with few unexcused absences and who progressed from one grade to the next on time) to "better" teachers in a way that could not be controlled for in the model; the opposite was true at the high school level, where predicted differences understated actual differences (i.e., coefficient greater than 1 sd ). This suggests that bias in teacher effects on outcomes beyond test scores may not be easily quantified or classified across contexts.

## 3. Data and Sample

As in Bacher-Hicks et al. (2015) and Blazar and Kraft (2015), this paper draws on data from the National Center for Teacher Effectiveness (NCTE), whose goal was to develop valid measures of effective teaching in mathematics. Over the course of three school years (2010-11 through 2012-13), the project collected data from participating fourth- and fifth-grade teachers $(\mathrm{N}=310)$ in four anonymous districts from three states on the East coast of the United States. Participants were generalists who taught all subject areas. This is important, as it provided an opportunity to estimate the contribution of
individual teachers to students' attitudes and behaviors that was not confounded with the effect of another teacher with whom a student engaged in the same year. Teacher-student links were verified for all study participants based on class rosters provided by teachers.

Measures of students' attitudes and behaviors came from a survey administered in the spring of each school year (see Table 1 for a full list of items and descriptive statistics generated from all available data). Based on theory and exploratory factor analyses (see Blazar, Braslow, Charalambous, \& Hill, 2015), I divided items into three constructs: Behavior in Class (internal consistency reliability ( $\alpha$ ) is 0.74 ), Self-Efficacy in Math ( $\alpha=$ $0.76)$, and Happiness in Class $(\alpha=0.82)$. Importantly, teacher reports of student behavior and self-reports of versions of the latter two constructs have been linked to labor market outcomes even controlling for cognitive ability (Chetty et al., 2011; Dee \& West, 2011; Lyubomirsky, King, \& Diener, 2005; Mueller \& Plug, 2006), lending strong consequential validity to these metrics. Blazar and Kraft (2015) describe additional validity evidence, including convergent validity, for these constructs. For each of these outcomes, I created final scales by averaging student responses across all available items and then standardizing to mean of zero and standard deviation of one. ${ }^{32}$ Standardization occurred within school year but across grades.

Student demographic and achievement data came from district administrative records. Demographic data included gender, race/ethnicity, free- or reduced-price lunch (FRPL) eligibility, limited English proficiency (LEP) status, and special education (SPED) status. These records also included current- and prior-year test scores in math and

[^26]English Language Arts (ELA) on state assessments, which were standardized within district by grade, subject, and year using the entire sample of students in each district, grade, subject, and year.

I focused on two subsamples from the larger group of 310 teachers. The primary analytic sample includes the subset of 41 teachers who were part of the random assignment portion of the NCTE study in the third year of data collection. I describe this sample and the experimental design in detail below. The second sample includes the set of teachers whose students took the project-administered survey in both the current and prior years. This allowed me to test the sensitivity of teacher effect estimates to different model specifications, including those that controlled for students' prior survey responses, from a balanced sample of teachers and students. As noted above, the student survey only was administered in the spring of each year; therefore, this sample consisted of the group of fifth-grade teachers who happened to have students who also were part of the NCTE study in the fourth grade $(\mathrm{N}=51) .{ }^{33}$

Generally, I found that average teacher characteristics, including their gender, race, math course taking, math knowledge, route to certification, years of teaching experience, and value-added scores calculated from state math tests, were similar across samples. ${ }^{34}$ Given that teachers self-selected into the NCTE study, I also tested whether

[^27]these samples differed from the full population of fourth- and fifth-grade teachers in each district with regard to value-added scores on the state math test. Although I found a marginally significant difference between the full NCTE sample and the district populations ( 0.02 sd in former and 0 sd in the latter; $p=.065$ ), I found no difference between the district populations and either the experimental or non-experimental subsamples used in this analysis ( $p=.890$ and .652 , respectively; not shown in Table 2). These similarities lend important external validity to findings presented below.

## 4. Experimental Design

In the spring of 2012, the NCTE project team worked with staff at participating schools to randomly assign sets of teachers to class rosters of the same grade level (i.e., fourth- or fifth-grade) that were constructed by principals or school leaders. To be eligible for randomization, teachers had to work in schools and grades in which there was at least one other participating teacher. In addition, their principal had to consider these teachers as capable of teaching any of the rosters of students designated for the group of teachers.

In order to fully leverage this experimental design, it was important to limit the most pertinent threat to internal validity: attrition caused by non-compliance amongst participating teachers and students (Murnane \& Willet, 2011). My general approach here was to focus on randomization blocks in which attrition and non-compliance was not a concern. As these blocks are analogous to individual experiments, dropping them should

[^28]not threaten the internal validity of my results. First, I restricted the sample to randomization blocks where teachers had both current-year student outcomes and prioryear teacher effect estimates. Of the original 79 teachers who agreed to participate and were randomly assigned to class rosters within schools, seven teachers dropped before the beginning of the 2012-13 school year for reasons unrelated to the experiment. ${ }^{35}$ One teacher left the district, one left teaching, one was on maternity leave for part of the year, and four moved teaching positions making them ineligible for random assignment (e.g., team teaching, moved to third grade, grade departmentalized). An additional 11 teachers only were part of the NCTE study in the third year and, therefore, did not have the necessary data from prior years to calculate non-experimental teacher effects on students' attitudes and behaviors. This is because student surveys only were collected through the NCTE project and were not available in pre-existing administrative data. I further dropped the seven teachers whose random assignment partner left from the study for either of the two reasons above. ${ }^{36}$

Next, I restricted the remaining sample to randomization blocks with low levels of non-compliance amongst participating students. Here, non-compliance refers to the fact that some students switched out of their randomly assigned teacher's classroom. Other studies that exploit random assignment between teachers and students, such as MET,

[^29]have accounted for non-compliance through instrumental variables estimation and calculation of treatment on the treated (Bacher-Hicks et al., 2015; Glazerman \& Protik, 2015; Kane et al., 2013). However, this approach was not possible in this study, given that students who transferred out of an NCTE teacher's classroom no longer had survey data to calculate teacher effects on these outcomes. Further, I would have needed to know the prior student survey results for these students' actual teachers, which I did not. In total, $28 \%$ of students moved out of their randomly assigned teachers' classroom (see Appendix Table 1 for information on reasons for and patterns of non-compliance). However, non-compliance was nested within a small subset of six randomization blocks. In these blocks, rates of non-compliance ranged from $40 \%$ to $82 \%$, due predominantly to principals and school leaders who made changes to the originally constructed class rosters. By eliminating these blocks, I am able to focus on a sample with a much lower rate of non-compliance ( $11 \%$ ) and where patterns of non-compliance are much more typical. The remaining 18 blocks had a total of 67 non-compliers and an average rate of non-compliance of 9\% per block; three randomization blocks had full compliance.

In Table 3, I confirm the success of the randomization process among the teachers in my final analytic sample $(\mathrm{N}=41)$ and the students on their randomly assigned rosters $(\mathrm{N}=598) .{ }^{37}$ In a traditional experiment, one can examine balance at baseline by calculating differences in average student characteristics between the treatment and control groups. In this context, though, treatment consisted of multiple possible teachers within a given randomization block. Thus, to examine balance, I instead examined the relationship between the assigned teacher's predicted effectiveness at improving students'

[^30]state math test scores in the 2012-13 school year and baseline student characteristics captured in 2011-12. ${ }^{38}$ Specifically, I regressed these teacher effect estimates on a vector of observable student characteristics and fixed effects for randomization blocks. As expected, observable student characteristics were not related to teacher effects on math test scores, either tested individually or as a group ( $p=.279$ ), supporting the fidelity of the randomization process. Even though this sample includes some non-compliers, these students looked similar to compliers on observable baseline characteristics, as well as the observed effectiveness of their randomly assigned teacher at improving state math test scores in years prior to random assignment (see Table 4). ${ }^{39}$ This latter comparison is particularly important, as it suggests that students were not more likely to leave their teachers' classroom if they were assigned to a low-quality one. If the opposite were true, this could lead to bias, as I would be left only with students who liked their randomly assigned teacher. As such, I am less concerned about having to drop the few noncompliers left in my sample from all subsequent analyses.

