



# Analyzing slowdown and meltdowns in the African countries: New evidence using Fourier quantile unit root test



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## ARTICLE INFO

### JEL classification:

C22  
O47  
O55

### Keywords:

GDP per capita  
Unit root  
Quantile regression  
Fourier expansion  
Smooth breaks  
Africa

## ABSTRACT

In this paper, we analyze growth dynamics in the 25 African countries over the period 1950–2016. To this end, first, we test the stochastic properties of real per capita GDP series. While conventional unit root and standard quantile unit root tests do not reject a unit root, using a novel quantile unit root test which allows for smooth breaks, we could find the results in favor of trend stationarity of 16 out of 25 real per capita GDP series. Our results indicate that in some countries positive shocks to real per capita GDP series have permanent effect and in some of them, the negative shocks. Whereas all of African countries in our sample specialized in producing and exporting primary products, hence to have favorable growth performance, they have to manage terms of trade shocks to avoid large swings in the real per capita GDP.

## 1. Introduction

Economic theories offer different explanations for one of the stylized facts in the postwar growth literature namely stability of growth process. While neoclassical growth theory predicts the output per capita of countries converge to steady state and when approach to the station, the economy will grow at a long-run constant rate. Hence the theory predicts that all shocks to the income per capita have transitory effect. In contrast, the endogenous growth theories pioneered by Romer (1986), Lucas (1988), Grossman and Helpman (1991), and Aghion and Howitt (1992) predict that due to spillover effects of physical capital, human capital, and research and development activities, the economy will growth in a permanent increasing rate. Empirical studies prepared mixed findings on output per capita dynamics. While Kaldor (1961) found evidence for sustainable growth rate over the postwar period, Romer (1986) and Maddison (1982) found evidence for increasing growth rates.

Most of empirical studies on stability of economic growth process, used unit root/stationary tests. Ben-David and Papell (1995) tested the growth stability for 16 OECD countries using Vogelsang's (1997) test approach and found most of OECD countries experienced increasing growth rate over post world wars I and II. Ben-David and Papell (1998) tested the growth stability for 74 countries over the post wars. The findings indicate that most of developing countries especially for Latin American countries experienced growth slowdown over the 1980s. Ben-David, Lumsdaine, and Papell (2003) using Lumsdaine and Papell (1997) unit root test with two sharp

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<https://doi.org/10.1016/j.iref.2019.10.008>

Received 9 June 2018; Received in revised form 28 September 2019; Accepted 17 October 2019

Available online 23 October 2019

1059-0560/© 2019 Published by Elsevier Inc.

**Table 1**  
Dynamics and distribution of RPCGDP.

| Country       | Panel A: Average real GDP per capita |             |             |             |             |             |             | Panel B: Statistical properties |          |          |                     |
|---------------|--------------------------------------|-------------|-------------|-------------|-------------|-------------|-------------|---------------------------------|----------|----------|---------------------|
|               | 1950s                                | 1960s       | 1970s       | 1980s       | 1990s       | 2000s       | 2010s       | Standard deviation              | Skewness | Kurtosis | Jarque-Bera P-Value |
| Algeria       | 1530                                 | 1840        | 2548        | 3220        | 2754        | 3302        | 3738        | 0.316                           | -0.614   | 2.139    | 0.043               |
| Angola        | 1136                                 | <u>1522</u> | 1359        | 828         | 716         | 1091        | 1452        | 0.337                           | -0.054   | 1.764    | 0.117               |
| Burkina Faso  | 534                                  | 681         | 723         | 786         | 869         | 1084        | 1174        | 0.282                           | 0.286    | 2.454    | 0.418               |
| Cameroon      | 746                                  | 882         | 1039        | 1452        | 1035        | 1091        | 1046        | 0.209                           | 0.108    | 2.872    | 0.916               |
| Côte d'Ivoire | 1118                                 | <u>1533</u> | <u>1867</u> | 1760        | 1339        | 1262        | 1195        | 0.190                           | 0.236    | 1.847    | 0.115               |
| DR Congo      | 704                                  | 748         | 735         | <u>575</u>  | <u>327</u>  | <u>207</u>  | <u>237</u>  | 0.514                           | -0.522   | 1.616    | 0.015               |
| Egypt         | 913                                  | 1129        | 1500        | <u>2351</u> | <u>2788</u> | <u>3542</u> | <u>3657</u> | 0.538                           | -0.137   | 1.542    | 0.046               |
| Ethiopia      | 412                                  | 521         | 614         | 607         | 504         | 607         | 852         | 0.252                           | 1.004    | 4.189    | 0.001               |
| Ghana         | 1204                                 | 1375        | 1324        | 1030        | 1188        | 1551        | 1948        | 0.233                           | 1.103    | 3.970    | 0.000               |
| Kenya         | 705                                  | 770         | 971         | 1047        | 1044        | 1043        | 1087        | 0.188                           | -0.521   | 2.393    | 0.132               |
| Madagascar    | 1042                                 | 1126        | 1129        | 854         | 695         | 686         | <u>610</u>  | 0.227                           | 0.014    | 1.342    | 0.022               |
| Malawi        | 359                                  | 410         | 569         | 578         | 581         | 633         | 673         | 0.247                           | -0.420   | 2.117    | 0.126               |
| Mali          | <u>492</u>                           | <u>551</u>  | <u>648</u>  | 698         | 742         | 954         | 973         | 0.264                           | 0.317    | 2.051    | 0.163               |
| Morocco       | <u>1442</u>                          | 1418        | <u>1846</u> | <u>2369</u> | <u>2740</u> | <u>3524</u> | <u>4008</u> | 0.406                           | 0.299    | 1.907    | 0.114               |
| Mozambique    | <u>1222</u>                          | 1412        | 1535        | 1069        | 1274        | 2236        | 2869        | 0.369                           | 0.993    | 2.987    | 0.004               |
| Niger         | 673                                  | 861         | 739         | 666         | <u>484</u>  | <u>481</u>  | <u>496</u>  | 0.222                           | 0.087    | 1.820    | 0.137               |
| Nigeria       | 819                                  | 842         | 1276        | 1070        | 1176        | 1746        | 2189        | 0.365                           | 0.753    | 2.699    | 0.037               |
| Senegal       | <u>1355</u>                          | 1474        | 1385        | 1281        | 1236        | 1412        | 1383        | 0.080                           | 0.088    | 2.019    | 0.250               |
| South Africa  | <u>2781</u>                          | <u>3478</u> | <u>4186</u> | <u>4123</u> | <u>3710</u> | <u>4395</u> | <u>4454</u> | 0.183                           | -0.546   | 2.691    | 0.166               |
| Sudan         | 907                                  | 968         | 949         | 876         | 858         | 1282        | 1313        | 0.204                           | 0.952    | 2.876    | 0.006               |
| Tanzania      | 451                                  | 505         | 600         | 553         | 531         | 646         | 742         | 0.189                           | 0.918    | 3.573    | 0.006               |
| Tunisia       | 1199                                 | <u>1571</u> | <u>2378</u> | <u>3065</u> | <u>3831</u> | <u>5428</u> | <u>5742</u> | 0.574                           | -0.098   | 1.789    | 0.123               |
| Uganda        | 676                                  | 773         | 785         | <u>575</u>  | 649         | 938         | 1090        | 0.241                           | 0.731    | 2.765    | 0.047               |
| Zambia        | 763                                  | 1016        | 1038        | 819         | 701         | 787         | 973         | 0.189                           | 0.058    | 1.796    | 0.130               |
| Zimbabwe      | 813                                  | 974         | 1334        | 1339        | 1360        | 1019        | 843         | 0.221                           | -0.311   | 1.794    | 0.077               |

Note: figure with double underline (underline) indicate countries which have the most (the least) average GDP per capita or yearly average value of GDP per capita. Data for decade 2010s cover the period 2010–2016.

breaks found about half of the countries experience postwar slowdowns and most of them exhibit faster growth after the second structural breaks. Chang, Chu, and Ranjbar (2014) tested the stochastic properties of real per capita GDP of African countries using sequential panel selection method and found that real GDP per capita are stationary in 50 out of the 52 African countries. More recently, Ranjbar, Li, Chang, and Lee (2015) test growth stability in East Asian region using panel stationarity test with a sharp break. Their findings indicate that most of countries experienced a growth slowdown after structural breaks (which related to Asian financial crisis for some countries).

Regarding the African countries, there are scarce literature (to the best of our knowledge, only Ben-David and Papell (1998)) investigated the growth stability in the countries. While sustained and a substantial economic growth is a pre-request to reduce the poverty in the countries. Since the early 1990s many African countries have been on a trajectory of higher growth, so, African poverty, infrastructure, education access and infant mortality have improved significantly. In a recent study, Sy (2016) point out that: "If the region was able to regain its 2004–2014 growth rate GDP per capita could be doubled in 20.5 years, by 2036. In contrast, at a growth rate of 1.4% as currently predicted, this achievement would only be realized in 50 years, by the year 2065". Economic growth across the region is likely to remain slower in coming years than it has been over the past 10–15 years. The International Monetary Fund's (IMF) baseline projection for 2016 is now down to 3%, from what was a forecasted 6.1% in April 2015(1). The main reasons for a relative slowdown are not unique to Africa and are the same as those weighing down the global economy: a general slowdown in emerging market economies, and in particular the rebalancing of China's economy; ongoing stagnation in most developed economies; lower commodity prices, especially softening oil prices; and higher borrowing costs.

