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Real-Time Modeling of Gas-Electric Dependencies: An Optimal Control Approach

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Real-Time Modeling of Gas-Electric Dependencies:
An Optimal Control Approach

by

Qinxu Gu

Presented to the Graduate and Research Committee
of Lehigh University
in Candidacy for the Degree of
Master of Science
in
Industrial and Systems Engineering

Lehigh University

May 2018

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Approved and recommended for acceptance as a thesis in partial fulfillment of the requirements for the degree of Master of Science.

Date

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Contents

Acknowledgements	iv
List of Tables	vii
List of Figures	viii
Abstract	1
1 Introduction	2
1.1 Gas Turbine	2
1.2 PID controller	2
1.3 Hierarchical control	3
2 GAST Model	5
2.1 Simulation of GAST Model	6
2.2 Non-Windup Limit	7
3 GGOV1 Governor-Turbine System	14
4 Two-Area System Models	20
4.1 Two-Area System With Only Primary Speed Control	21
4.2 Two-Area System With Supplementary Control	24
5 Summary and future work	28
Bibliography	29

List of Tables

2.1	GAST Parameter	8
3.1	GGOV1 Parameter as described in [4]	19

List of Figures

2.1	The GAST model to represent dynamic behavior of the gas governor-turbine [9] . . .	5
2.2	Simulation of GAST model	6
2.3	Non-windup subsystem	7
2.4	PELEC	7
2.5	$\Delta\omega$	7
2.6	Fuel flow	7
2.7	integrator with non-windup limits	8
2.8	single time constant block with non-windup limits	8
2.9	lead-lag function with non-windup limits	8
2.10	Input signal	9
2.11	Integrator with non-windup limits (version 1)	9
2.12	Output signal (version 1)	10
2.13	Output signal (version 2)	10
2.14	Integrator with non-windup limits (version 2)	10
2.15	integrator with non-windup limits (version 3)	11
2.16	Input signal (version 3)	11
2.17	Output signal (version 3)	11
2.18	single time constant function with non-windup limits (version 1)	12
2.19	Input signal (version 1)	12
2.20	Output signal (version 1)	12
2.21	single time constant lag function with non-windup limits (version 2)	13
2.22	Input signal	13

2.23	output signal	13
3.1	GGOV1 [1]	14
3.2	Implementation of the GGOV1 model in Simulink	15
3.3	GGOV1 temperature control	16
3.4	GGOV1 acceleration control	16
3.5	GGOV1 speed governor	17
3.6	GGOV1 fsrn regulator	17
3.7	GGOV1 non-windup subsystem	18
3.8	GGOV1 speed	18
3.9	GGOV1 fuel flow	18
3.10	GGOV1 Pmech	18
4.1	Two-area system[7]	20
4.2	Two-area system electrical equivalent[7]	20
4.3	Two-Area System With Speed Control [7], page 603	21
4.4	Implementation of Two-area system with speed control	22
4.5	P_{L1}	23
4.6	P_{L2}	23
4.7	P_{12}	23
4.8	Fuel flow	23
4.9	Two-Area System With Supplementary Control[7](page608)	24
4.10	Two-Area System With Supplementary Control	26
4.11	Input signal in area 1	27
4.12	Input signal in area 2	27
4.13	ΔP_{12}	27
4.14	Fuel flow	27

Abstract

In this thesis, several turbine-governor models such as GAST model and GGOV1 model are implemented. The simulation of the models takes electric power and speed as the variable input, respectively, to see what will influence the fuel consumption and mechanical power. These two models are implemented in detail and incorporated with non-windup limiters. Different implementations for the non-windup limiters are considered and compared. In addition to the single gas turbine model, its integration to a power system model is developed as well. We consider two-area systems, one with simple primary speed droop control and one with supplementary automatic generation control.

Chapter 1

Introduction

1.1 Gas Turbine

Gas turbine plays an important role in power systems, which takes the duty of converting natural energy into electricity. Usually a gas turbine consists of three or four parts, a gas compressor, a turbine on the shaft and a combustor, and with a fourth component-electric generator, the energy can be converted into electric form.

Firstly, the air will be compressed within the compressor. Fuel will be then mixed with the compressed air and burnt in the combustor. After which, the exhausted gas flow rotate the blades of the turbine and consequently the shaft of the generator connected to it.

In turbine-governor model, the governor model with given speed reference(SPEED ref) determines gate value(GATE) for the turbine model, and turbine model determines the mechanical power(P_{mech}) or torque for the generator model.

Turbine-Governor models like GAST model, Rowens model, GGOV1 model are commonly used in research.

1.2 PID controller

Power systems tend to be unstable under severe load disturbance. Severe disturbances can trigger a plant shutdown. Therefore, a lot of controllers are designed to maintain system stability.

PID controller [2] offers continuously modulated control to a power system. The overall control

function can be expressed as:

$$u(t) = K_p e(t) + K_i \int_0^t e(t') dt' + K_d \frac{de(t)}{dt}, \quad (1.1)$$

It consists of three parts, proportional term, integral term and derivative term, $e(t)$ is the error, the proportional term gives the directly correction, the integral term makes up the cumulated error, and the proportional term was for possible future error.

The proportional term K_p will decrease rise time but also lead to oscillatory performance. The derivative control K_d reduces the oscillations by providing proper damping but may be detrimental to transient performance and stability. The K_i integral control considers the cumulated error and reduces the steady-state error to zero. The primary design goal is to obtain a good load disturbance response by optimally selecting PID controller parameters. Tuning of PID controller coefficients can be made by heuristic algorithm such as genetic algorithm [3], bat algorithm [5] and partial swarm algorithm [6].

1.3 Hierarchical control

The generation of power units and consumption of loads connected needs to be controlled and monitored. Hierarchical control consists of three control levels, each with different characteristics and qualities, and all depending on each other [11]:

Level 1 (Primary control): The primary control monitor the normal operation to keep the balance between generation and consumption. Droop control method is one of the methods normally used as a primary control method in modeling. In this level, the control loops of all generating units respond almost within a few seconds.

Level 2 (Secondary control): The objective of secondary control is keeping the balance between generation and consumption within each control area based on secondary control reserve. In this level, centralized and continuous automatic generation control is chosen to balance the load after an incident, usually in the time-frame of seconds up to typically 15 minutes.

Level 3 (Tertiary control): Similar to secondary control, tertiary control works based on secondary reserves as well. It is mainly used to release secondary reserves in a balanced system,

but sometimes also used as a supplementary method to restore system frequencies after large incidents. At this level, the balance of power will be taken into consideration.

The power system control problem can be regarded as a optimization problem which involves random process and stochastic control in continuous time.

