

Basic Semiconductor Detector

Requirement:
Large sensitive region ...

We know:

$$d \approx x_p \approx \sqrt{\frac{2\epsilon U}{eN_A}}$$

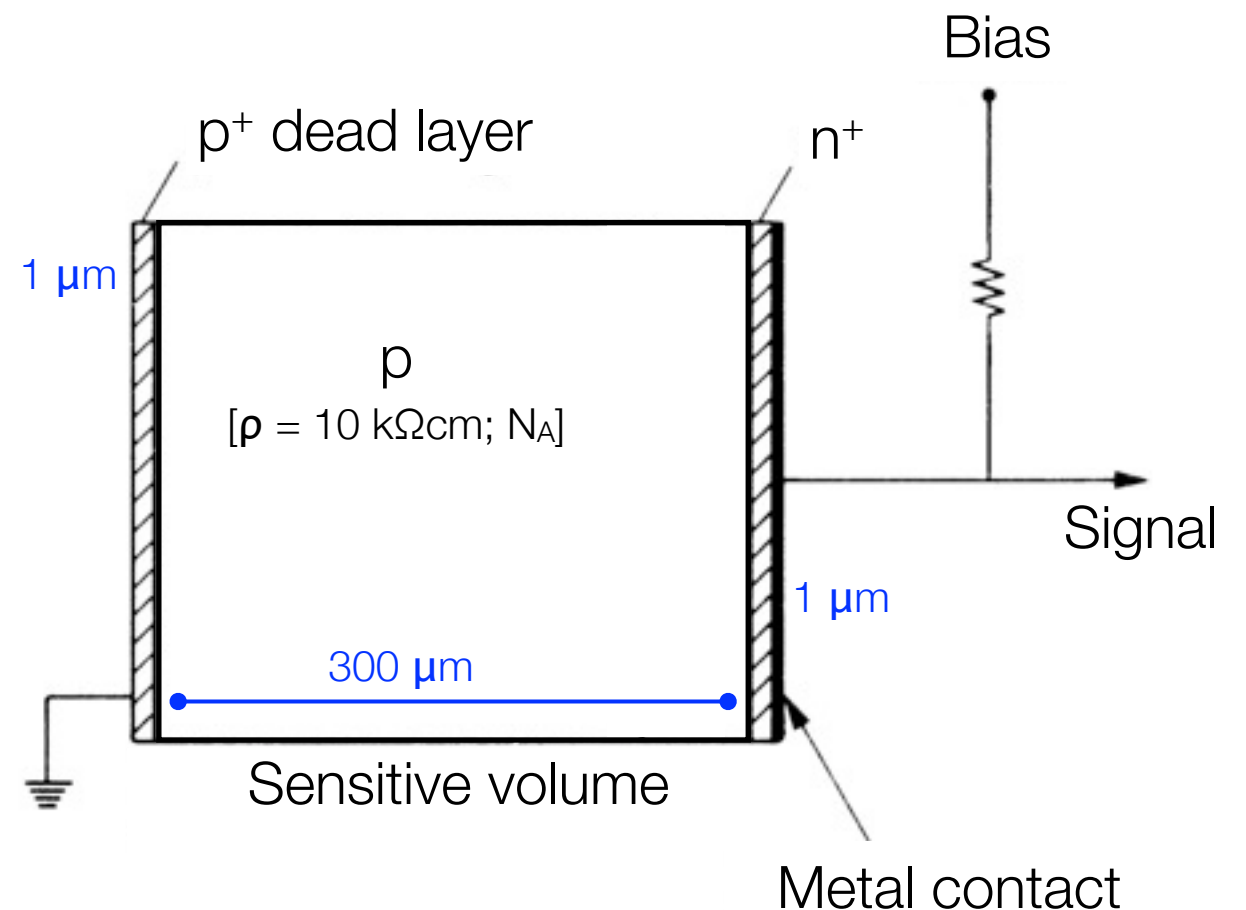
Typical: $N_A = 10^{15}/\text{cm}^3$
 n^+ region highly doped: $N_D \gg N_A$

$$U = \frac{e}{2\epsilon} N_A d^2$$
$$= 100 \text{ V}$$

Electric field:

$$E = \frac{U}{d} = \frac{100 \text{ V}}{300 \cdot 10^{-6} \text{ m}} \approx 3 \cdot 10^5 \frac{\text{V}}{\text{m}}$$

[Safe. Breakdown limit at 10^7 V/m]



n^+ and p^+ needed to
allow metallic contacts ...
[High doping = small depletion zone]

Bias voltage supplied
through series resistor ...

Pulse Shape Estimate

Electric pulse
arises from induction ...

Movement of electron from $x \rightarrow x+dx$
yields change in potential energy:

$$dW = e dU = e |\vec{E}| dx = e \frac{U_B}{d} dx$$

also: $dW = dQ U_B$
[dQ = charge collected by capacitor]

Thus:

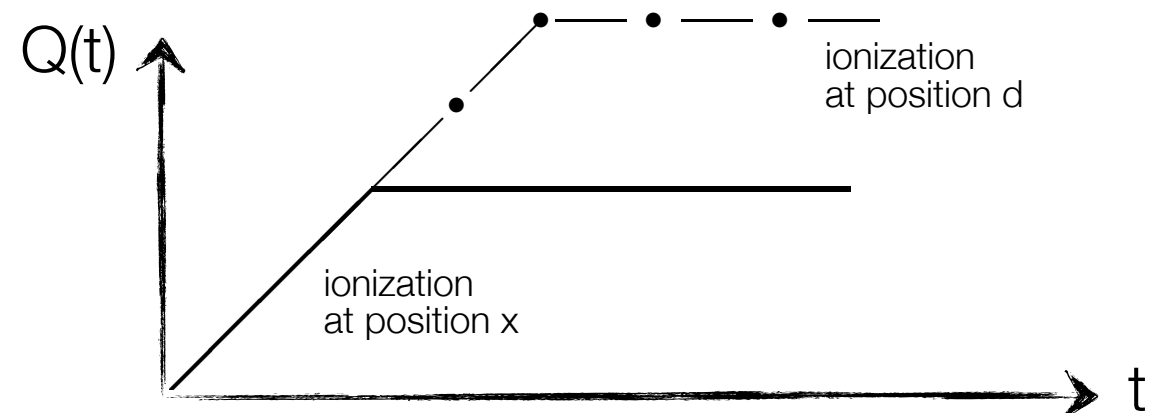
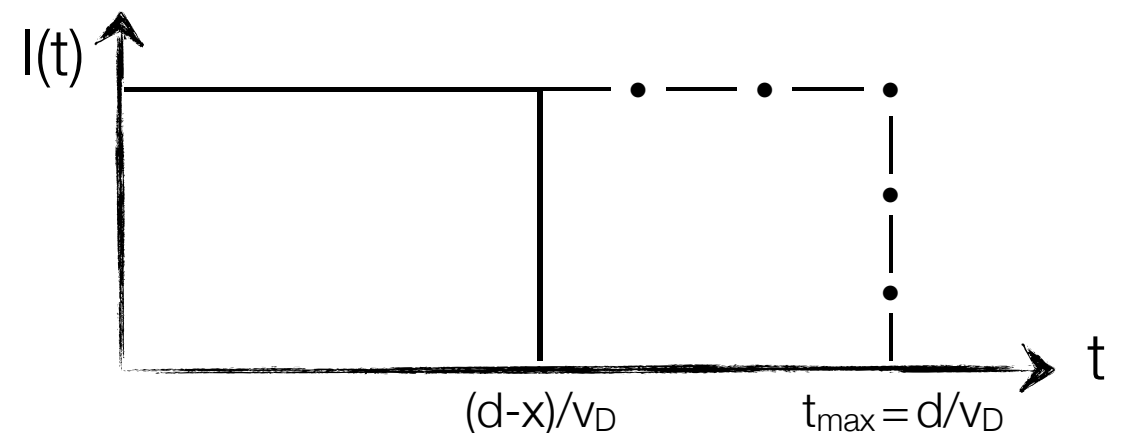
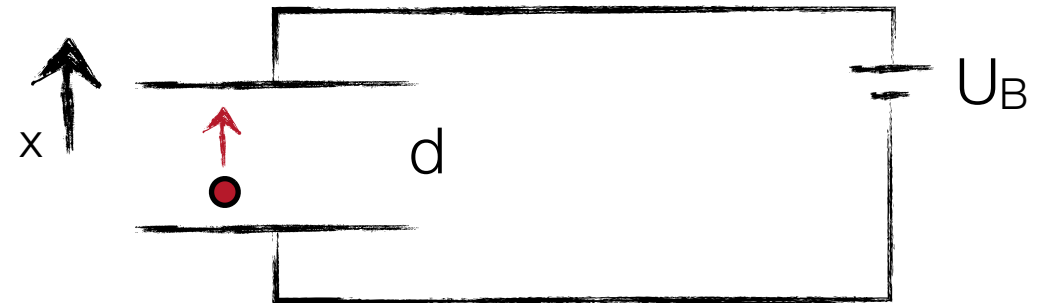
$$dQ = \frac{e dx}{d}$$

$$I = \frac{dQ}{dt} = \frac{dQ}{dx} \frac{dx}{dt} = \frac{e v_D}{d}$$

$$Q = e \frac{v_D}{d} \cdot t = e \frac{v_D}{d} \cdot \frac{d-x}{v_D}$$

$$= e \frac{d-x}{d}$$

Induced charge depends on
location of electron-hole production ...



Signal Pulse Shape

Pulse form for line source:
[simple estimate]

Current:

$$I(t) = e \frac{v_D}{d} \cdot N_0 \frac{d-x}{d} \Theta \left(\frac{d-x}{d} \right)$$

'location' of first pair; $x(t) \dots$

$$= e \frac{v_D}{d} \cdot N_0 \frac{d-v_D t}{d} \Theta \left(\frac{d-v_D t}{d} \right)$$

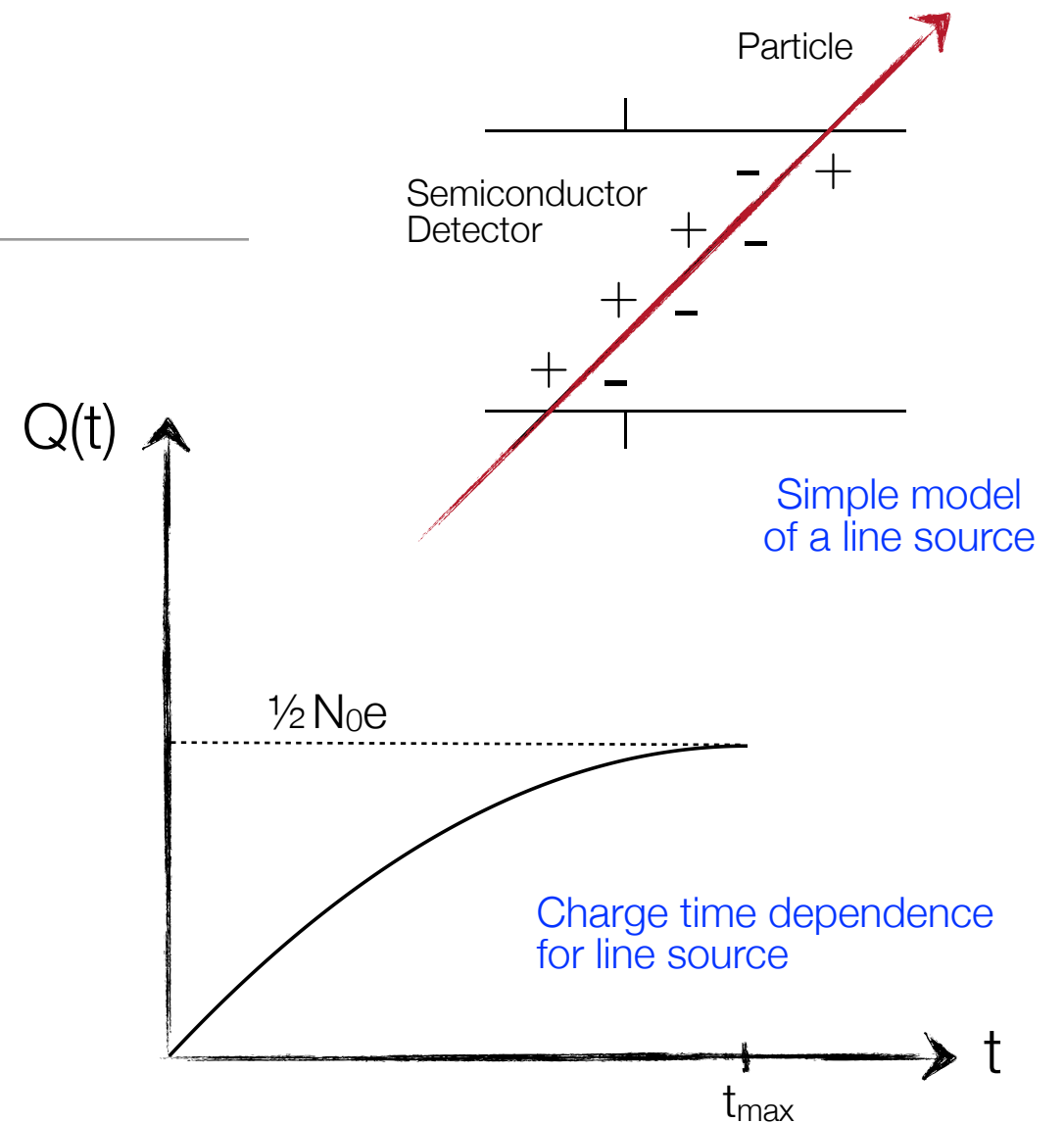
Charge:

$$Q(t) = N_0 e \frac{v_D}{d} \int_0^t \left(1 - \frac{tv_D}{d} \right) \Theta \left(1 - \frac{tv_D}{d} \right)$$

$$= N_0 e \frac{v_D}{d} \left(t - \frac{t^2 v_D}{2d} \right) \Theta \left(1 - \frac{tv_D}{d} \right)$$

Total charge after $t_{\max} = d/v_D$:

$$Q(t_{\max}) = N_0 e \frac{v_D}{d} \left(\frac{d}{v_D} - \frac{d^2}{v_D^2} \frac{v_D}{2d} \right) = \frac{N_0 e}{2}$$



Remark: such a signal is e.g. seen in LAr ionization chambers.

Electrons : $Q_{\max} = \frac{1}{2} N_0 e$

Holes : $Q_{\max} = \frac{1}{2} N_0 e$

$$Q_{\text{tot}} = N_0 \cdot e$$

Signal Pulse Shape

More realistic treatment:
Electric field is x-dependent ...

Electric field:

$$E = -\frac{eN_A}{\epsilon} \cdot x$$

assuming simple model for charge
distribution over depletion zone ...
[see above]

Conductivity:

$$\sigma = e(n\mu_e + p\mu_h) \approx eN_A\mu_h$$

[as here: $p \approx N_A$, $n \approx 0$]

Thus:

$$E = \frac{x}{\mu_h \tau} \quad \text{with } \tau = \epsilon / \sigma$$

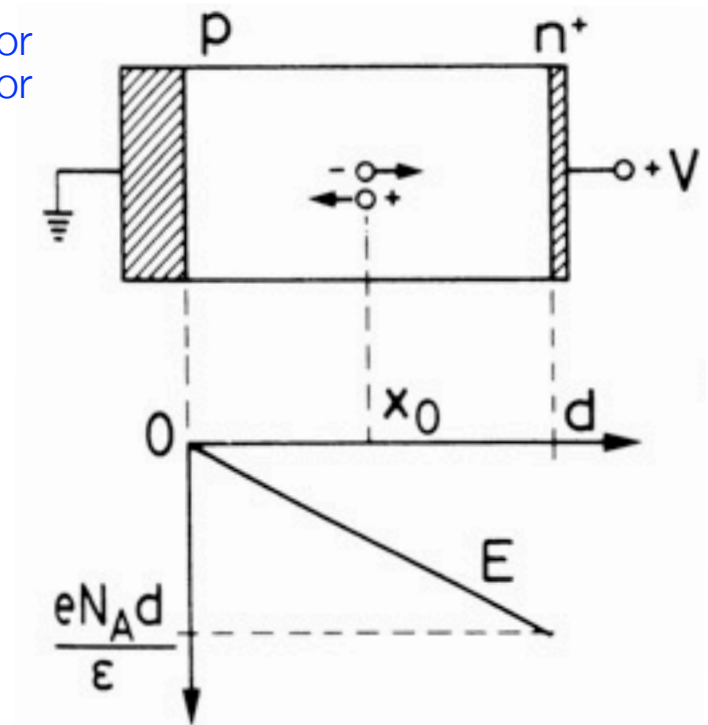
[typical: $\tau = \text{O}(\text{few ns})$]

For an electron at location x within
the depletion zone:

$$v = \frac{dx}{dt} = -\mu_e E = \frac{\mu_e}{\mu_h} \frac{x}{\tau}$$

i.e. drift velocity not constant!

Use our example for
typical Si-Detector



Assuming μ_e , μ_h to be independent
of E and thus of location x ...

$$x = x_0 \exp \frac{\mu_e t}{\mu_h \tau} \quad \left[\text{and } t = \tau \frac{\mu_h}{\mu_e} \cdot \ln \frac{x}{x_0} \right]$$

$$Q_e(t) = -\frac{e}{d} \int_0^t \frac{dx}{dt} dt = \frac{e}{d} x_0 \left(1 - \exp \frac{\mu_e t}{\mu_h \tau} \right)$$

Charge induced by electron
as a function of time ...