However, although growth in region has relatively slowed, two-thirds of Sub-Saharan African economies are still growing at rates above the global average, and will remain the second fastest-growing region in the world for the foreseeable future, after Emerging Asia. This is further supported by the year-on-year increase in FDI project numbers in Africa in 2015 that occurred in a context in which the total number of FDI projects globally dropped by 5%. In fact, Africa was one of only two regions in the world in which there was growth in the number of FDI projects over the past year.

To fill the gap in the economic growth literature regarding to stability of growth in the African countries, in this paper, we analyze growth stability in the countries over the period 1950–2016. To this end, we use a novel quantile unit root test that developed by Bahmani-Oskooee, Chang, Elmi, and Ranjbar (2018a). The test has several advantages over traditional unit root and standard quantile unit root test. First, exogenous growth theory predicts that output per capita converge toward a steady state level. Thus whether it is above or below the steady state level, may show different (or asymmetric) behavior to shocks. Without specification of a special assumption regarding the functional form of nonlinearities, using the quantile regression, we able to allow for different speed of adjustment at various quantiles of output per capita distribution and capture its asymmetric behavior. Second, as noted by Basu, Calamitsis, and Ghura (2005), most of African countries involve(d) in the civil wars, armed conflicts, and political instabilities and also most of them specialize in the producing and exporting primary products, therefore, there is possible that their output per capita experience breaks in various times. To capture the nonlinearities, the Bahmani-Oskooee et al. (2018a) test allows for smooth breaks in

**Table 2**  
Conventional, Fourier type, and quantile unit root test.

$$\Delta e_t = \varpi e_{t-1} + \sum_{i=1}^l \iota_i \Delta e_{t-i} + \xi_t$$

$$t_{KSS} = \frac{\hat{\varpi}}{se(\hat{\varpi})}$$

$$\Delta e_t = \varpi e_{t-1} + \sum_{i=1}^l \iota_i \Delta e_{t-i} + \xi_t$$

$$t_{ADF} = \frac{\hat{\varpi}}{se(\hat{\varpi})}$$

| Commodity     | Panel A: Conventional unit root tests |              |            |             | Panel B: Fourier type unit root tests |                | Panel C: Quantile unit root tests |      |      |      |
|---------------|---------------------------------------|--------------|------------|-------------|---------------------------------------|----------------|-----------------------------------|------|------|------|
|               | ADF                                   | DF-GLS       | PP         | NP          | FADF                                  | FKSS           | QKS                               | 10%  | 5%   | 1%   |
| Algeria       | -1.899 (9)                            | -1.974 (9)   | -1.986 [5] | -5.860 [5]  | -4.364** (9)                          | -3.718** (9)   | 1.626                             | 3.17 | 3.66 | 4.23 |
| Angola        | -1.378 (6)                            | -1.600 (6)   | -0.936 [3] | -3.095 [3]  | -5.382*** (11)                        | -4.962*** (1)  | 3.198**                           | 2.87 | 3.01 | 3.29 |
| Burkina Faso  | -1.387 (10)                           | -1.855 (10)  | -1.688 [1] | -6.177 [1]  | -3.569 (10)                           | -3.995* (1)    | 1.472                             | 3.03 | 3.27 | 4.65 |
| Cameroon      | -1.774 (9)                            | -1.428 (9)   | -1.919 [5] | -4.888 [5]  | -3.634 (11)                           | -3.425* (8)    | 9.367***                          | 2.76 | 3.3  | 3.74 |
| Côte d'Ivoire | -2.034 (2)                            | -1.528 (2)   | -1.856 [4] | -2.675 [4]  | -4.037* (8)                           | -2.181 (11)    | 2.569                             | 3.4  | 3.89 | 4.74 |
| DR Congo      | -1.804 (3)                            | -1.948 (3)   | -1.999 [5] | -3.485 [5]  | -4.035* (11)                          | -2.092 (11)    | 1.719                             | 3.26 | 3.72 | 6.92 |
| Egypt         | -2.275 (1)                            | -2.170 (1)   | -1.933 [4] | -5.756 [4]  | -4.642** (6)                          | -4.603** (1)   | 2.155                             | 3.22 | 3.63 | 5.95 |
| Ethiopia      | -2.732 (10)                           | -2.977 (10)  | -0.371 [4] | -2.177 [4]  | -2.048 (7)                            | -0.433 (7)     | 1.917                             | 3.36 | 3.54 | 3.98 |
| Ghana         | -1.460 (8)                            | -2.148 (8)   | 0.033 [4]  | -0.743 [4]  | -4.131** (11)                         | -5.281*** (3)  | 2.824                             | 3.62 | 4.05 | 5.24 |
| Kenya         | -2.813 (9)                            | -2.476 (9)   | -2.052 [0] | -6.662 [0]  | -3.557 (9)                            | -1.759 (7)     | 1.537                             | 3.13 | 3.47 | 3.81 |
| Madagascar    | -1.788 (8)                            | -1.339 (0)   | -2.253 [3] | -2.974 [3]  | -2.831 (11)                           | -5.897** (3)   | 2.421                             | 3.22 | 3.38 | 4.4  |
| Malawi        | -1.838 (3)                            | -1.599 (3)   | -2.133 [3] | -6.701 [3]  | -3.604 (5)                            | -4.254** (5)   | 2.076                             | 3.57 | 3.97 | 4.87 |
| Mali          | -2.859 (0)                            | -2.927 (0)   | -2.790 [1] | -13.114 [1] | -1.919 (6)                            | -4.093*** (11) | 2.207                             | 3.01 | 3.59 | 4.08 |
| Morocco       | -2.649 (10)                           | -2.211 (10)  | -2.476 [4] | -1.426 [4]  | -1.505 (10)                           | -2.03 (3)      | 2.916                             | 3.6  | 4.02 | 5.87 |
| Mozambique    | -2.234 (9)                            | -2.614 (9)   | -0.345 [4] | -1.244 [4]  | -4.229** (9)                          | -3.04 (9)      | 1.667                             | 3.18 | 3.69 | 4.31 |
| Niger         | -2.256 (9)                            | -2.022 (9)   | -1.874 [4] | -4.451 [4]  | -4.250** (9)                          | -0.937 (10)    | 1.808                             | 3.32 | 3.47 | 3.93 |
| Nigeria       | -1.937 (5)                            | -2.077 (5)   | -1.441 [2] | -5.083 [2]  | -1.968 (5)                            | -2.606 (5)     | 1.987                             | 3.63 | 4.23 | 6.18 |
| Senegal       | -1.295 (0)                            | -1.066 (4)   | -0.992 [2] | -3.331 [2]  | -5.809*** (0)                         | -1.688 (10)    | 1.988                             | 2.84 | 2.99 | 3.24 |
| South Africa  | -4.194** (10)                         | -2.076 (6)   | -1.764 [4] | -2.650 [4]  | -3.208 (1)                            | -1.881 (1)     | 1.682                             | 2.88 | 3.29 | 3.68 |
| Sudan         | -2.238 (6)                            | -2.358 (6)   | -1.182 [0] | -3.675 [0]  | -3.352 (9)                            | -2.508 (6)     | 1.674                             | 2.85 | 3.12 | 3.79 |
| Tanzania      | -1.831 (8)                            | -2.123 (8)   | -0.394 [5] | -2.197 [5]  | -0.021 (11)                           | 1.923 (11)     | 2.614                             | 3.63 | 4.43 | 5.25 |
| Tunisia       | -3.001 (9)                            | -3.422** (9) | -2.500 [3] | -10.909 [3] | -0.999 (10)                           | -0.94 (10)     | 2.307                             | 3.68 | 4.14 | 4.73 |
| Uganda        | -2.131 (6)                            | -2.324 (6)   | -0.378 [3] | -1.009 [3]  | -4.293** (7)                          | -2.683 (6)     | 1.427                             | 3.05 | 3.43 | 4.05 |
| Zambia        | -2.493 (9)                            | -3.027 (9)   | -1.109 [4] | -2.586 [4]  | -3.407 (11)                           | -1.372 (10)    | 2.892                             | 3.1  | 3.27 | 4.99 |
| Zimbabwe      | -0.941 (7)                            | -1.621 (5)   | -1.734 [3] | -2.538 [3]  | -5.032*** (5)                         | -3.525* (5)    | 2.063                             | 3.23 | 3.63 | 4.1  |

Note:

(1) [Christopoulos and Leon-Ledesma \(2011\)](#) developed a new version of [Kapetanios, Shin, and Snell \(2003\)](#), KSS) and ADF unit root tests which allows for smooth breaks using Fourier function. To this end, first we obtain estimates of the residuals from equation (1) which was denoted by  $e_t$  in the text and then test the null hypothesis of a unit root using KSS-Fourier unit root test, we obtain the t-statistic from the following equation:

The test statistic is calculated as follows:

To test the null hypothesis of a unit root using ADF-Fourier unit root test, we obtain the t-statistic from the following equation:

(3) We determine optimum lag(s) for ADF, DF-GLS, FADF, FKSS, and QKS unit root tests based on the recursive t-statistic. For the Ng-Perron and PP tests, we select bandwidth by the Bartlett Kernel.