Chapter 2

GAST Model

In gas turbine energy is converted into power. The GAST model [9] is one of the most commonly used models, which consists of two parts, the generator and the gas turbine. In this thesis, we will use this model as the main research entity. The implementation and parameters will be presented in this chapter. The block diagram is shown in Figure 2.1:

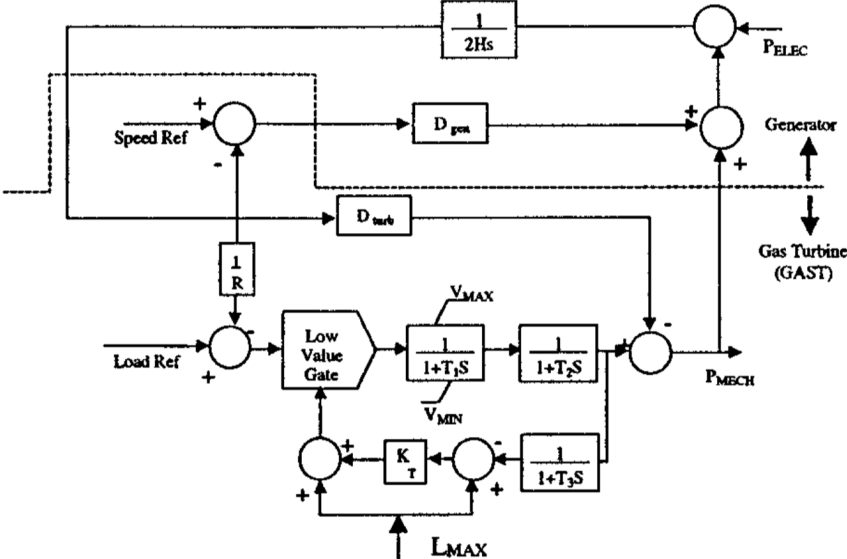


Figure 2.1: The GAST model to represent dynamic behavior of the gas governor-turbine [9]

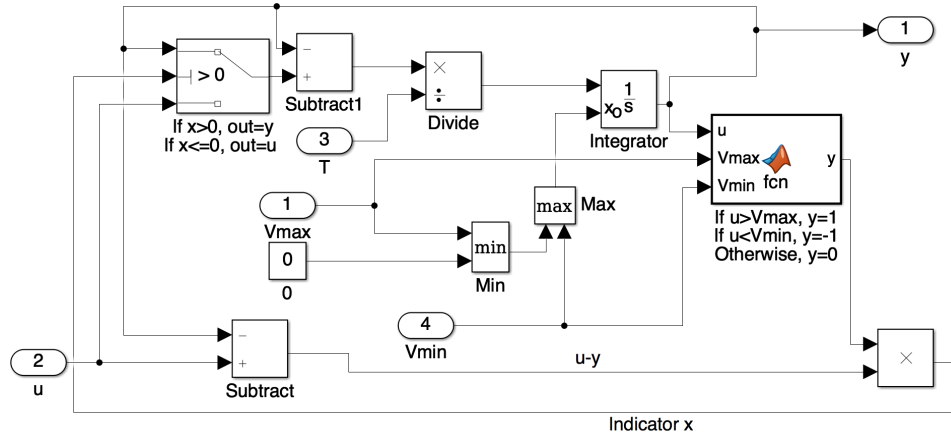


Figure 2.3: Non-windup subsystem

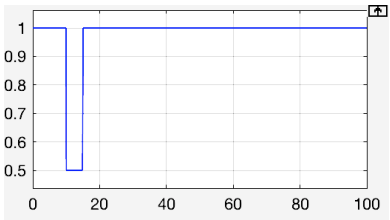


Figure 2.4: PELEC

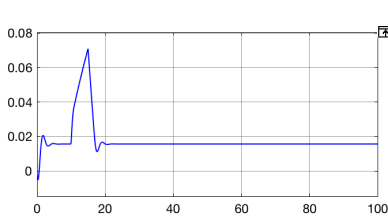


Figure 2.5: $\Delta\omega$

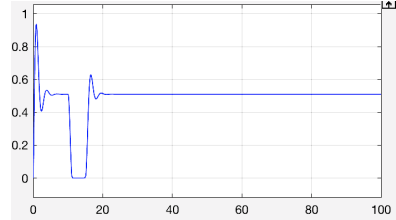


Figure 2.6: Fuel flow

exhausted temperature, and controls the fuel flow. The temperature, however, is influenced by both air flow and the fuel flow. The mechanical power (P_{mech}) is the output of the turbine, to which the input of the generator is connected. The droop control in this model balances the generation and load.

In our simulation, we vary the electric power to see the response to a sudden variation of electric load. As shown in Figure 2.4, Figure 2.5 and Figure 2.6, the decrease of Pelec gives rotor a speed up. The fuel flow drop afterwards. when the power demand suddenly drops to 0.5pu, the fuel flow drop as well.

2.2 Non-Windup Limit

The transfer functions with non-windup limits are not readily available in Simulink. There are three types of non-windup blocks: integrator with non-windup limits, single time constant block with non-windup limits, lead-lag function with non-windup limits. The single time constant block

Parameter	Representation	Value[9]	Range[1]
R	Governor Droop	0.032	(0,1)
T1	Fuel valve time constant	0.4	(0.04,0.5)
T2	Fuel system lag time constant	0.1	(0.04,0.5)
T3	Turbine exhaust temperature time constant	3	(0.04,5.0)
Lmax	Ambient temperature load limit	1	NA
Kt	Temperature control loop gain	1	(0,5)
Vmax	Maximum valve position	1	(0.5,1.2)
Vmin	Minimum valve position	0	(0,1.0)
Dt	Turbine damping factor	0.15	(0,0.5)
Dg	Generator damping factor	0.5	NA

Table 2.1: GAST Parameter

with non-windup limits is in the GAST model and thus need to be implemented in Simulink.

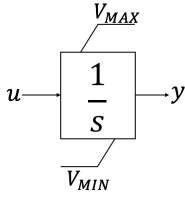


Figure 2.7: integrator with non-windup limits

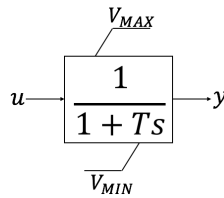


Figure 2.8: single time constant block with non-windup limits

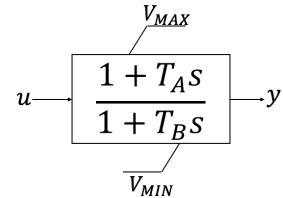


Figure 2.9: lead-lag function with non-windup limits

If the integrator with non-windup limiter can be successfully implemented, the method may offer some inspiration for the implementation of the remaining two. The integral non-windup operation is defined in [7], page 359, as follows:

The system equation is: $f = u$

The limiting action is: If $V_{min} < y < V_{max}$, then $dy/dt = f$

If $y \geq V_{max}$ and $f > 0$, then set $dy/dt = 0, y = V_{max}$

If $y \leq V_{min}$ and $f < 0$, then set $dy/dt = 0, y = V_{min}$

Set $V_{max} = -0.025, V_{min} = -0.25$

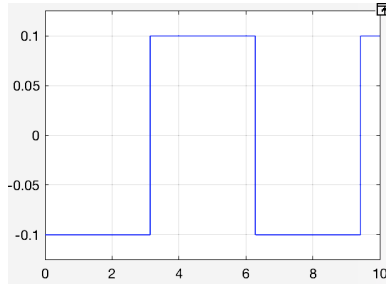


Figure 2.10: Input signal

Several methods have been tried. The first method is to subtract the input signal when the output touches the bound, the block diagram is shown in Figure 2.11:

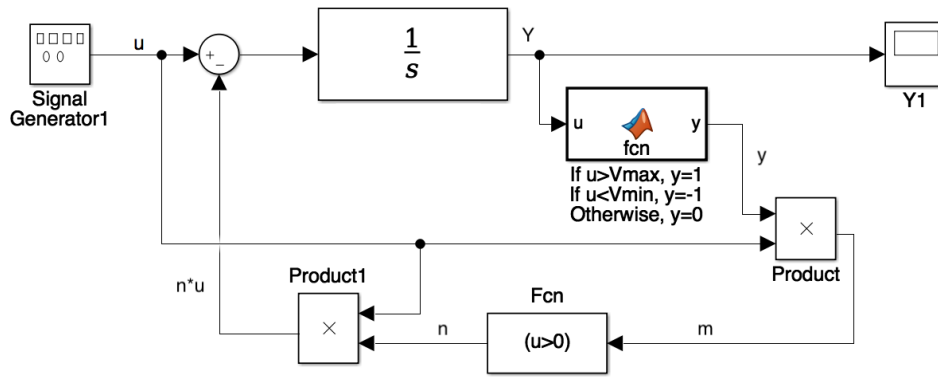


Figure 2.11: Integrator with non-windup limits (version 1)

In Simulink, all the input data will be set as u , so here the indicators are set over the real line. When Y is greater than V_{max} , y equals to one, and if u is greater than zero, the product m will be positive, and n will equal to one, then n times u to be subtracted by u , the input signal will be offset to zero. If Y is less than V_{min} and u is less than 0, the signal will be offset in the same way.