Signal Pulse Shape

Induced charge
from electrons:

$$Q_e(t) = \frac{e}{d} x_0 \left(1 - \exp \frac{\mu_e t}{\mu_h \tau} \right)$$

Similar for holes:

$$v = \frac{dx}{dt} = \mu_h E = -\frac{\mu_h x}{\mu_h \tau} = -\frac{x}{\tau}$$

$$x = x_0 \exp \left(-\frac{t}{\tau} \right)$$

and thus:

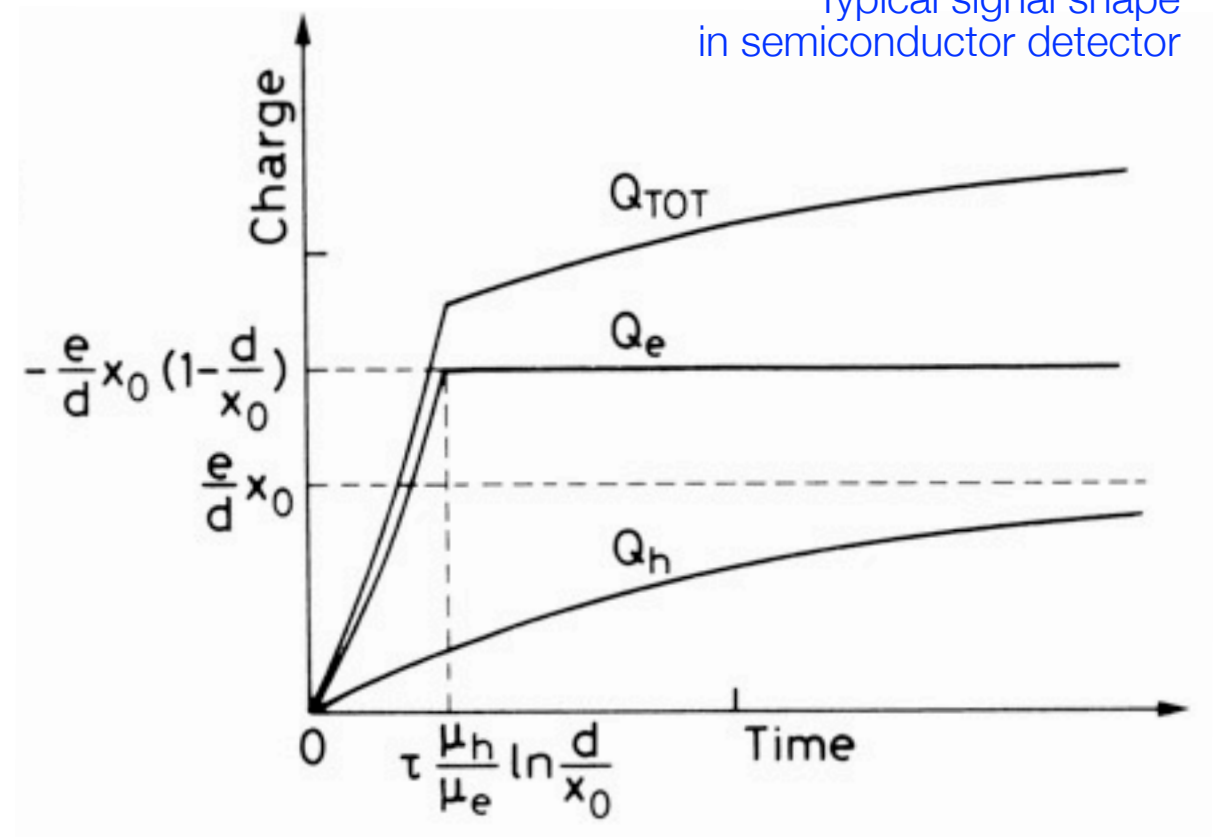
$$Q_h(t) = -\frac{e}{d} x_0 \left(1 - \exp \left(-\frac{t}{\tau} \right) \right)$$

Summation yields:

$$Q_{\text{tot}}(t) = Q_e(t) + Q_h(t)$$

$$Q_{\text{tot}} = Q_e(t_d) + Q_h(t \rightarrow +\infty) = \frac{e}{d} x_0 \left(1 - \frac{d}{x_0} \right) - \frac{e}{d} x_0 = -e$$

Typical signal shape
in semiconductor detector



Using:
 $t = \tau \frac{\mu_h}{\mu_e} \cdot \ln \frac{x}{x_0}$ and $d = x$

Signal Pulse Shape

Signal rise time
essentially determined by

$$\tau = \epsilon / \sigma$$

i.e. typically in the order of nanoseconds.
[Typical: $1/\sigma = \rho = 10000 \text{ } \Omega\text{cm}$; $\epsilon \approx 10^{-12} \text{ s}/\Omega\text{cm}$]

Further complications:

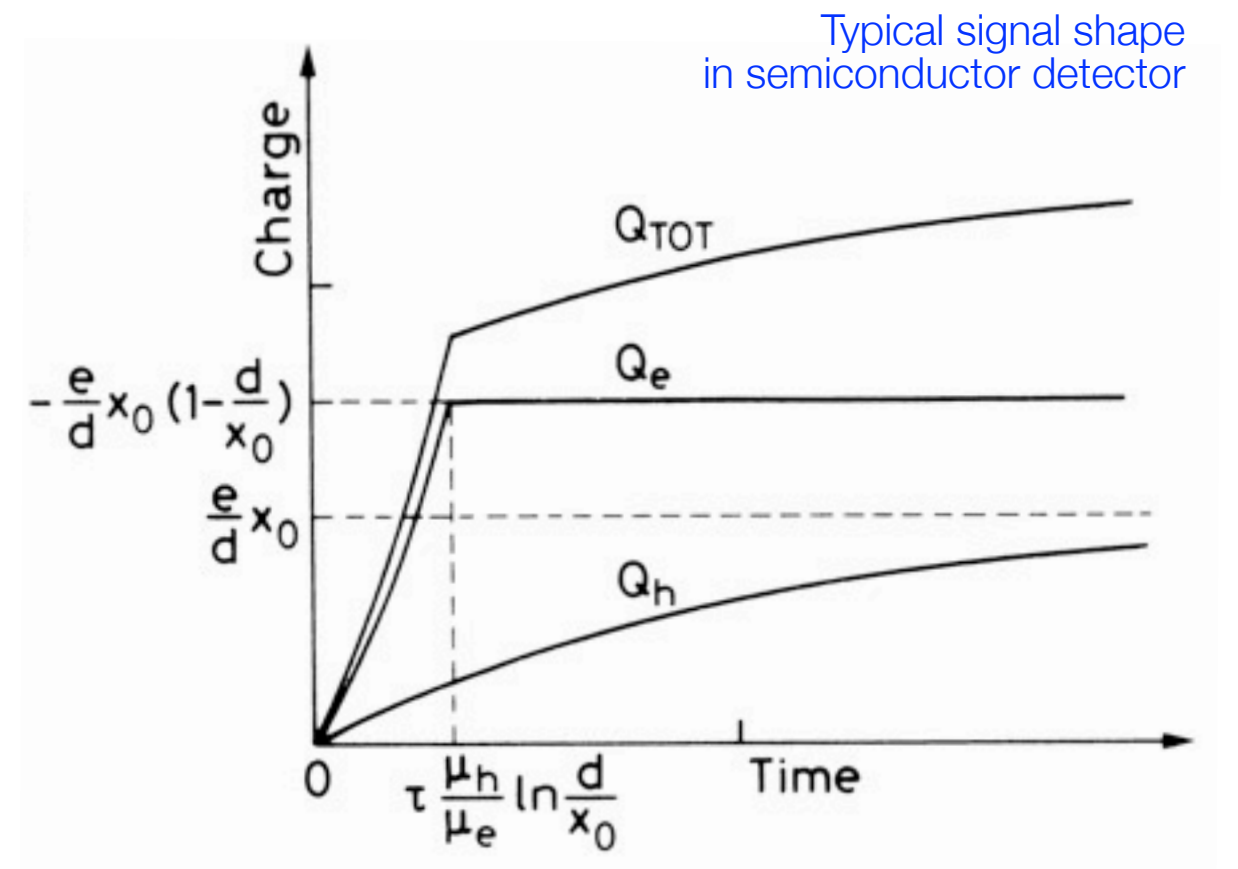
Consider particle trajectory
[here only for one electron-hole pair]

Tracks not exact line charge
[distributed over typically 50 - 100 μm width]

μ_e and μ_h not independent of E-field
[i.e. need to introduce $\mu(x)$...]

Potential losses due to traps
[loss or delayed charge induction]

...



Using:

$$t = \tau \frac{\mu_h}{\mu_e} \cdot \ln \frac{x}{x_0} \quad \text{and} \quad d = x$$

Ionization Yield and Fano Factor

Energy resolution:

$$\mathcal{R} = \frac{\Delta E}{E}$$

with ΔE defined
as **full width half maximum** ...

Electron-hole pairs:
[or number of ionizations ...]

$$N_i = \frac{E}{\epsilon_0}$$

with ϵ_0 defined as average
energy per ionization ...

Resolution estimate:

$$E \sim N_i, \quad \sigma^2 \sim N_i, \quad \Delta E \sim 2.35\sigma \sim 2.35\sqrt{N_i}$$

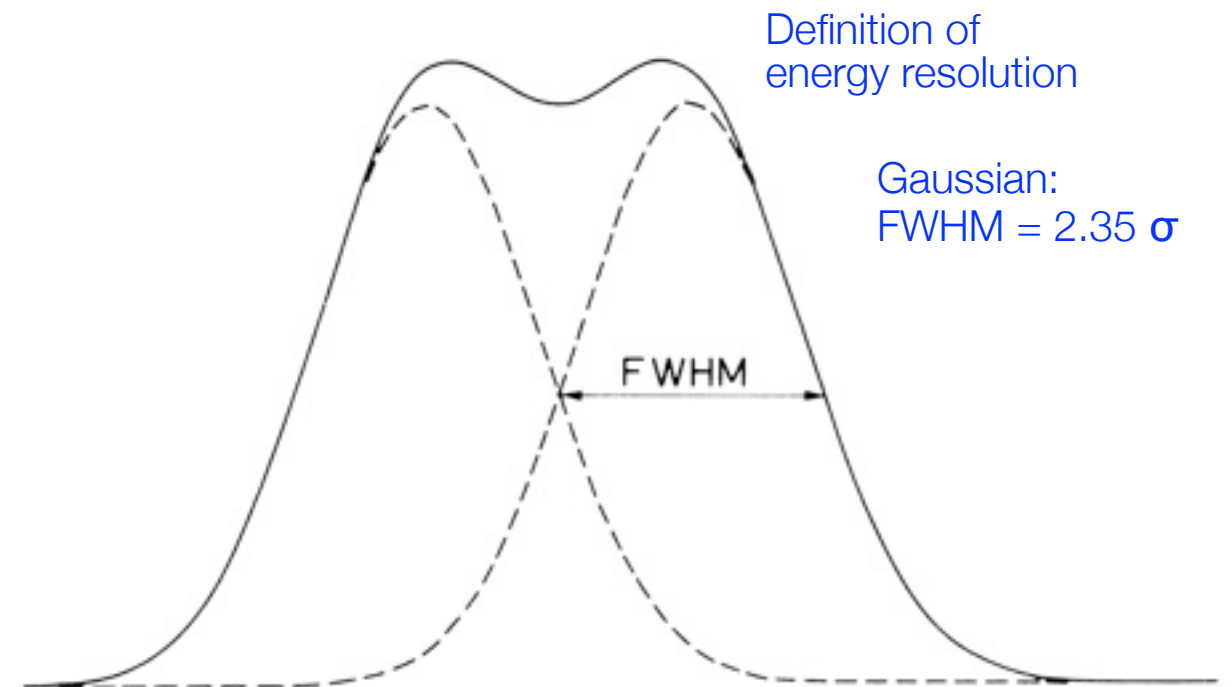
$$\mathcal{R} = 2.35 \frac{\sqrt{N_i}}{N_i} = 2.35 \sqrt{\frac{\epsilon_0}{E}} \sim \frac{1}{\sqrt{E}}$$

If full energy is absorbed this estimate is incorrect, as E is fixed and thus cannot fluctuate, i.e. fluctuations are not all independent and ...

$$\sigma^2 = F N_i \quad \rightarrow \quad \mathcal{R} = 2.35 \frac{\sqrt{F N_i}}{N_i} = 2.35 \sqrt{\frac{F \epsilon_0}{E}}$$

[F: Fano Factor]

For many detectors $F < 1$;
yields better resolution ...
[e.g. semiconductors or gases]



Ionization Yield and Fano Factor

Energy loss:

Only ~1/3 of the energy loss produces electron-hole pairs;
About 2/3 is used for lattice excitations, i.e. phonons ...

Energy loss per process:

Phonon excitation : $E_x \sim 0.037$ eV

Ionization : $E_i = E_{\text{gap}} \sim 1$ eV [e.g. 1.1 eV for Si]

	ϵ_0 [@ 300 K]	ϵ_0 [@ 77 K]	E_{gap}
Si	3.6 eV	2.8 eV	1.1 eV
Ge	–	2.9 eV	0.7 eV

ϵ_0 : mean energy per electron-hole pair

Energy conservation:

$$E_0 = E_i \cdot N_i + E_x \cdot N_x$$

$$E_x \cdot \Delta N_x + E_i \cdot \Delta N_i = 0$$

as fluctuations in N_i are compensated
by fluctuations in N_x to keep E_0 constant ...

with E_0 : total energy deposited; fixed ...
 N_x : number of excited phonons
 N_i : number of ionization, i.e. electron-hole pairs
 ΔN_x : fluctuations of N_x
 ΔN_i : fluctuations of N_i

On average:

$$E_x \sigma_x = E_i \sigma_i$$

$$\left[\begin{array}{l} \text{with } \sigma_i = \sqrt{N_i}, \sigma_x = \sqrt{N_x} \end{array} \right]$$

$$\rightarrow \sigma_i = \frac{E_x}{E_i} \sigma_x = \frac{E_x}{E_i} \sqrt{N_x}$$

Ionization Yield and Fano Factor

Variance of N_i :

using $N_i = E_0 / \epsilon_0$

$$E_0 = E_i \cdot N_i + E_x \cdot N_x$$

$$\rightarrow N_x = (E_0 - E_i N_i) / E_x$$

$$\sigma_i = \frac{E_x}{E_i} \sqrt{N_x} = \frac{E_x}{E_i} \sqrt{\frac{E_0}{E_x} - \frac{E_i}{E_x} N_i}$$

$$= \frac{E_x}{E_i} \sqrt{\frac{E_0}{E_x} - \frac{E_i}{E_x} \frac{E_0}{\epsilon_0}} = \sqrt{\frac{E_0}{\epsilon_0}} \underbrace{\sqrt{\frac{E_x}{E_i} \left(\frac{\epsilon_0}{E_i} - 1 \right)}}_{\text{Fano Factor } F} = \sqrt{N_i F}$$

Yields resolution
better than expected ...

Numbers:

$$\text{Si} : \quad \epsilon_0 = 3.6 \text{ eV @ 300 K} \quad F \approx 0.1$$

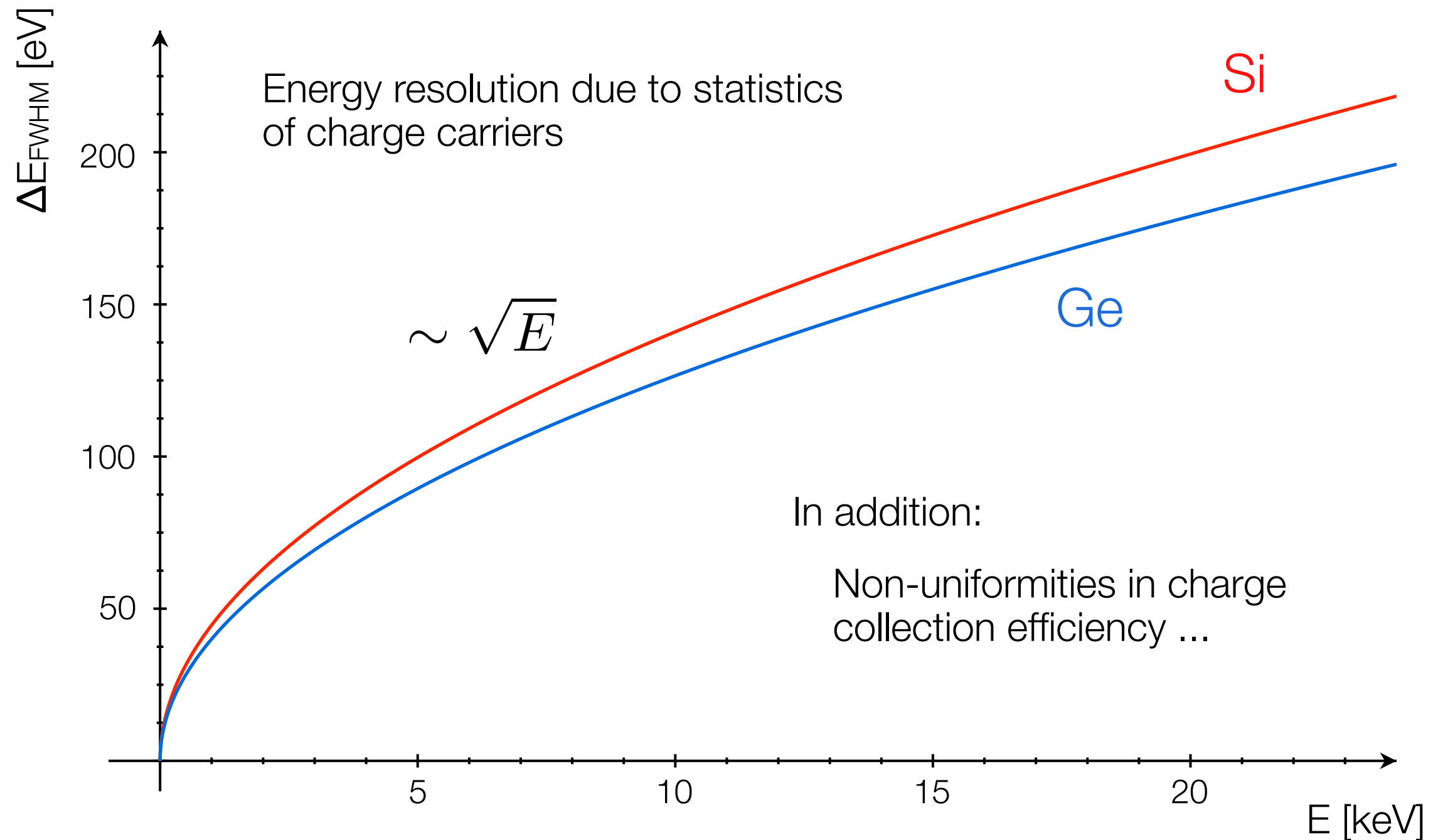
$$\text{Ge} : \quad \epsilon_0 = 2.9 \text{ eV @ 77 K} \quad F \approx 0.1$$

Resolution:

$$\Delta E_{\text{FWHM}} = 2.35 \cdot \epsilon_0 \sqrt{N_i F} = 2.35 \cdot \sqrt{\epsilon_0 F E_0}$$

Example: Photon of 5 keV; $E_\gamma = E_0 \rightarrow \Delta E = 100 \text{ eV}$, $\Delta E/E = 2\%$ [instead of 6%]

Energy Resolution



Energy Resolution

Comparison
of energy resolutions ...

Scintillator [NaI(Tl)]:

1 MeV photon; $\sigma/E \approx 2\%$; $\Delta E/E \approx 5\%$

[$N_i = 40000$ photons/MeV $\times \eta \times$ Q.E.; $\eta = 0.2$, Q.E. = 0.25; $\sigma/E = 1/\sqrt{N_i}$]

Semiconductor [Si]:

1 MeV photon; $\sigma/E \approx 0.06\%$; $\Delta E/E \approx 0.15\%$

[$N_i = 300000$ e/h-pairs/MeV; $\eta \approx 1$, Q.E. ≈ 1 ; $F = 0.1$ $\sigma/E = \sqrt{F}/\sqrt{N_i}$]

Energy resolution of a semiconductor detector
can be better by a factor 25 to 30.