(3) We computed critical values for FADF and FKSS using Monte Carlo simulation and 5000 replications as described in [Christopoulos and Leon-Ledesma \(2011\)](#) and [Becker, Enders, and Lee \(2006\)](#). To save the space, we did not report them but they are available from the authors upon request. Also, we computed the critical values for QKS unit root test using Monte Carlo simulations and 5000 replications.

(4) \*, \*\*, and \*\*\* denote the null of unit root is rejected at 10%, 5%, and 1%, respectively.

the trend function components using Fourier expansion. Whereas we use annual GDP per capita as proxy for output per capita and due to it has low frequency, we think using Fourier expansion, we are able to capture breaks in the GDP per capita. Third, as explained, due to various factors, GDP per capita series may be experience breaks in some years and thus may be they have outliers that using the quantile regression, we are able to control for non-normality distribution and for the presence of such outliers.

The rest of the paper proceeds as follows. Section 2 prepare the data, section 3 discusses the methodology. The empirical results are discussed in Section 4. In section 5, we speak about growth dynamics and conclusion is presented in the final section.

## 2. Data

We use Maddison Project Database of annual per capita real GDP in 1990 PPP-adjusted dollars for 25 African countries over the

**Table 3**  
OLS estimator's results of equation (1).

| Countries     | k   | Coefficients |            |            |            | t-student statistics |            |            |            | F statistics | critical values |       |        |
|---------------|-----|--------------|------------|------------|------------|----------------------|------------|------------|------------|--------------|-----------------|-------|--------|
|               |     | $\alpha_1$   | $\alpha_2$ | $\alpha_3$ | $\alpha_4$ | $\alpha_1$           | $\alpha_2$ | $\alpha_3$ | $\alpha_4$ |              | 90%             | 95%   | 99%    |
| Algeria       | 1.4 | 7.368        | 0.015      | -0.123     | -0.092     | 349.394              | 27.702     | -8.334     | -6.096     | 53.863       | 3.248           | 4.209 | 6.405  |
| Angola        | 1.2 | 6.815        | 0.005      | 0.483      | -0.110     | 193.403              | 5.118      | 19.374     | -4.629     | 187.805      | 8.214           | 9.885 | 13.763 |
| Burkina Faso  | 1.2 | 6.164        | 0.015      | 0.101      | -0.020     | 519.525              | 49.421     | 11.998     | -2.527     | 71.979       | 2.710           | 3.574 | 5.666  |
| Cameroon      | 1.4 | 6.744        | 0.007      | -0.167     | -0.085     | 289.437              | 11.786     | -10.231    | -5.102     | 65.921       | 3.683           | 4.821 | 7.293  |
| Côte d'Ivoire | 1.1 | 7.140        | 0.004      | 0.123      | -0.255     | 353.258              | 8.076      | 8.144      | -21.709    | 241.175      | 4.536           | 5.635 | 8.149  |
| DR Congo      | 1.3 | 6.883        | -0.021     | -0.036     | -0.332     | 223.009              | -26.172    | -1.699     | -14.932    | 116.730      | 5.712           | 7.191 | 10.200 |
| Egypt         | 1.5 | 6.665        | 0.028      | -0.062     | 0.069      | 493.830              | 80.653     | -6.364     | 7.392      | 47.296       | 2.677           | 3.589 | 5.571  |
| Ethiopia      | 1.5 | 6.080        | 0.008      | -0.066     | -0.208     | 270.217              | 14.681     | -4.093     | -13.330    | 97.541       | 4.184           | 5.247 | 7.699  |
| Ghana         | 1.1 | 6.800        | 0.011      | 0.286      | 0.106      | 408.331              | 25.384     | 23.074     | 10.919     | 403.265      | 4.932           | 6.101 | 9.431  |
| Kenya         | 1.5 | 6.584        | 0.009      | -0.100     | -0.031     | 689.885              | 35.402     | -14.520    | -4.721     | 116.964      | 2.826           | 3.653 | 5.864  |
| Madagascar    | 1.3 | 7.078        | -0.009     | 0.060      | -0.147     | 616.869              | -30.075    | 7.565      | -17.784    | 174.852      | 3.203           | 4.135 | 6.426  |
| Malawi        | 1.5 | 5.911        | 0.011      | -0.094     | -0.069     | 381.211              | 28.784     | -8.366     | -6.411     | 55.859       | 2.821           | 3.738 | 5.839  |
| Mali          | 2.3 | 6.106        | 0.013      | 0.025      | 0.047      | 437.879              | 36.286     | 2.615      | 4.780      | 15.638       | 2.386           | 3.184 | 5.125  |
| Morocco       | 2.2 | 7.036        | 0.020      | 0.053      | 0.083      | 561.776              | 62.571     | 5.994      | 9.585      | 70.243       | 2.797           | 3.717 | 5.871  |
| Mozambique    | 1.2 | 6.735        | 0.016      | 0.395      | 0.041      | 248.400              | 23.259     | 20.613     | 2.214      | 235.290      | 6.932           | 8.514 | 11.791 |
| Niger         | 1   | 6.410        | 0.001      | 0.311      | -0.048     | 244.802              | 1.254      | 15.671     | -3.859     | 127.755      | 3.867           | 4.923 | 7.378  |
| Nigeria       | 2   | 6.629        | 0.014      | -0.164     | 0.099      | 197.115              | 15.810     | -6.846     | 4.483      | 33.014       | 3.594           | 4.566 | 6.714  |
| Senegal       | 1.2 | 7.148        | 0.002      | 0.116      | -0.013     | 891.334              | 9.548      | 20.388     | -2.372     | 209.859      | 2.881           | 3.783 | 6.003  |
| South Africa  | 1.5 | 8.023        | 0.007      | -0.063     | -0.127     | 1054.728             | 37.292     | -11.483    | -24.060    | 356.991      | 3.147           | 4.081 | 6.252  |
| Sudan         | 1.2 | 6.604        | 0.008      | 0.197      | 0.037      | 267.721              | 12.896     | 11.263     | 2.225      | 74.620       | 3.716           | 4.725 | 6.833  |
| Tanzania      | 1.7 | 6.144        | 0.006      | -0.116     | -0.079     | 426.653              | 16.404     | -11.561    | -7.911     | 103.875      | 3.096           | 4.167 | 6.521  |
| Tunisia       | 2.2 | 6.969        | 0.029      | -0.035     | 0.061      | 623.109              | 99.390     | -4.481     | 7.925      | 38.320       | 2.552           | 3.314 | 5.119  |
| Uganda        | 1.2 | 6.275        | 0.010      | 0.293      | 0.016      | 329.134              | 19.647     | 21.705     | 1.268      | 253.721      | 4.917           | 6.209 | 9.036  |
| Zambia        | 1.2 | 6.595        | 0.005      | 0.248      | -0.181     | 460.727              | 13.310     | 24.447     | -18.656    | 393.572      | 4.690           | 5.914 | 8.783  |
| Zimbabwe      | 0.8 | 6.825        | 0.003      | 0.182      | -0.261     | 109.437              | 1.608      | 4.651      | -8.536     | 112.922      | 4.829           | 6.040 | 9.034  |

Note: k\* is optimum frequency. The critical values for F statistics are computed using Monte Carlo simulation.