Figure 2.12 shows that the initial point can be out of bound and the line does not strictly lay between the bounds, it has little fluctuation in area near the bounds. As the given input signal and the constraints, the gradient k is in $\text{set}(-0.1, 0.1, 0)$. But in Figure 2.12 above, in the area near the bounds, the line becomes smooth. The second method multiplies the signal with zero when it touches the bounds.

The block diagram is shown in Figure 2.14. When Y is greater than V_{max} , y equals to one,

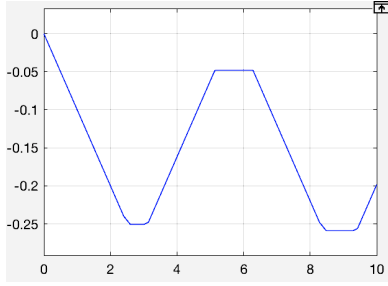


Figure 2.12: Output signal (version 1)

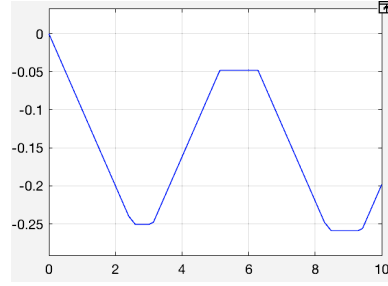


Figure 2.13: Output signal (version 2)

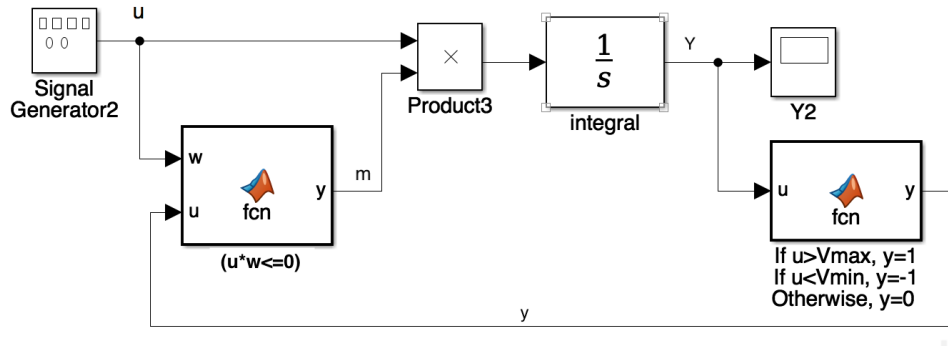


Figure 2.14: Integrator with non-windup limits (version 2)

and if u is greater than zero, the indicator m will be zero, then the input signal u will be multiplied by m and become zero. If Y is less than V_{min} and u is less than 0, the signal will be processed in the same way. The output is shown in Figure 2.13, which is exactly the same as Figure 2.12.

In third method, we do not try to control the input signal by subtraction or multiplication, but switch the signal to zero when the bound is reached. The block diagram is shown in Figure 2.15:

The initial point of Y is zero, and in this diagram the initial point will be checked and modified if zero is out of the bound. After that, when Y is greater than V_{max} , y equals to one, and if u is greater than zero, the product m will be positive, then the input signal will be switched to zero. If Y is less than V_{min} and u is less than 0, the signal will be processed in the same way. The input and output is shown in Figure 2.16 and Figure 2.17:

This method gives perfect output, there is no smoothing line near the bound and the output is strictly bounded.

The simple time constant non-windup limiter needed in GAST model, is defined as follows [7],

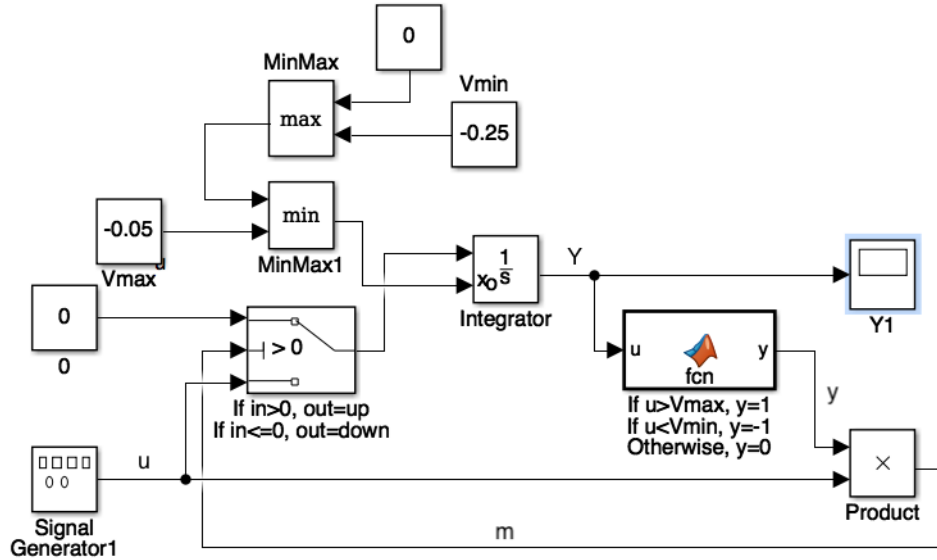


Figure 2.15: integrator with non-windup limits (version 3)

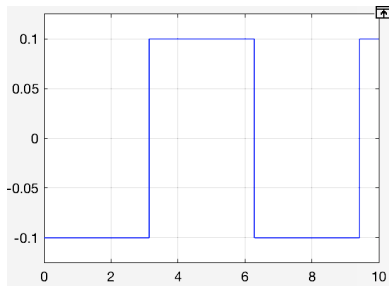


Figure 2.16: Input signal (version 3)

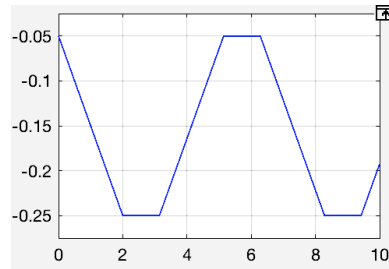


Figure 2.17: Output signal (version 3)

page 360.

The system equation is: $f = \frac{u-y}{T}$

The limiting action is: If $V_{min} < y < V_{max}$, then $dy/dt = f$

If $y \geq V_{max}$ and $f > 0$, then set $dy/dt = 0, y = V_{max}$

If $y \leq V_{min}$ and $f < 0$, then set $dy/dt = 0, y = V_{min}$

Set $T=10, V_{max}=0.8, V_{min}=0.2$. The block diagram is drawn by the same method from the integrator with non-windup limits.