This is indeed observed:
[for $E_\gamma = 1.33$ MeV]

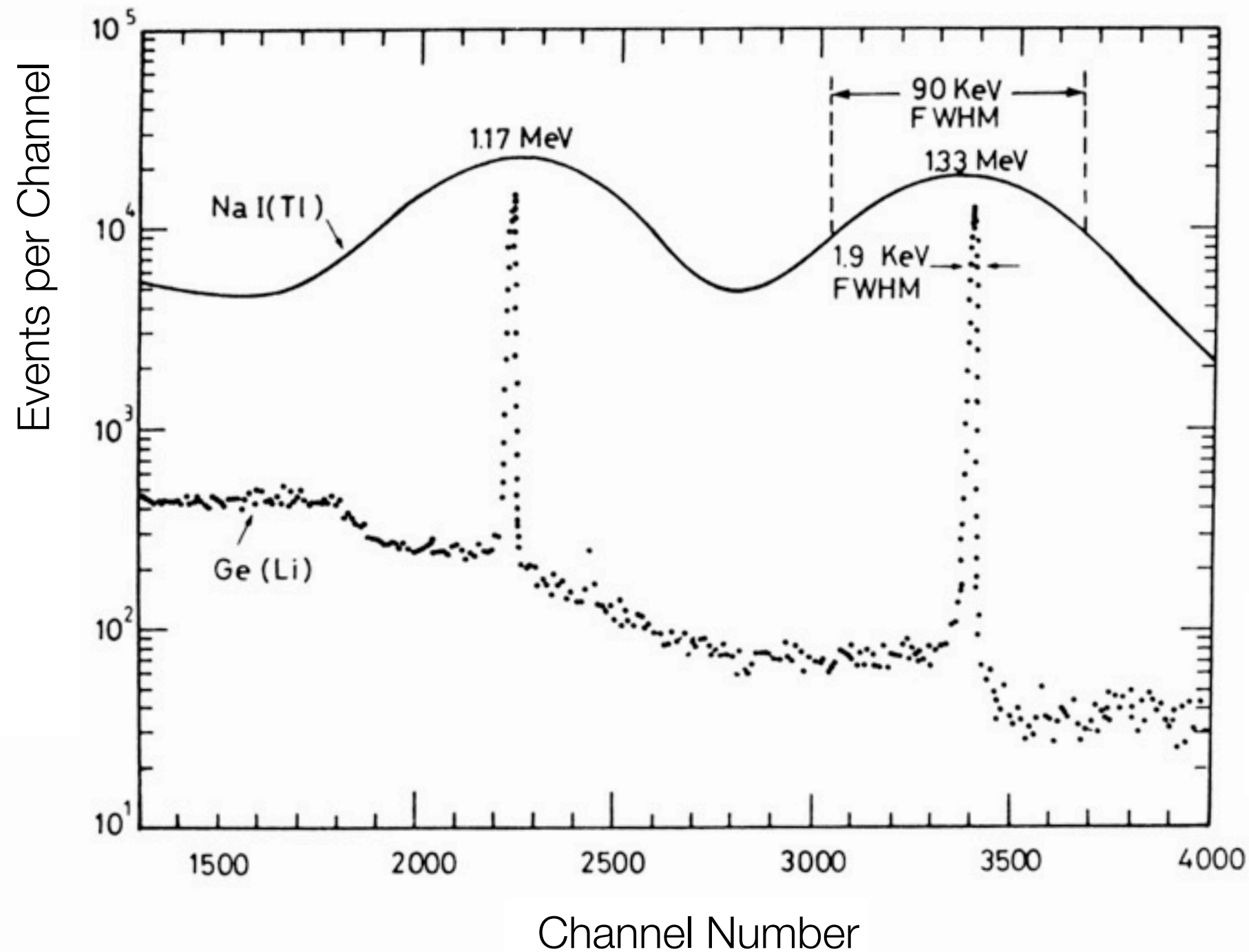
Ge(Li) Counter:

Resolution of 0.15% possible (at ~ 1 MeV)

NaI(Tl) Detector:

Resolution of about 6% (at ~ 1 MeV)

Energy Resolution



Comparison
of two ^{60}Co γ -spectra
one measured with NaI(Tl)
and With Ge(Li) Detector

Energy Measurement – Realization

Diffused Barrier Detectors

[or Diffused Junction Diodes]

[see above]

Material: p-type semiconductor
with n^+ and p^+ surface contacts ...

Impurities [e.g. phosphorus for n^+]
are diffused into one end of homogeneous
p-type semiconductor at high $T \sim 1000^\circ\text{C}$

Typical dimensions:

Surface layers (n^+/p^+) : 0.1 to 2 μm

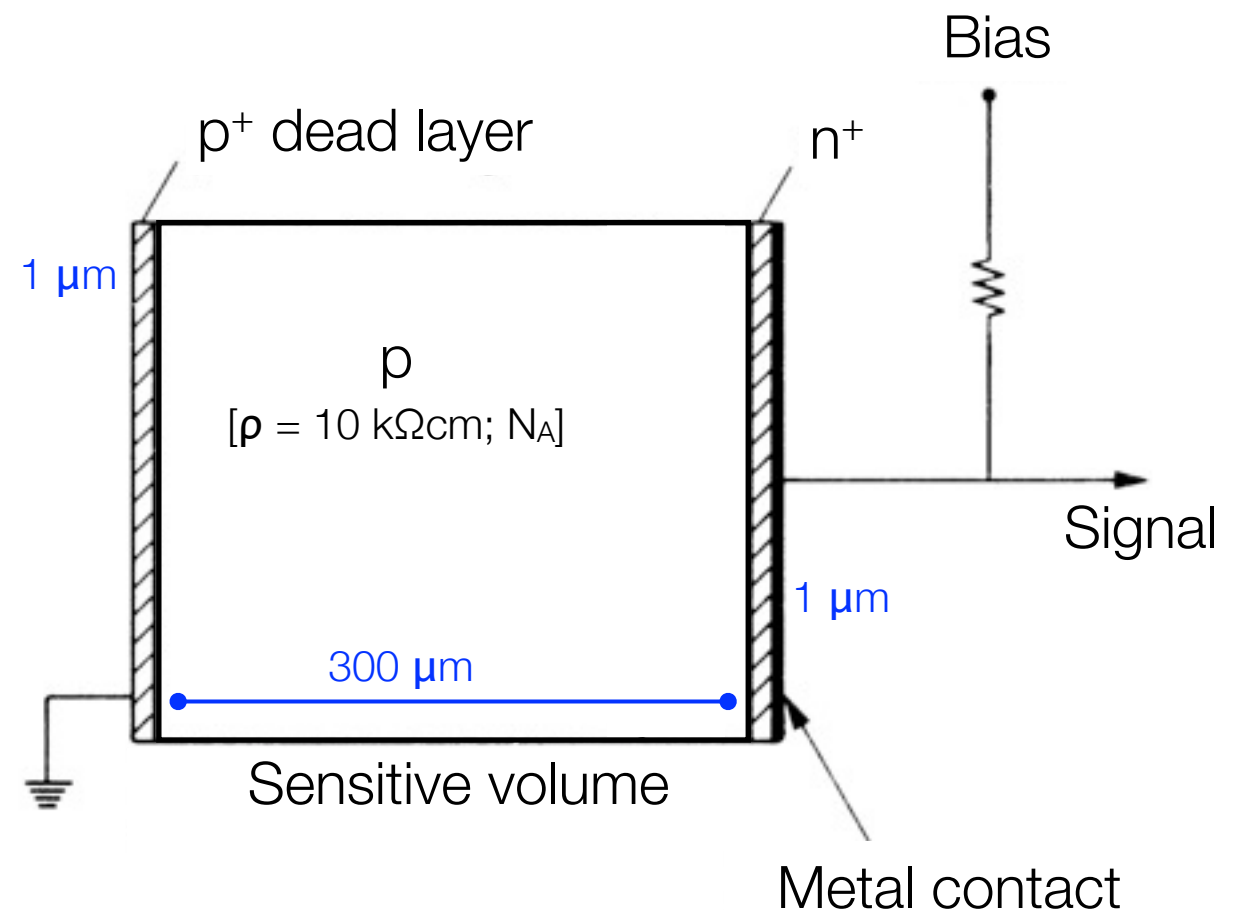
Depletion layer (p-type) : 300 μm

Disadvantages:

Highly doped n^+ surface leaves relatively thick dead layer for particles entering the detector ...
i.e. soft or short range particles (e.g. α 's) not measured as they don't reach depletion layer ...
or part of the deposited energy is not measured \rightarrow degraded energy resolution

Alternative: Ion-implanted Diodes

[Advantage: Thinner entrance windows of $\sim 50\text{ nm}$; lower $T \sim 500^\circ\text{C}$ yielding higher lifetime]



Energy Measurement – Realization

Surface Barrier Detectors

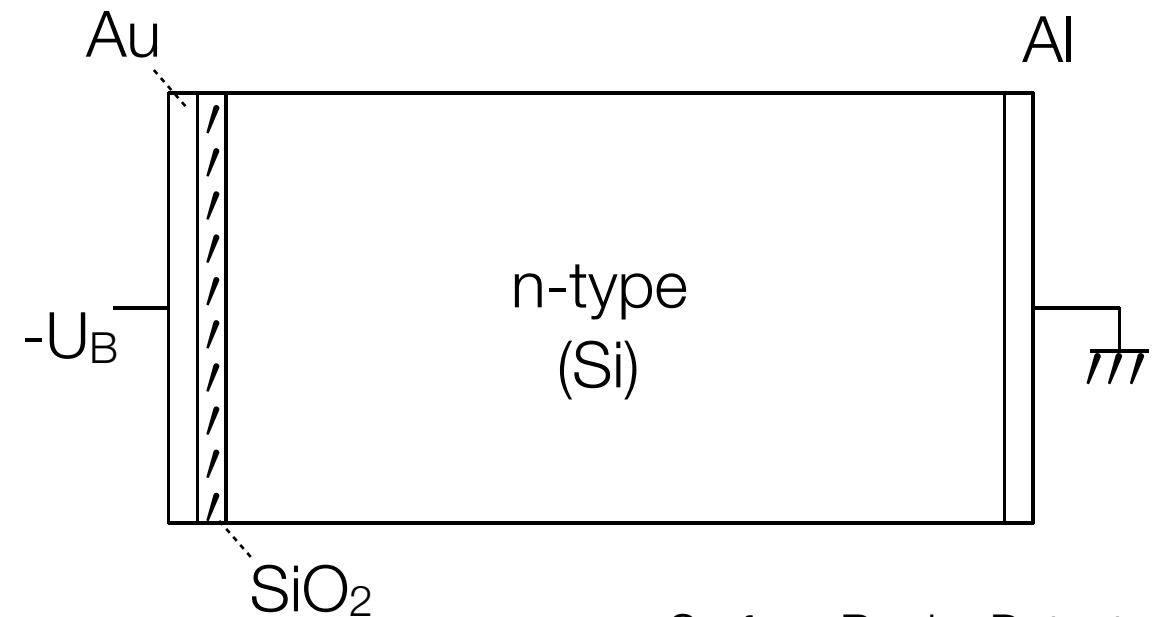
Very thin metal contact layers (~ 20 nm)

[n-type Si with gold or p-type Si with Aluminum]

Fabrication process: etching silicon surface and depositing thin Au layer by evaporation ...

Processing temperature: 20°C

Si-Surface must be oxidized before Au deposition ...



Surface Barrier Detectors
with thin gold layer
[Schottky Diode]

Electrons diffuse into metal ...

Different Fermi levels lead to contact electromotive force (emf); potential arises via equilibration process ...

Yields depletion depths of up to 5 mm [$\sim \sqrt{U_B}$]

Depletion zone extends through entire thickness of the silicon layer
[high depletion possible due to high resistance]

Advantages:

Thin entrance window ...

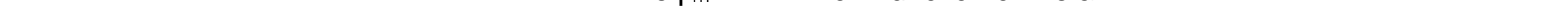
Full depletion allows dE/dx measurement

Applying $-U_B$ at metal: high potential barrier; no dark currents

Increasing bias voltage beyond full depletion \rightarrow faster signal rise

Disadvantage:

Sensitivity to visible light ...
requires light enclosure



Occurrence of electromotive force ...
Electrons diffuse into metal until
Fermi levels become equal ...

$$\begin{aligned} e\phi_{\Delta} &= e\phi_m - e\chi_s && \text{(potential well)} \\ eV_{\text{int}} &\approx e\phi_m - e\phi_s && \text{(potential difference seen by carriers)} \end{aligned}$$

Results in strong E field at surface ...

Energy Measurement – Realization

Surface Barrier Detectors
can be operated as a diode.

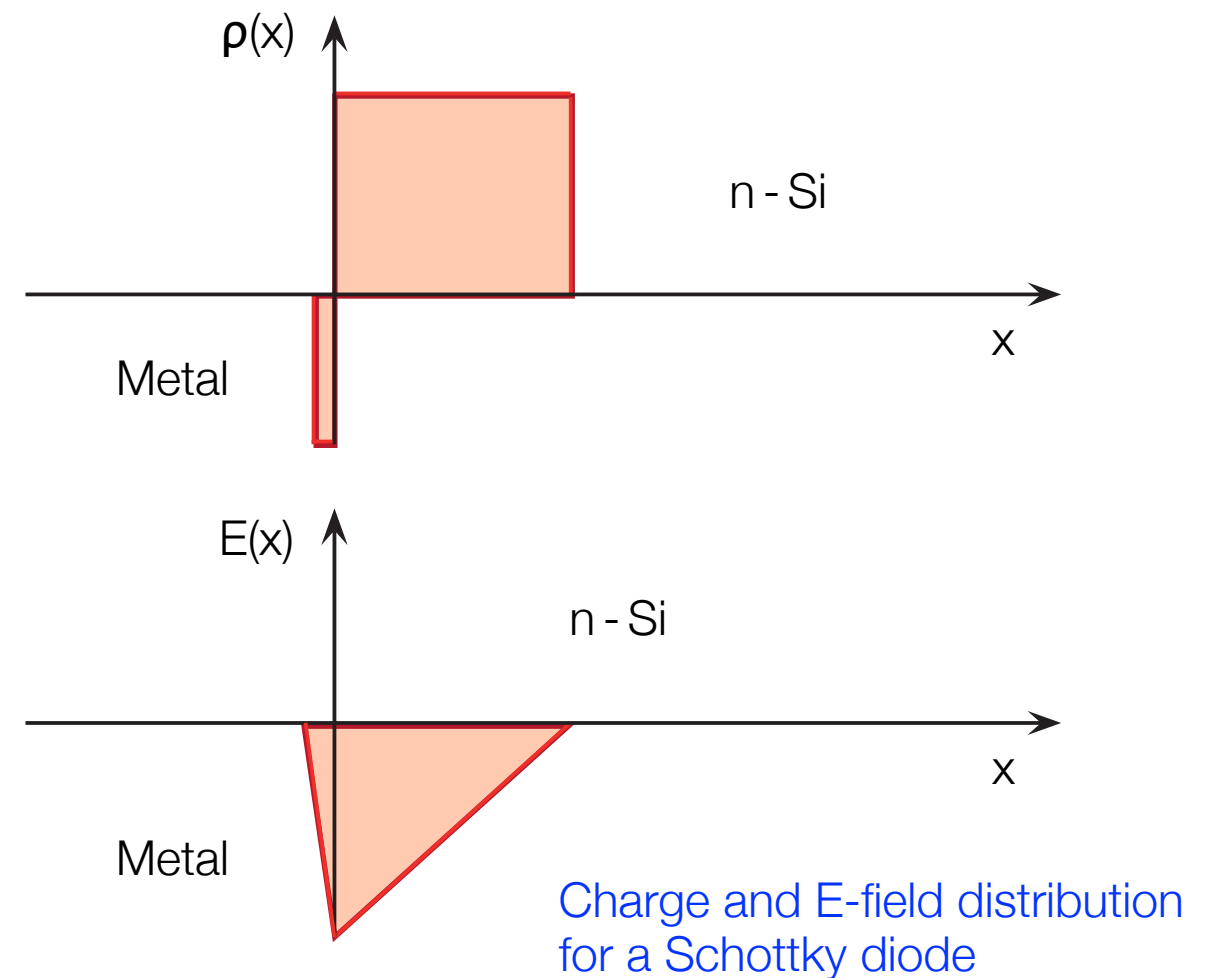
[Schottky Diode]

Metal-Si contact:

Electrons diffuse from metal to Si until

$$E_F(\text{metal}) = E_F(\text{Si});$$

Strong electric field at boundary prevents
further electron diffusion into metal



With bias voltage:

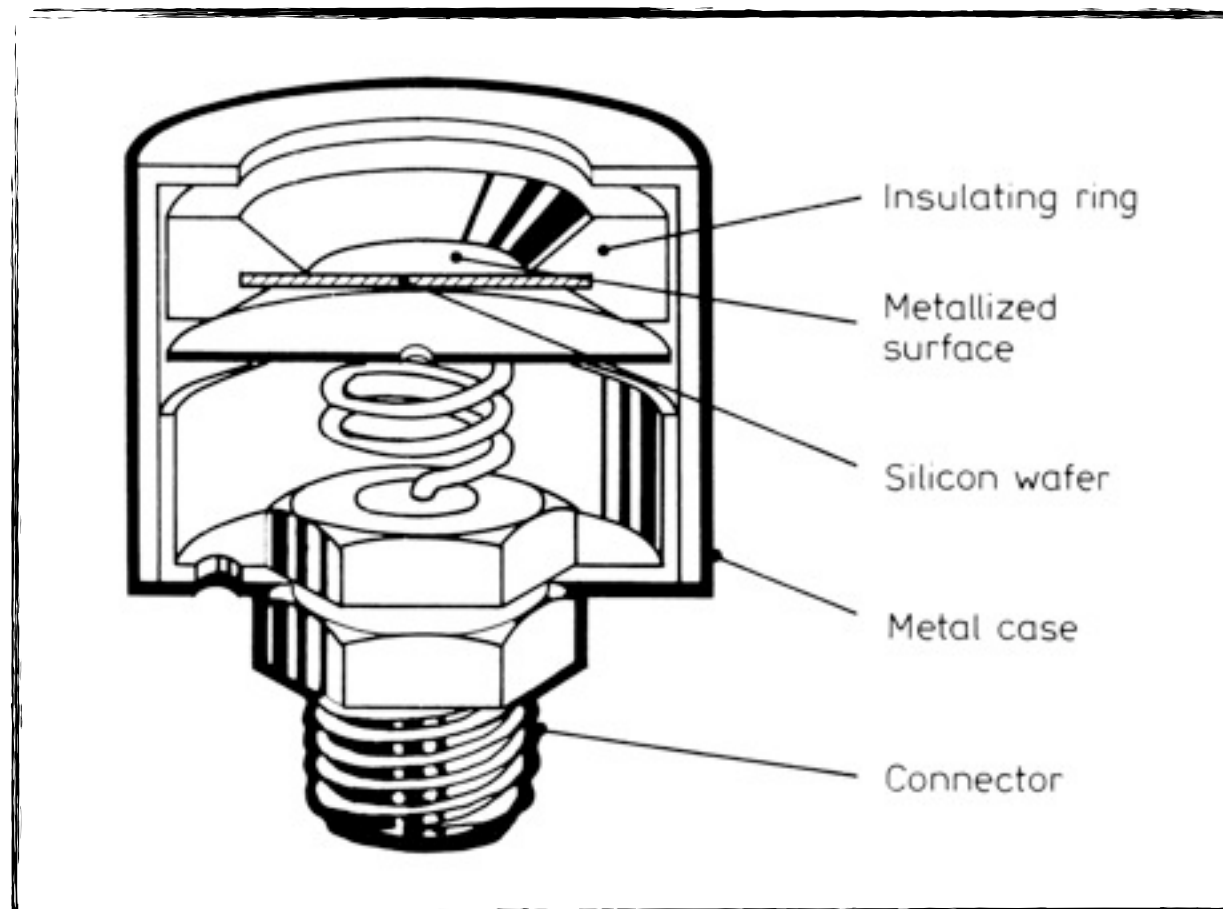
Reverse bias: positive potential of n - Si
w.r.t metal; increased potential well, electron carriers cannot tunnel from Si to metal.