**Table 4**  
Fourier quantile unit root test results.

| Country       | Panel A: P – values of $t_{\tau_1}(\tau_i)$ |       |       |       |       |       |       |       |       | Panel B: Fourier QKS statistic |      |      |      |
|---------------|---|-------|-------|-------|-------|-------|-------|-------|-------|--------------------------------|------|------|------|
|               | 0.1   | 0.2   | 0.3   | 0.4   | 0.5   | 0.6   | 0.7   | 0.8   | 0.9   | FQKS                           | 10%  | 5%   | 1%   |
| Algeria       | 0.170                                       | 0.260 | 0.050 | 0.040 | 0.050 | 0.140 | 0.400 | 0.200 | 0.400 | 2.477                          | 3.23 | 3.65 | 4.64 |
| Angola        | 0.020                                       | 0.170 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.020 | 0.180 | 3.673**                        | 2.93 | 3.6  | 5.2  |
| Burkina Faso  | 0.220                                       | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.100 | 0.140 | 0.140 | 4.676***                       | 3.02 | 3.28 | 3.54 |
| Cameroon      | 0.080                                       | 0.050 | 0.000 | 0.010 | 0.000 | 0.000 | 0.030 | 0.030 | 0.070 | 3.972**                        | 3.33 | 3.77 | 5.47 |
| Côte d'Ivoire | 0.600                                       | 0.440 | 0.070 | 0.090 | 0.140 | 0.010 | 0.000 | 0.000 | 0.000 | 5.572***                       | 3.37 | 3.67 | 4.68 |
| DR Congo      | 0.140                                       | 0.130 | 0.050 | 0.020 | 0.200 | 0.220 | 0.180 | 0.510 | 0.280 | 2.929                          | 3.53 | 4.48 | 5.05 |
| Egypt         | 0.010                                       | 0.010 | 0.130 | 0.220 | 0.110 | 0.160 | 0.400 | 0.070 | 0.210 | 3.323**                        | 3.03 | 3.29 | 4.6  |
| Ethiopia      | 0.290                                       | 0.360 | 0.290 | 0.150 | 0.800 | 0.860 | 0.890 | 0.970 | 0.500 | 2.033                          | 3.68 | 3.9  | 5.22 |
| Ghana         | 0.000                                       | 0.010 | 0.020 | 0.000 | 0.000 | 0.020 | 0.160 | 0.410 | 0.770 | 4.806**                        | 3.72 | 4.43 | 4.94 |
| Kenya         | 0.130                                       | 0.050 | 0.040 | 0.050 | 0.070 | 0.010 | 0.000 | 0.000 | 0.000 | 4.575***                       | 3.29 | 3.75 | 4.53 |
| Madagascar    | 0.050                                       | 0.000 | 0.010 | 0.000 | 0.320 | 0.210 | 0.710 | 0.880 | 0.650 | 2.951*                         | 2.75 | 2.99 | 3.83 |
| Malawi        | 0.490                                       | 0.450 | 0.280 | 0.330 | 0.020 | 0.050 | 0.000 | 0.030 | 0.020 | 3.389*                         | 3.28 | 3.55 | 5.79 |
| Mali          | 0.060                                       | 0.070 | 0.070 | 0.050 | 0.190 | 0.150 | 0.080 | 0.000 | 0.010 | 4.335**                        | 2.79 | 3.31 | 4.48 |
| Morocco       | 0.400                                       | 0.570 | 0.470 | 0.160 | 0.080 | 0.080 | 0.250 | 0.210 | 0.030 | 3.117                          | 3.38 | 3.63 | 3.93 |
| Mozambique    | 0.070                                       | 0.070 | 0.080 | 0.040 | 0.020 | 0.000 | 0.010 | 0.100 | 0.550 | 3.681**                        | 3.01 | 3.65 | 5.01 |
| Niger         | 0.220                                       | 0.120 | 0.010 | 0.000 | 0.010 | 0.000 | 0.040 | 0.020 | 0.010 | 4.566***                       | 3.07 | 3.49 | 4.13 |
| Nigeria       | 0.530                                       | 0.600 | 0.470 | 0.900 | 0.930 | 0.610 | 0.630 | 0.640 | 0.250 | 1.85                           | 3.14 | 3.32 | 3.91 |
| Senegal       | 0.110                                       | 0.090 | 0.010 | 0.000 | 0.000 | 0.000 | 0.000 | 0.020 | 0.020 | 6.879***                       | 2.92 | 3.51 | 4.26 |
| South Africa  | 0.120                                       | 0.050 | 0.000 | 0.010 | 0.080 | 0.050 | 0.120 | 0.330 | 0.330 | 3.234*                         | 3.14 | 3.33 | 3.87 |
| Sudan         | 0.300                                       | 0.220 | 0.040 | 0.120 | 0.030 | 0.130 | 0.010 | 0.060 | 0.250 | 2.970*                         | 2.84 | 3.48 | 5.94 |
| Tanzania      | 0.120                                       | 0.100 | 0.050 | 0.030 | 0.380 | 0.460 | 0.630 | 0.800 | 0.640 | 2.854                          | 3.55 | 3.79 | 4.63 |
| Tunisia       | 0.710                                       | 0.690 | 0.300 | 0.240 | 0.300 | 0.680 | 0.120 | 0.110 | 0.100 | 2.269                          | 3.28 | 3.51 | 4.86 |
| Uganda        | 0.170                                       | 0.580 | 0.300 | 0.480 | 0.250 | 0.230 | 0.130 | 0.020 | 0.470 | 2.799                          | 3.27 | 3.69 | 4.31 |
| Zambia        | 0.030                                       | 0.090 | 0.010 | 0.230 | 0.150 | 0.110 | 0.020 | 0.030 | 0.170 | 2.711                          | 2.99 | 3.46 | 4.19 |
| Zimbabwe      | 0.330                                       | 0.210 | 0.060 | 0.000 | 0.000 | 0.000 | 0.000 | 0.030 | 0.180 | 5.042***                       | 3.36 | 3.89 | 4.43 |

Notes: The P - values for  $t_{\tau_1}(\tau_i)$  and critical values for F-QKS statistics computed using bootstrapping procedure and 5000 replications.

period 1950–2016 which was prepared by [The Conference Board \(2016\)](#). Our sample includes Algeria, Angola, Burkina Faso, Cameroon, Côte d'Ivoire, DR Congo, Egypt, Ethiopia, Ghana, Kenya, Madagascar, Malawi, Mali, Morocco, Mozambique, Niger, Nigeria, Senegal, South Africa, Sudan, Tanzania, Tunisia, Uganda, Zambia, and Zimbabwe.

### 3. Methodology

To analyze the slowdowns, meltdowns and long run growth, we have to test the stochastic properties of RPCGDP series and then estimate a trend function. Due to non-normal distribution of and structural breaks in the RPCGDP series, application of quantile type unit root test will appropriate for the case. First candidate will be the standard quantile unit root test which developed by [Koenker and Xiao \(2004\)](#). But whereas most of African countries experienced wars, political instability and also huge shocks to their terms of trade over the period, we would like to allow for breaks in the trend component. To this end, we apply a new versions of quantile unit root test which developed by [Bahmani-Oskooee et al. \(2018a\)](#)<sup>1</sup> and [Bahmani-Oskooee, Chang, and Ranjbar \(2017\)](#) allows for smooth breaks in the trend components. In this section we prepare a short account of the test.

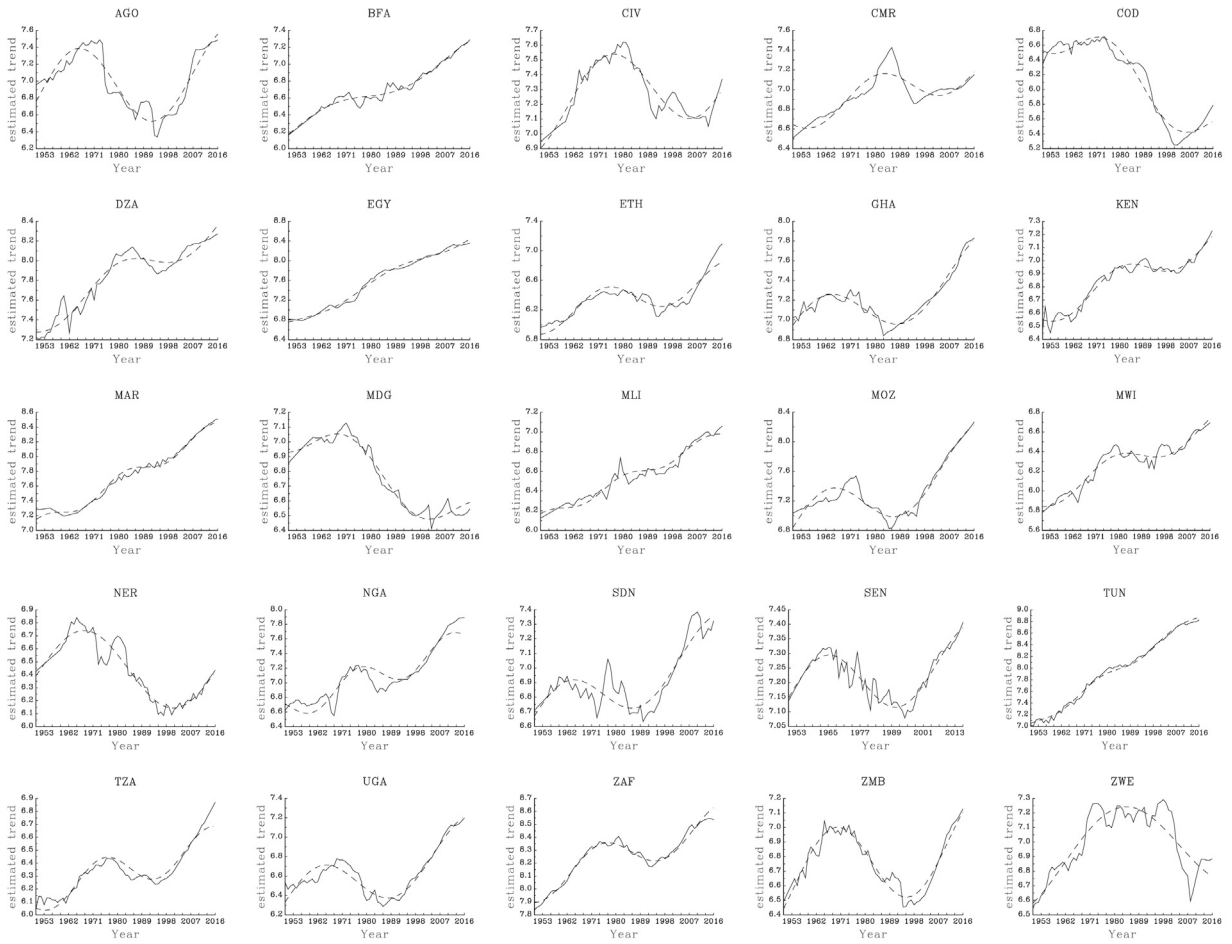
We present time series variable  $RPCGDP_t$  with unknown number and form of break points by a Fourier expansion as follows:

$$RPCGDP_t = \alpha_1 + \alpha_2 t + \alpha_3 \sin\left(\frac{2\pi kt}{N}\right) + \alpha_4 \cos\left(\frac{2\pi kt}{N}\right) + o_t \quad (1)$$