In the block diagram shown in Figure 2.18, when y touches the upper bound V_{max} , m equals to one, and if $u-y$ is greater than zero, the product x will be positive, then the input signal will be switched to y , and in this transfer function, f equals to $(u-y)/T$, when u equals to y , the output

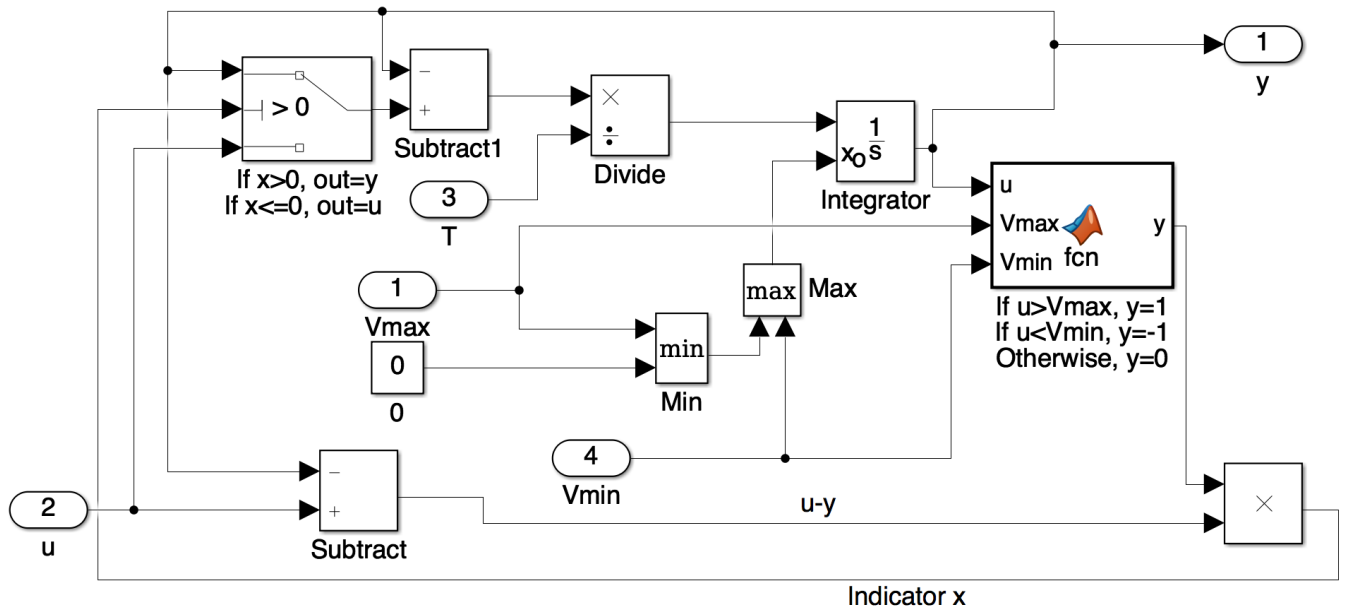


Figure 2.21: single time constant lag function with non-windup limits (version 2)

point will be the V_{max} in this instance, or V_{min} when zero is less than the lower bound. The input and output signal is shown in Figure 2.22 and Figure 2.23:

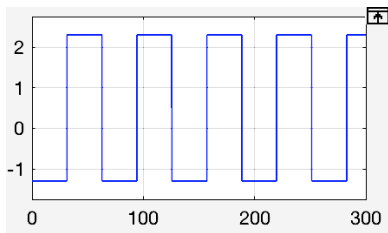


Figure 2.22: Input signal

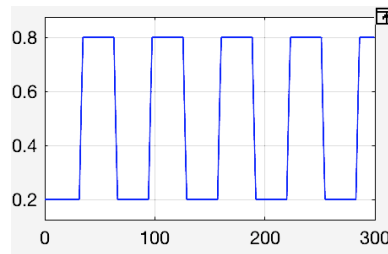


Figure 2.23: output signal

This method can implement the non-windup operation perfectly. In next chapter, this non-windup limiter blocks will be incorporated in GAST model and GGOV1 model, which is one of the simplest turbine-governor models and one of the more recent models.

Chapter 3

GGOV1 Governor-Turbine System

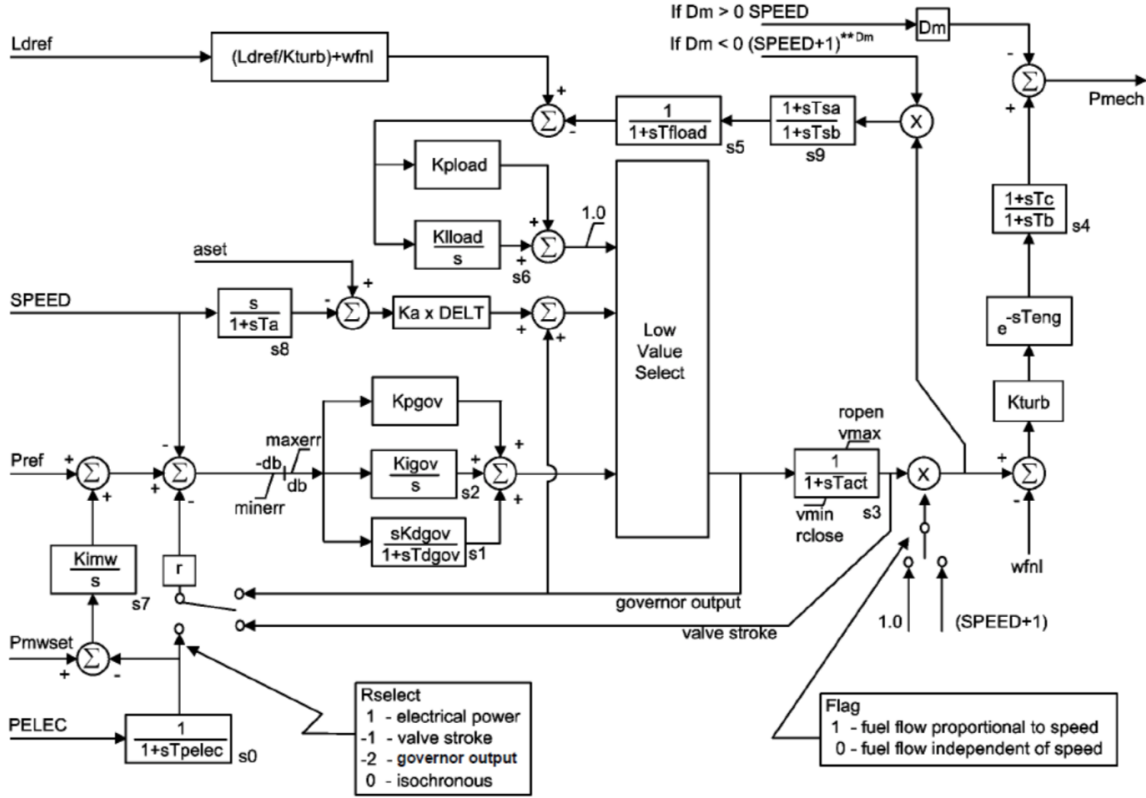


Figure 3.1: GGOV1 [1]

The GAST model is not recommended because it only considers simple droop control, constant load limitation, and the fuel valve response, turbine response, and load limit response using three

time constants. More recent digital model usually considers a PI or PID controller, which is not able to be fully represented in the GAST model implemented in last chapter.

Nowadays, GGOV1 model, studied in [8] [10], is one of the leading models to represent gas turbines with various controls. As shown in Figure 3.1, various controls are presented in blocks in this model: valve position and actuation, fuel system dynamics, load limiter for exhaust temperature controls, load controller for plant-level or outer loop controls, acceleration limiter and governor deadband. In this chapter, the GGOV1 model is implemented in detail, with the table of parameters of GE gas turbine obtained from [4].

