



## Characteristic of an adiabatic charging reversible circuit with a Lithium ion capacitor as an energy storage device

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### ABSTRACT

An adiabatic reversible circuit was designed for charging a Lithium ion capacitor. The duty ratio of the switching transistors is digitally controlled by a microprocessor. A Lithium ion capacitor has the minimum and the maximum operating voltage. Therefore, the charging voltage is set to be in that range. Using this energy storage system, it is clarified from the experiment that the efficiency is 95.5% during charging and also discharging process. Then the total efficiency is 91.2% during one cycle, which is the best value in the proposed stepwise adiabatic charging circuit.

Reversible circuit is attracting much attention in physics and also electrical engineering [1–11] because it has the characteristic of dissipationless charging of a supercapacitor. Until now, the previous experiment shows that charging efficiency is 94.0% when an electric double-layer capacitor (EDCL) is used [11]. However, the charging and discharging efficiency during one cycle is not discussed well. Therefore, the total efficiency is discussed in this article. In this experiment, to charge a capacitor fast and also efficiently, electric components, such as an inductor and transistors, are set on a printed wiring board by soldering. Due to this, circuit resistance is much decreased. Also a Lithium ion capacitor (LiC) is used because of its higher energy density per volumes than EDCL. This enables a compact energy storage system.

Fig. 1 shows an adiabatic circuit. A microprocessor (PIC16F627A) is used to output the Pulse Width Modulation (PWM) signal [9,11]. Power supply voltage is 5.0 V. Therefore, high and low voltage is 5 and 0 V. The PWM signal is input to inverter (4049B) for increasing current drivability. The output of the inverter is input to the gate of power MOSFETs. The pMOS and nMOS transistors are 2SJ438, and 2SK2231, respectively. The output of two power MOSFETs, is connected to LiC through the inductor. In this article, for realizing a compact storage system, LiC is used instead of EDCL as discussed already. The LiC has the maximum operating voltage, 3.8 V, and the minimum, 2.2 V. Therefore, the output voltage is set to be in this range. The power supply voltage of power MOSFETs is set as 3.56 V. During charging,  $d$  is changed from 64/96, 68/96, ..., 92/96, 1. During discharging,  $d$  is changed from 1, 92/96, ..., 68/96, 64/96. Three physical values were measured. One is the capacitor voltage,  $V_C$ , another is the current from the inductor to the capacitor,  $I_C$ , and the other is the current from the power supply to the inductor,  $I_P$ . These were measured with three

digital multimeters.

Fig. 2 shows the timewise change in  $V_C$ . Here, the number of voltage steps is eight.  $V_C$  is in the range of 2.4–3.5 V, which corresponds to  $d = 0.667$  and  $d = 1$ . If charging time is sufficiently long,  $V_C$  will reach to the power supply voltage, 3.56 V. Fig. 3 shows the timewise change in  $I_C$ . During charging ( $0 \leq t \leq 380$  s),  $I_C$  is positive, while it is negative during discharging ( $380 \leq t \leq 760$  s). This means the current direction is opposite. Fig. 4 shows charge amount  $Q$  flowing into capacitor, which is written as  $Q = \int I_C dt$ . The charge amount difference  $\Delta Q$  between the maximum and the minimum is 38.9C from Fig. 4. On the other hand, the voltage difference  $\Delta V$  between the maximum and the minimum is 1.08 V from Fig. 2. Then, the capacitance value is estimated as  $38.9/1.08 = 35.9$ F.

Fig. 5 shows the timewise change in  $I_P$ . When the capacitor is charged and discharged,  $I_P$  is positive and negative. This means that, during discharging, the current flows from the capacitor to the power supply through the inductor.

Here, charging efficiency  $\eta_1$  is considered. During charging, the work done by the power supply  $W_1$  is written as  $Q_1 V$ , where  $Q_1$  is the charge amount flowing from power supply and  $V$  is the power supply voltage.  $Q_1$  is written as  $Q_1 = \int I_P dt$ . Then,  $Q_1$  is shown in Fig. 6 and the value is 33.3C. The  $V$  is 3.56 V, so  $W_1$  is estimated to be 118.4 J. On the other hand, the increase in electrostatic energy during charging  $E_1$  is written as  $E_1 = C(V_M^2 - V_{m1}^2)/2$ , where  $V_M$  is the maximum capacitance voltage and  $V_{m1}$  is the minimum one during charging. The  $V_M$  and  $V_{m1}$  are 3.48 and 2.41 V, respectively. The  $C$  is 35.9F. Using these values,  $E_1$  is calculated to be 113.0 J. The  $\eta_1$  is defined as  $E_1/W_1$  and calculated to be 95.5%.