Where  $\alpha$ ,  $N$ , and  $t$  are vector of coefficients, sample size and a trend term, respectively, and  $\pi = 3.1416$ .  $o_t$  is the residuals of regression models.<sup>2</sup>  $K$  is the number of frequencies of the Fourier function and apply in the model to capture the smooth breaks in the  $RPCGDP_t$  series. The integer value of  $k$  related to transitory shocks and fractional value related to permanent shocks. To find the optimum frequency ( $k^*$ ), we consider  $k \in [0.1, 5]$  and using the [Becker, Enders, and Lee \(2004\)](#) method, set  $k$  at a value that minimizes the sum of squared residuals when OLS is applied to (1). Once  $k^*$  is determined, the residuals from (1) yields adjusted RPCGDP to which we apply the quantile unit root test. From equation (1), we define the  $\tau_{th}$  conditional quantile of  $\hat{o}_t$  as follows:

<sup>1</sup> Over the recent years, applications of quantile unit root test have increased to test the various economic hypothesis for example see [Bahmani-Oskooee, Chang, Elmi, and Ranjbar \(2018b\)](#), [Bahmani-Oskooee et al. \(2019\)](#), [Bahmani-Oskooee and Ranjbar \(2016\)](#), [Ma, Li, and Park \(2017\)](#).

<sup>2</sup> Various factors may be result in deviation of GDP per capita from its long run steady state situation. For example, interest rates, confidence, the credit cycle technological shocks, terms of trade shocks, wars, political and economic instabilities. Some of them have permanent effect and others have transitory effects.



**Fig. 1.** RPCGDP dynamics and fitted nonlinearities.

Note: Solid line is the RPCGDP series and dashed lines are estimated trend function (equation (2)). The abbreviations are: Algeria (DZA), Angola (AGO), Burkina Faso (BFA), Cameroon (CMR), Côte d'Ivoire (CIV), DR Congo (COD), Egypt (EGY), Ethiopia (ETH), Ghana (GHA), Kenya (KEN), Madagascar (MDG), Malawi (MWI), Mali (MLI), Morocco (MAR), Mozambique (MOZ), Niger (NER), Nigeria (NGA), Senegal (SEN), South Africa (ZAF), Sudan (SDN), Tanzania (TZA), Tunisia (TUN), Uganda (UGA), Zambia (ZMB), and Zimbabwe (ZWE).

$$Q_{\hat{\tau}_t}(\tau|\zeta_{t-1}) = \delta_0(\tau) + \delta_1(\tau)\hat{\tau}_{t-1} + \sum_{p=1}^{p^*} \delta_{1+p}(\tau)\Delta\hat{\tau}_{t-p} + \theta_t \tag{2}$$

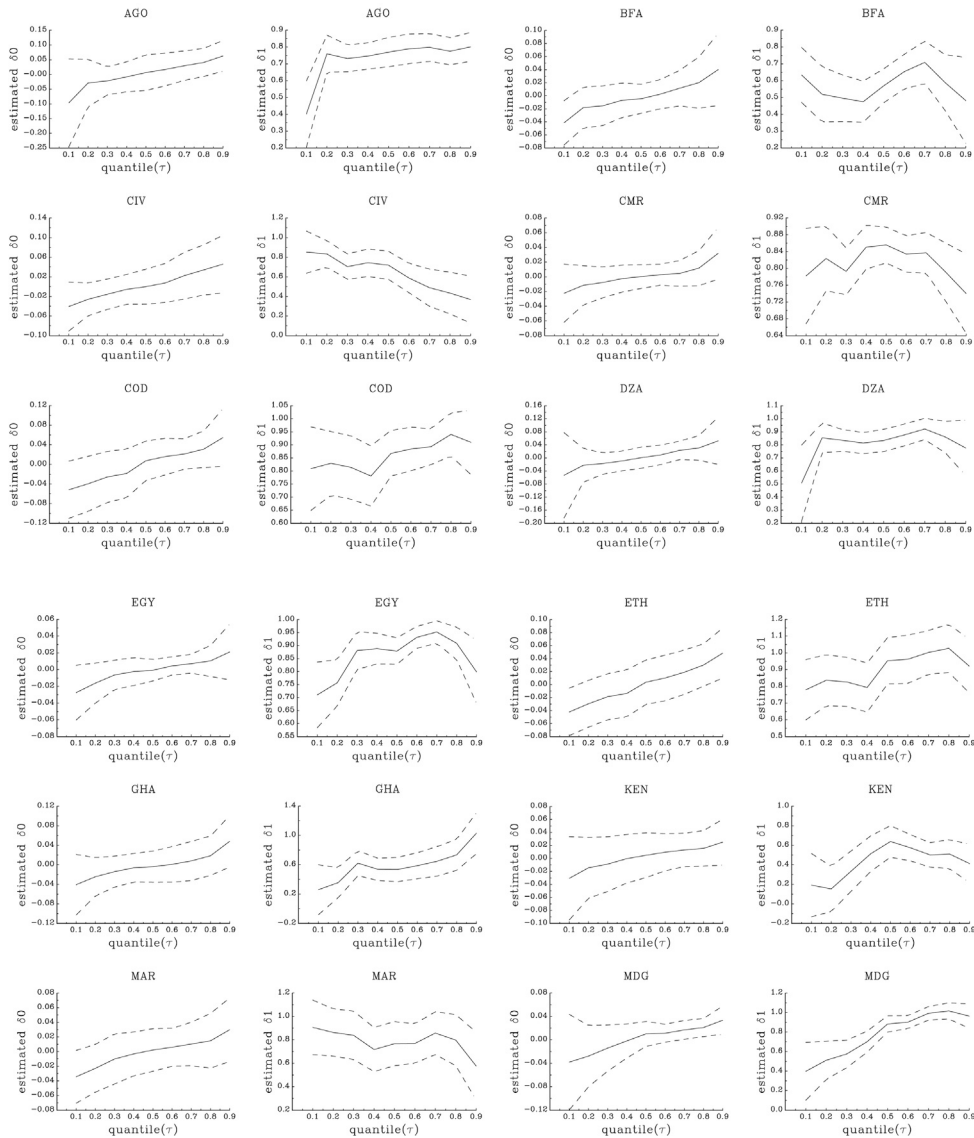
where  $Q_{\hat{\tau}_t}(\tau|\zeta_{t-1})$  is  $\tau_{th}$  quantile of  $\hat{\tau}_t$  conditional on the past information set,  $\zeta_{t-1}$ .  $\delta_0(\tau)$  is  $\tau_{th}$  conditional quantile of  $\theta_t$  and its estimated values captures the magnitude of RPCGDP shock in each quantile. Optimum lags ( $p^*$ ) are selected by the AIC information criteria. As noted by Tsong and Lee (2011), the intercept terms in the regression (2), i.e.  $\delta_0(\tau)$ , denotes the size of the observed shock within the  $\tau_{th}$  quantile that hits the GDP per capita. Negative (positive) sign represents negative (positive) shock which might result, for example, from terms of trade shocks, civil wars, political instabilities.

While equation (2) follows standard ADF test at each quantile, the special attention related to estimate the vector  $\delta$ . Following to Bahmani-Oskooee et al. (2018a), we use the following *t ratio* statistic to test the unit root hypothesis within the  $\tau_{th}$  quantile:

$$t_n(\tau_i) = \frac{\hat{f}(F^{-1}(\tau_i))}{\sqrt{\tau_i(1-\tau_i)}}(E_{-1}P_xE_{-1})^{1/2}(\hat{\delta}_1(\tau_i) - 1) \tag{3}$$

where  $E_{-1}$  is the vector of lagged dependent variable ( $\hat{\tau}_{t-1}$ ),  $P_x$  is the projection matrix onto the space orthogonal to  $X = (1, \Delta\hat{\tau}_{t-1}, \dots, \Delta\hat{\tau}_{t-k})$ .  $\hat{f}(F^{-1}(\tau_i))$  is a consistent estimator of  $f(F^{-1}(\tau_i))$ .<sup>3</sup> Bahmani-Oskooee et al. (2018a) recommend the following

<sup>3</sup> For details see Koenker and Xiao (2004).