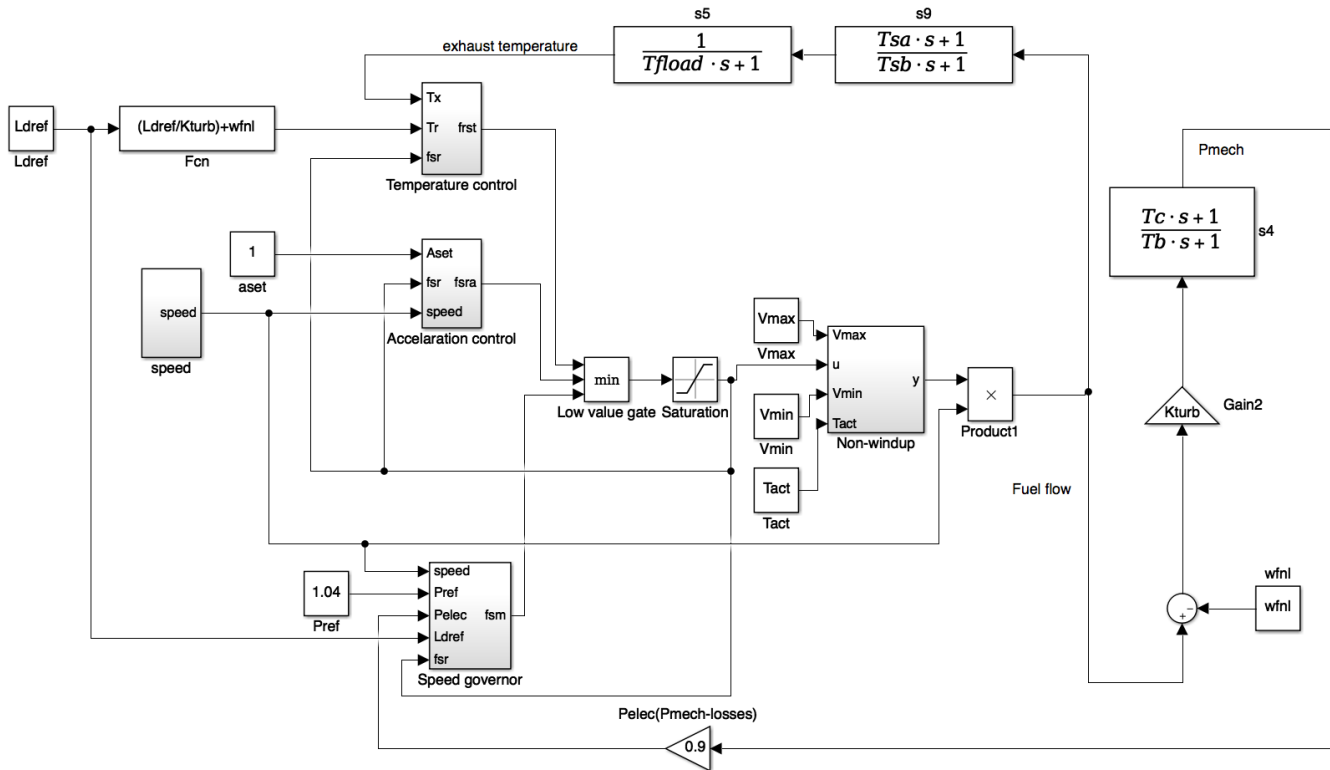


Figure 3.2: Implementation of the GGOV1 model in Simulink

The turbine-governor model is used for determining the mechanical power of the shaft (P_{mech}). In this implementation, the load control block in Figure 3.1 is set to limit a maximum output of exhaust temperature, so called temperature control here. T_{load} represents the time constant in the measurement of temperature. In the temperature control, $T_r - T_x$ represents the exhausted temperature error followed by the proportional controller with gain(K_{pload}). The PI controller

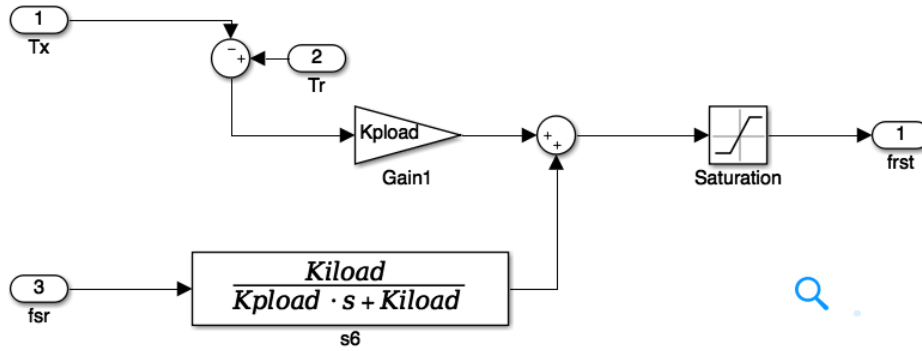


Figure 3.3: GGOV1 temperature control

with Kpload and Kiload accounts for the "fsr" (governor output which represents the fuel flow command determined by the lowest level of fsrt, fsra, and fsrn), which represents the feedback for tracking logic here.

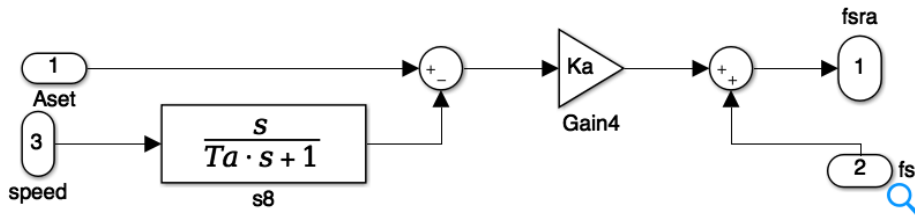


Figure 3.4: GGOV1 acceleration control

The acceleration controller, which is required for startup of the gas turbine. The acceleration control used in GGOV1 with a proportional controller with gain Ka is implemented in Figure 3.4. The setpoint(Aset) of the acceleration limiter can disable the control when gets large enough. The s8 block with time constant(Ta) taking the derivative of speed works as a filter to remove the noise amplified during this process.

When speed decreases, the electrical power will be changing. At the speed governor section, the negative feedback of electrical power (Pelec) will be also changing. We can see that in the above model, the loop speed governor incorporated with PID controller brings the system back to steady state.

The speed governor implemented in Figure 3.5 includes a fsrn regulator where a PID controller is implemented as shown in Figure 3.6. The proportional, integral and derivative controller with

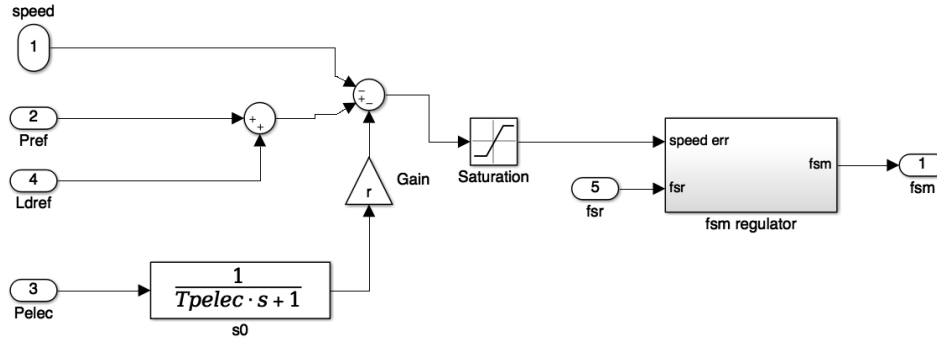


Figure 3.5: GGOV1 speed governor

coefficient K_{pgov} , K_{dgv} and T_{dgv} balance the speed error, and the K_{igov}/K_{pgov} controller works with feedback of the signal f_{sr} (the fuel flow command the minimal among the outputs of the three controllers) provided as an input for the tracking logic.