Forward bias: negative potential of n - Si
w.r.t metal; decreased potential barrier, current can flow.

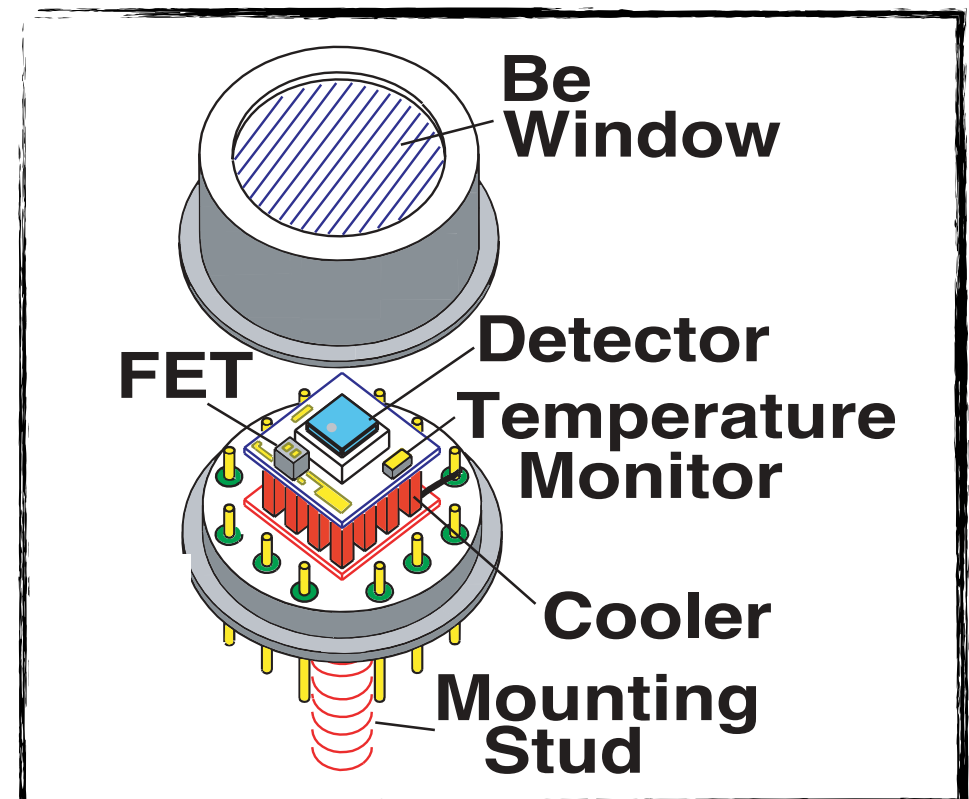
Energy Measurement – Realization

Examples of Surface Barrier Detectors [SSB]

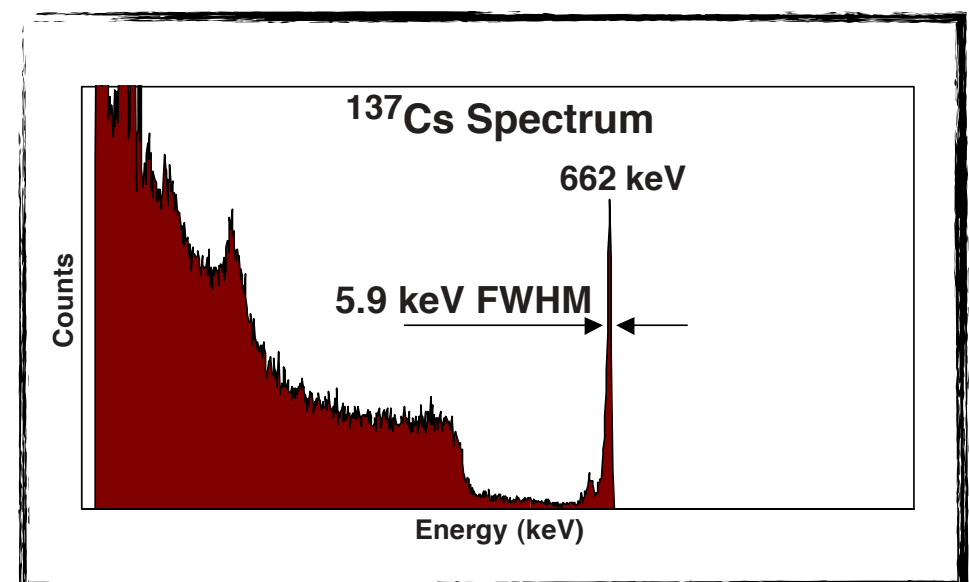
[Cross section of typical SSB]



[CdTe x-ray and γ -ray detector]



Amptek



Amptek

Energy Measurement – Realization

p-i-n Detectors:

[Lithium drift diodes]

Obtain thicknesses
greater than few millimeter ...

[needs very high resistivity; intrinsic semiconductor]

Idea:

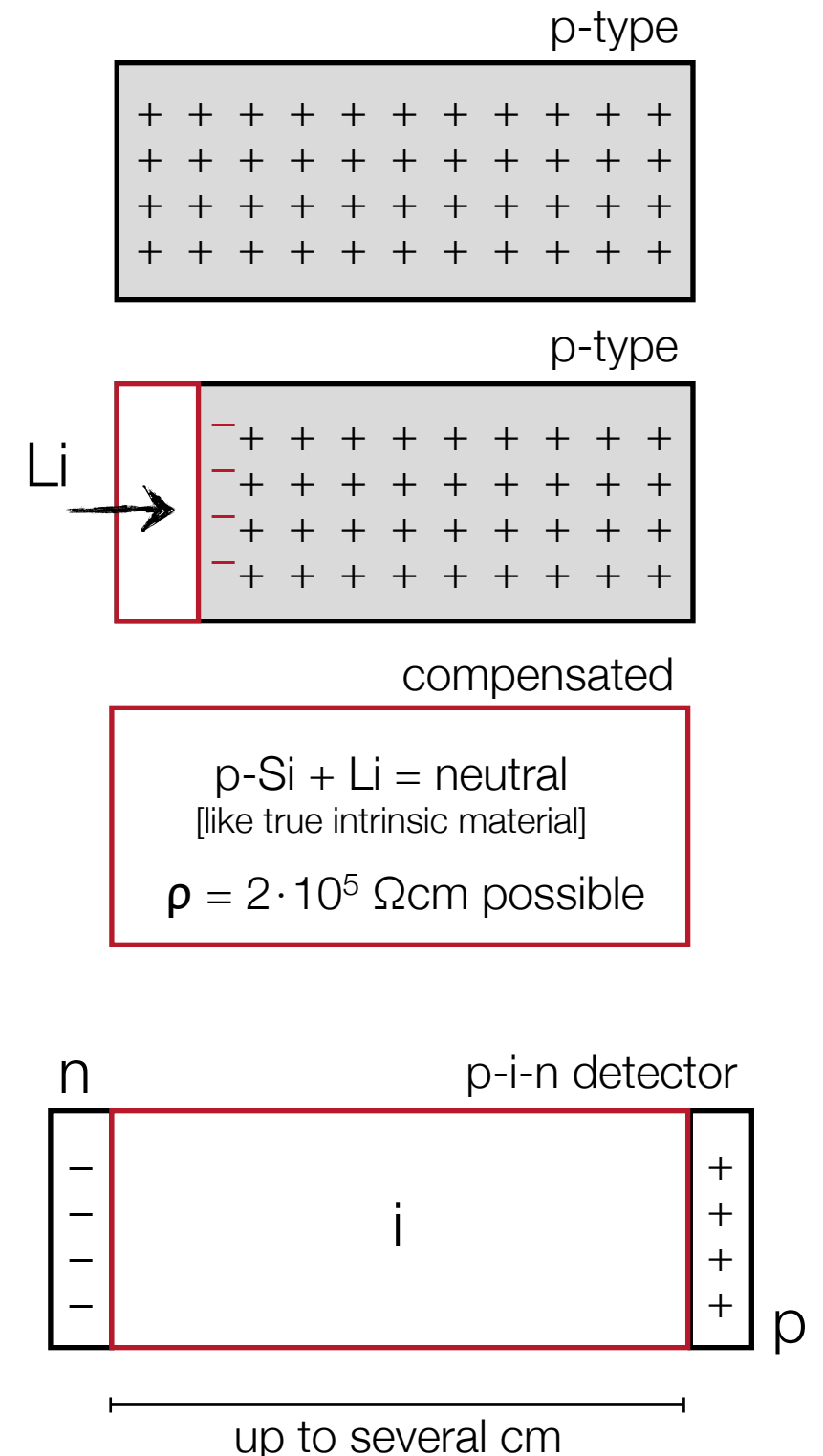
Create thick depletion layer by
compensation of donors or acceptors ...

[i.e. produce intrinsic layer]

Compensation process:

- i. Start with high purity p-type Ge or Si
[acceptor typically B (boron)]
- ii. Bring semiconductor in contact
with Li bath @ 350-400 °C;
[Li diffuses into p-layer]
- iii. Apply external field; Li drifts far into
crystal and compensates B locally
[equilibration process]

Ge(Li) detectors need
permanent cooling



Energy Measurement – Realization

Intrinsic Ge Detectors:

[High Purity Ge Detectors]

Since 1980ies: possibility to produce very pure Germanium,
i.e. produce intrinsic semiconductor without need for compensation ...

Advantage: no cooling needed
[except for noise reduction]

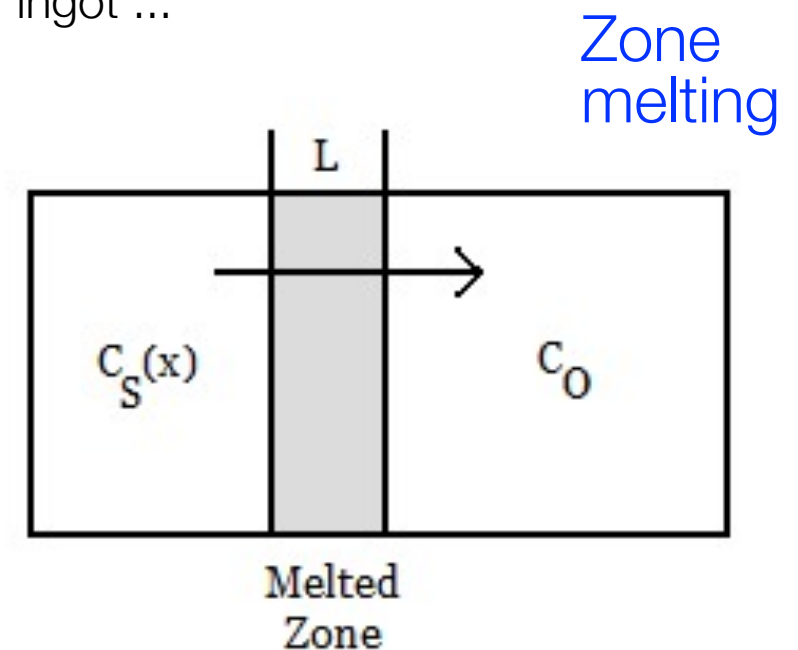
Purification process: zone melting

Successively melting narrow regions of a crystal moves impurities to end of ingot ...
Repeating process yields very high purities [$< 10^9$ impurity atoms per cm^3]

Applications:

[depends on detector size and energy range]

- γ -spectroscopy
- low energy electron detection
- detection of strongly ionizing particles
- dE/dx for particle ID
- ...



Position Sensitive Detectors

Motivation:

b-Quark tagging & life time measurements
via secondary vertex finding ...

e.g.: $p\bar{p} \rightarrow t\bar{t} + X$ [Tevatron]

$\hookrightarrow b\bar{b}W^+W^-$

$pp \rightarrow H + X$ [LHC]

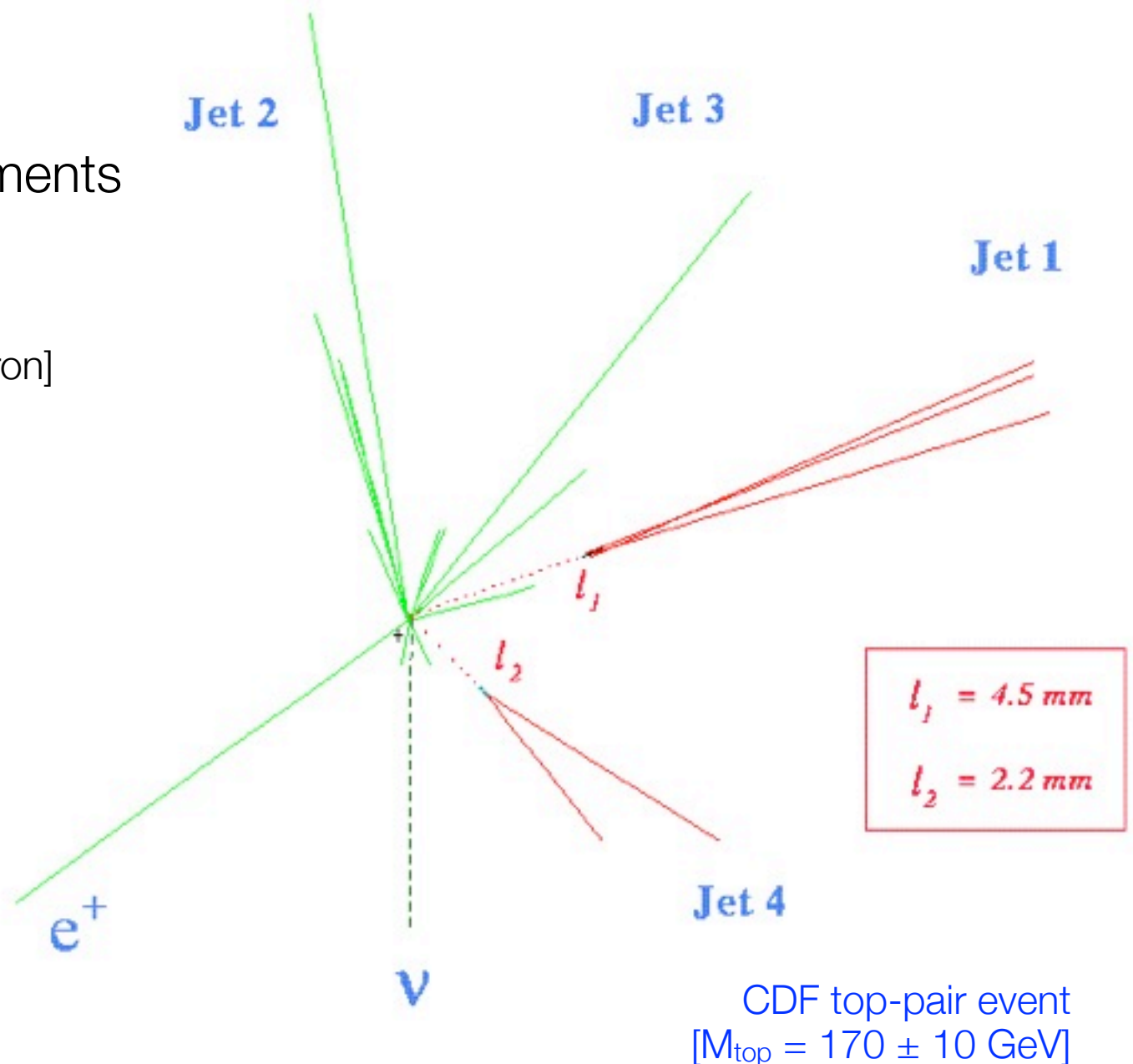
$\hookrightarrow b\bar{b}$

Typical lifetime: $\tau = 10^{-12} \dots 10^{-13}$ s

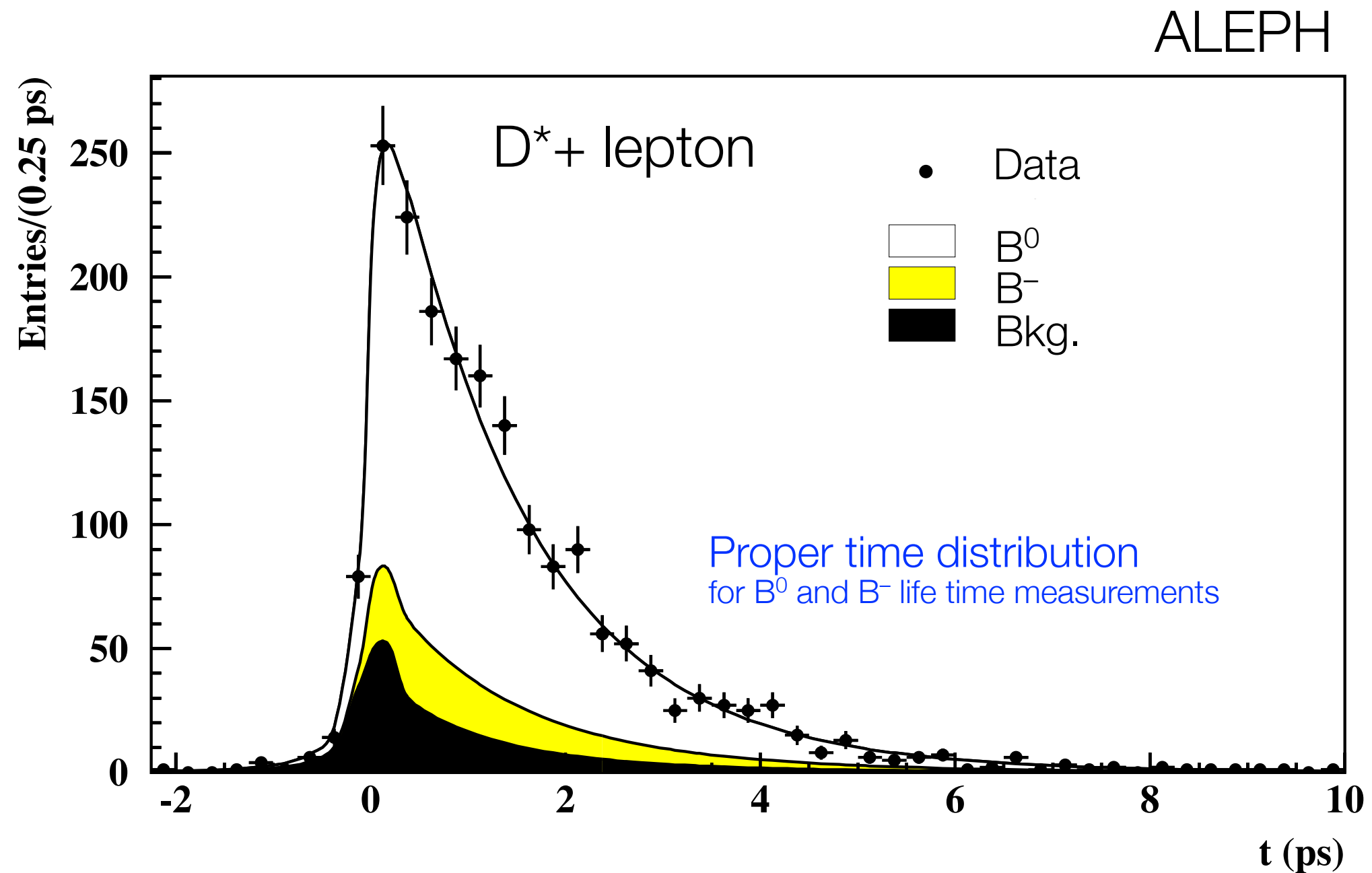
$$\begin{aligned}\gamma c\tau &= \gamma \cdot 3 \cdot 10^{10} \text{ cm/s} \cdot 10^{-13} \text{ s} \\ &= \gamma \cdot 30 \text{ } \mu\text{m}\end{aligned}$$

Thus:

To measure lifetime in picosecond regime
one needs spacial resolution of the order of 5 - 30 μm ...