## 5. Empirical Strategy

For all analyses, I began with the following model of student production:

$$
\begin{gather*}
\text { OUTCOME }_{\text {idsgjt }}=\alpha f\left(A_{i t-1}\right)+\zeta O U T C O M E E_{i t-1}+\pi X_{i t}+\varphi \bar{X}_{i t}^{c}+\varphi \bar{X}_{i t}^{s}+  \tag{1}\\
\phi_{d g t}+
\end{gather*}
$$

[^31]
## $\varepsilon_{i d s g j t}$

OUTCOME $E_{\text {idsgjct }}$ was used interchangeably for each student survey construct - i.e., Behavior in Class, Self-Efficacy in Math, and Happiness in Class - for student $i$ in district $d$, school $s$, grade $g$ taught by teacher $j$ in year $t$. Throughout the paper, I test a variety of alternative value-added models that include different combinations of control variables. The full set of controls includes a cubic function of students' prior achievement, $A_{i t-1}$, in both math and ELA; a prior measure of the outcome variable, OUTCOME ${ }_{i t-1}$; student demographic characteristics, $X_{i t}$, including gender, race, free or reduced-price lunch eligibility, special education status, and limited English proficiency; these same test-score variables and demographic characteristics averaged to the class level, $\bar{X}_{i t}^{c}$, and school level, $\bar{X}_{i t}^{s}$; school fixed effects, $\sigma_{s}$, or school-by-grade fixed effect, $\sigma_{s g}$, which replace school characteristics in some models; and district-by-grade-by-year fixed effects, $\phi_{d g t}$, that account for scaling of prior-year test scores at this level.

To generate teacher effect estimates, $\hat{\tau}_{j t}^{S}$, from Equation (1), I took two approaches. Each has both strengths and limitations. First, I calculated teacher effects by averaging student-level residuals to the teacher level. I did so separately for each outcome measure, as well as with several different model specifications denoted by the superscript, $S$. This approach is intuitive, as it creates estimates of the contribution of teachers to student outcomes above and beyond factors already controlled for in the model. It also is computational simple. ${ }^{40}$ At the same time, measurement error in these estimates due to

[^32]sampling idiosyncrasies, adverse conditions for data collection, etc. will lead me to overstate the variance of true teacher effects; it also will attenuate the relationship between different measures of teacher effectiveness (e.g., measures at two points in time), even if they capture the same underlying construct. Therefore, I also calculated Empirical Bayes (EB) estimates that take into account measurement error and shrink teacher effects back toward the mean based on their precision. To do so, I included a teacher-level random effect in the model in order to generate model-based estimates. These models were fit using restricted maximum likelihood. While shrinking teacher effects is commonplace in both research and policy (Koedel, Mihaly, \& Rockoff, 2015), EB estimates are biased downward relative to the size of the measurement error (Jacob \& Lefgren, 2005).

I utilized these teacher effect estimates for three subsequent analyses. First, I estimated the variance of $\hat{\tau}_{j t}^{S}$ in order to examine whether teachers vary in their contributions to students' attitudes and behaviors. I compared the variance of teacher effects generated from the experimental sample, my preferred estimates, to those generated from the non-experimental sample. Given that the true variance of teacher effects are bounded between the unshrunken and shrunken estimates (Raudenbush \& Bryk, 2002), I present an average of the two (see Kraft \& Grace, 2016 for a similar approach).

Second, I examined the sensitivity of $\hat{\tau}_{j t}^{S}$ to different model specifications. Here, I focused on the non-experimental, balanced sample of teachers and samples with full data
on all possible background measures. Prior experimental and quasi-experimental research indicates that controlling for students' prior test scores accounts for the vast majority of bias in teacher effects on students' academic achievement (Chetty et al., 2014a; Kane et al., 2013; Kane \& Staiger, 2008). If bias in these teacher effects is due predominantly to sorting mechanisms, then this approach may also work to reduce bias in teacher effects on student outcomes beyond test scores. This is because sorting is an organizational process in schools that should operate in the same way no matter the outcome of interest. At the same time, there may be unobservable characteristics that are related to students' attitudes and behaviors but not to achievement outcomes. Therefore, I examined whether teacher effects were sensitive to additional controls often available in administrative datasets (e.g., student, class, and school characteristics), as well as students' prior survey responses. Some researchers also have raised concern about "reference bias" in students' self-reported survey responses (Duckworth \& Yeager, 2015; West et al., 2016). By reference bias I mean that school-wide norms around behavior or engagement likely create an implicit standard of comparison that students use when they judge their own behavior or engagement. Thus, I also examined models that estimated teacher effects using school fixed effects, which compare students and teachers only to others within the same school.

In my third and final set of analyses, I examined whether non-experimental teacher effect estimates calculated in years prior to 2012-13 predicted student outcomes following random assignment. The randomized design allowed for a straightforward analytic model:
(2) OUTCOME $_{i j s g 2012-13}=\delta \hat{\tau}_{j t<2012-13}^{S}+v_{s g}+\epsilon_{i j s g t}$

As above, OUTCOME $E_{i j s g 2012-13}$ was used interchangeably for each of my measures of students' attitudes and behaviors. I predicted these outcome measures in the random assignment year, 2012-13, with predicted, pre-experimental teacher effect estimates, $\hat{\tau}_{j t<2012-13}^{S} \cdot{ }^{41}$ That is, when Behavior in Class is the outcome of interest, $\hat{\tau}_{j t<2012-13}^{S}$, represents teachers' effectiveness at improving Behavior in Class in prior years; when Self-Efficacy in Math is the outcome of interest, $\hat{\tau}_{j t<2012-13}^{S}$, represents teachers' effectiveness at improving Self-Efficacy in Math in prior years. Following the research design, I included fixed effects for each randomization block, $v_{s g}$. In order to increase the precision of my estimates, I estimated non-experimental teacher effects using all available teacher-years outside of the experimental sample. For the same reason, in Equation (2), I also controlled for students' prior achievement, demographic characteristics, and class characteristics captured from the randomly assigned rosters. Standard errors were clustered at the class level to account for the nested structure of the data.

My parameter of interest is $\delta$, which describes the relationship between nonexperimental teacher effect estimates and current student outcomes. As in Kane and Staiger (2008), I examined whether these estimates had any predictive validity (i.e., whether they were statistically significantly different from 0 sd ) and whether they contained some degree of bias (i.e., whether they were statistically significantly different from 1 sd ).

## 6. Results

[^33]
### 6.1. Magnitude of Teacher Effects on Students' Attitudes and Behaviors

In Table 5, I present results describing the extent to which teachers vary in their contribution to students' attitudes and behaviors. Estimates represent the standard deviation of the teacher-level variance, averaged across the model-based EB estimates and the unshrunken estimates. For both the experimental and non-experimental samples, I vary the control set within certain constraints. All models control for students' prior achievement in math and ELA, which is standard practice when estimating teacher effects. All models drawing on the non-experimental sample further control for student characteristics, class characteristics, and either school or school-by-grade fixed effects to attempt to limit bias due to non-random sorting. Classroom-level controls in these models and some of the experimental sample models also aim to remove the contribution of peer effects from the teacher effect estimates. It was not possible to model classroom-level shocks directly, as data were not available over multiple school years. In the experimental sample, class characteristics describe the set of students included on the randomly assigned rosters rather than the students who ultimately stayed in that classroom. Finally, all models drawing on the experimental sample include school-by-grade fixed effects to match the randomized design.