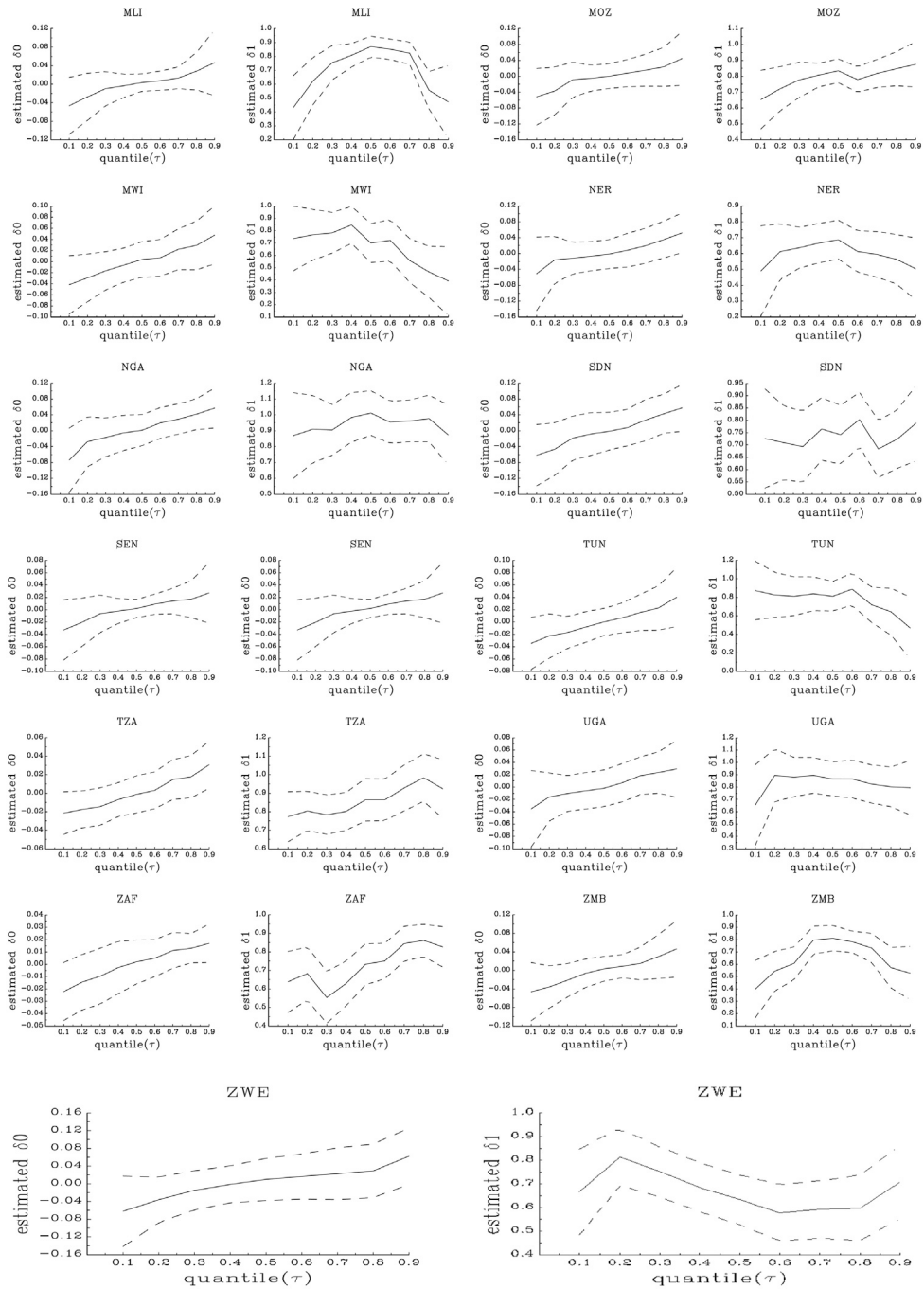
**Fig. 2.** Quantile intercepts ( $\delta_0(\tau)$ ) and autoregressive coefficients ( $\delta_1(\tau)$ ).  
 Note: Solid line is the values of  $\delta_1(\tau)$  and  $\delta_0(\tau)$  and dashed lines are 95% confidence intervals.

quantile Kolmogorov–Smirnov (FQKS) test statistics to assess the unit root behavior over a range of quantiles between  $\underline{\mu} = 0.1$  and  $\bar{\mu} = 0.9$ :

$$FQKS = \sup_{\tau_i \in [\underline{\mu}, \bar{\mu}]} |t_n(\tau)| \tag{4}$$

We construct the FQKS statistics by selecting maximum  $|t_n(\tau)|$  statistics over range quantiles between  $\underline{\mu} = 0.1$  and  $\bar{\mu} = 0.9$ . Due to nonstandard distribution of  $t_n(\tau_i)$  and FQKS test statistics, we compute their critical values using the re-sampling procedures which outlined in detail in Bahmani-Oskooee et al. (2018a). After rejection of unit root hypothesis for a RCGDP series, using the OLS estimated coefficients of equation (1), we compute its derivation for any year and then calculate the average its derivation for any decades as estimated growth rate using Fourier expansion. To analyze the meltdowns, slowdowns, and increasing growth, we use following method:

If average growth rate in decade t be positive and in decade t+1 be negative, in the case we say country experienced meltdowns over decade t+1. If average growth rate in decade t be positive and in decade t+1 be positive but less than period t, in the case, we say country experienced slowdowns in growth rate over decade t+1. If average growth rate in decade t be positive and in decade t+1 be positive but greater than period t, in the case, we say country experienced increasing growth rate over decade t+1.



Note: Solid line is the values of  $\delta_1(\tau)$  and  $\delta_0(\tau)$  and dashed lines are 95% confidence intervals.

Fig. 2. . (continued).

#### 4. Empirical results

We prepare average real per capita GDP (RPCGDP, hereafter) for any decade in panel A. We show the most value in any decade using double underline and the least value using underline. The results indicate countries namely, South Africa, Algeria, Morocco, Tunisia, and Egypt have the highest RPCGDP in our sample and in contrast the countries namely, Malawi, Tanzania, Ethiopia, DR Congo, and Niger have the lowest RPCGDP over most of decades. So over the 1950s, the RPCGDP of South Africa was 2781 \$ about 1.7 times RPCGDP of Malawi (which was 359 \$). The gap between richest and poorest countries in our sample increased to 24 fold over the 2010s, so, RPCGDP of Tanzania (richest country) and DR Congo (poorest country) were 5742 \$ and 237 \$. In panel B, we prepare statistical



**Table 5**  
Slowdowns and meltdowns in African countries growth rate.

| Country       | Average slope of Fourier trend function for any decade |       |       |       |       |       |       | Ratio of growth rates any decade to previous decade |               |             |             |             |             |
|---------------|--|-------|-------|-------|-------|-------|-------|---|---------------|-------------|-------------|-------------|-------------|
|               | 1950s  | 1960s | 1970s | 1980s | 1990s | 2000s | 2010s | 1960s–1950s   | 1970s to 1960 | 1980s–1970s | 1990s–1980s | 2000s–1990s | 2010s–2000s |
| Angola        | 5.4%   | 0.7%  | −4.2% | −3.8% | 1.4%  | 5.6%  | 4.6%  | 0.1   | −5.6          | 0.9         | −0.4        | 3.9         | 0.8         |
| Burkina Faso  | 2.5%   | 1.6%  | 0.6%  | 0.7%  | 1.8%  | 2.6%  | 2.4%  | 0.6   | 0.4           | 1.2         | 2.7         | 1.5         | 0.9         |
| Cameroon      | −0.2%  | 2.5%  | 2.5%  | −0.2% | −1.6% | 0.5%  | 2.7%  | −16.8   | 1.0           | −0.1        | 6.6         | −0.3        | 5.7         |
| Côte d'Ivoire | 2.8%   | 2.9%  | 0.6%  | −1.9% | −2.1% | 0.1%  | 2.4%  | 1.0   | 0.2           | −3.0        | 1.1         | −0.1        | 18.0        |
| Egypt         | 1.6%   | 2.5%  | 3.9%  | 3.4%  | 1.9%  | 1.8%  | 3.1%  | 1.6   | 1.6           | 0.9         | 0.5         | 1.0         | 1.7         |
| Ghana         | 3.0%   | 0.0%  | −1.8% | −0.8% | 2.1%  | 4.1%  | 3.5%  | 0.0   | −111.4        | 0.4         | −2.7        | 1.9         | 0.9         |
| Kenya         | 0.2%   | 1.9%  | 1.8%  | 0.1%  | −0.4% | 1.2%  | 2.3%  | 9.1   | 1.0           | 0.1         | −3.5        | −3.1        | 1.9         |
| Madagascar    | 0.7%   | 0.5%  | −1.5% | −2.7% | −1.5% | 0.5%  | 0.9%  | 0.7   | −3.0          | 1.8         | 0.6         | −0.3        | 1.8         |
| Malawi        | 0.9%   | 2.6%  | 1.8%  | −0.1% | 0.0%  | 2.0%  | 2.7%  | 2.9   | 0.7           | 0.0         | −0.5        | 63.4        | 1.4         |
| Mali          | 0.7%   | 1.0%  | 2.2%  | 0.6%  | 1.2%  | 2.1%  | 0.6%  | 1.5   | 2.1           | 0.3         | 2.2         | 1.8         | 0.3         |
| Mozambique    | 4.8%   | 0.5%  | −2.5% | −0.8% | 3.7%  | 5.9%  | 3.9%  | 0.1   | −5.2          | 0.3         | −4.6        | 1.6         | 0.7         |
| Niger         | 2.7%   | 0.9%  | −1.7% | −2.8% | −1.5% | 1.0%  | 2.7%  | 0.3   | −2.0          | 1.6         | 0.5         | −0.7        | 2.6         |
| Senegal       | 1.3%   | 0.1%  | −1.0% | −0.7% | 0.6%  | 1.4%  | 1.1%  | 0.1   | −7.8          | 0.8         | −0.8        | 2.5         | 0.8         |
| South Africa  | 1.3%   | 2.5%  | 0.7%  | −1.1% | 0.1%  | 2.3%  | 2.2%  | 2.0   | 0.3           | −1.5        | −0.1        | 23.2        | 0.9         |
| Sudan         | 2.3%   | 0.1%  | −1.3% | −0.2% | 2.0%  | 2.9%  | 1.8%  | 0.0   | −16.7         | 0.2         | −8.1        | 1.5         | 0.6         |
| Zimbabwe      | 2.3%   | 2.6%  | 1.6%  | 0.0%  | −1.5% | −2.0% | −1.5% | 1.1   | 0.6           | 0.0         | 98.1        | 1.4         | 0.7         |