Position Sensitive Detectors



Position Sensitive Detectors

Principle:

Segmentation
into strips, pads, pixels ...

Typical parameters:

Thickness: 150 - 500 μm

Strip separation (pitch): 20 - 150 μm

Resolution: 5 - 40 μm (pitch/ $\sqrt{12}$)

Charge collection: 20 ns

Charge integration: 120 ns

Operation voltage: 160 V

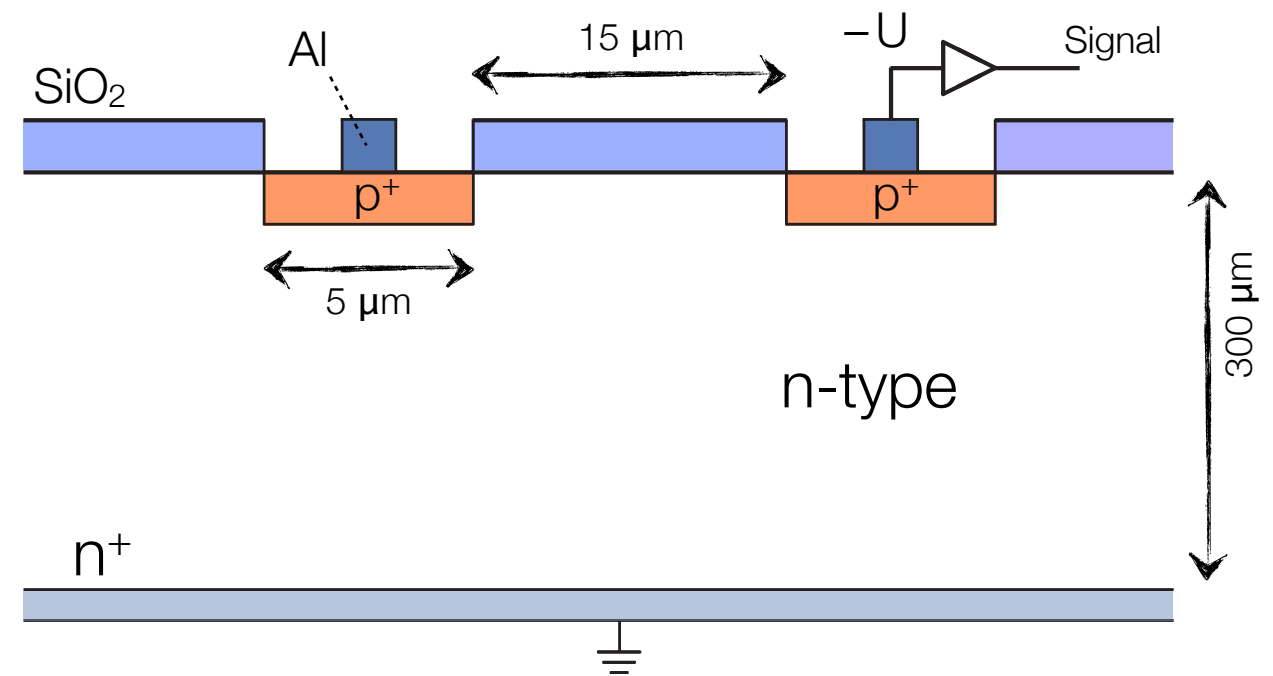
Output signal:

Total charge: $Q_{\text{out}} \sim 4 \text{ fC}$

Average energy loss of MIP: 300 eV/ μm ; Si: 3.6 eV/pair.

Thus 80 electron-hole pairs per μm ;

300 μm thickness \rightarrow 25000 pairs/MIP



Schematics of
Silicon Strip Detector

[from 1983]

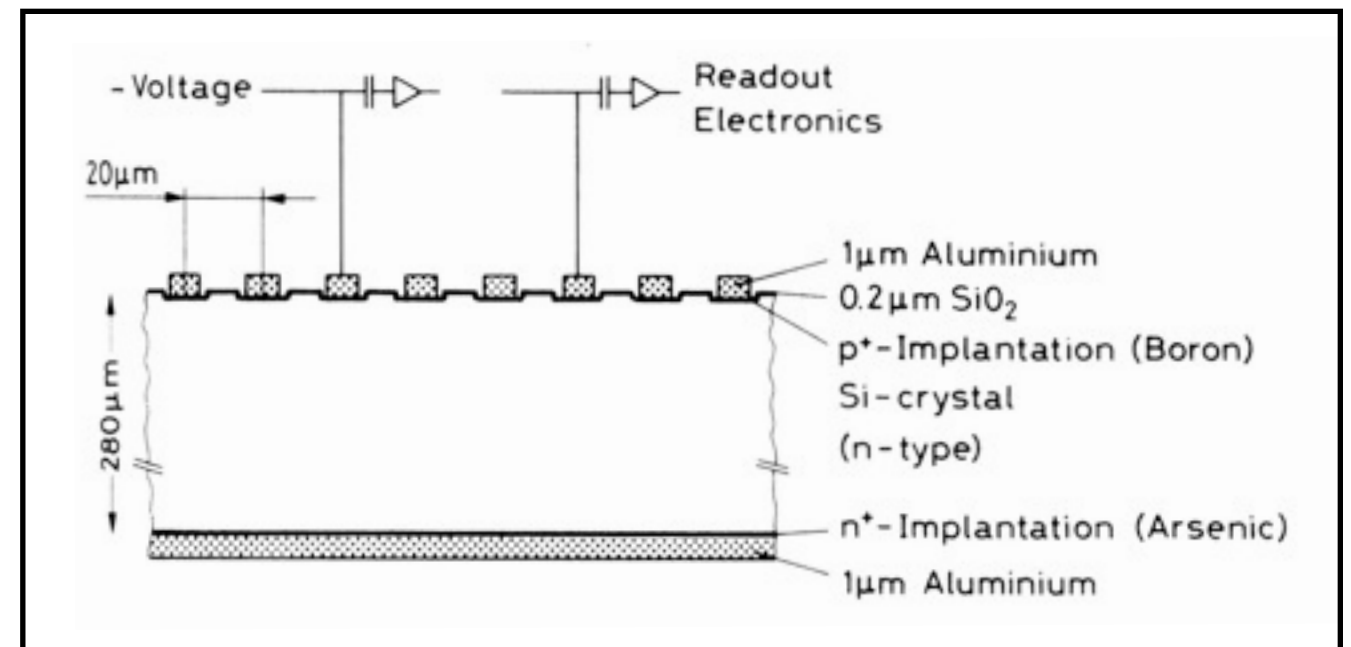
High resistive n-type silicon
onto which p⁺ diode strips with
aluminum contacts are implanted

Position Sensitive Detectors

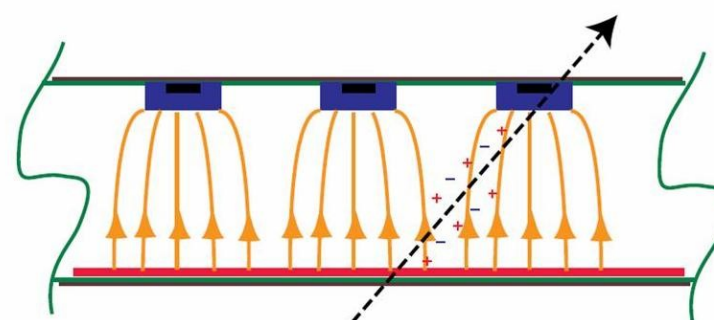
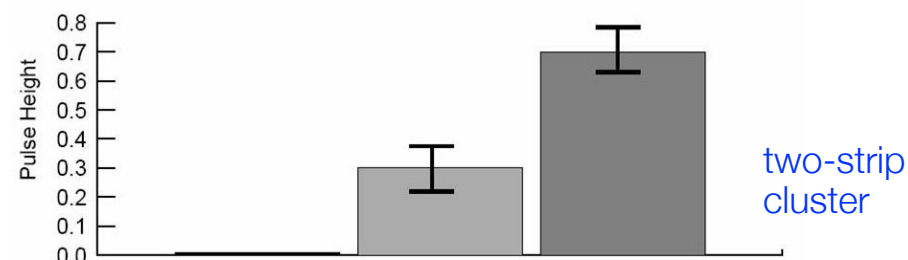
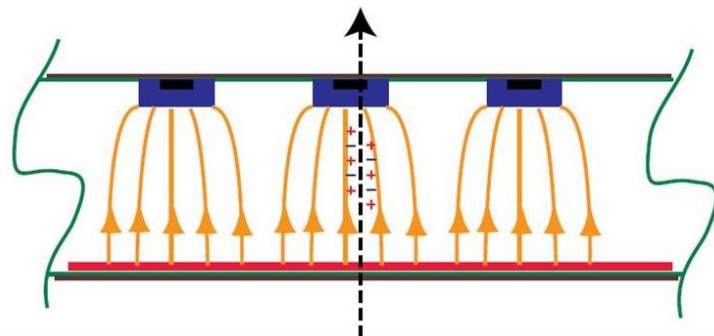
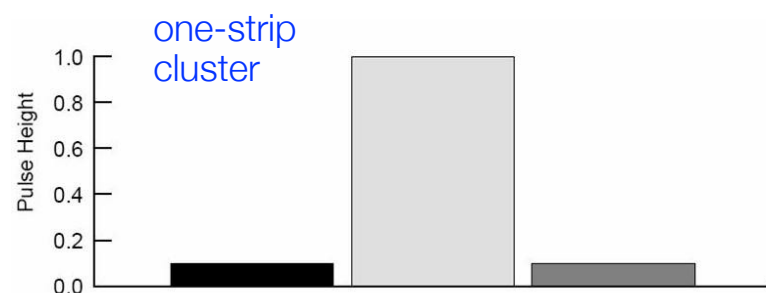
Readout:

Reduction of electronic channels
using charge division method ...

Calculate center of gravity
of collected charges ...



Original schematics
of first micro-strip detector
[Hyams et al., 1983]



Position Sensitive Detectors

Limitations:

High energy δ -electrons limit spatial resolution as they shift center of gravity of the signal ...

Rough estimate:

[Perpendicular scattering; $\delta \perp$ track]

r_δ : average range of δ -electron

N_δ : number of electron-hole pairs from δ -electron

N_p : number of electron-hole pairs from primary track

Then:

$$\Delta x = \frac{N_\delta \cdot \frac{r_\delta}{2}}{N_\delta + N_p}$$

Example:

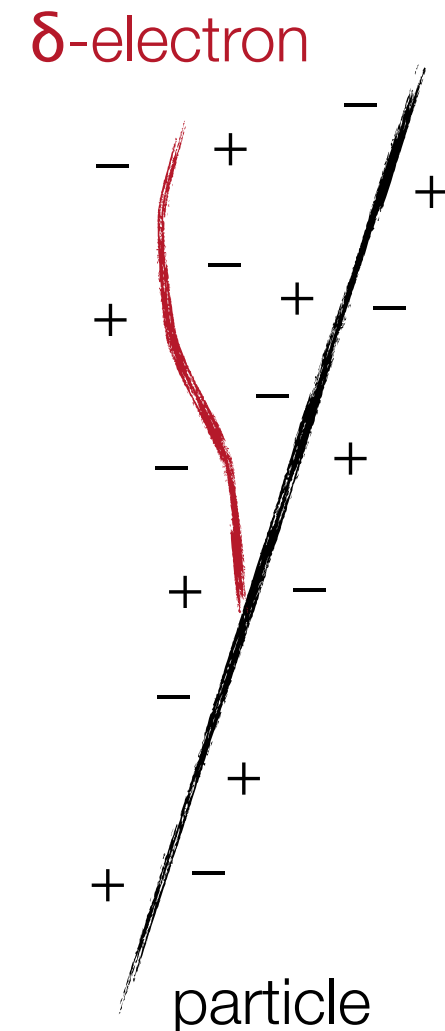
100 μm thick Si-counter

Pion [5 GeV] : 240 eV/ μm \rightarrow 6700 electron-hole pairs

δ -electron : with 10% probability $T > 20$ keV; $r_\delta = 5 \mu\text{m}$
complete absorption \rightarrow 5500 electron-hole pairs

$$\rightarrow \Delta x = \frac{5500 \cdot 2.5 \mu\text{m}}{6700 + 5500} = 1.1 \mu\text{m}$$

resolution limitation;
increases with thickness



Position Sensitive Detectors

Limitations:

Landau fluctuations: production of δ -electrons can disturb charge division ...

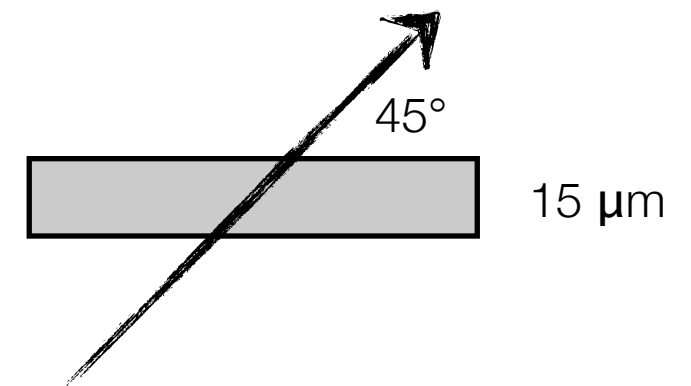
[worse for thick counters; see figure]

Noise: position measurement requires $S \gg N$; center of gravity influenced by S/N.

Diffusion: smearing of charge cloud deteriorates double hit resolution

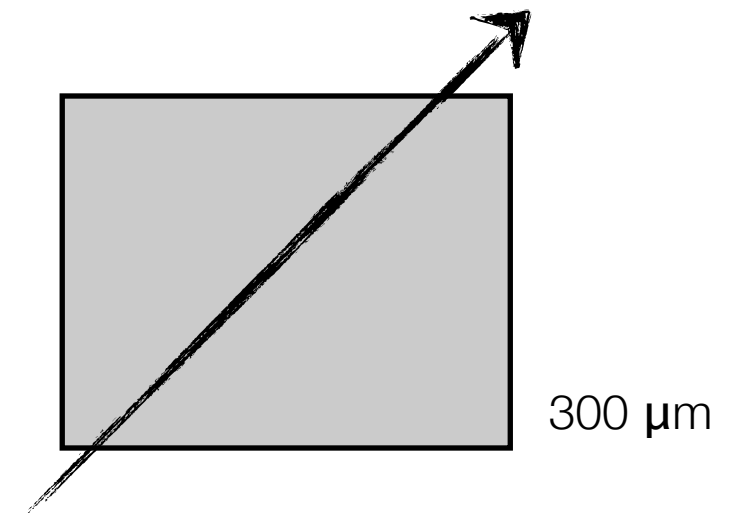
Magnetic field: Lorentz force has impact on drifting electrons and holes.