Drawing on the preferred experimental sample, I find that indeed teachers have substantive impacts on students' Behavior in Class, Self-Efficacy in Math, and Happiness in Class. The largest of these effects is for Happiness in Class, where a 1 sd increase in teacher effectiveness leads to a roughly 0.30 sd increase in this self-reported outcome. To place this estimate in perspective, average within-school teacher effects on students’ academic performance are 0.15 sd in math and 0.11 sd in reading (Hanushek \& Rivik,
2010). In the experimental sample from this dataset, I find teacher effects on student test scores between 0.14 sd and 0.18 sd. The magnitude of teacher effects on students' Behavior in Class and Self-Efficacy in Math are much closer to these estimates, in the range of 0.12 sd to 0.17 sd. Unlike for Self-Efficacy in Math and Happiness in Class, results for Behavior in Class are somewhat sensitive to the set of controls included in the model, with the smallest estimate for the model that includes student and class characteristics. This is consistent with other literature suggesting that, if anything, controlling for observable class or peer characteristics produces a conservative estimate of the magnitude of teacher effects on student test scores (Kane et al., 2013; Thompson, Guarino, \&Wooldridge, 2015).

Compared to estimates from the experimental sample, those in the nonexperimental sample are similar in magnitude for Behavior in Class and Happiness in Class but smaller for Self-Efficacy in Math. These differences may be due to sampling idiosyncrasies. Or, it could be that non-experimental conditions understate the variance of true teacher effects on students'Self-Efficacy in Math. Notably, limiting variation to school-by-grade cells as opposed to schools or excluding prior-year survey responses does not appear to change results.

### 6.2. Sensitivity of Teacher Effects Across Model Specifications

In Tables 6 a and 6 b , I present results describing the relationship between teacher effects on students' attitudes and behaviors across model specifications. I only present correlations between EB teacher effect estimates, as patterns of results are almost identical when using the unshrunken estimates.

In the first of these tables, I examine the correlations between teacher effects that control for prior achievement (Model 1), for prior measures of the survey outcomes (Model 2), or both (Model 3). For all three outcome measures - Behavior in Class, SelfEfficacy in Math, and Happiness in Class - I find correlations of teacher effects across model specifications above 0.86 . As expected, the smallest of these correlations describe the relationship between teacher effects that control either for prior achievement (Model 1) or for students' prior survey responses (Model 2), of 0.90 for teacher effects on Behavior in Class, 0.86 for Self-Efficacy in Math, and 0.96 for Happiness in Class. However, these correlations still are quite strong. Correlations between teacher effects from models that have overlapping sets of controls (i.e., between Models 1 and 3 or between Models 2 and 3 ) are stronger, between 0.90 and 0.99 . This suggests that teacher effects on these student attitudes and behaviors are not particularly sensitive to inclusion of prior achievement or prior survey responses. In light of these findings, I exclude prior measures of students' attitudes and behaviors from all subsequent analyses, which allows me to retain the largest possible sample of teachers and students. As noted above, only a subset of students completed the survey in the prior year, while all students had prior test scores.

Next, I examine the sensitivity of teacher effects on students' attitudes and behaviors from this baseline model (Model 1) to models that control for additional student, class, and school characteristics (see Table 6b). Here, I find that teacher effects on these outcomes are not sensitive to student demographic characteristics but are sensitive to additional control variables. Correlations between teacher effect estimates from Model 1 (which controls for prior test scores) and from Model 4 (which builds on

Model 1 by adding student demographic characteristics) are between 0.98 and 0.99 . For Behavior in Class and Self-Efficacy in Math, correlations between estimates from Model 1 and from Model 5 (which builds on previous models by adding classroom characteristics) are substantively smaller, at 0.69 and 0.82 , respectively; for Happiness in Class, the correlation stays above 0.90 . Adding school characteristics to teacher effect specifications appears to have the largest impact on teacher rankings. Correlations between estimates from Model 1 and from Model 6 (which builds on previous models by adding school characteristics) range from 0.63 to 0.71 , while correlations between estimates from Model 1 and from Model 7 (which replaces school characteristics with school fixed effects) range from 0.41 to 0.66 . Correlations between estimates from Models 6 and 7 (not shown in Table 6) are 0.70, 0.71, and 0.92 for Behavior in Class, Self-Efficacy in Math, and Happiness in Class, respectively.

One explanation for these lower correlations in models that do and do not control for school fixed effects may be related to reference bias, which has been shown to influence measurement of students' survey responses across school settings (West et al., 2016). This may be particularly relevant for Behavior in Class, where management policies - and, thus, students' perception of what good or bad behavior looks like - often are set at the school level. At the same time, these correlations are well within the range reported in other studies looking at the sensitivity of teacher effects on test scores across models that control for school characteristics or school fixed effects, between roughly 0.5 and 0.9 (Aaronson et al., 2007; Goldhaber \& Theobald, 2012; Hill et al., 2011).

### 6.3. Predictive Validity of Non-Experimental Teacher Effects

In Table 7, I report estimates describing the relationship between nonexperimental teacher effects on students' attitudes and behaviors and these same outcomes following random assignment. Non-experimental estimates in Panel A are EB estimates, while those in Panel B are unshrunken estimates. Cells contain estimates from separate regression models of each attitude or behavior listed in each column on teacher effects on this same outcome modeled from five separate equations. As noted above, I exclude teacher effects calculated from Models 2 and 3, both of which controlled for prior measures of students' attitudes and behaviors. $P$-values testing the null hypothesis that effect sizes are equal to 1 sd are presented next to each estimate.

Comparison of estimates across Panel A and Panel B reveals two patterns. First, estimates relating non-experimental EB teacher effect estimates to current student outcomes are larger than estimates relating unshrunken estimates to current outcomes. This makes sense, as EB estimates are adjusted for the amount of measurement error the unshrunken estimates contain. Measurement error will attenuate the relationship between two teacher effect estimates, even if the true relationship is equal to 1 sd . At the same time, relationships between EB estimates and current student outcomes are measured less precisely than relationships drawing on unshrunken teacher effect estimates in Panel B. This also makes sense, as EB estimates provide a lower bound on the variation of true teacher effects, and decreased variation in the independent variable decreases statistical power. Thus, in interpreting the predictive validity of non-experimental teacher effects, I focus on trends across these two sets of results.

For Behavior in Class, I find that non-experimental teacher effect estimates have strong predictive validity. Examining the EB estimates, I find that teacher effects with the
best predictive validity come from Model 1 , which calculates non-experimental teacher effects only controlling for students' prior achievement. Here, I find an estimate of 1.06 sd that is close to the hypothesis described by Kane and Staiger (2008), that predicted differences across classroom should equal observed differences. At the same time, the standard error around this estimate is large (0.25) and, thus, does not allow me to rule out potentially large and important degrees of bias. In other models in Panel A, predicted differences in student outcomes understate actual differences (i.e. coefficient greater than 1 sd ), suggesting that students with lower self-reported behavior are sorted to higherquality teachers. Examining the unshrunken estimates, predicted differences all overstate actual differences (i.e., coefficient less than 1 sd ). This contradictory finding likely can be attributed to measurement error in the unshurnken estimates, which attenuate the relationship between prior- and current-year outcomes. Here, too, the relationships between non-experimental teacher effects and current student outcomes come close to 1 sd but still do not allow me to rule out bias completely.

For both Self-Efficacy in Math and Happiness in Class, non-experimental teacher effect estimates have moderate predictive validity. Generally, I can distinguish estimates from 0 sd , indicating that they contain some information content on teachers. The exception is EB estimates for Self-Efficacy in Math. Here, magnitudes fall in the range of 0.49 sd to 0.57 sd, which is similar to patterns of results drawing on the unshrunken estimates. However, standard errors are much larger, and in all cases the $90 \%$ confidence intervals cross 0 sd. For these two outcomes, in almost all cases I also can distinguish these estimates from 1 sd, indicating that they do contain some bias. For Happiness in

Class, the sample size is reduced by one teacher who did not have non-experimental teacher effects on this outcome.