Note: We calculate the yearly growth rate of RPCGDP using the derivation of estimated Fourier trend function, Equation (1). We compute the simple average yearly growth rate for any decades as average growth rate of decade.

properties (standard deviation, Skewness, Kurtosis, and P-Value of Jarque-Bera) of RPCGDP series. The Jarque–Bera test results indicate that 12 out of 25 RPCGDP series clearly exhibit a clear sign of non-normal distribution and as noted by [Koenker and Xiao \(2004\)](#), in the cases the quantile autoregressive based unit root test has higher power than conventional unit root tests.

To analyze the growth dynamics of African countries, first we have to test the stochastic properties of RPCGDP series (in logs form) (see [Table 1](#)). To this end, as a preliminary exercise we apply four conventional linear unit root test, including ADF, [Elliot, Rothenberg, Stock. \(1996, DF-GLS\)](#), [Phillips and Perron \(1988, PP\)](#), and Ng-Perron ([Ng & Perron, 2001](#)). The results of abovementioned tests are presented in panel A of [Table 2](#). As can be seen, using the ADF test, the null of unit root is rejected only for RPCGDP series of South Africa and using DF-GLS test, the null is rejected only for Tunisia. According to PP and NP unit root tests, the null of unit root is not reject for all RPCGDP series. As can be seen, using the conventional unit root tests, we could not find favorable results favor of stationary properties of RPCGDP series. It may relate to low power of conventional unit root tests when RPCGDP series exhibit structural breaks (due to wars or terms of trade's shocks) and/or non-normal distribution.

In panel B of [Table 2](#), we prepare the results for two Fourier type unit root tests namely Fourier-ADF (FADF) and Fourier-Kapetanios et al.'s (2003) (FKSS) which allows for smooth breaks using Fourier expansion in the ADF and KSS unit root tests. Using FADF unit root test, we could reject the null of unit root test for 11 out of 25 RPCGDP series including Algeria, Angola, Côte d'Ivoire, DR Congo, Egypt, Ghana, Mozambique, Niger, Senegal, Uganda, and Zimbabwe. Using to FKSS test, the null hypothesis of unit root is rejected for 10 out of 25 RPCGDP series including Algeria, Angola, Burkina Faso, Cameroon, Egypt, Ghana, Madagascar, Malawi, Mali, and Zimbabwe. As can be seen, inclusion of smooth breaks in the conventional unit root tests, we could find more evidence favor of stationary properties of RPCGDP series.

In panel C of [Table 2](#), we prepare the results for standard quantile unit root test proposed by [Koenker and Xiao \(2004\)](#) and its critical values at 10%, 5%, and 1%.<sup>4</sup> The results indicate that the null of unit root is rejected only for two countries Angola and Cameroon.

To incorporate the Fourier expansions in the quantile unit root tests, first we estimate equation (1) using OLS estimators. The results, coefficients, related t-student statistics, optimum frequency, and F-statistics, are presented in [Table 3](#). After a grid-search we find the integer optimum frequency to be 1 ( $K^* = 1$ ) for RPCGDP of Niger and 2 ( $K^* = 2$ ) Nigeria. For other RPCGDP series, we found fractional and low frequencies. The results indicate almost RPCGDP series experienced permanent changes in the level and growth rates over the period. The results of the F statistics and its critical values for both sine and cosine terms indicate that these two terms should be included in the model for most of RPCGDP series. Dynamics of RPCGDP series and estimated nonlinear trend functions clearly show that the actual nature of break(s) (number and form of break(s)) is generally unknown (see [Fig. 1](#)) (see [Table 4](#)).

In the next step, using the OLS residuals from equation (1), we tested the unit root hypothesis using quantile regression. The results presented in [Table 3](#). The P-values of  $t_{\tau_i}(\tau_i)$  statistics are presented in panel A which are used to measure the degree of persistence in each quantile. Its results indicate that for RPCGDP series of Angola, Cameroon, Kenya, Mali, Mozambique, Niger, and Senegal, the null of unit root is rejected in most of quantiles. The values of  $\hat{\rho}_1(\tau)$  in [Fig. 2](#) indicate that the RPCGDP of abovementioned countries show three types response to shocks. The PCR GDP series of Angola and Niger show same response to negative and positive shocks. The RPCGDP series of Cameroon, Kenya, and Mali display concave patterns. So the negative shocks to RPCGDP of the countries have more long lasting effect than positive shocks. In contrast the values of  $\hat{\rho}_1(\tau)$  of RPCGDP series of Mozambique and Senegal show straight-line upward patterns, so positive shocks are more persistence than negative shocks.

For RPCGDP series of Burkina Faso, Ghana, Madagascar, South Africa, and Zambia, the null of unit root is rejected in low quantiles. The values of  $\hat{\rho}_1(\tau)$  of RPCGDP series of Ghana, Madagascar, and Zambia indicate straight-line upward patterns in low quantile, so greater negative shocks (in absolute values) are more transitory than moderate shocks. In contrast, The values of  $\hat{\rho}_1(\tau)$  of RPCGDP series of Ghana and South Africa show straight-line upward patterns in low quantile that indicate negative shocks to these RPCGDP series are more persistent than positive shocks.

For the RPCGDP series of Côte d'Ivoire, Malawi, and Zimbabwe, the null of unit root is rejected in high quantiles. The values of  $\hat{\rho}_1(\tau)$  of RPCGDP series of Côte d'Ivoire and Malawi indicate straight-line downward patterns in high quantile. The finding indicates positive shocks to the RPCGDP series of the countries have more transitory than moderate shocks. In contrast, the RPCGDP series of Zimbabwe indicate upward pattern in high quantiles that represent the positive shocks are more persistence than negative shocks.

## 5. Analyzing slowdowns and meltdowns in growth rates

To analyze the slowdowns and meltdowns in the growth rates of African countries, we use the coefficients of estimated Fourier-trend function in equation (2) for RPCGDP series that the null of unit root is rejected for them by Fourier quantile unit root test (i.e. 16 out of 25 series). According to the estimated coefficients of Equation (1), we calculate the its derivation for any year as estimated growth rate and calculate the average value of its derivation for any decades as average growth rate of any decade and prepare the results in [Table 5](#). According to the method presented in section 3, we decide about slowdowns and meltdowns. The results indicate that all of 16 African countries in our sample experienced positive growth rate over the decade 1960 and 1970 except Angola, Ghana, Madagascar, Mozambique, Niger, Senegal, and Sudan which experienced negative growth rate over the period 1970s. Also, all of them except Egypt and Mali (that had increasing growth rate) experienced slowdowns in growth rates over two decades 1960 and 1970. The evidence related to high growth performance of industrialized countries over the decades and high demand for primary products and whereas all of African countries specialized in produce and export of raw materials, hence experienced expansion in their terms of trade and increasing (slowdowns) positive growth rate. Due to by the recessionary period of the late 1970s and early 1980s in the industrialized

<sup>4</sup> We compute the critical values using re-sampling procedures which outlined in [Koenker and Xiao \(2004\)](#).

countries and deterioration of African countries terms of trade, 7 out of 16 countries, namely Angola, Ghana, Madagascar, Mozambique, Niger, Senegal, and Sudan, experienced meltdowns in the growth rate over the decade 1980.8 out of the countries namely, Cameroon, Côte d'Ivoire, Egypt, Kenya, Malawi, Mali, South Africa, and Zimbabwe experienced slowdowns in the RPCGDP growth rates. Only Burkina Faso had small increasing growth over the decade. As noted by Kaminski (2011, pp. 107–124), The cotton sector in Burkina Faso accounted for about 60 percent of its exports. Cotton booms over 1970s accelerate improvement infrastructure in the Burkina Faso since 1980s and also increase investment in the cotton sector to adapt new technology, high-quality research, cooperation between French and local researchers, farmer organizations, and top-down implementation policies.

Over two decades 1990s and 2000s, most countries experienced increasing growth rate, so over the decade 2000s, due to terms of trade boom from 2004 onwards, 14 out of 16 countries, experienced increasing growth rate. Egypt experienced slowdowns in the growth rate over the two decades 2000s and 2010s. Egypt experienced increasingly growth rate until 2008, so in 2008 it experienced highest growth rates over last three decades. But after the year, due to the global economic crisis (2007–2009) and “January 25th revolution” its growth rates lie in decreasing path Tsuchiya (2016). Zimbabwe experienced meltdowns in the growth rate from 1990s onward. Since 1997, Zimbabwe has been embroiled in an increasingly severe economic and political crisis including fiscal deficit, hyperinflation over 2004–2009, the government of land reform program, intimidation of the judiciary, and economic difficulties due to sanctions imposed by US and the EU (Sibanda & Makwata, 2017).