[track signal displaced if E not parallel to B-field]



Energy loss ≈ 5 keV

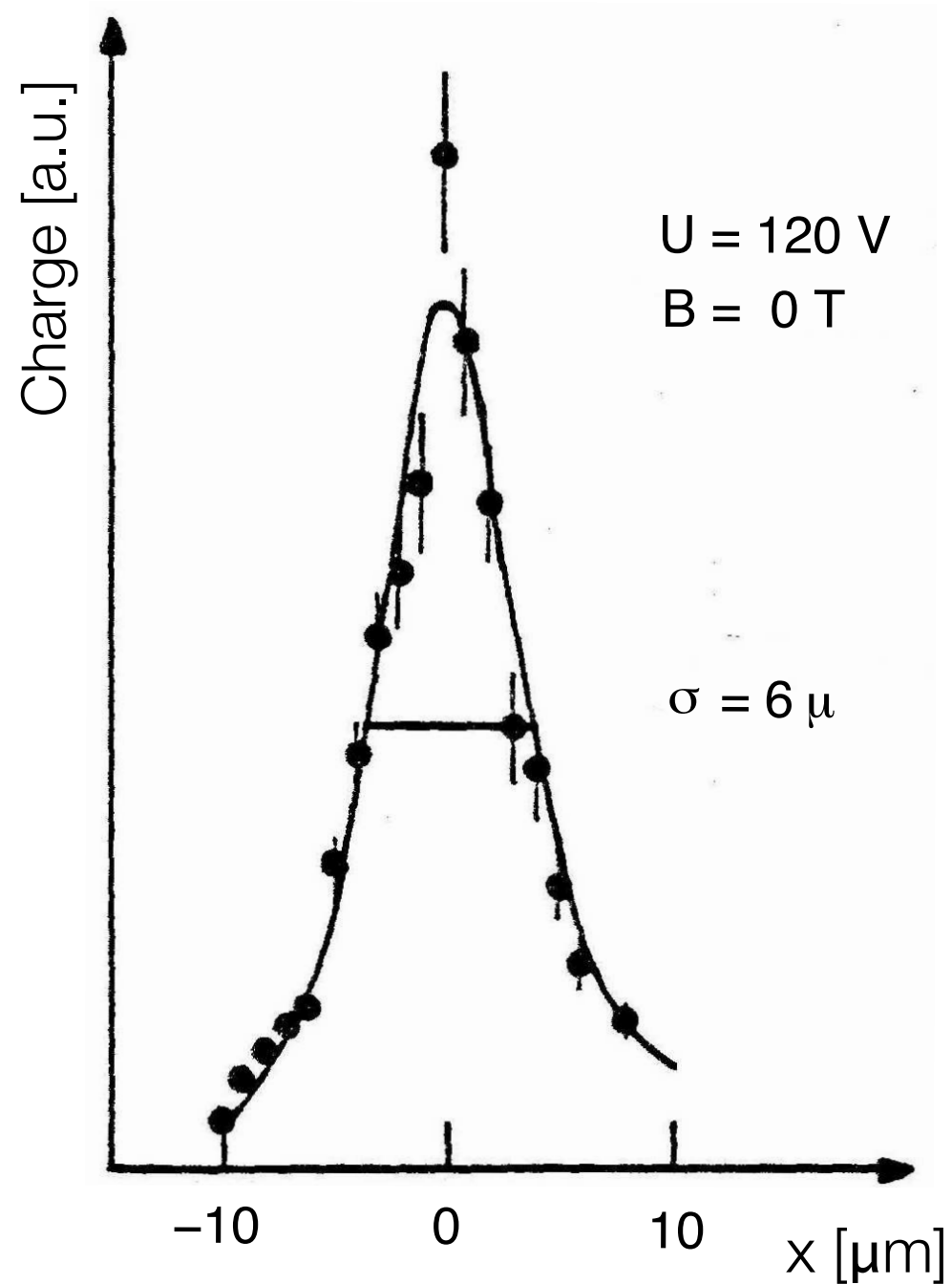
10% probability to produce 5 keV δ
Resolution limited to $15 \mu\text{m}/\sqrt{12} \approx 4 \mu\text{m}$



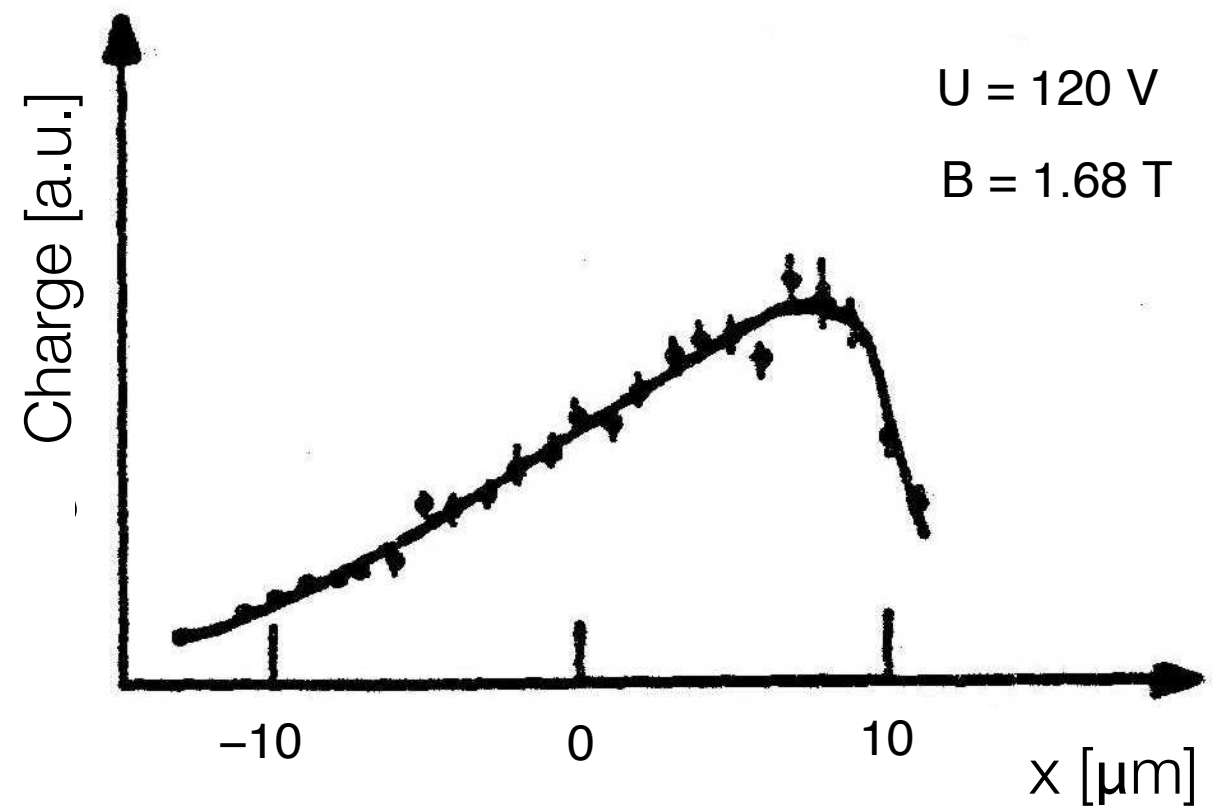
Energy loss ≈ 100 keV

10% probability to produce 100 keV δ
Resolution limited to $300 \mu\text{m}/\sqrt{12} \approx 90 \mu\text{m}$

Position Sensitive Detectors



Spatial distribution of collected charge
in presence of magnetic field

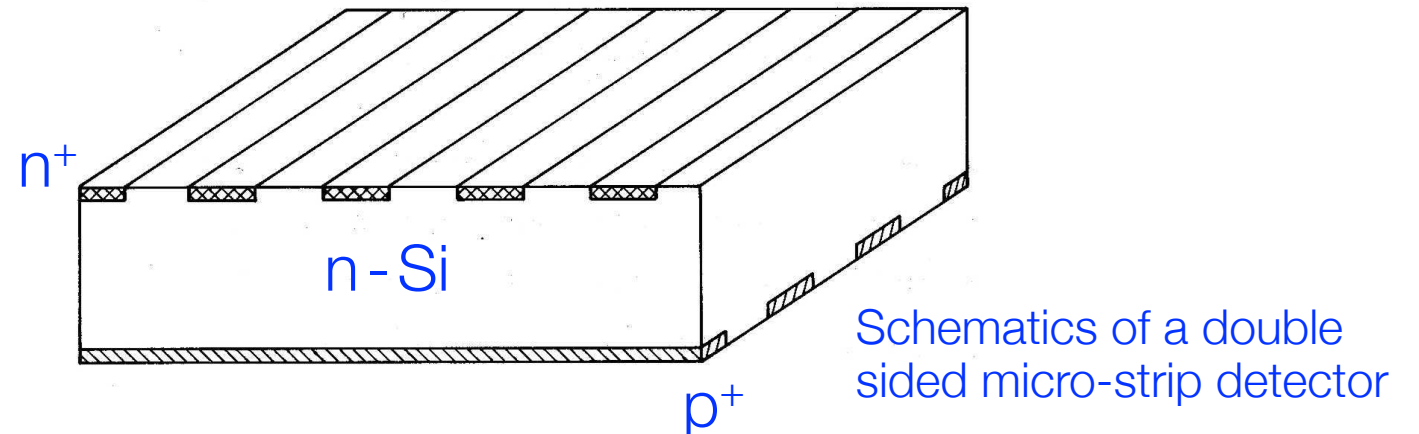


Position Sensitive Detectors

Next step:
Double sided
micro-strip detectors ...

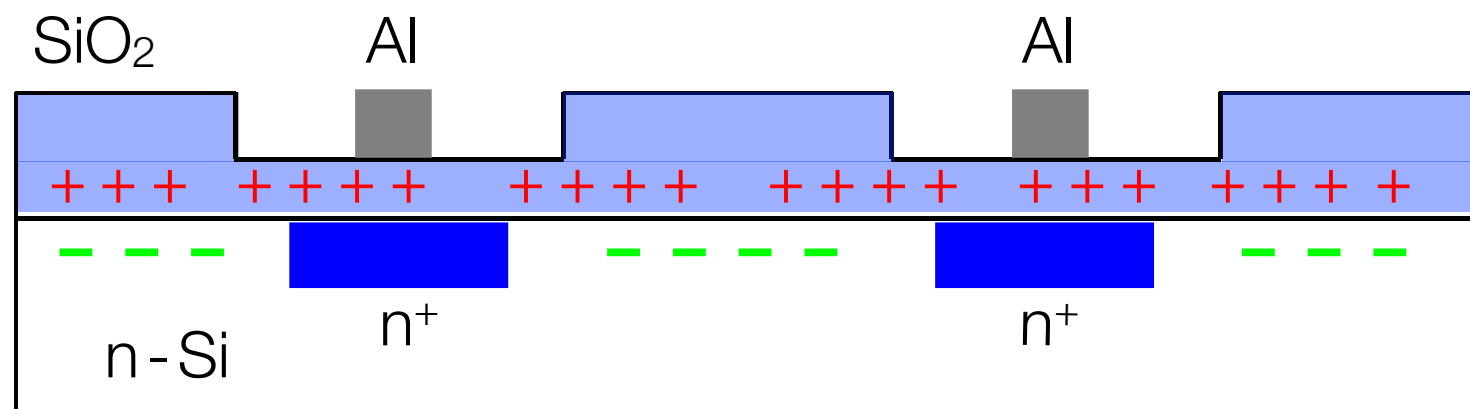
n^+ strips on one side
 p^+ strips on other side

Yields high spatial resolution
in both x and y direction ...



But:

Strips need insulation to avoid that positive
space charge attracts electrons from n-layer



Need blocking electrodes
to separate n^+ strips ...

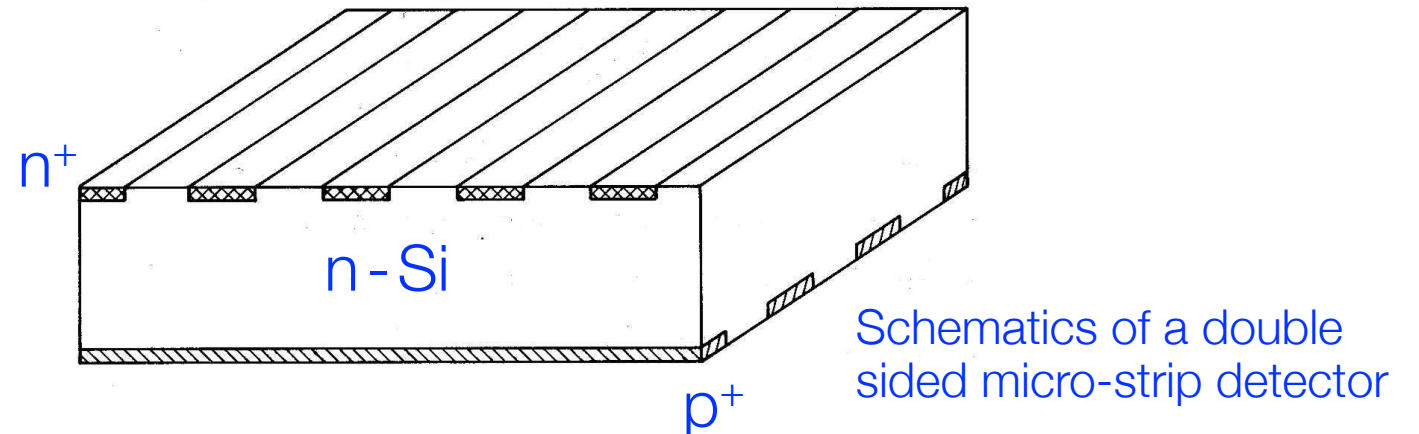
Closeup of of n^+ side of
double sided micro-strip detector

Position Sensitive Detectors

Next step:
Double sided
micro-strip detectors ...

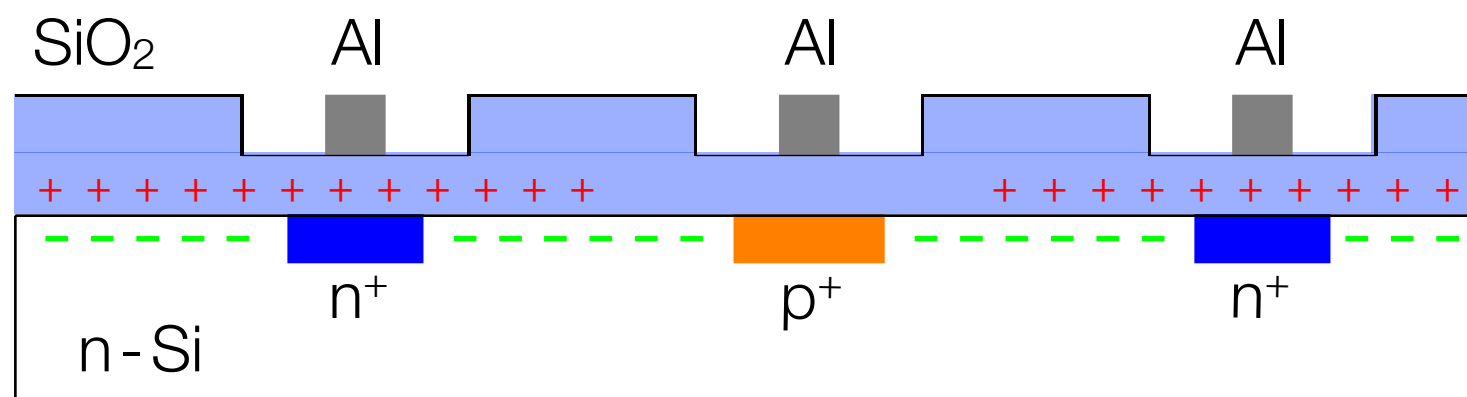
n^+ strips on one side
 p^+ strips on other side

Yields high spatial resolution
in both x and y direction ...



But:

Strips need insulation to avoid that positive space charge attracts electrons from n-layer

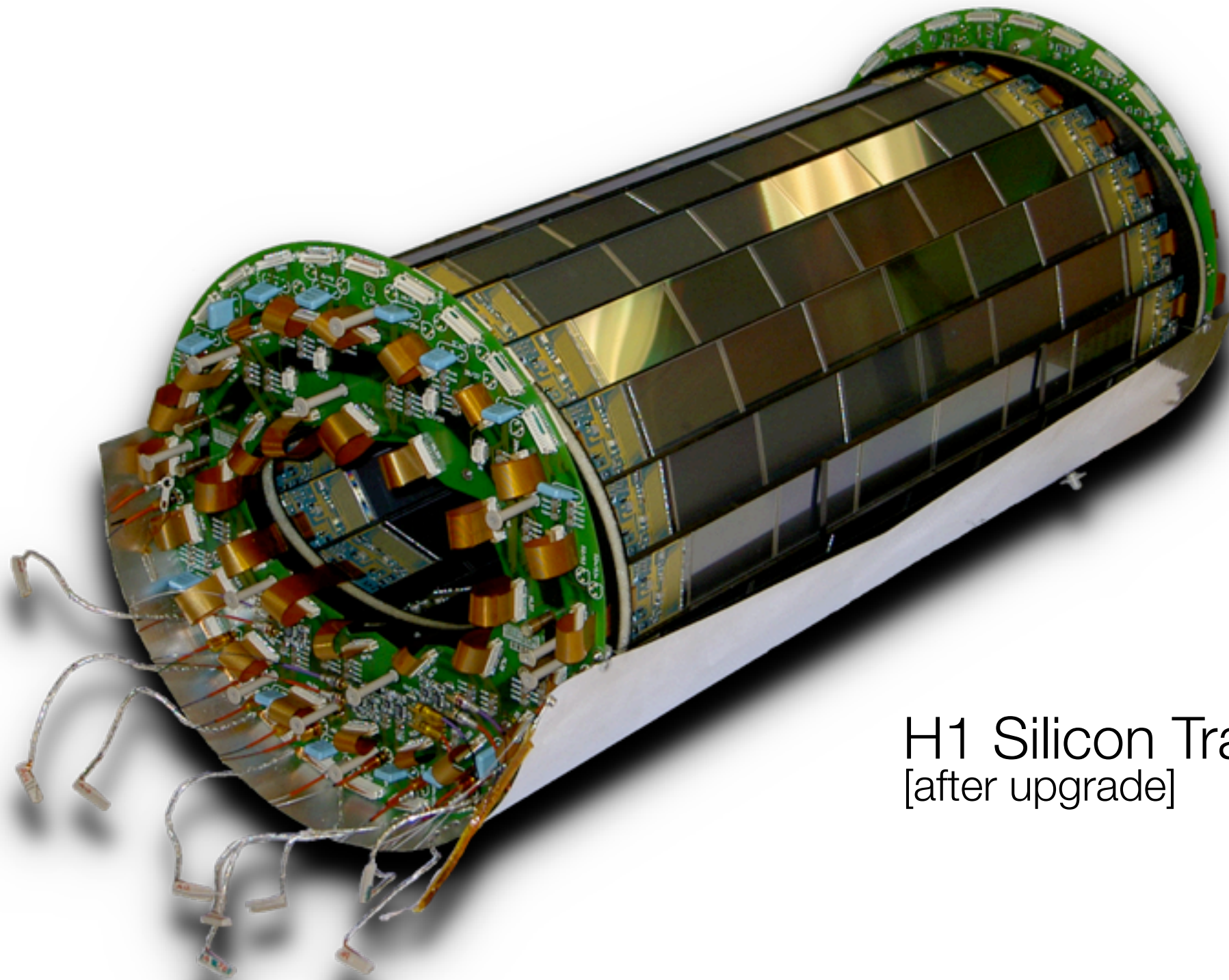


Need blocking electrodes
to separate n^+ strips ...

Add p^+ electrodes ...

Alternative: add Al contact
with negative bias voltage ...

Position Sensitive Detectors



H1 Silicon Tracker
[after upgrade]

Position Sensitive Detectors



BaBar Vertex Detector

Position Sensitive Detectors

Pixel detectors:

Like micro-strips, but 2-dim. segmentation ...