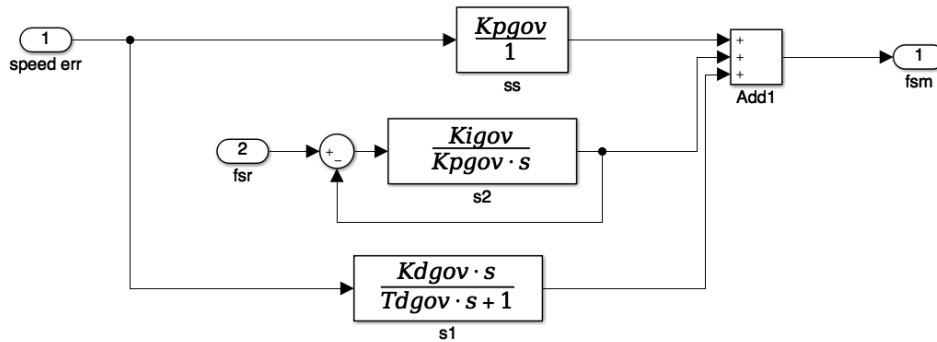


Figure 3.6: GGOV1 fsm regulator

The non-windup block developed in last chapter was utilized in the GGOV1 model as well to prevent the windup. In this system, the fuel flow was determined by the fuel flow command "fsm" influenced by both valve position and speed. The valve changing rate limit is included in this block right before the integrator.

In the GGOV1 model, when the speed is changing as in Figure 3.8, fuel flow and P_{mech} react as shown in Figure 3.9 and Figure 3.10.

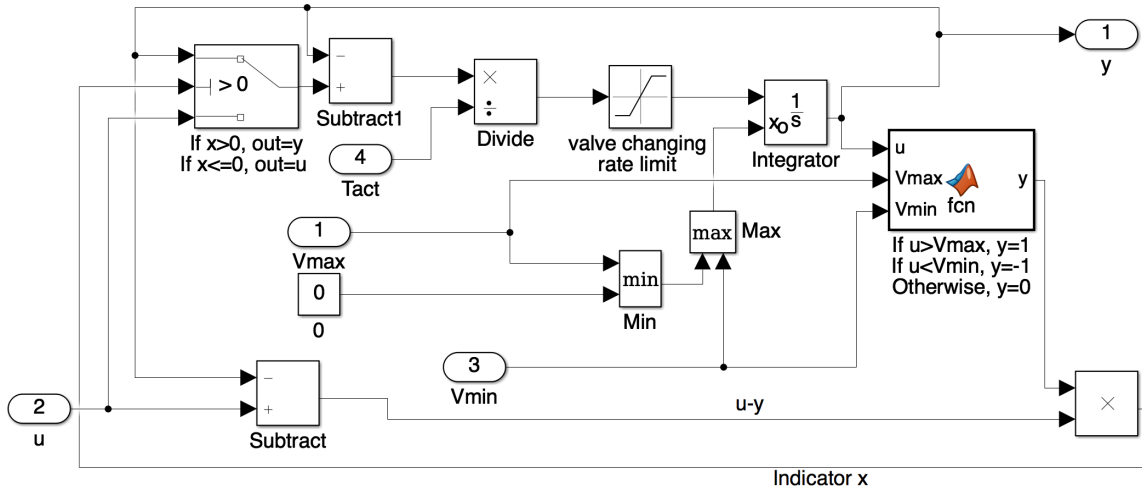


Figure 3.7: GGOV1 non-windup subsystem

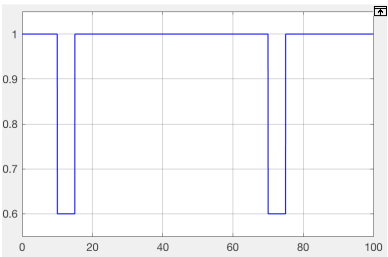


Figure 3.8: GGOV1 speed

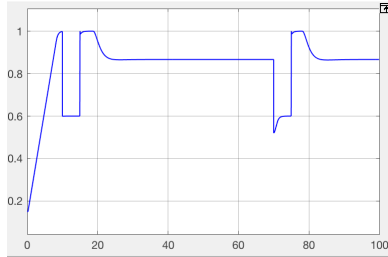


Figure 3.9: GGOV1 fuel flow

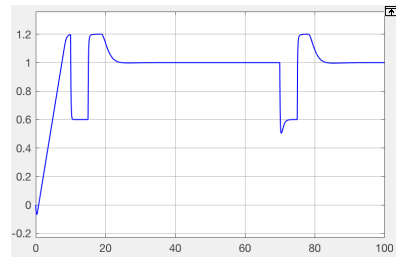


Figure 3.10: GGOV1 Pmech

Parameter	Representation	Value
R	Governor Droop	0.04
Tpelec	Electrical power transducer time constant	1
Maxerr	Maximum value for speed error signal	0.05
Minerr	Minimum value for speed error signal	-0.05
Kpgov	Gov. proportional gain	10
Kigov	Gov. integral gain	2
Kdgov	Gov. derivative gain	0
Tdgov	Gov. derivative controller time constant	1
Vmax	Maximum valve position limit	1
Vmin	Minimum valve position limit	0.15
Tact	Actuator time constant	0.5
Kturb	Turbine gain	1.5
wfnl	No load fuel flow	0.2
Tb	Turbine lag time constant	0.1
Tc	Turbine lead time constant	0
Tfload	Load Limiter time constant	3
Kpload	Load limiter proportional gain for PI controller	2
Kiload	Load limiter integral gain for PI controller	0.67
Ldref	Load limiter reference value	1
Ropen	Maximum valve opening rate	0.1
Rclose	Maximum valve closing rate	-0.1
Aset	Acceleration limiter setpoint	0.01
Ka	Acceleration limiter gain	10
Ta	Acceleration limiter time constant	0.1
Tsa	Temperature detection lead time constant	4
Tsb	Temperature detection lag time constant	5

Table 3.1: GGOV1 Parameter as described in [4]

Chapter 4

Two-Area System Models

In the real world, in a grid there are several generators and associated control systems. A combination of plants can meet dynamic load more economical.

In this section, two kinds of two-area systems will be introduced and implemented. The fuel flows of each generator and the power flow between two areas will be presented, respectively.

The basic idea of two-area system can be represented by these picture below.

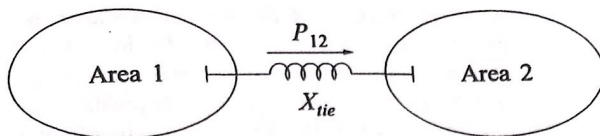


Figure 4.1: Two-area system[7]

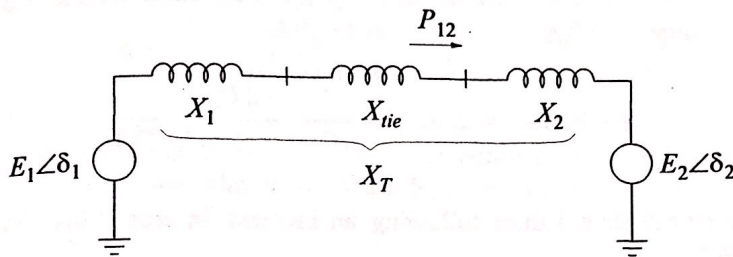


Figure 4.2: Two-area system electrical equivalent[7]

The two areas are connected and there is power flow between them. Thus, there may be a tertiary control to be designed in this system.

4.1 Two-Area System With Only Primary Speed Control

The simplified block diagram is shown in Figure 4.3.