Over the recent decade 2010s, increasing growth rate in the African countries was stopped that may be related to the unfavorable terms of trade after huge reduction in the crude oil prices.<sup>5</sup>

Among African countries in our sample, six countries namely, Burkina Faso, Egypt, Kenya, Malawi, Mali, and South Africa do not experience negative growth rate (on the average) in any decades and among them, Malawi and Mali have experienced increasing growth rate over 4 decades. In contrast, Zimbabwe, Niger and Madagascar experienced meltdowns in the growth rate over 3, 2, and 2 decades, respectively. Some of unfavorable growth performance in African countries may be related to domestic political instability, military conflicts and wars, for example, Angola (1974), Madagascar (1971), and Mozambique (1974).

The major policy implications of our study is that to reduce the unfavorable growth performance in African countries, it is very important for the governments of the African countries (for those experienced meltdown growth) to set up policies to create a political stable environment, reduce the military conflicts and wars either in domestic or international and balance their terms of trade. As we know that a stable and secure environment is very important for the people to survive and work hard. War and military conflicts only damage the economic growth and the people living.

## 6. Conclusion

In this paper, we tested the stochastic properties of RPCGDP of African countries and their growth rates dynamics over the period 1950–2016. Using the conventional/quantile unit root tests, we could not find results favor of trend stationarity of RPCGDP series. But when we allow for both smooth breaks using Fourier expansion in the trend function and nonlinear response using quantile regression, we could find evidence in favor of trend stationarity for 16 out of 25 RPCGDP series. Our results indicate: (1) RPCGDP series of African countries response to shocks different behavior. In some of them the negative shocks have permanent effects and in some positive shocks. In some of them, both of two types shock have transitory effects. Our results indicate that due to negative shock from unfavorable terms of trade, most of African countries experienced meltdowns growth rate over the decades 1980s and 1990s. in contrast due to terms of trade booms over send half of 2000s, most of them experienced positive and increasing growth rate.

## Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.iref.2019.10.008>.

## References

- Aghion, P., & Howitt, P. (1992). A model of growth through creative destruction. *Econometrica*, 60(2), 323–351.
- Bahmani-Oskooee, M., Chang, T., Elmi, Z., & Ranjbar, O. (2018a). Re-testing prebisch-singer hypothesis: New evidence using fourier quantile unit root test. *Applied Economics*, 50(4), 441–454.
- Bahmani-Oskooee, M., Chang, T., Elmi, Z. M., & Ranjbar, O. (2018b). Re-examination of the convergence hypothesis among OECD countries: Evidence from Fourier quantile unit root test. *International economics*, 156, 77–85.
- Bahmani-Oskooee, M., Chang, T., & Ranjbar, O. (2017). The fourier quantile unit root test with an application to the PPP hypothesis in the OECD. *Applied Economics Quarterly (formerly: Konjunkturpolitik)*, 63(3), 295–317.
- Bahmani-Oskooee, M., & Ranjbar, O. (2016). Quantile unit root test and PPP: Evidence from 23 OECD countries. *Applied Economics*, 48(31), 2899–2911.
- Bahmani-Oskooee, M., Chang, T., Elmi, Z., & Ranjbar, O. (2019). Real interest rate parity and fourier quantile unit root test. *Bulletin of Economic Research*, 71(3), 348–358.
- Basu, A., Calamitsis, E. A., & Ghura, D. (2005). *Adjustment and growth in Sub-Saharan Africa*. Economic Issue is based on IMF Working Paper 99/51.
- Becker, R., Enders, W., & Lee, J. (2006). A stationarity test in the presence of an unknown number of smooth breaks. *Journal of Time Series Analysis*, 27(3), 381–409.
- Becker, R., Enders, W., & Lee, J. (2004). A general test for time dependence in parameters. *Journal of Applied Econometrics*, 19, 899–906.

<sup>5</sup> For more details on the relationship between primary commodity prices and the terms of trade, see Cashin and Pattillo (2006), Bidarkota and Crucini (2000), Collier, Gunning, and Associates (1999), and Romero-Avila (2009).

- Ben-David, D., Lumsdaine, R. L., & Papell, D. H. (2003). Unit roots, postwar slowdowns and long-run growth: Evidence from two structural breaks. *Empirical Economics*, 28(2), 303–319.
- Ben-David, D., & Papell, D. H. (1995). The great wars, the great crash, and steady state growth: Some new evidence about an old stylized fact. *Journal of Monetary Economics*, 36(3), 453–475.
- Ben-David, D., & Papell, D. H. (1998). Slowdowns and meltdowns: Postwar growth evidence from 74 countries. *The Review of Economics and Statistics*, 80, 561–571.
- Bidarkota, P., & Crucini, M. J. (2000). Commodity prices and the terms of trade. *Review of International Economics*, 8(4), 647–666.
- Cashin, P., & Pattillo, C. (2006). African terms of trade and the commodity terms of trade: Close cousins or distant relatives? *Applied Economics*, 38(8), 845–859.
- Chang, T., Chu, H. P., & Ranjbar, O. (2014). Are GDP fluctuations transitory or permanent in African countries? Sequential panel selection method. *International Review of Economics & Finance*, 29, 380–399.
- Christopoulos, D. K., & Leon-Ledesma, M. A. (2011). International output convergence, breaks, and asymmetric adjustment. *Studies in Nonlinear Dynamics and Econometrics*, 15, 1–33.
- Collier, P., Gunning, J. W., & Associates. (1999). *Trade shocks in developing countries*. Oxford: Oxford University Press.
- Elliott, G., Rothenberg, T. J., & Stock, J. H. (1996). Efficient tests for an autoregressive unit root. *Econometrica*, 64, 813–836.
- Grossman, R., & Helpman, E. (1991). Quality ladders in the theory of growth. *The Review of Economic Studies*, 58, 43–61.
- Kaldor, N. (1961). Economic growth and capital accumulation. In F. Lutz, & D. C. Hague (Eds.), *The theory of capital*. London: Macmillan.
- Kaminski, J. (2011). *Cotton dependence in Burkina Faso: Constraints and opportunities for balanced growth. Yes Africa can: Success stories from a dynamic continent*.
- Kapetanios, G., Shin, Y., & Snell, A. (2003). Testing for a unit root in the non-linear STAR Framework. *Journal of Econometrics*, 112, 359–379.
- Koenker, R., & Xiao, Z. (2004). Unit root quantile autoregression inference. *Journal of the American Statistical Association*, 99, 775–787.
- Lucas, R. E. (1988). On the mechanics of economic development. *Journal of Monetary Economics*, 22(1), 3–42.
- Lumsdaine, R. L., & Papell, D. H. (1997). Multiple trend breaks and the unit-root hypothesis. *The Review of Economics and Statistics*, 79(2), 212–218.
- Maddison, A. (1982). *Phases of capitalist development*. Oxford: Oxford University Press.
- Ma, W., Li, H., & Park, S. Y. (2017). Empirical conditional quantile test for purchasing power parity: Evidence from East Asian countries. *International Review of Economics & Finance*, 49, 211–222.
- Ng, S., & Perron, P. (2001). Lag length selection and the construction of unit root tests with good size and power. *Econometrica*, 69, 1519–1554.
- Phillips, P. C. B., & Perron, P. (1988). Testing for unit roots in time series. *Biometrika*, 75, 335–346.
- Ranjbar, O., Li, X. L., Chang, T., & Lee, C. C. (2015). Stability of long-run growth in East Asian countries: New evidence from panel stationarity test with structural breaks. *Journal of International Trade & Economic Development*, 24(4), 570–589.
- Romer, P. M. (1986). Increasing returns and long-run growth. *Journal of Political Economy*, 94, 1002–1037.
- Romero-Avila, D. (2009). Multiple breaks, terms of trade shocks and the unit-root hypothesis for African per capita real GDP. *World Development*, 37(6), 1051–1068.
- Sibanda, V., & Makwata, R. (2017). *Zimbabwe post independence economic policies: A critical review*. LAP LAMBERT Academic Publishing.
- Sy, A. (2016). *Managing economic shocks: African prospects in the evolving external environment. Foresight Africa: Top priorities for the continent in 2016*. Brookings.
- The Conference Board. (2016). In *The conference board total economy Database™*. <http://www.conference-board.org/data/economydatabase/>.
- Tsong, C. C., & Lee, C. F. (2011). Asymmetric inflation dynamics: evidence from quantile regression analysis. *Journal of Macroeconomics*, 33(4), 668–680.
- Tsuchiya, I. (2016). *Poverty in Egypt during the 2000s. Interim report for household expenditure patterns in Egypt during the 2000s*. IDL-JETRO.
- Vogelsang, T. J. (1997). Wald-type tests for detecting breaks in the trend function of a dynamic time series. *Econometric Theory*, 13(06), 818–848.