Advantage:

As for micro-strips 2-dim. information,
but higher occupancy allowed;

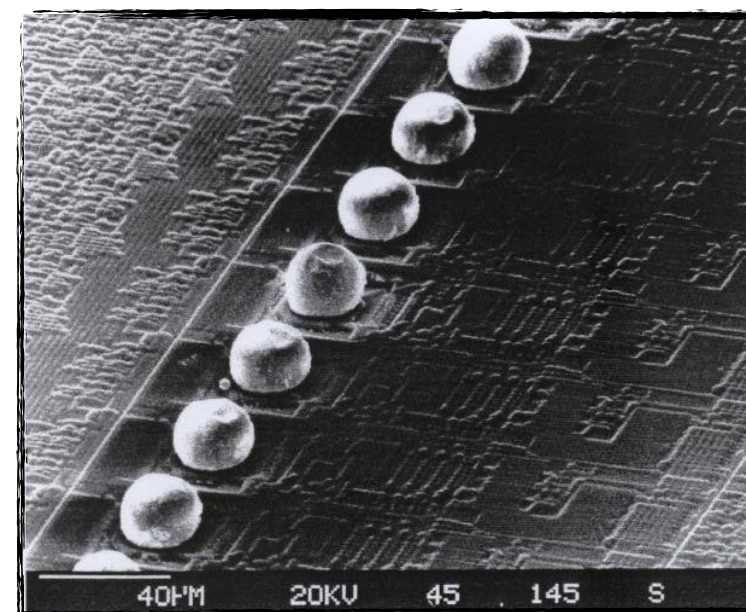
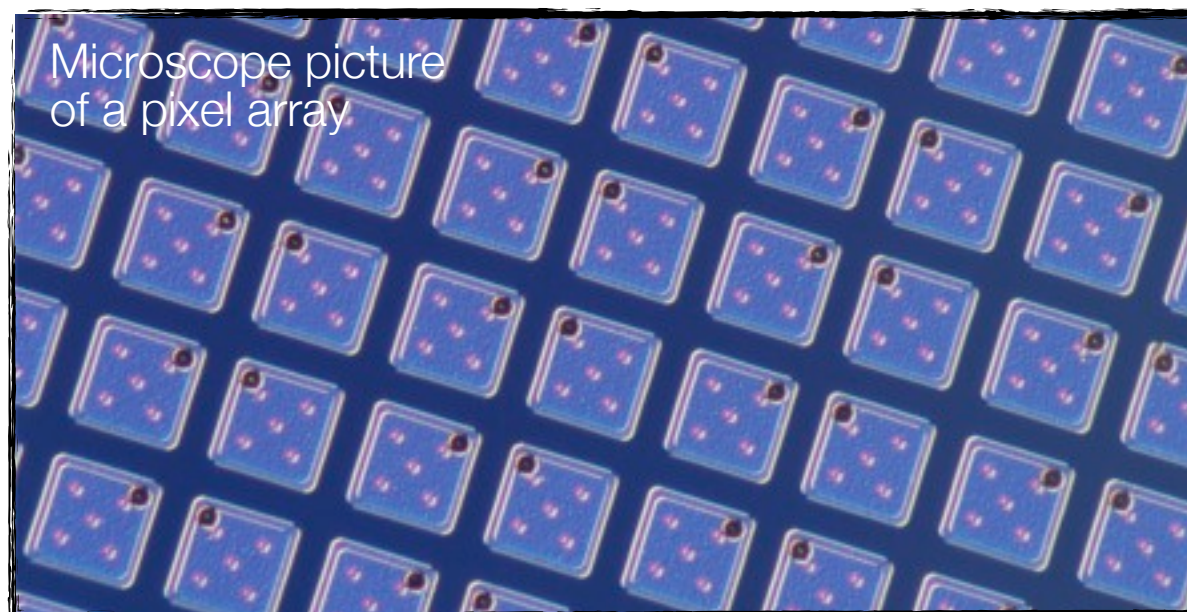
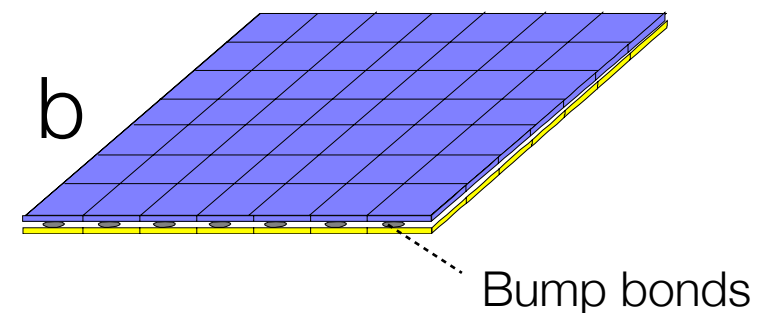
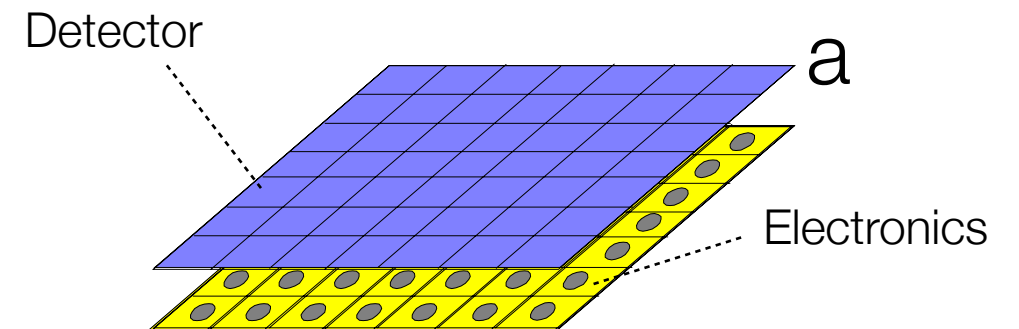
Lower noise due to lower capacitance ...

Disadvantage:

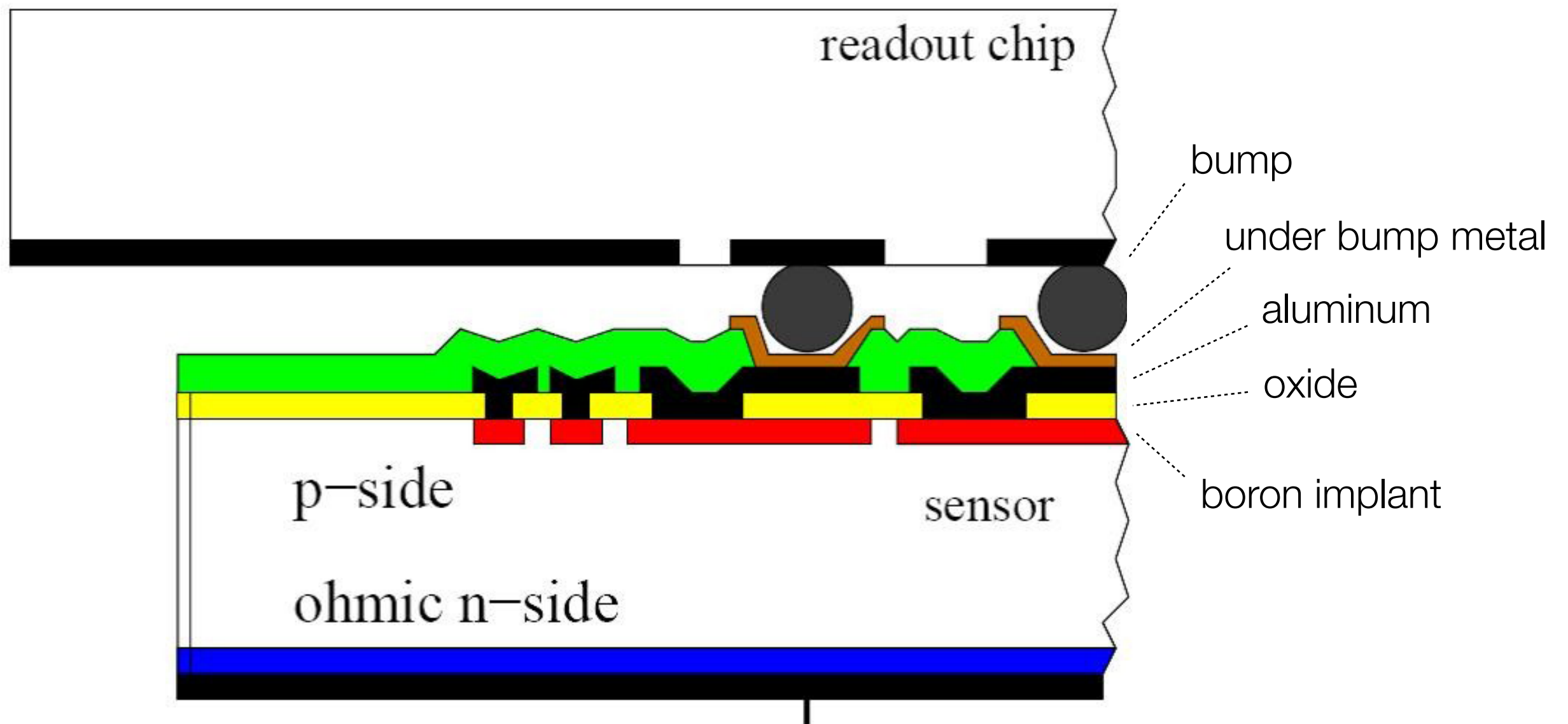
Huge number of readout channels;

Complicated technology ("bump bonding")

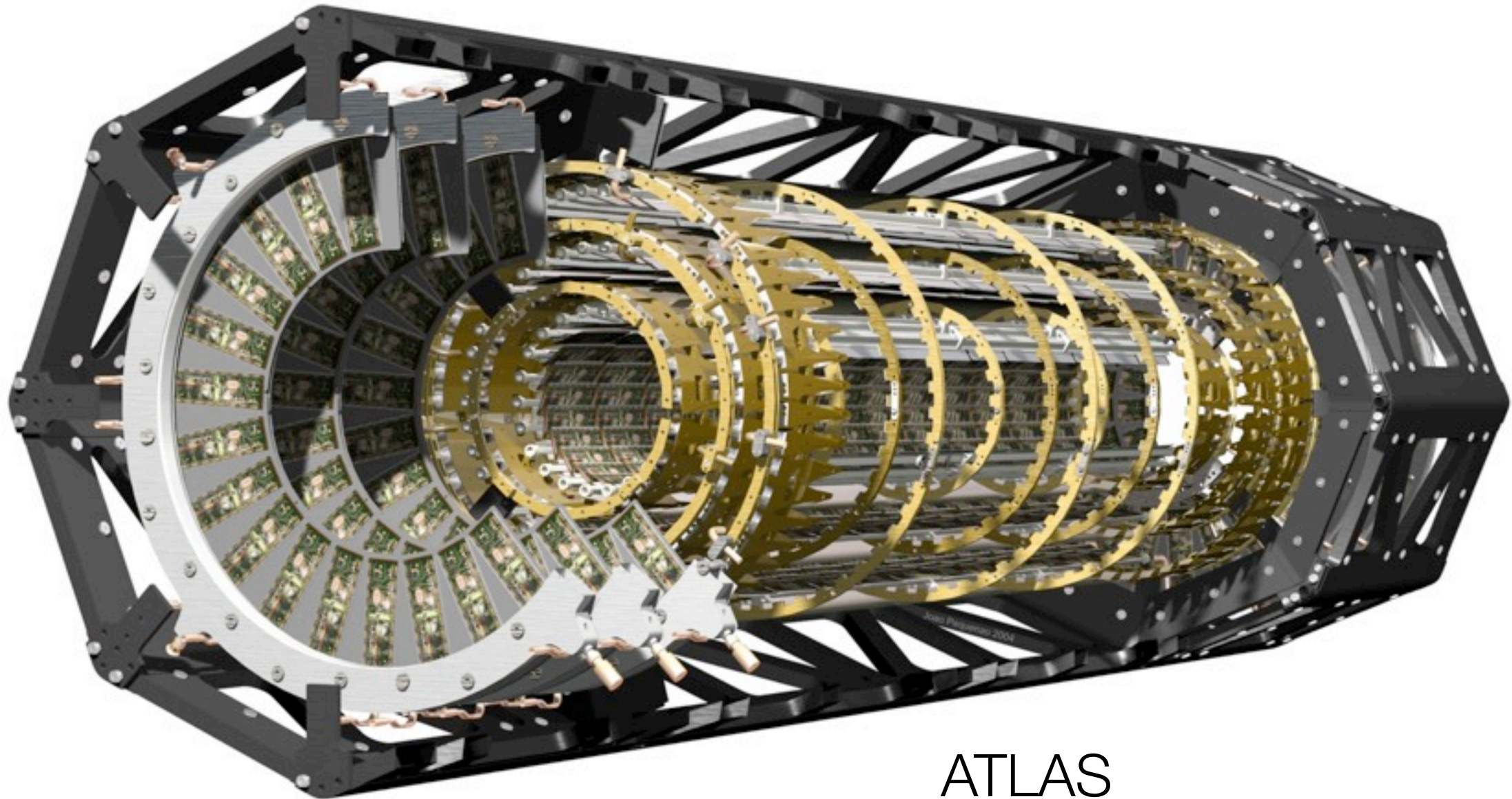
Requires sophisticated readout architecture ...



Position Sensitive Detectors

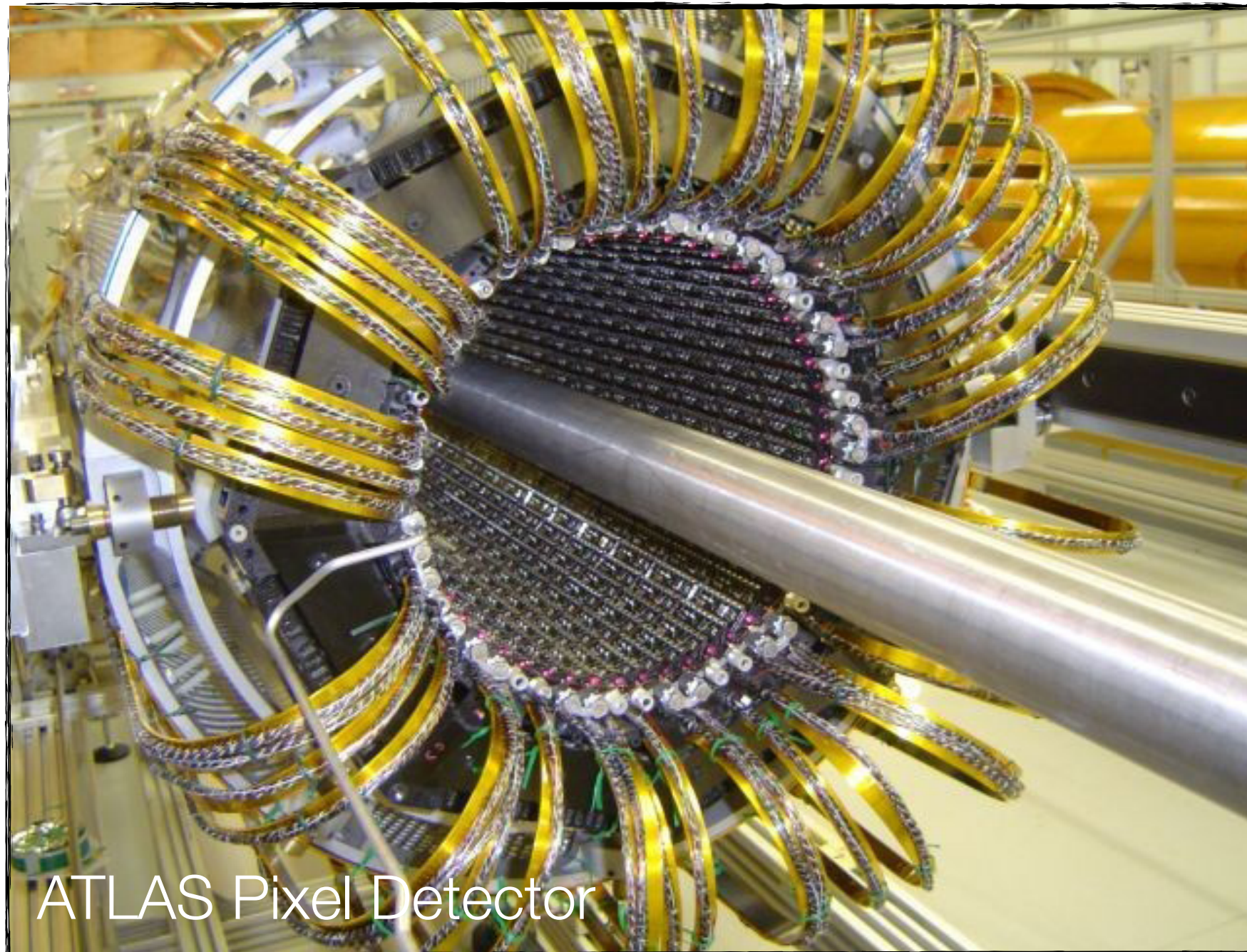


Position Sensitive Detectors



ATLAS
Pixel Detector
[nominal resolution: $R\phi \sim 12 \mu\text{m}$]

Position Sensitive Detectors



CCD – Charge Coupled Devices



The Nobel Prize in Physics 2009

"for groundbreaking achievements concerning the transmission of light in fibers for optical communication"

"for the invention of an imaging semiconductor circuit – the CCD sensor"



Photo: U. Montan

Charles K. Kao

🏆 1/2 of the prize



Photo: U. Montan

Willard S. Boyle

🏆 1/4 of the prize



Photo: U. Montan

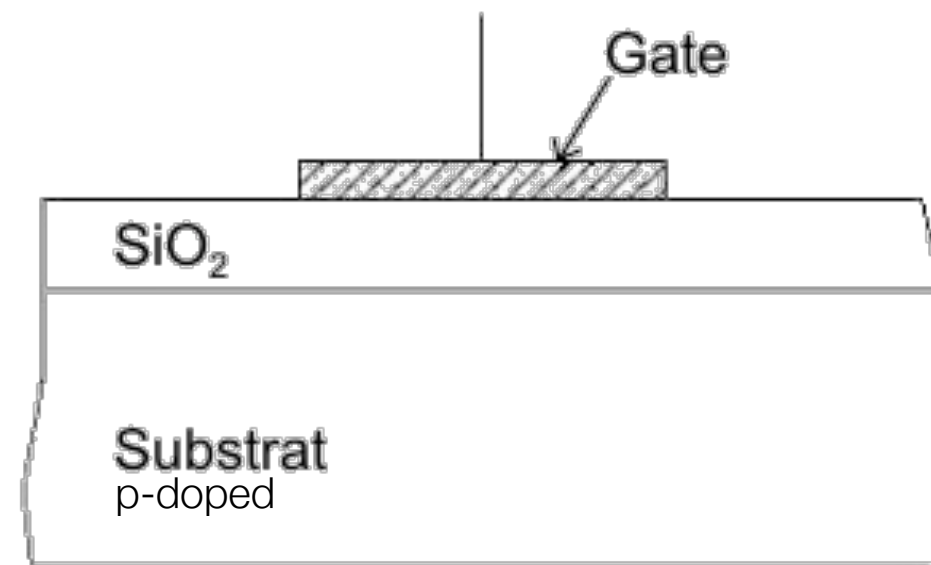
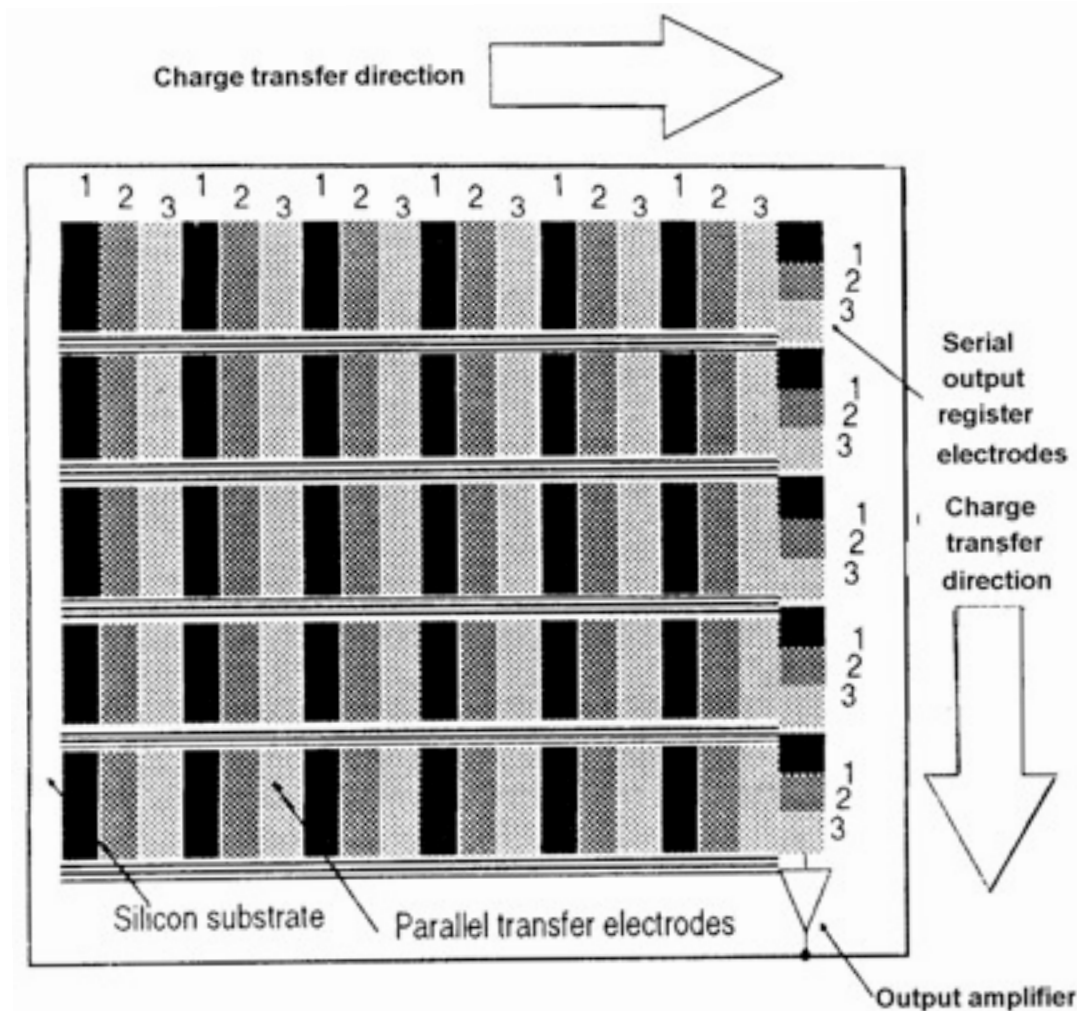
George E. Smith