## 7. Conclusion

Random assignment of teachers to students provides a unique opportunity to validate different measures of teacher effectiveness. In the Project STAR experiment from the 1970s, random assignment helped researchers confirm the substantive effect that teachers have on their students' academic performance (Nye et al., 2004). Over the last decade, researchers have leveraged data from subsequent experiments to validate the use of non-experimental methods for estimating teacher effects on students' test scores (Bacher-Hicks et al., 2015; Kane et al., 2013; Kane \& Staiger, 2008; Glazerman \& Protik, 2015). These studies have been consistent in their findings: controlling for students' prior achievement accounts for the vast majority of bias in teacher effects on students' current achievement. Thus, the evidence to date suggests that researchers and policymakers may no longer not need to rely on experiments and random assignment in order to identify teachers who are effective at raising test scores.

It is not clear that the same conclusion holds with regard to identifying teachers who are effective at improving students' attitudes and behaviors beyond test scores. In this study, I leverage random assignment of teachers to students in order to confirm the effect that teachers have on students' self-reported attitudes and behaviors. Indeed, teachers do vary in their contributions to students' Behavior in Class, Self-Efficacy in Math, and Happiness in Class. In fact, teacher effects on this latter outcome (roughly $0.30 \mathrm{sd})$ are almost twice as large as teacher effects on students' academic performance,
both in this and a number of other studies (Hanushek \& Rivkin, 2010). These results are consistent with findings from the other random assignment study examining the magnitude of teacher effects on students' growth mindset, grit, and effort in class (Kraft \& Grace, 2016). They also are consistent with a handful of non-experimental studies examining the magnitude of teacher effects on other attitudes and behaviors reported from surveys (Jennings \& DiPrete, 2010; Ruzek et al., 2014), as well as students’ observed school behaviors (Backes \& Hansen, 2015; Gershenson, 2016; Jackson, 2012; Koedel, 2008; Ladd \& Sorenson, 2015).

Unlike for teacher effects on students' academic performance, though, prior test scores (and other data easily available in administrative datasets) often are insufficient to account for bias due to the non-random sorting of students to teachers and the confounding effects of past experiences on current student outcomes. For all three attitudes and behaviors assessed in this study, non-experimental teacher effects predict the same outcomes following random assignment with estimates that can be distinguished from 0 sd. Thus, these non-experimental teacher effect estimates do contain important information content on teachers' true underlying ability. At the same time, I can confirm that many of these teacher effects also contain important degrees of bias. For SelfEfficacy in Math and Happiness in Class, in particular, predicted differences fall short of actual differences following random assignment. One exception here is teacher effects on students' Behavior in Class, where I find estimates relating non-experimental teacher effects to current student outcomes quite close to 1 sd. However, the confidence intervals around these estimates are sizeable. Thus, additional evidence from larger studies with greater statistical power is necessary before determining that teacher effects on students’

Behavior in Class contain no bias. In the only other study to assess the validity of teacher effects on student outcomes beyond test scores, Backes and Hansen (2015) also find variation in the degree of bias across measures. For example, non-experimental teacher effects on students' suspensions and percent of classes failed seem to contain little bias (with estimates of $0.92 \mathrm{sd}[\mathrm{se}=0.12$ ] and 0.94 [ $\mathrm{se}=0.08$ ], respectively), while teacher effects on GPA do contain bias (estimate of 1.23 sd [ $\mathrm{se}=0.07]$ ). The degree of bias also changes substantively across grade levels.

It is still possible that, with access to additional sets of controls, value-added approaches may be able to produce non-biased estimates of teacher effects on students’ attitudes and behaviors. Notably, though, the sorts of control variables that may be necessary to reduce bias even further likely are not easily accessible in administrative datasets. In this study, teacher effects on students' attitudes and behaviors were not particularly sensitive to inclusion of students' prior survey responses in addition to their prior achievement. Although I did not assess the degree of bias in teacher effects that controlled for both prior achievement and prior survey responses due to a small sample in the experimental portion of the study with both sets of measures, correlations across model specification in the non-experimental sample suggest that findings would not be any different. Backes and Hansen (2016) controlled for prior measures of their non-tested outcomes in all models and still found large degrees of bias in some instances. If prior measures of the outcome, in addition to prior achievement, are insufficient to eliminate bias, it is unclear what would be sufficient.

Where does this leave policy and research? As I (Blazar \& Kraft, 2015) and others (Duckworth \& Yeager, 2015; Kraft \& Grace, 2016; West et al., 2016) have argued
elsewhere, there are a number of reasons to be concerned about incorporating these sorts of measures into policy settings. The discussion of possible bias that others discuss in the abstract (Duckworth \& Yeager, 2015) and that I show empirically suggest that these measures are not currently appropriate for use in accountability systems, such as teacher evaluation, despite the fact that many states and districts already are moving in this direction. As of 2016, 36 states list student surveys or "non-cognitive" school behaviors as possible sources of data when evaluating their teacher workforces (Center of Great Teachers and Leaders, 2013). The Every Student Succeeds Act (ESSA) also mandates that states select a non-academic indicator with which to assess students' success in school (ESSA, 2015). Perhaps teacher effects on students' behavior in class is an exception. However, it is still important to remind readers that results from this study come from data collected under low-stakes conditions. It is quite possible that high-stakes environments may introduce additional sources of bias including cheating. Prior to using student surveys - or even more objective measures of students' attitudes and behaviors such as absences and suspensions - when evaluating teachers, school leaders will need assurance that use of these measures does not result in "corrupt[ion of] the social processes [they are] intended to monitor" (Campbell, 1977, p. 85), which many argue already has occurred with use of test scores (Fuller, Wright, Gesicki, \& Kang, 2007; Koretz, 2008).

Instead, the important task of identifying ways for teachers to improve students' attitudes and behaviors likely falls on researchers. In particular, we likely want to conduct more and learn as much as possible from random assignment studies.

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Tables
Table 1

|  | Univariate Statistics |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | SD | Cronbach's Alpha | Behavior in Class | SelfEfficacy in Math | Happiness |
| Behavior in Class | 4.10 | 0.93 | 0.74 | 1.00 |  |  |
| My behavior in this class is good. | 4.23 | 0.89 |  |  |  |  |
| My behavior in this class sometimes annoys the teacher. | 3.80 | 1.35 |  |  |  |  |
| My behavior is a problem for the teacher in this class. | 4.27 | 1.13 |  |  |  |  |
| Self-Efficacy in Math | $4.17$ | 0.58 | 0.76 | 0.35*** | 1.00 |  |
| I have pushed myself hard to completely understand math in this class. | 4.23 | 0.97 |  |  |  |  |
| If I need help with math, I make sure that someone gives me the help I need. | 4.12 | 0.97 |  |  |  |  |
| If a math problem is hard to solve, I often give up before I solve it. | 4.26 | 1.15 |  |  |  |  |
| Doing homework problems helps me get better at doing math. | 3.86 | 1.17 |  |  |  |  |
| In this class, math is too hard. | 4.05 | 1.10 |  |  |  |  |
| Even when math is hard, I know I can learn it. | 4.49 | 0.85 |  |  |  |  |
| I can do almost all the math in this class if I don't give up. | 4.35 | 0.95 |  |  |  |  |
| I'm certain I can master the math skills taught in this class. | 4.24 | 0.90 |  |  |  |  |
| When doing work for this math class, focus on learning not time work takes. | 4.11 | 0.99 |  |  |  |  |
| I have been able to figure out the most difficult work in this math class. | 3.95 | 1.09 |  |  |  |  |
| Happiness in Class | 4.10 | 0.85 | 0.82 | $0.27^{* * *}$ | 0.62*** | 1.00 |
| This math class is a happy place for me to be. | 3.98 | 1.13 |  |  |  |  |
| Being in this math class makes me feel sad or angry. | 4.38 | 1.11 |  |  |  |  |
| The things we have done in math this year are interesting. | 4.04 | 0.99 |  |  |  |  |
| Because of this teacher, I am learning to love math. | 4.02 | 1.19 |  |  |  |  |
| I enjoy math class this year. | 4.12 | 1.13 |  |  |  |  |