Next, the discharging efficiency  $\eta_2$  is calculated in the same way.

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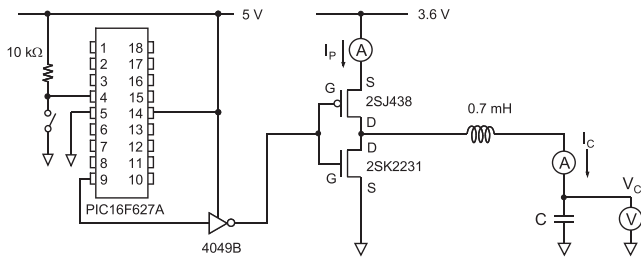


Fig.1. Circuit controlled by microprocessor and measurement system.

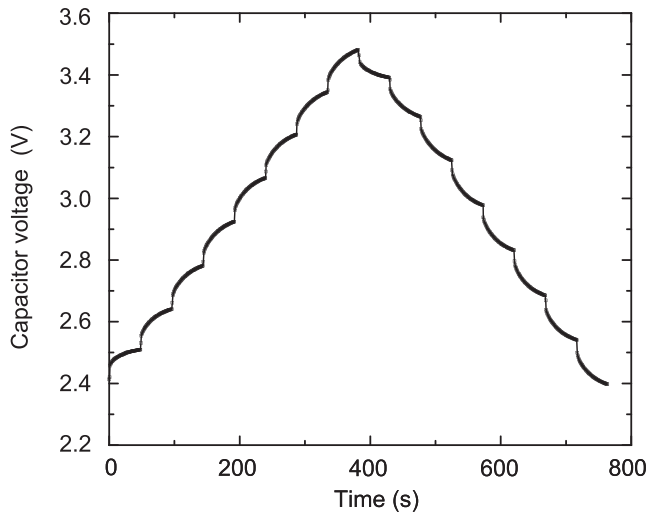


Fig. 2. Capacitor voltage as a function of time.

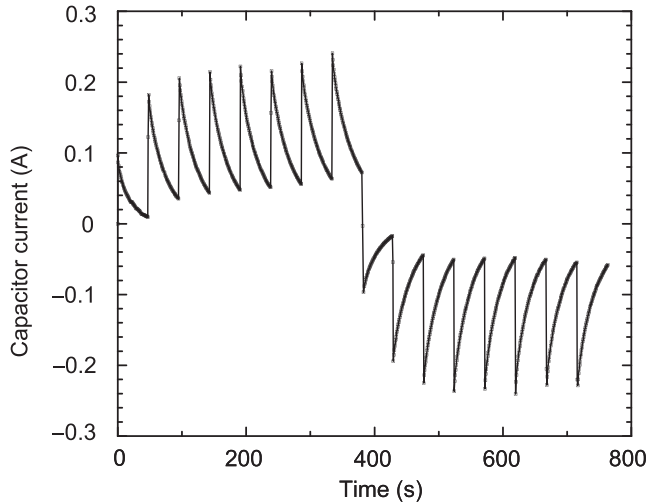


Fig. 3. Capacitor charging current as a function of time.

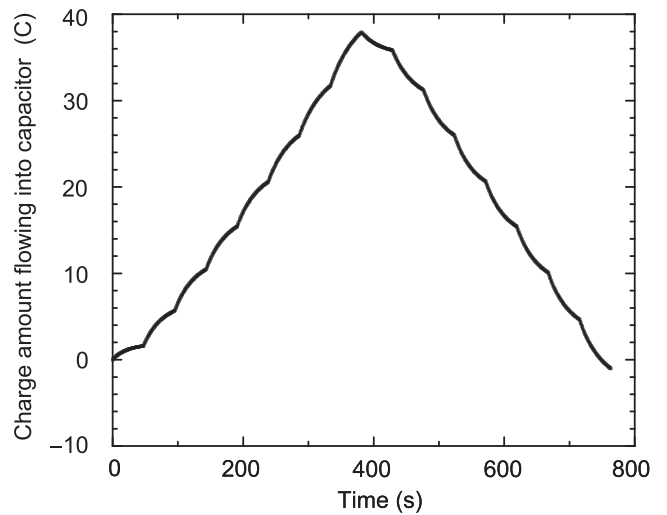


Fig. 4. Charge amount flowing into capacitor.