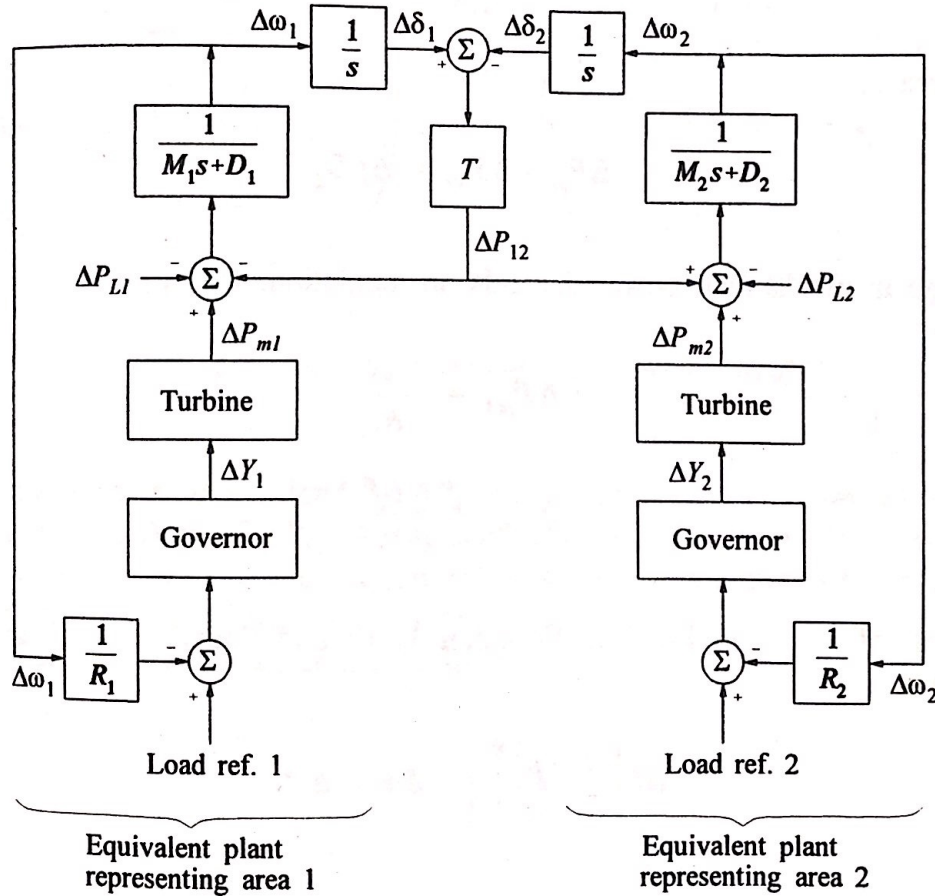


Figure 4.3: Two-Area System With Speed Control [7], page 603

In this block diagram above, ΔP_{12} represents the power flow from area 1 to area 2, ΔP_{L1} and ΔP_{L2} represent the power demand (Pelec) of two areas. ΔP_{m1} and ΔP_{m2} represent the mechanical power (Pmech) of two areas. $\Delta\omega_1$ and $\Delta\omega_2$ represent the angular velocities, $\Delta\delta_1$ and $\Delta\delta_2$ represent the angular displacements. T is the synchronizing torque coefficient.

In the block diagram shown in Figure 4.4, there are two identical GAST models linked with each other. There is a power flow from area 1 to area 2. In the implementation, the transfer function $1/(Ms+D)$ was represented by several blocks with the same function. In our implementation, we used the identical GAST models in each area, to see how it react when one of two areas

is subject to a sudden change of power demand. The power demands in two areas are shown in Figure 4.5 and Figure 4.6:

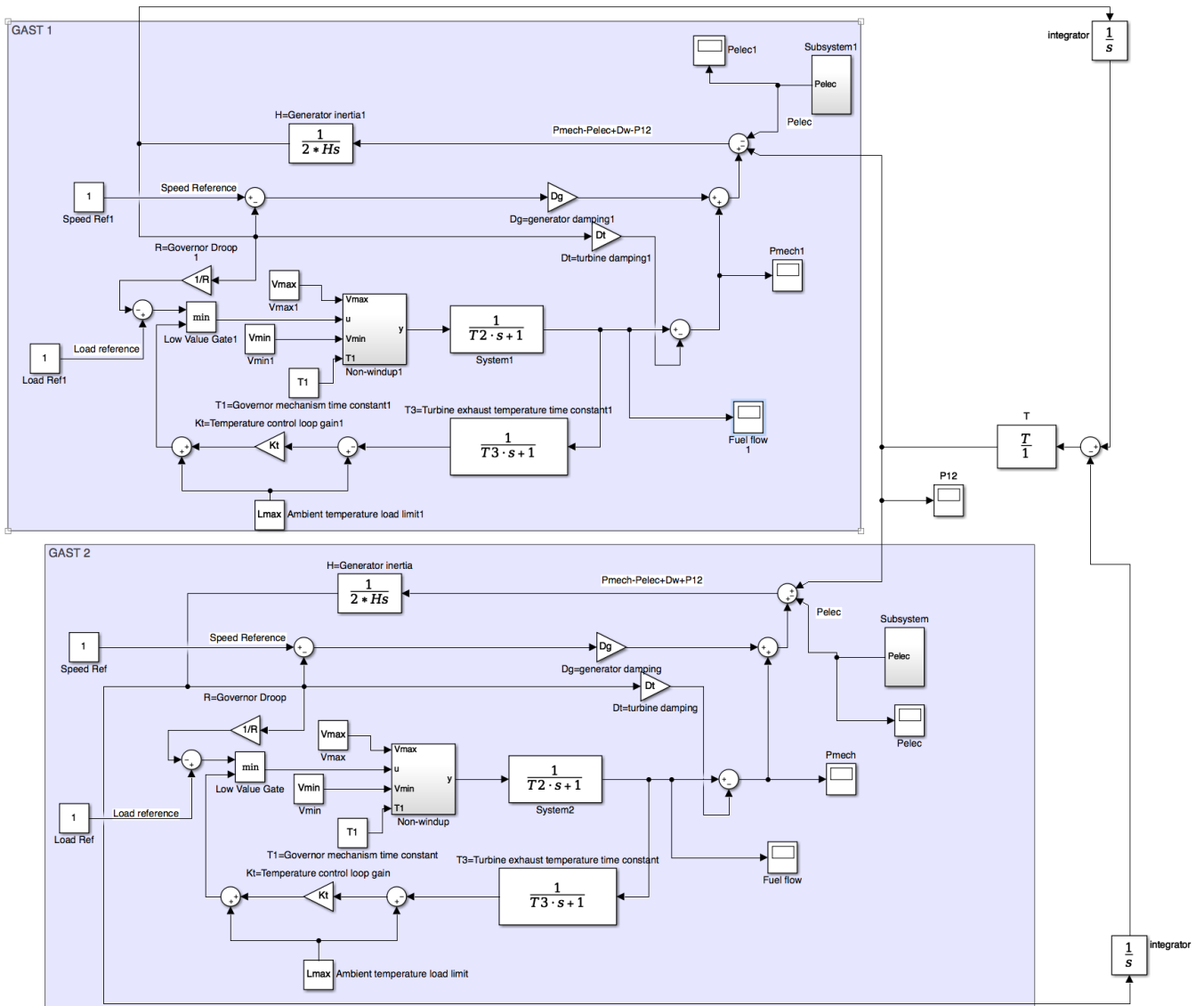


Figure 4.4: Implementation of Two-area system with speed control

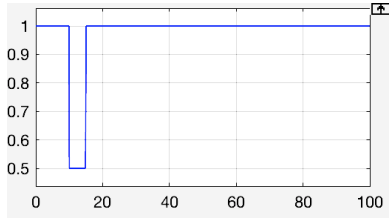


Figure 4.5: P_{L1}

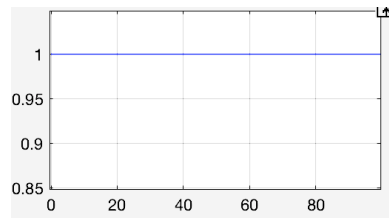


Figure 4.6: P_{L2}

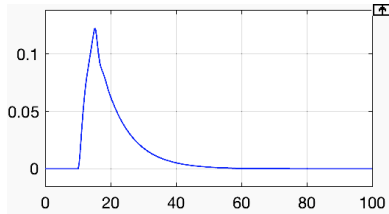


Figure 4.7: P_{12}

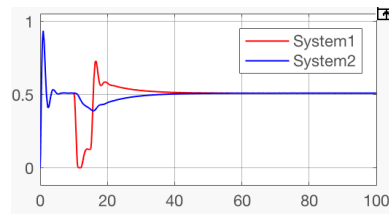


Figure 4.8: Fuel flow

From these Figure 4.5 and Figure 4.8, the initial blue spike may be an effect of initial conditions that are not properly initialized. The important part of the figure are the response starting at $t=10s$. When there is a suddenly drop demand in area1, the fuel flow in area 1 react immediately and the fuel flow in area 2 reacts more slowly.