Table 2

|  | $\begin{gathered} \text { Full } \\ \text { NCTE } \\ \text { Sample } \end{gathered}$ | Experimental Sample |  | Non-ExperimentalSample |  | District Populations |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mean | $\begin{aligned} & P \text {-Value } \\ & \text { on } \\ & \text { Difference } \end{aligned}$ | Mean | $\begin{aligned} & P \text {-Value } \\ & \text { on } \\ & \text { Difference } \end{aligned}$ | Mean | $\begin{gathered} P \text {-Value } \\ \text { on } \\ \text { Difference } \end{gathered}$ |
| Male | 0.16 | 0.15 | 0.95 | 0.19 | 0.604 | -- | -- |
| African-American | 0.22 | 0.18 | 0.529 | 0.24 | 0.790 | -- | -- |
| Asian | 0.03 | 0.05 | 0.408 | 0.00 | 0.241 | -- | -- |
| Hispanic | 0.03 | 0.03 | 0.866 | 0.02 | 0.686 | -- | -- |
| White | 0.65 | 0.70 | 0.525 | 0.67 | 0.807 | -- | -- |
| Mathematics Coursework | 2.58 | 2.62 | 0.697 | 2.54 | 0.735 | -- | -- |
| Mathematical Content Knowledge | 0.01 | 0.05 | 0.816 | 0.07 | 0.671 | -- | -- |
| Alternative Certification | 0.08 | 0.08 | 0.923 | 0.12 | 0.362 | -- | -- |
| Teaching Experience | 11.04 | 14.35 | 0.005 | 11.44 | 0.704 | -- | -- |
| Value Added on State Math Test | 0.02 | 0.00 | 0.646 | 0.01 | 0.810 | 0.00 | 0.065 |
| $P$-value on Joint Test |  |  | 0.533 |  | 0.958 |  | NA |
| Teachers | 310 | 41 |  | 51 |  | 3,454 |  |

Table 3
Balance Between Randomly Assigned Teacher Effectiveness and Student Characteristics

|  | Teacher Effects on <br> State Math Scores <br> from Randomly <br> Assigned Teacher <br> $(2012-13)$ |
| :--- | :---: |
| Male | -0.005 |
|  | $(0.009)$ |
| African American | 0.028 |
|  | $(0.027)$ |
| Asian | 0.030 |
|  | $(0.029)$ |
| Hispanic | 0.043 |
|  | $(0.028)$ |
| White | 0.010 |
|  | $(0.028)$ |
| FRPL | 0.002 |
|  | $(0.011)$ |
| SPED | -0.023 |
|  | $(0.021)$ |
| LEP | 0.004 |
|  | $(0.014)$ |
| Prior Achievement on State Math Test | 0.009 |
|  | $(0.007)$ |
| Prior Achievement on State ELA Test | -0.001 |
|  | $(0.007)$ |
| $P$-Value on Joint Test | 0.316 |
| Students | 598 |
| Teachers | 41 |
| Notes: $\sim$ p $<10, * p<.05, * * \mathrm{p}<.01, * * * \mathrm{p}<.001$. Columns contain |  |
| estimates from separate regression models of teacher effect |  |
| estimates on student characteristics and fixed effects for |  |
| randomization block. Robust standard errors in parentheses. |  |

Table 4
Comparison of Student Compliers and Non-Compliers in Randomization Blocks with Low Levels of Non-Compliance

|  | Non- <br> Compliers | Compliers | $P$-Value on <br> Difference |
| :--- | :---: | :---: | :---: |
| Student Characteristics | 0.38 | 0.49 | 0.044 |
| Male | 0.38 | 0.33 | 0.374 |
| African American | 0.12 | 0.15 | 0.435 |
| Asian | 0.15 | 0.21 | 0.128 |
| Hispanic | 0.31 | 0.27 | 0.403 |
| White | 0.64 | 0.66 | 0.572 |
| FRPL | 0.06 | 0.05 | 0.875 |
| SPED | 0.11 | 0.21 | 0.016 |
| LEP | 0.30 | 0.26 | 0.689 |
| Prior Achievement on State Math Test | 0.28 | 0.30 | 0.782 |
| Prior Achievement on State ELA Test |  |  | 0.146 |
| $P$-Value on Joint Test |  |  |  |
| Teacher Characteristics | -0.01 | -0.01 | 0.828 |
| Prior Teacher Effects on State Math | 67 | 531 |  |
| Scores |  |  |  |
| Students |  |  |  |

Table 5

|  | Experimental Sample |  |  | Non-Experimental Sample |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) |
| Behavior in Class | 0.17 | 0.12 | 0.11 | 0.15 | 0.15 | 0.13 |
| Self-Efficacy in Math | 0.13 | 0.13 | 0.12 | 0.07 | 0.51 | 0.07 |
| Happiness in Class | 0.34 | 0.33 | 0.30 | 0.29 | 0.29 | 0.30 |
| Prior Achievement | X | X | X | X | X | X |
| Prior Survey Responses |  |  |  | X | X |  |
| Student Characteristics |  | X | X | X | X | X |
| Class Characteristics |  |  | X | X | X | X |
| School Fixed Effects |  |  |  | X |  |  |
| School-by-Grade Fixed Effects | X | X | X |  | X | X |
| Teachers | 41 | 41 | 41 | 51 | 51 | 51 |
| Students | 531 | 531 | 531 | 548 | 548 | 548 |

Table 6a
Pairwise Correlations Between Empirical Bayes Teacher Effects Across Model Specifications

|  | $\rho_{\text {Model 1,Model 2 }}$ | $\rho_{\text {Model } 1, \text { Model } 3}$ | $\rho_{\text {Model } 2, \text { Model } 3}$ |
| :--- | :---: | :---: | :---: |
| Teacher Effects on Behavior in Class | $0.90^{* * *}$ | $0.91^{* * *}$ | $1.00^{* * *}$ |
| Teacher Effects on Self-Efficacy in Math | $0.86^{* * *}$ | $0.90^{* * *}$ | $0.97^{* * *}$ |
| Teacher Effects on Happiness in Class | $0.96^{* * *}$ | $0.96^{* * *}$ | $0.99^{* * *}$ |

Notes: ~ $\mathrm{p}<.10,{ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<.01,{ }^{* * *} \mathrm{p}<.001$. Model 1 calculates teacher effectiveness ratings that only control for students' prior achievement in math and ELA. Model 2 only controls only for a prior measure of students' attitude or behavior. Model 3 controls for prior scores on both prior achievement and prior attitude or behavior. Samples includes 51 teachers.

Table 6b
Pairwise Correlations Between Empirical Bayes Teacher Effects from Model 1 and Other Model Specifications

|  | $\rho_{\text {Model 1,Model 4 }}$ | $\rho_{\text {Model 1,Model 5 }}$ | $\rho_{\text {Model 1,Model } 6}$ | $\rho_{\text {Model 1,Model 7 }}$ |
| :--- | :---: | :---: | :---: | :---: |
| Teacher Effects on Behavior in Class | $0.98^{* * *}$ | $0.69^{* * *}$ | $0.63^{* * *}$ | $0.41^{* * *}$ |
| Teacher Effects on Self-Efficacy in Math | $0.99^{* * *}$ | $0.82^{* * *}$ | $0.68^{* * *}$ | $0.42^{* * *}$ |
| Teacher Effects on Happiness in Class | $0.99^{* * *}$ | $0.90^{* * *}$ | $0.71^{* * *}$ | $0.66^{* * *}$ |

Notes: $\sim \mathrm{p}<.10,{ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<.01,{ }^{* * *} \mathrm{p}<.001$. Baseline model to which others are compared (Model 1) calculates teacher effectiveness ratings that only control for students' prior achievement in math and ELA. Model 4 adds student demographic characteristics, including gender, race, free or reduced-price lunch eligibility, special education status, and limited English proficiency status; Model 5 adds classroom characteristics; Model 6 adds school characteristics; Model 7 replaces school characteristics with school fixed effects. Samples includes 51 teachers.