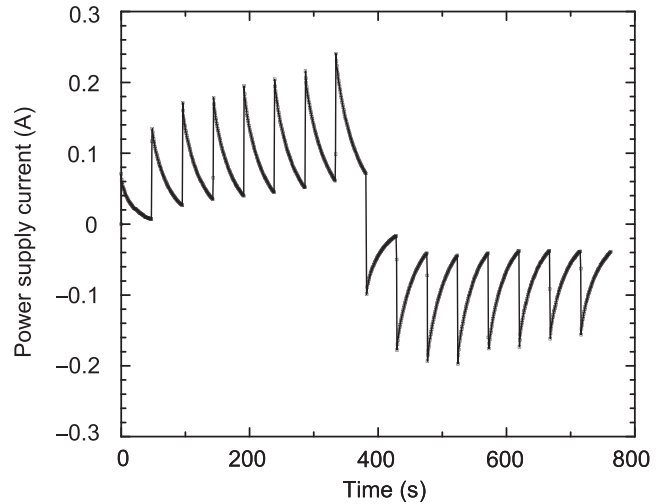


Fig. 5. Power supply current as a function of time.

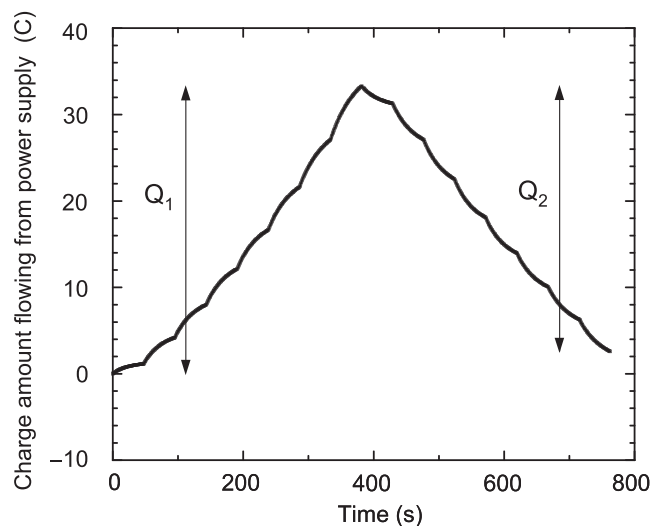


Fig. 6. Charge amount flowing from power supply.

During discharging, the work received by the power supply  $W_2$  is written as  $Q_2V$ , where  $Q_2$  is the charge amount flowing into power supply during discharging. The  $Q_2$  is shown in Fig. 6 and the value is 30.7C. So  $W_2$  is estimated to be 109.3 J. On the other hand, the decrease in electrostatic energy during discharging  $E_2$  is written as  $E_2 = C(V_M^2 - V_{m2}^2)/2$ , where  $V_{m2}$  is the minimum capacitance voltage during discharging. The  $V_{m2}$  is 2.40 V. Then,  $E_2$  is calculated to be 114.4 J. The  $\eta_2$  is defined as  $(W_2/E_2)$  and calculated to be 95.5%.

The total efficiency  $\eta$  during charging and discharging is calculated as  $\eta = \eta_1\eta_2$  and it is 91.2%. Next, the relation between  $\eta$  and the value of  $Q_2/Q_1$  is considered. The  $\eta_1$  and  $\eta_2$  are  $E_1/W_1$  and  $W_2/E_2$ . The  $E_1$  is almost equal to  $E_2$  in this experiment, and this is satisfied in the usual

case. So,  $\eta$  is almost equal to  $W_2/W_1 = Q_2/Q_1$ . Therefore, if  $Q_2$  is close to  $Q_1$ ,  $\eta$  approaches to 1. In the previous work, the value of  $Q_2/Q_1$  is 0.75, which means  $\eta$  is not high [11]. On the other hand, in this work,

the value of  $Q_2/Q_1$  is high and it is 0.923 from Fig. 6: it is not just the same as  $\eta$  because  $E_1$  is not equal to  $E_2$  strictly.