4.2 Two-Area System With Supplementary Control

In this section a two-area system with supplementary control will be introduced and implemented. The basic objective of supplementary control is used to balance load and generation in case of large disturbance. In this system, the load control must maintain the frequency at the scheduled value. The simplified block diagram of two-area system with supplementary control is shown in Figure 4.9.

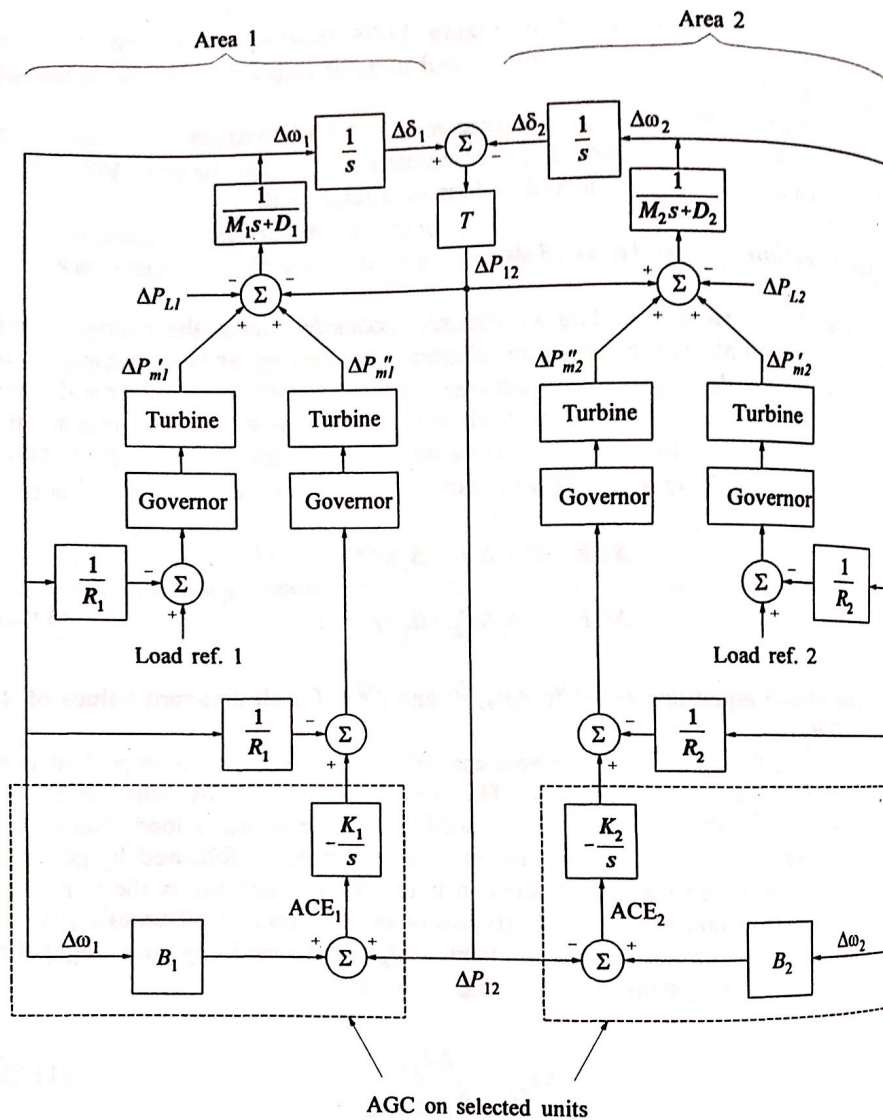


Figure 4.9: Two-Area System With Supplementary Control[7](page608)

In two-area system with supplementary control, only the area has disturbance should be set a supplementary control. The block diagram of the implementation is shown in Figure 4.10. In this implementation, the area 2 has no supplementary control block and three GAST models are set with different parameters.

As shown in Figure 4.11 and Figure 4.12, the electric power signal in area 1 has a disturbance, and the electric power signal in area 2 is stable. When this disturbance occurs, the turbine in area 1 will react immediately, then the turbine in area 2 reacts. We observe that the supplementary control does not seem to play a significant role in this test.

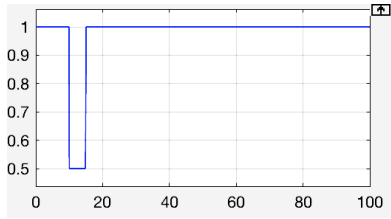


Figure 4.11: Input signal in area 1

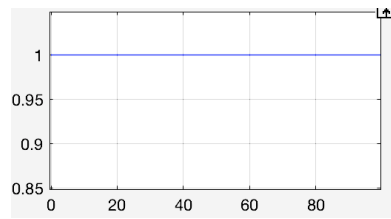


Figure 4.12: Input signal in area 2

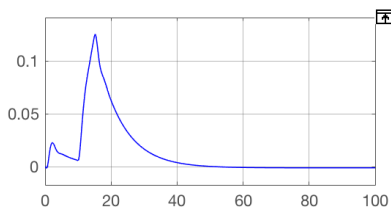


Figure 4.13: ΔP_{12}

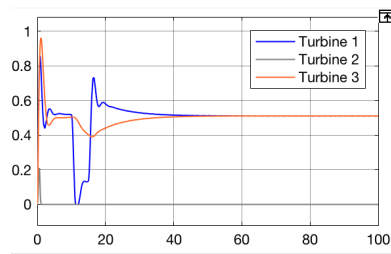


Figure 4.14: Fuel flow

Chapter 5

Summary and future work

In this thesis, we explore some of the key components in a turbine-governor model. Implementation of GAST model and GGOV1 model are studied in detail. In particular, we compare possible implementations for the non-windup blocks. During this study, the tuning of the PID controller caught my attention. The tuning can be considered as an optimization problem whose objective is minimizing the disturbance influence and the cost. Usually, tuning the PID gains insists in finding the best gains to minimize the error. The exploration to find the optimal gains of the PID controllers can be taken into account for future work.

Besides, in this thesis more complicated models including two-area system were also implemented. Usually in these hybrid system the turbine model which only contains governor and turbine was chosen for simplicity. Thus, the speed droop control can be represented by a single block. In our simulation the GAST model which already contains a droop control was used, therefore the speed droop control block was represented by several blocks with same function. Ideally, we should try to incorporate the GGOV1 model included in this system. One should represent the droop control and the supplementary control by blocks with the same function. In future work, we could try to include various controllers in the two-area model and measure their impact on system performance and control.

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Biography

Qinxu Gu was born in 1994 in China. She graduated from Tianjin University with a Bachelor of Engineering in Logistics Engineering in June 2016. And she is now attending Lehigh University for her graduate education. She was highly interested in the fields like mathematics and algorithms. She is grateful that Industrial Systems Engineering department gave her knowledge and courage to explore these fields. She is now completing a Master of Science degree in Industrial Systems Engineering, and is expected to graduate in May 2018.