Table 7

|  | Behavior in Class |  | Self-Efficacy in Math |  | Happiness in Class |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Estimate/SE | $P$-value on Difference from 1 sd | Estimate/SE | $P$-value on Difference from 1 sd | Estimate/SE | $P$-value on <br> Difference from 1 sd |
| Panel A: EB Estimates |  |  |  |  |  |  |
| Teacher Effects Calculated from Model 1 | $\begin{gathered} 1.055^{* * *} \\ (0.248) \end{gathered}$ | 0.826 | $\begin{gathered} 0.500 \\ (0.350) \end{gathered}$ | 0.160 | $\begin{aligned} & 0.430^{*} \\ & (0.185) \end{aligned}$ | 0.004 |
| Teacher Effects Calculated from Model 4 | $\begin{gathered} 1.148 * * * \\ (0.247) \end{gathered}$ | 0.552 | $\begin{gathered} 0.493 \\ (0.353) \end{gathered}$ | 0.158 | $\begin{aligned} & 0.441^{*} \\ & (0.182) \end{aligned}$ | 0.004 |
| Teacher Effects Calculated from Model 5 | $\begin{gathered} 1.292^{* * *} \\ (0.281) \end{gathered}$ | 0.304 | $\begin{gathered} 0.545 \\ (0.388) \end{gathered}$ | 0.248 | $\begin{aligned} & 0.413^{*} \\ & (0.174) \end{aligned}$ | 0.002 |
| Teacher Effects Calculated from Model 6 | $\begin{gathered} 1.551^{* * *} \\ (0.335) \end{gathered}$ | 0.108 | $\begin{gathered} 0.550 \\ (0.396) \end{gathered}$ | 0.263 | $\begin{aligned} & 0.491^{*} \\ & (0.182) \end{aligned}$ | 0.008 |
| Teacher Effects Calculated from Model 7 | $\begin{gathered} 1.877 * * * \\ (0.421) \end{gathered}$ | 0.044 | $\begin{gathered} 0.573 \\ (0.374) \end{gathered}$ | 0.260 | $\begin{aligned} & 0.524^{* *} \\ & (0.181) \end{aligned}$ | 0.012 |
| Panel B: Unshrunken Estimates |  |  |  |  |  |  |
| Teacher Effects Calculated from Model 1 | $\begin{gathered} 0.718^{* * *} \\ (0.153) \end{gathered}$ | 0.073 | $\begin{aligned} & 0.405 \sim \\ & (0.203) \end{aligned}$ | 0.006 | $\begin{aligned} & 0.353 * \\ & (0.148) \end{aligned}$ | $<0.001$ |
| Teacher Effects Calculated from Model 4 | $\begin{gathered} 0.739^{* * *} \\ (0.134) \end{gathered}$ | 0.058 | $\begin{aligned} & 0.401 ~ \\ & (0.206) \end{aligned}$ | 0.006 | $\begin{aligned} & 0.364^{*} \\ & (0.146) \end{aligned}$ | $<0.001$ |
| Teacher Effects Calculated from Model 5 | $\begin{gathered} 0.747^{* * *} \\ (0.130) \end{gathered}$ | 0.059 | $\begin{aligned} & 0.435 \sim \\ & (0.232) \end{aligned}$ | 0.020 | $\begin{aligned} & 0.347 * \\ & (0.139) \end{aligned}$ | $<0.001$ |
| Teacher Effects Calculated from Model 6 | $\begin{gathered} 0.777 * * * \\ (0.128) \end{gathered}$ | 0.089 | $\begin{aligned} & 0.450 \sim \\ & (0.235) \end{aligned}$ | 0.025 | $\begin{gathered} 0.403 * * \\ (0.143) \end{gathered}$ | $<0.001$ |
| Teacher Effects Calculated from Model 7 | $\begin{gathered} 0.804 * * * \\ (0.129) \\ \hline \end{gathered}$ | 0.137 | $\begin{aligned} & 0.438 \sim \\ & (0.223) \\ & \hline \end{aligned}$ | 0.016 | $\begin{gathered} 0.402 * * \\ (0.141) \\ \hline \end{gathered}$ | $<0.001$ |
| Teachers | 41 |  | 41 |  | 40 |  |
| Students | 531 |  | 531 |  | 509 |  |

Notes: $\sim \mathrm{p}<.10,{ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<.01,{ }^{* * *} \mathrm{p}<.001$. Cells include estimates from separate regression models that control for students' prior achievement in math and ELA, student demographic characteristics, classroom characteristics from randomly assigned rosters, and fixed effects for randomization block. Robust standard errors clustered at the class level in parentheses. Model 1 calculates teacher effectiveness ratings that only control for students' prior achievement in math and ELA; Model 4 adds student demographic characteristics; Model 5 adds classroom characteristics; Model 6 adds school characteristics; Model 7 replaces school characteristics with school fixed effects.

## Appendix

## Appendix Table 1

Summary of Random Assignment Student Compliance

|  | Number of <br> Students | Percent of <br> Total |
| :--- | :---: | :---: |
| Remained with randomly assigned teacher | 677 | 0.72 |
| Switched teacher within school | 168 | 0.18 |
| Left school | 40 | 0.04 |
| Left district | 49 | 0.05 |
| Not sure | 9 | 0.01 |
| Total | 943 | 1.00 |

## Conclusion

This study is among the first attempts to identify teacher and teaching effects using observations of instruction inside teachers' own classrooms. To my knowledge, it is the only study to date to use random assignment to estimate the predictive validity of teacher effects on students' attitudes and behaviors. Therefore, results from this work are likely to inform policy and practice in at least two ways.

First, exploring the impact of specific types of mathematics teaching on student outcomes may help policymakers and school leaders ways to get more teachers who engage in these effective teaching practices into classrooms. This may occur either through evaluation or development practices. That is, when observing classrooms, school leaders may look specifically for those elements of instruction shown to contribute to student outcomes - either academic or non-tested. Further, school leaders may use this information to link teachers to professional development opportunities aimed at improving their skill in a particular instructional domain.

Second, results showing substantive teacher effects on a range of student attitudes and behaviors, as well as weak correlations between teacher effects across outcome types, highlight the multidimensional nature of teaching. Thus, improvement efforts likely need to account for this complexity. However, in light of persistent concerns about how best to measure these outcomes and potential bias in teacher effect estimates on these outcomes, it likely is not appropriate to incorporate these specific survey items directly into teacher evaluation systems. Instead, evidence linking specific teaching practices to non-tested outcomes suggests that evaluations might place greater weight on these measures. Further, as above, these teaching practices may be a focus of development efforts.

Filling elementary classrooms with teachers who engage in effective mathematics teaching practices will take time. Doing so likely will entail a variety of efforts, including improvements in professional development offerings that engage teachers substantively around their own teaching practices and stronger efforts to hire teachers with deep knowledge of mathematics. Importantly, though, the education community is beginning to gain an understanding of the types of teaching that students are exposed to that raise outcomes.


[^0]:    ${ }^{1}$ Paper currently published at Economics of Education Review. Full citation: Blazar, D. (2015). Effective teaching in elementary mathematics: Identifying classroom practices that support student achievement. Economics of Education Review, 48, 16-29.

[^1]:    ${ }^{2}$ This project also includes a fourth district that I exclude here due to data and sample limitations. In the first year of the study, students did not take the baseline achievement test. In the second year, there were only three schools in which all teachers in the relevant grades participated in data collection, which is an important requirement of my identification strategy. At the same time, when I include these few observations in my analyses, patterns of results are the same.

[^2]:    ${ }^{3}$ Reliability estimates for the MQI from the MET study were lower. One reason for this may be that MET used the MQI Lite and not the full MQI instrument used in this study. The MQI Lite has raters provide only overarching dimension scores, while the full instrument asks raters to score teachers on up to five items before assessing an overall score. Another reason likely is related to differences in scoring designs. MET had raters score 30 minutes of instruction from each lesson. Comparatively, in this study, raters provided scores for the whole lesson, which is in line with recommendations made by Hill, Charalambous, and Kraft (2012) in a formal generalizability study. Finally, given MET's intent to validate observation instruments for the purpose of new teacher evaluation systems, they utilized a set of raters similar to the school leaders and staff who will conduct these evaluations in practice. In contrast, other research shows that raters who are selectively recruited due to a background in mathematics or mathematics education and who complete initial training and ongoing calibration score more accurately on the MQI than those who are not selectively recruited (Hill et al., 2012).