🏆 1/4 of the prize

CCD – Charge Coupled Devices

MOS Structure
[Metal-Oxide-Silicon]

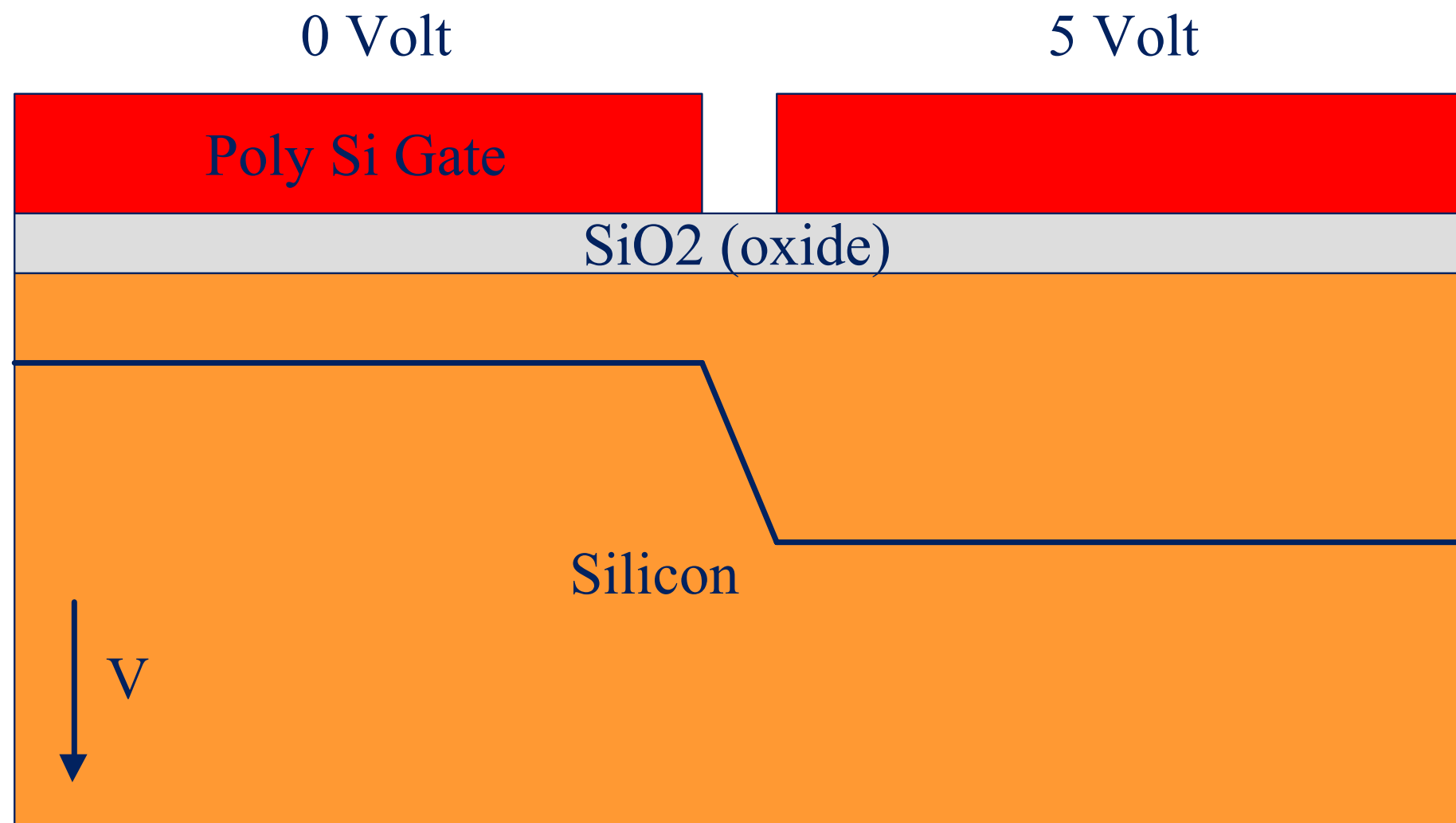
CCD: Many independent and
separately switchable gates ...
[electronically shielded potential wells]



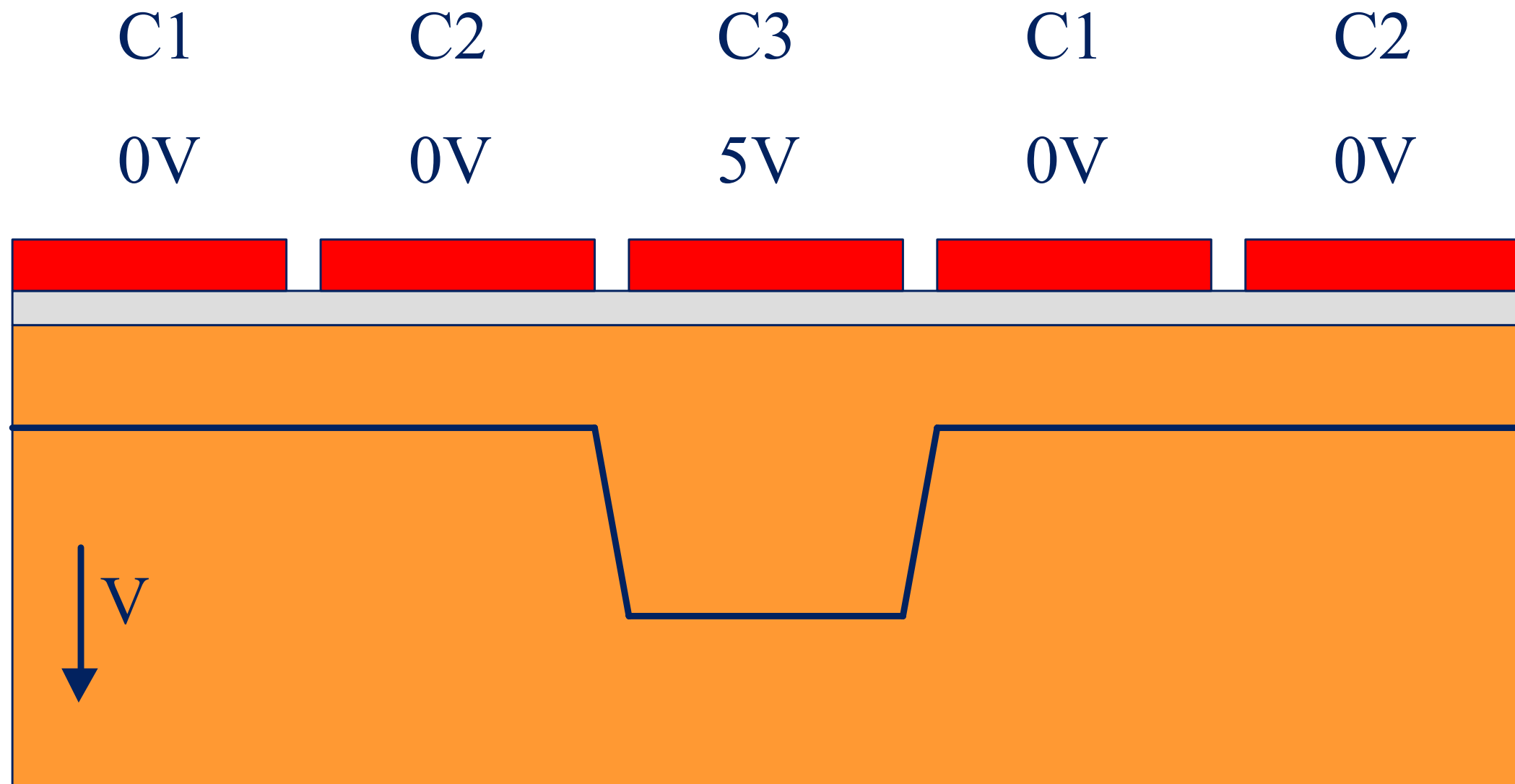
Gates/pixels store charges produced
by ionizing tracks/light;
[pixel size: 50 x 50 μm^2 ; sometimes 20 x 20 μm^2]

Information is transferred sequentially
to charge sensing pre-amplifier ...

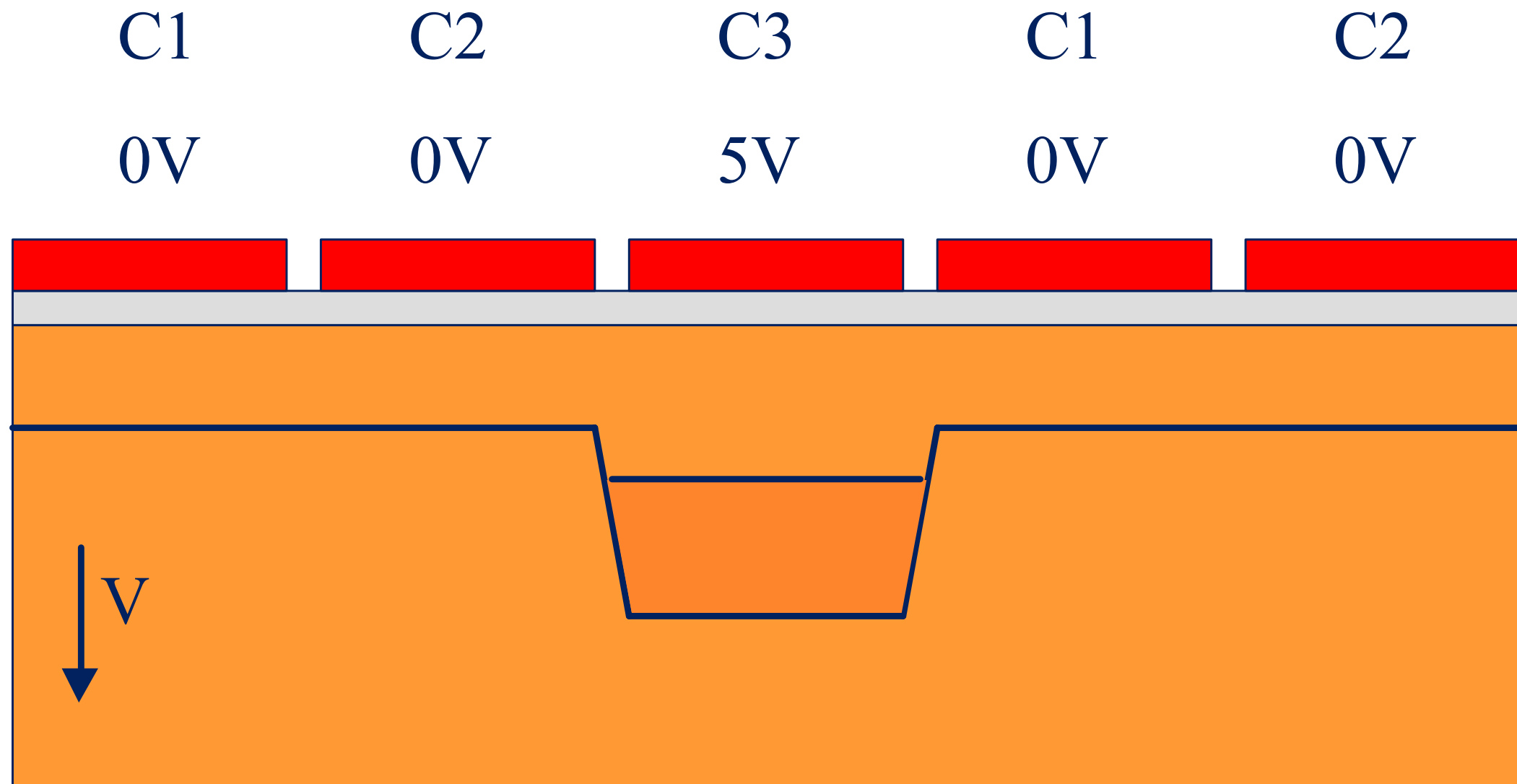
CCD – Charge Coupled Devices



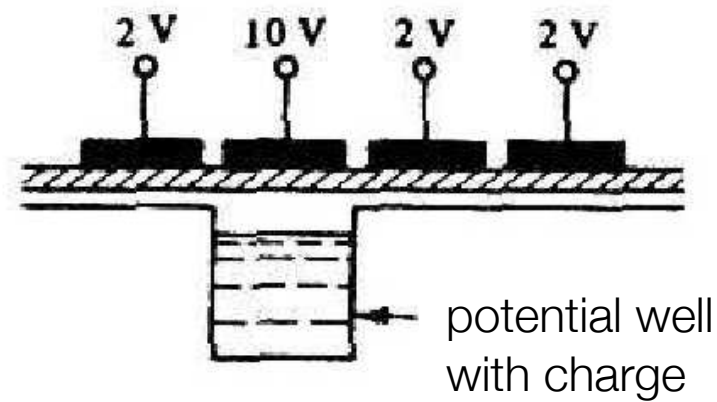
CCD – Charge Coupled Devices



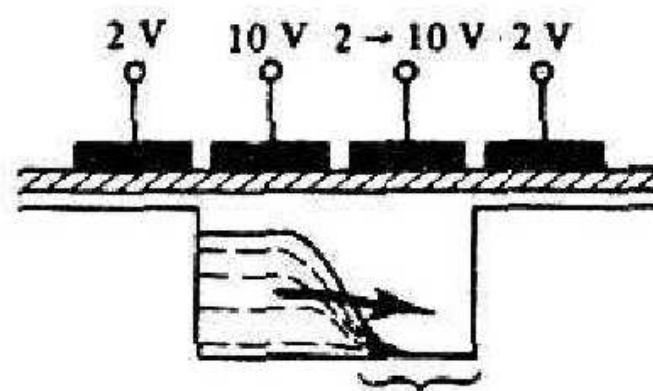
CCD – Charge Coupled Devices



CCD – Charge Coupled Devices

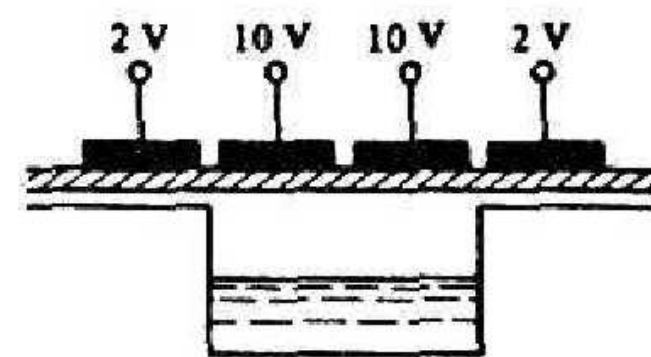


(a)

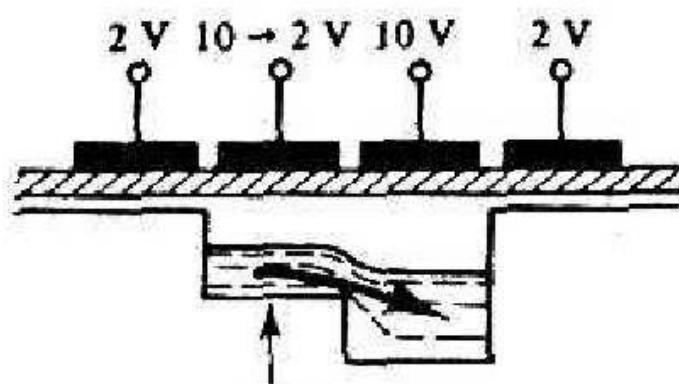


Extended potential well

(b)

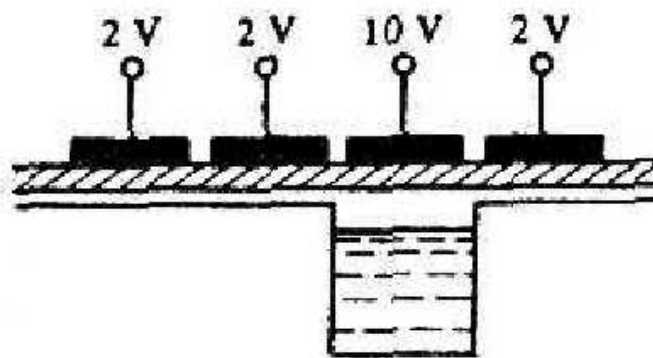


(c)

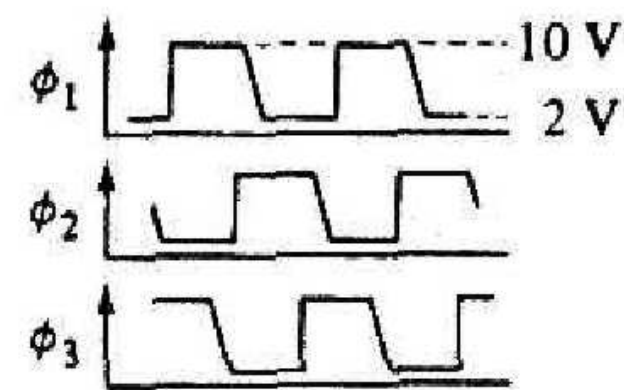


Turning off of
primary potential well

(d)



(e)



(f)

CCD – Charge Coupled Devices