Here, the resistance of the circuit  $R$  is discussed. In [11],  $R$  was  $3\ \Omega$ . This value is mainly due to the resistance of the wire on the breadboard and also the contact resistance between electronic components and the wire. On the other hand, due to the soldering,  $R$  in this article decreases to  $0.6\ \Omega$ . This results from the switching transistor resistance,  $0.2\ \Omega$ , inductor resistance,  $0.1\ \Omega$ , and the wire resistance,  $0.3\ \Omega$ .

As the resistance of pMOS and nMOS transistor is the same value as  $0.2\ \Omega$ , the energy dissipation of the circuit  $E_{diss}$  is calculated to be  $\int RI_C^2 dt$ . The  $R$  is  $0.6\ \Omega$ . The average current flowing into or from the capacitor is  $0.15\ \text{A}$  from Fig. 3. The charging time  $T$  is  $380\ \text{s}$ . Then,  $E_{diss}$  is estimated to be  $0.6 \times 0.15^2 \times 380 = 5.13\ \text{J}$ . During charging,  $W_1$  is  $118.4\ \text{J}$  and  $E_1$  is  $113.0\ \text{J}$ . Then,  $E_{diss}$  is calculated as  $W_1 - E_1 = 5.4\ \text{J}$ , which is almost consistent with the estimated value. During discharging,  $E_2$  is  $114.4\ \text{J}$  and  $W_2$  is  $109.3\ \text{J}$ . In this case,  $E_{diss}$  is calculated as  $E_2 - W_2 = 5.1\ \text{J}$ , which is consistent with the estimated value. This discussion shows that the circuit resistance  $0.6\ \Omega$  is valid.

If SiC transistors and the inductor with the lower resistance are used, it will reduce  $R$  more. The charging circuit with the low resistance would enable a large current flow. This means high speed operation would be possible.

Next, the theoretical charging efficiency  $\eta_{1th}$  is discussed. Here,  $V_C$  is assumed to change from  $2V/3$  to  $V$ , which is the same as the experimental situation. The stepwise value of  $V_C$  is changed as  $2V/3$ ,  $17V/24$ ,  $18V/24$ , ...,  $23V/24$ , and  $24V/24$ . In the first step during charging,  $V_C$  is charged from  $2V/3$  to  $17V/24$ . Then, the charge amount of  $CV/24$  flows into capacitor. The  $d$  is  $2/3 + 1/24 = 17/24$ , so the charge amounts from the power supply and GND are  $17CV/24^2$  and  $7CV/24^2$ , respectively [9]. We define  $W_{si}$  as the work done by the power supply during the  $i$ th step charging. Then,  $W_{s1}$  during the first step is written as  $W_{s1} = 17CV^2/24^2$ . Similarly, in the second step,  $V_C$  is charged from  $17V/24$  to  $18V/24$ , and the charge amount of  $CV/24$  flows into capacitor. From  $d = 18/24$ , the charge amount from the power supply is  $18CV/24^2$ . Therefore,  $W_{s2}$  during the second step is written as  $W_{s2} = 18CV^2/24^2$ . Then, the total work  $W_{s1-8}$  during charging is calculated as  $W_{s1-8} = (17 + 18 + \dots + 23 + 24)CV^2/24^2 = 41CV^2/144$ . On the other hand,  $E_1$  is written as  $E_1 = C(V^2 - 4V^2/9)/2 = 5CV^2/18$ . Therefore,  $\eta_{1th}$  is calculated to be  $\eta_{1th} = E_1/W_{s1-8} = 97.6\%$ . This value is almost consistent with the experimental value. The theoretical discharging efficiency  $\eta_{2th}$  is calculated in the same way and it is  $97.5\%$ ,

which is also almost consistent with the experiment.

Next, we consider the situation that the step width is not equal. Here, the following case of  $V_C$  change is considered:  $2V/3$ ,  $2V/3$ ,  $13V/18$ ,  $13V/18$ ,  $14V/18$ ,  $15V/18$ ,  $16V/18$ ,  $17V/18$ ,  $18V/18$ , which is the same as the six-step charging. In this case,  $\eta_{1th}$  is similarly calculated to be  $96.8\%$ . Therefore, inequality of the steps causes the decrease in charging efficiency. However, this decrease is very small and negligible in eight-step charging.

In this experiment, the high  $\eta$  value is realized. It is due to the realization of low resistance in the circuit due to setting on a printed wiring board. This high efficiency shows the proposed circuit is suitable for an energy storage application.

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