[^3]:    ${ }^{4}$ Kane et al. (2011) argue that cotemporaneous measurement of teacher observation scores and student outcomes may bias estimates due to class characteristics that affect both the predictor and the outcome. I do not do so here for both practical and substantive reasons. The sample of school-grade-years in which all teachers have out-of-year observation scores is too limited to conduct the same sort of analysis. In addition, as this study is interested in the effect of instruction on student outcomes, I want to utilize scores that capture the types of practices and activities in which students themselves are engaged.

    At the same time, I am able to examine the extent to which Kane et al.'s hypothesis plays out in my own data. To do so, I explore whether changes in classroom composition predict changes in instructional quality for those 45 teachers for whom I have two years of observation data. In Appendix Table A1, I present estimates from models that regress each instructional quality dimension on a vector of observable class characteristics and teacher fixed effects. Here, I observe that classroom composition only predicts within-teacher, cross-year differences in Classroom Emotional Support ( $F=2.219, p=0.035$ ). This suggests that attention to omitted variables related both to Classroom Emotional Support and student achievement may be important.

[^4]:    ${ }^{5}$ Between three and six teachers are missing data for each of these constructs. Given that these data are used for descriptive purposes and as controls, in these instances I impute the mean value for the district. For more information on these scales, see Hill, Blazar, and Lynch (2015).

[^5]:    ${ }^{6}$ Value-added scores are calculated from a model similar to equation (2). Here, I regress end-of-year student mathematics test scores on state assessments on a vector of prior achievement; student-, class-, and school-level covariates; and district-by-grade-by-year fixed effects. I predict a teacher-level random effect as the value-added score. I utilize all years of data and all teachers in the sample districts and grades to increase the precision of my estimates (Goldhaber \& Hansen, 2012; Koedel \& Betts 2011; Schochet \& Chiang, 2013).
    ${ }^{7}$ In some instances, mean scores for both switchers and non-switchers on standardized variables fall below or above zero (e.g., Classroom Emotional Support). This is possible given that variables were standardized across all teachers in the study, not just those in the identification sample.

[^6]:    ${ }^{8}$ I identify these specialized classes in cases where more than $50 \%$ of students have this designation.

[^7]:    ${ }^{9}$ I also test the robustness of results to clustering of standard errors at the school-year level, and find that standard errors and significance levels presented below do not change substantively.

[^8]:    10 Paper is a collaboration with Matthew A. Kraft.

[^9]:    ${ }^{11}$ Although student outcomes beyond test scores often are referred to as "non-cognitive" skills, our preference, like others (Duckworth \& Yeager, 2015; Farrington et al., 2012), is to refer to each competency by name. For brevity, we refer to them as "attitudes and behaviors." We adopt these terms because they most closely characterize the measure we focus on in this paper.

[^10]:    ${ }^{12}$ We conducted factor analyses separately by year, given that there were fewer items in the first year. The NCTE project added additional items in subsequent years to help increase reliability. In the second and third years, each of the two factors has an eigenvalue above one, a conventionally used threshold for selecting factors (Kline, 1994). Even though the second factor consists of three items that also have loadings on the first factor between 0.35 and 0.48 - often taken as the minimum acceptable factor loading (Field, 2013; Kline, 1994) - this second factor explains roughly $20 \%$ more of the variation across teachers and, therefore, has strong support for a substantively separate construct (Field, 2013; Tabachnick \& Fidell, 2001). In the first year of the study, the eigenvalue on this second factor is less strong (0.78), and the two items that load onto it also load onto the first factor.

[^11]:    ${ }^{13}$ Depending on the outcome, between $4 \%$ and $8 \%$ of students were missing a subset of items from survey scales. In these instances, we created final scores by averaging across all available information.

[^12]:    ${ }^{14}$ As described by Blazar (2015), capture occurred with a three-camera, digital recording device and lasted between 45 and 60 minutes. Teachers were allowed to choose the dates for capture in advance and directed to select typical lessons and exclude days on which students were taking a test. Although it is possible that these lessons were unique from a teachers' general instruction, teachers did not have any incentive to select lessons strategically as no rewards or sanctions were involved with data collection or analyses. In addition, analyses from the MET project indicate that teachers are ranked almost identically when they choose lessons themselves compared to when lessons are chosen for them (Ho \& Kane, 2013).
    ${ }^{15}$ Developers of the CLASS instrument identify a third dimension, Classroom Instructional Support. Factor analyses of data used in this study showed that items from this dimension formed a single construct with items from Emotional Support (Blazar et al., 2015). Given theoretical overlap between Classroom Instructional Support and dimensions from the MQI instrument, we excluded these items from our work and focused only on Classroom Emotional Support.

[^13]:    ${ }^{16}$ Information on teachers' background and knowledge were captured on a questionnaire administered in the fall of each year. Survey items included gender, race/ethnicity, years teaching math, route to certification, and amount of undergraduate or graduate coursework in math and math courses for teaching (scored on a Likert scale from 1 to 4). For simplicity, we averaged these last two items to form one

[^14]:    ${ }^{18}$ We controlled for prior-year scores only on the high-stakes assessments and not on the low-stakes assessment for three reasons. First, including prior low-stakes test scores would reduce our full sample by more than 2,200 students. This is because the assessment was not given to students in District 4 in the first year of the study ( $\mathrm{N}=1,826$ students). Further, an additional 413 students were missing fall test scores given that they were not present in class on the day it was administered. Second, prior-year scores on the high- and low-stakes test are correlated at 0.71 , suggesting that including both would not help to explain substantively more variation in our outcomes. Third, sorting of students to teachers is most likely to occur based on student performance on the high-stakes assessments since it was readily observable to schools; achievement on the low-stakes test was not.

[^15]:    ${ }^{19}$ It is important to note that adding prior survey responses to the education production function is not entirely analogous to doing so with prior achievement scores. While achievement outcomes have roughly the same reference group across administrations, the surveys do not. This is because survey items often asked about students' experiences "in this class." All three Behavior in Class items and all five Happiness in Class items included this or similar language, as did five of the 10 items from Self-Efficacy in Math. That said, moderate year-to-year correlations of $0.39,0.38$, and 0.53 for Self-Efficacy in Math, Happiness in Class, and Behavior in Class, respectively, suggest that these items do serve as important controls. Comparatively, year-to-year correlations for the high- and low-stakes tests are 0.75 and 0.77 .

[^16]:    ${ }^{20}$ We estimated these variance components using restricted maximum likelihood estimation because full maximum likelihood estimates tend to be biased downward (Harville, 1977; Raudenbush \& Bryk, 2002) and may be particularly problematic in our smaller subsample of students and teachers who had prior-year measures of their attitudes and behaviors.
    ${ }^{21}$ Models were fit using full maximum likelihood, given our focus in this analysis on the fixed rather than the stochastic portion of the model; full maximum likelihood allows us to compare estimates from the fixed portion of the equation between nested models (Harville, 1977; Raudenbush \& Bryk, 2002).

[^17]:    ${ }^{22}$ In our dataset, observable classroom characteristics do not appear to influence teachers' observation ratings. Correlations between observation scores adjusted for classroom characteristics, including gender, race, free or reduced-price lunch eligibility, special education status, limited English proficiency, and prior achievement in both math and English language arts - and unadjusted scores range from 0.93 (for Classroom Organization) to 0.97 (for Mathematical Errors). Further, patterns of results in our teaching effect estimates are almost identical when we use adjusted versus unadjusted scores. Below, we present findings with unadjusted scores.
    ${ }^{23}$ To estimate these scores, we specified the following hierarchical linear model separately for each school year:

    $$
    \text { OBSERVATION }_{l j,-t}=\gamma_{j}+\varepsilon_{l j t}
    $$

[^18]:    ${ }^{24}$ For our main analyses, we chose not to control for other observable characteristics of teachers (e.g., teaching experience, math content knowledge, certification pathway, education), as these factors may be tied directly to teachers' practices. From a policy perspective, we are less interested in where and how teachers picked up good practices, so long as they have them. That said, in separate analyses (available upon request), we re-ran models controlling for the four background characteristics listed above and found that patterns of results were unchanged. None of these teacher characteristics predicted student outcomes when also controlling for dimensions of teaching quality.

[^19]:    ${ }^{25}$ We find that teacher effects from models that exclude class effects are between $13 \%$ to $36 \%$ larger in magnitude than effects from models that include these class effects. This suggests that analyses that do not take into account classroom level shocks likely produce upwardly biased estimates of stable teacher effects.

[^20]:    ${ }^{26}$ When we adjusted $p$-values for estimates presented in Table 5 to account for multiple hypothesis testing using both the Šidák and Bonferroni algorithms (Dunn, 1961; Šidák, 1967), relationships between Emotional Support and both Self-Efficacy in Math and Happiness in Class, as well as between Mathematical Errors and Self-Efficacy in Math remained statistically significant.

[^21]:    ${ }^{27}$ In similar analyses in a subset of the NCTE data, Blazar (2015) did find a statistically significant relationship between Ambitious Mathematics Instruction and the low-stakes math test of 0.11 sd . The $95 \%$ confidence interval around that point estimate overlaps with the $95 \%$ confidence interval relating Ambitious Mathematics Instruction to the low-stakes math test in this analysis. Estimates of the relationship between the other three domains of teaching practice and low-stakes math test scores were of smaller magnitude and not statistically significant. Differences between the two studies likely emerge from the fact that we drew on a larger sample with an additional year of data, as well as slight modifications to our identification strategy.

[^22]:    ${ }^{28}$ We estimated the reliability of our teacher effects estimate through the signal-to-noise ratio:

    $$
    \frac{\operatorname{Var}\left(\mu_{j}\right)}{\operatorname{Var}\left(\mu_{j}\right)+\left(\frac{\sum_{j=1}^{n} s e_{j}}{n}\right)}
    $$

    The numerator is the observed variance in the teacher effect, or the squared value of the standard deviation of $\mu_{j}$, which is our main parameter of interest. The denominator is an estimate of the true teacher-level variance, which we approximate as the sum of the estimated variance in the teacher effect and the average squared standard error of individual teacher effect estimates. The number of teachers in the sample is detonated by $n$, and $s e_{j}$ is the standard error of the teacher effect for teacher $j$. See McCaffrey, Sass, Lockwood, \& Mihaly (2009) for a similar approach.

    In Appendix Table 2, we calculate two sets of estimates. The first calculates the precision of our main teacher effect estimates, which we use to calculate disattenuated correlations in Appendix Table 3. Given that these teacher effect estimates are derived from models with slightly different samples, which could impact reliability, we also calculated these estimates of precision in a balanced sample of teachers and students who had complete data on all measures (column 2; $\mathrm{N}=51$ teachers and 548 students). Here, we found that precision was quite comparable across teacher effects, ranging from 0.50 (for teacher effects on Self Efficacy in Math) to 0.56 (for teacher effects on Happiness in Class).

    In Appendix Table 3, relative differences in disattenuated correlations are similar to those presented above. We still observe much stronger relationships between teacher effects on the two math tests and between teacher effects on Behavior in Class and Self-Efficacy in Math than between other outcome measures. In some cases, these disattenuated correlations are close to 1 , which we argue are unlikely to be the true relationships in the population. Overcorrections likely are driven by moderate reliabilities and moderate sample sizes (Zimmerman \& Williams, 1997).

[^23]:    ${ }^{29}$ See Bacher-Hicks et al., 2015 for an empirical analysis of persistent sorting in the classroom data used in this study.

[^24]:    ${ }^{30}$ Glazerman and Protik (2015) exploited random assignment of teachers across schools as part of a merit pay program. Here, findings were more mixed. In the elementary sample, the authors estimated a standardized effect size relating non-experimental value-added scores (stacking across math and ELA) to student test scores following random assignment of roughly 1 sd . However, in their smaller sample, the standard error was large ( 0.34 ), meaning that they could not rule out potentially important degrees of bias. Further, in the middle school sample, they found no statistically significant relationship.

[^25]:    ${ }^{31}$ In the MET project, Kane et al. (2013) examined whether a composite measure of teacher effectiveness predicted students' attitudes and behaviors (i.e., grit, happiness in class, implicit theory of intelligence, student effort) following random assignment. However, given that measures used to calculate teacher effects differed across time, "there [was] no reason to expect the coefficient to be equal to one" (p.35). Thus, findings should not be interpreted as evidence for or against bias in teacher effects on these outcomes.

[^26]:    ${ }^{32}$ For all three outcomes, composite scores that average across raw responses are correlated at 0.99 and above with scales that incorporate weights from the factor analyses.

[^27]:    ${ }^{33}$ This sample size is driven by teachers whose students had current- and prior-year survey responses for Happiness in Class, which was only available in two of the three years of the study. Additional teachers and students had current- and prior-year data for Behavior in Class $(\mathrm{N}=111)$ and Self-Efficacy in Math ( N $=108)$, both of which were available in all three years of the study. However, for consistency, I limit this sample to teachers and students who had current- and prior-year scores for all three survey measures.
    ${ }^{34}$ Information on teachers' background and knowledge were captured on a questionnaire administered in the fall of each year. Survey items included years teaching math, route to certification, amount of undergraduate or graduate coursework in math and math courses for teaching ( $1=$ No classes, $2=$ One or two classes, $3=$ Three to five Classes, $4=$ Six or more classes). For simplicity, I averaged these last two items to form one construct capturing teachers' mathematics coursework. Further, the survey included a

[^28]:    test of teachers' mathematical content knowledge, with items from both the Mathematical Knowledge for Teaching assessment (Hill, Schilling, \& Ball, 2004) and the Massachusetts Test for Educator Licensure. Teacher scores were generated by IRTPro software and standardized in these models, with a reliability of 0.92. (For more information about these constructs, see Hill, Blazar, \& Lynch, 2015).

[^29]:    ${ }^{35}$ Two other teachers from the same randomization block also agreed to participate. However, the principal decided that it was not possible to randomly assign rosters to these teachers. Thus, I exclude them from all analyses.
    ${ }^{36}$ One concern with dropping teachers in this way is that they may differ from other teachers on postrandomization outcomes, which could bias results. Comparing attriters for whom I had post-randomization data ( $\mathrm{N}=21$, which excludes the four teachers who either left teaching, left the district, moved to third grade and therefore out of my dataset, or were on maternity leave) to the remaining teachers ( $\mathrm{N}=54$ ) on their observed effectiveness at raising student achievement in the 2012-13 school year, I found no difference $(p=.899)$. Further, to ensure strong external validity, I compared attriters to the experimental sample on each of the teacher characteristics listed in Table 2 and found no difference on any (results available upon request).

[^30]:    ${ }^{37}$ Thirty-eight students were hand placed in teachers' classrooms after the random assignment process. As these students were no part of the experiment, they were excluded from these analyses.

[^31]:    ${ }^{38}$ See Equation (1) below for more details on these predictions.
    ${ }^{39}$ Twenty-six students were missing baseline data on at least one characteristic. In order to retain all students, I imputed missing data to the mean of the students' randomization block. I take the same approach to missing data in all subsequent analyses. This includes the 19 students who were part of my main analytic sample but happened to be absent on the day that project managers administered the student survey and, thus, were missing outcome data. This approach to imputation seems reasonable given that there was no reason to believe that students were absent on purpose to avoid taking the survey.

[^32]:    ${ }^{40}$ An alternative fixed-effects specification is preferred by some because it does not assume that teacher assignment is correlated with factors that predict student achievement (Guarino, Maxfield, Reckase, Thompson, \& Woolridge, 2015). However, in these data, this approach returned similar estimates in models

[^33]:    ${ }^{41}$ In order to increase the precision of these estimates, I included all available teacher-years outside of the experimental sample.

